

## A collection of Galilean satellite eclipse observations, 1652–1983: Part I

J. H. Lieske

Jet Propulsion Laboratory/Caltech, Mail Stop 264/664, 4800 Oak Grove Drive, Pasadena, California 91109, USA

Received May 22, accepted June 19, 1985

**Summary.** The most complete collection of extant Galilean satellite eclipse observations since 1652 has been assembled. Since many of the old data exist only in manuscript form or in archaic forms (e.g. apparent time, local time, sidereal time, Julian calendar, etc.), they have been reduced to a modern proleptic Universal Time (UT) system (where the day begins at midnight) on the Gregorian calendar. Many of the data had been presumed to be lost for more than a century and since they are very valuable for discussion of long-term effects on the satellites, I present them here for present as well as future generations of astronomers. The data are invaluable for long-term studies of Galilean satellite motion and for the determination of physical parameters.

**Key words:** Planets and satellites – Jupiter – Galilean satellites – eclipses — ephemerides — celestial mechanics — observational methods —

### 1. Introduction

Since the 19th century a well-known but “non-existent” set of eclipse observations of the Galilean satellites made prior to the 19th century was referred to as the “Delambre collection.” J.-B. Delambre (1749–1822) constructed tables of the satellites’ motion in 1792 (Lalande, 1792) and 1817 (Delambre, 1817) which were widely used at the time. In the construction of those tables he analyzed approximately 6000 observations. Since the early 19th century those reductions had disappeared and most astronomers (Tisserand, 1896, p. 84) believed them irretrievably lost.

It has been only recently that the “pedigree” of this lost collection has been clarified. J.N. Delisle (1688–1768), an avid student of historical and positional astronomy (which in those days placed great emphasis on eclipse observations of the Galilean satellites for purposes of longitude determinations), had widespread contacts and collected eclipse observations of the satellites. Another French cleric-astronomer, A.-G. Pingré (1711–1796) probably made extensive use of Delisle’s manuscript collection and over a period of 30 yr developed his monumental treatise on 17th century astronomy, *Annales Célestes du dix-septième siècle*, whose publication the French Academy authorized in 1791. Pingré’s historical work placed great emphasis on the listing of eclipse observations for determination of longitudes.

However, due to Pingré’s death in 1796 and due to consequences of the French Revolution, the manuscript was not published and the printer’s proofs were apparently destroyed. Delambre probably had access to these manuscripts and his human calculators reduced them for Delambre’s use in developing his tables of satellite motion.

Near the close of the 19th century a set of proofs for Pingré’s treatise was found and the French Academy in 1898 again authorized the publication of Pingré’s work which was edited by Bigourdan (1901). Subsequently many of the original manuscripts for Pingré’s treatise and Delisle’s collection were rediscovered (Bigourdan, 1897), having been hurriedly and frequently mistakenly filed in Paris at the time of the French Revolution. Bigourdan was astronomer-in-chief at the Paris Observatory from 1897 to 1925 and he became the first director of the Bureau International de l’Heure (BIH) in 1919. To my knowledge no one has employed the rich source of data contained in Pingré’s treatise until now.

Sampson (1910) apparently made a thorough search for the “lost” Delambre collection which according to Delambre (Sampson, 1910, p. 216) contained 3439 eclipse observations of Satellite I, 1100 of II, 590 of III, and 334 of IV made prior to circa 1808. After extensive effort Sampson was able to locate the “computer” records of observations of Satellite II and some of Satellite IV (but without reference to their place of observation) which he then published. These “records” are similar to the one depicted by Arlot et al. (1984) in their Fig. 1. The records contain reductions of original data apparently made for Delambre, but they are not the original observations and sometimes have been altered. Arlot et al. recently published a valuable paper which contained rediscovered “Delambre” records for Satellite I from 1775 to 1802 and state: “It seems that the observations, collected by Delambre, covering the years 1775 to 1802, were not at Sampson’s disposal and it turns out that no useful observations made during that period were available to him . . .”

While it in no way lessens the importance and value of the data for Satellite I which were published by Arlot et al., their statement regarding Sampson is not entirely correct. Sampson was aware of the Delambre reductions for Satellite I, but he elected to ignore them, feeling that his own discussion (Sampson, 1909) of the Harvard eclipses 1878–1903 adequately answered any questions about the motion of Satellite I. The Harvard series of eclipses were originally published only in residual form and

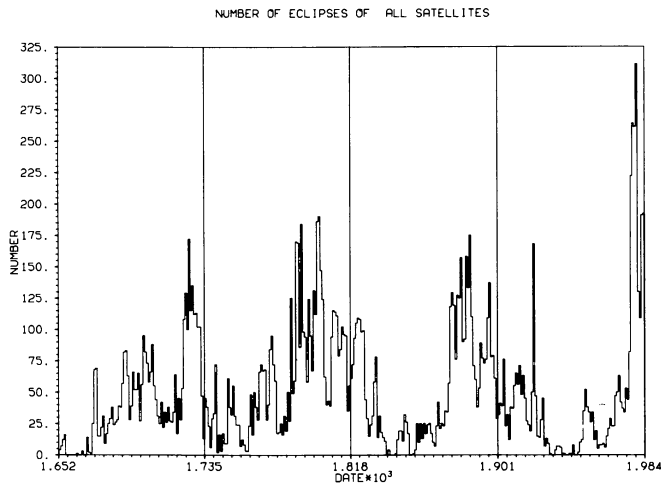


Fig. 1. Number of eclipse observations contained in the collection as a function of year

were reconstructed by Lieske (1978). In his discussion of the old Delambre data which he had found, Sampson (1910, p. 199) states (my comments are contained in brackets [ ]):

“I suppose this determination [that of Delambre] may now at length be considered generally superseded by discussion of photometric eclipses in the Harvard Annals, vol. lii, but it is not mere curiosity that would impel an inquiry into its [i.e. Delambre’s collection of 6000 eclipse observations] value. It has a bearing upon three elements requisite for determining the masses of the satellites and the ellipticity of Jupiter. These elements are the motion of the node of Satellite II, the motion of the apse of Satellite IV, and that part of the equation of the centre of Satellite III which refers to the apse of IV.”

In other words, Sampson was primarily interested in obtaining further information about  $\omega_2$ ,  $\pi_4$  and the coefficient of  $l_3 - \pi_4$ , using the notation of his theory (1921) or that of Lieske (1977). He then points out (p. 200) that the determination of the motion of  $\omega_2$  and  $\pi_4$  “require a compact set of ancient observations . . . to fix the positions of node and apse . . . at a remote epoch,” but that the determination of the coefficient of  $l_3 - \pi_4$  requires a long dedicated series of observations.

Furthermore, in his discussion of the Delambre reductions which he rediscovered, Sampson (p. 216) states:

“... The Bureau des Longitudes, where such observations as existed would naturally repose, on learning my purpose, caused a search to be made, and most courteously placed at my disposal a mass of papers which proved when I examined them to contain among other matters a complete set of Delambre’s collection of eclipses for Satellite II and Satellite IV.

“These papers are the work of two computers, made at the direction of Delambre . . . The earlier and less important part [in the sense of Sampson who was interested in  $\omega_2$  and  $\pi_4$ ] is referred to by the other calculator as ‘les calculs que Monsieur Delambre a anciennement fait faire en ville.’ They are computations of the time of occurrence of eclipses made with Delambre’s Tables of 1792 . . . There are about 500 eclipses of Satellite I, dating from 1775 to 1802, probably including the complete collection of picked eclipses of this satellite upon which the Tables of 1792 were founded, but the numbers for the other satellites are mere fragments of the whole.

“The work which remains of the second calculator [and which Sampson published in his paper] refers exclusively to Satellite II and Satellite IV. There are 1100 eclipses of II, and, after rejection of defective cases, 464 of IV.”

So the data which Sampson published in his 1910 paper are the “Calculator II” records for Satellites II and IV, while the data published recently by Arlot et al. (1984) are probably the “Calculator I” records. Of the 845 observation records of Satellite I published by Arlot et al. I had already located approximately 30% in other sources.

Another source which has recently been examined is the collection (Bigourdan, 1897) of Delisle manuscripts contained in the Paris observatory in Manuscripts A-5-1 through A-5-8. J.N. Delisle was a French astronomer who in 1721 received an invitation to go to Russia for four years and help found the observatory in St. Petersburg. He went there in 1725 and remained for 22 yr. Delisle collected eclipse observations from widespread sources, many of them via correspondence, and his hand-written manuscript is the richest source of early observations extant.

These latter two forgotten treasures contain listings of the original observations as obtained from manuscripts and correspondence and they generally include the observations which ultimately also are given in the “computer records” published by Sampson (1910) and by Arlot et al. (1984). Similar computer records are contained in the Delisle manuscripts, so they all probably belong to the reductions which were done for Delambre. We now have more than 7000 observations prior to 1800 recovered from the literature and from manuscript collections and have probably reconstituted the lost “Delambre collection” which properly ought to be called the Delisle and Pingré collections.

The attempt to reconstruct the “Delambre” collection began in 1980 when I visited the Paris Observatory library and was able to examine the manuscript collection of J. Delisle. After initial examination and confirmation that when reduced to a modern UT system [by accounting for the difference between apparent and mean time, local time, and by using some form of the difference between Ephemeris Time (ET) and Universal Time (UT)] I found that the data were quite accurate, I endeavored to locate as many of the old eclipse observations as possible. A description of some of the detective work involved is described in Lieske (1982, 1983).

Since the observations were presented in an inhomogeneous manner with numerous peculiarities and since they are so valuable for obtaining a long span of earth-based data that in many respects rivals the accuracy of the derived parameters from modern spacecraft-based results, it was decided to reduce them to a uniform UT system so that future researchers might more readily have access to these invaluable data. The compilation of eclipse observations is outlined in this paper and the detailed listings are given in an accompanying paper in the Supplement series.

## 2. Sources of data

The early data are largely contained in manuscript form in the works mentioned earlier by Delisle and by Pingré. No data were taken from the “computer records” (since they often did not indicate where the observations were made and what the ob-

...serving conditions were like) unless the original data were not available from other sources. Another valuable source for early observations is the data contained in the compilations which appeared in the annual volumes of the *Berliner Astronomisches Jahrbuch*, edited by J. Bode until his retirement in 1825 (the last issue edited by Bode was that of 1829, published in 1826). A list of the observers (or editors in some instances) of the data contained in the present collection is given in Table 1. The Table contains an Index which arbitrarily has been assigned to each source of observations. [The initial publication was labeled PA for "Publication A" and then the alphabet was wrapped-around from ZZ to AA after many other observations were found]. The table also gives the journal and its year of publication, the author of the paper and the number of observations contained in the collection. The table is sorted by authors in order that one might readily find the active observers in different time intervals. Tables in the Supplement paper present the same data but they are sorted by Index number or by journal, so that from the observations given in the Supplement paper one can easily determine who observed the eclipses. The initial literature survey conducted by Pierce (1974a,b) for locating observations of the Galilean satellites was supplemented by searches through other journals and manuscript collections.

As given in the table, there are 418 different sources and the total number of observations referenced is 16802 (including 1091 excluded observations). As will be noted later, some duplicate observations (notably published data which also appear in the generally unreferenced Sampson records of Calculator II or in the Arlot et al. compilation of Calculator I) are listed and marked as duplicates, while others are listed but marked as not useful for analysis until further information is obtained about them.

During the 17th century there was a great effort worldwide to make observations of eclipses of the Galilean satellites and they often formed the basis of early maps of the world, since a given event as observed at two different longitudes on the earth will yield the longitude difference between the observing sites. Most early observations were recorded in local apparent time and it often requires a bit of detective work to determine the modern location of an old observing site. Many names were spelled phonetically so that Otaheite is the modern Tahiti, Ulyssipone is the modern Lisbon, Hoai-Ngan (or Hoyaingan) is Hwaiian, China, etc.

In Table 2 I present a listing of the observing sites for the present collection of eclipses. Each location is assigned an Index (so that duplicate data could more readily be identified), initially starting at value LA (for "Location A"), then LB etc., but again the alphabet was wrapped-around after ZZ in defining indices for each site. The longitude of the observing site is also given, as is the name of the location. The comments field in the table gives further details about certain sites, such as when the modern name and the old name are different. The final column of the table contains the number of observations from that observing site in the collection. The 16802 observations contained in the collection were made at 432 different sites. The paper in the Supplement series gives the actual observations and also lists the observing sites shown in Table 2 but sorted by Index and by longitude.

Modern observations of eclipses are largely made by amateur astronomers who contribute significantly to the valuable series of observations. In Fig. 1 we present a histogram showing the number of observations made in each year for all of the satellites.

The histogram contains many historically important effects, such as the founding of the Paris observatory in 1667, the Greenwich observatory in 1675 and the early efforts of Ole Rømer in the 1670s to employ the eclipses to determine the finite speed of light (Nielsen, 1944). Also apparent are the increase in data upon Delisle's move to St. Petersburg in 1725 and the decrease during the French Revolution, during which many of the earlier manuscripts were hurriedly filed away and "misplaced" for a century or more. The extended paper in the Supplement series contains similar histograms for each satellite. Retirements (such as that of Bode in 1825, after which the *Berliner Astronomisches Jahrbuch* no longer contained an annual listing of observations) and the effects of wars are also evidenced.

### 3. Reduction of data

Most of the old observations were recorded in local apparent time. Hence in order to derive a mean time or Universal Time of the observation one needs to know the longitude of each observing site. Generally I obtained the longitude from *The Times Atlas of the World* (Comprehensive Edition of 1980), supplemented by old almanacs for established observatories, primarily the American Ephemeris of 1905 or the *Berliner Astronomisches Jahrbuch*. Although modern observations are recorded ab initio in UT, I still retained the longitudes and identification of observing sites so that duplicates could more readily be traced and removed.

As outlined in the Supplement paper, the local apparent times were reduced to proleptic Universal Times by the algorithm given in Smart (1931). It is only when calculating residuals (i.e., when computing the predicted time of an event in ET and comparing that prediction with the observed time of the event recorded in UT) that one requires the knowledge of the relationship between ET and UT. That introduces the problem of finding a good table of  $\Delta T$  values valid for more than 3 centuries, and brings in a discussion of lunar tidal dissipation, since most tables of  $\Delta T$  are based upon the analysis of the motion of the Earth's moon. The work of Brouwer (1952) is generally the standard for old observations, since it utilizes the tidal term  $\dot{n}_{\text{Moon}} = -22.44$  arcsec per century<sup>2</sup> of Spencer-Jones (1939), but Brouwer's results are not very accurate prior to 1850. Martin (1969) extended the Brouwer analysis prior to 1850 and the "Brouwer-Martin" values of  $\Delta T$  are perhaps the best representation of the classical Brouwer approach using the Spencer-Jones tidal term of  $\dot{n}_{\text{Moon}} = -22''.44$ .

The most accurate determination of  $\Delta T$  (leaving aside the question of what the lunar tidal deceleration ought to be) is probably that of Morrison (1979a,b, 1980) and of Morrison and Stephenson (1981) since they carefully reduced the data and determined values of  $\Delta T$  using a lunar tidal term of  $\dot{n}_{\text{Moon}} = -26''.0$  derived by Morrison and Ward (1975). Ten years ago there was great disparity in the determination of lunar tidal terms, with values ranging from the Spencer-Jones value of  $\dot{n}_{\text{Moon}} = -22''.44$  up to about  $-50$  arcsec/cy<sup>2</sup>. Each second of arc difference in the adopted lunar tidal term will produce about one second of time per century squared difference in the  $\Delta T$  values, so it is important to get good values of  $\Delta T$ , especially since one of the potential uses of the Galilean satellite eclipse data would be to investigate the possibility of tidal dissipation in the Galilean satellites as it might be evidenced in effects on their motion.

Table 1. Observer list (sorted by author)

Table with columns: Index, Year, Journal, Volume, Author, No. Obs. Rows include observers like PH 1965, PI 1966, PJ 1969, etc.

Table 1. Continued

Table with columns: Index, Year, Journal, Volume, Author, No. Obs. Rows include observers like TM 1909, TN 1886, TP 1925, etc.

Table 1. Continued

Table with columns: Index, Year, Journal, Volume, Author, No. Obs. Rows include observers like EI 1819, EJ 1820, EK 1820, etc.

Table 1. Continued

Table with columns: Index, Year, Journal, Volume, Author, No. Obs. Rows include observers like UC 1904, UD 1905, UE 1899, etc.

Table 1. Continued

Table with 5 columns: Index, Year, Journal, Volume, Author, No. Obs. Rows include astronomical publications from 1909 to 1989.

Table 1. Continued

Table with 5 columns: Index, Year, Journal, Volume, Author, No. Obs. Rows include astronomical publications from 1959 to 1989.

Table 1. Continued

Table with 5 columns: Index, Year, Journal, Volume, Author, No. Obs. Rows include astronomical publications from 1833 to 1929.

Table 1. Continued

Table with 5 columns: Index, Year, Journal, Volume, Author, No. Obs. Rows include astronomical publications from 1777 to 1896.



Table 2. Continued

Table with 6 columns: Index, Longitude, Location, Country, Comments, No. Obs. Rows include SI 100.31 E Louveau Siam, WT 1.18 E Louviers France, QN 13.19 E Lund Sweden, etc.

v

Table 2. Continued

Table with 6 columns: Index, Longitude, Location, Country, Comments, No. Obs. Rows include PJ 64.69 W St. Croix Virgin Islands, SW 14.31 E St. Elme Malta, UW 57.00 W St. Ignatius Paraguay, etc.

vii

Table 2. Continued

Table with 6 columns: Index, Longitude, Location, Country, Comments, No. Obs. Rows include XJ 38.18 E Omega USSR, PL 2.54 W Ormakirk England, VC 149.57 W Otahete Tahiti, etc.

vi

Table 2. Continued

Table with 6 columns: Index, Longitude, Location, Country, Comments, No. Obs. Rows include LT 139.67 E Tokyo Japan, AV 78.80 W Tonawanda, N. Y. USA, SG 5.56 E Toulouse France, etc.

viii

Nowadays most analysts obtain values of the lunar tidal dissipation somewhere between the Spencer-Jones value of  $\dot{n}_{\text{Moon}} = -22''.44$  and the Morrison value of  $\dot{n}_{\text{Moon}} = -26''.0$ . Since these two competing models differ by about 3.5 arcsec, then the appropriate  $\Delta T$  values differ by about  $3^s.24 T^2$  – or by about 30 s of time over three centuries. If the old data are accurate to that level, then one at least can discriminate between the two values for lunar tidal dissipation in tables of  $\Delta T$ . Upon adopting some values of  $\Delta T$  we can employ the old Galilean eclipses to investigate the possible existence of secular changes in their periods as mentioned by Goldstein (1975) and by Yoder and Peale (1981), or one can estimate corrections to the adopted  $\Delta T$  tables.

I have initially adopted the Spencer-Jones value for tidal friction,  $\dot{n}_{\text{Moon}} = -22''.44$  arcsec/cy<sup>2</sup> (the effect in lunar longitude is  $\frac{1}{2} \dot{n}_{\text{Moon}} T^2$ ), but I have employed the Morrison data because of their inherent superiority. In Fig. 2 I present a diagram of the  $\Delta T$  values as obtained by Morrison (1980) and by Morrison and Stephenson (1981) for the interval 1650 to the present which were communicated to me by Morrison (1980) prior to publication. In the figure one obtains the value of  $\Delta T$  by differencing the “observed” drift in time of the Moon for zero tidal acceleration [ $Z$  in the diagram] and the adopted tidal acceleration [ $F$  in the figure] to produce the appropriate value of  $\Delta T$  [ $T$  in the figure]. Hence, one can employ Morrison’s data (which essentially yield the  $Z$  curve) and the Spencer-Jones tidal acceleration for the  $F$  curve to produce the equivalent  $\Delta T$  values for the Spencer-Jones model but using the raw data of Morrison. The algorithm for calculating  $\Delta T$  from Morrison’s data for arbitrary  $\dot{n}_{\text{Moon}}$  is

$$\Delta T(\dot{n}_{\text{Moon}}) = \Delta T_{\text{Morrison}} - 0^s.911 (\dot{n}_{\text{Moon}} + 26''.0) T^2 \quad (1)$$

where  $\dot{n}_{\text{Moon}}$  is measured in arcsec/cy<sup>2</sup> and where  $T$  is measured in centuries from 1955.5. For the Spencer-Jones tidal acceleration of  $\dot{n}_{\text{Moon}} = -22''.44$  the correction to Morrison’s values of  $\Delta T$  is  $-3^s.24 T^2$ . There is no correction after 1955.5 since those values are based upon atomic time measurements and in that

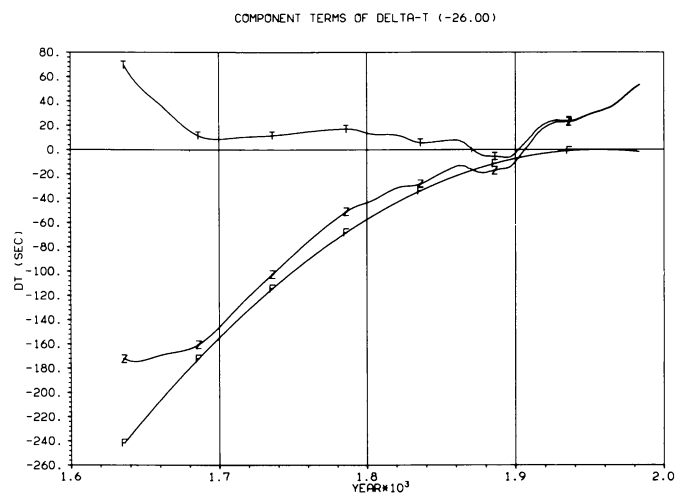


Fig. 2. Components of Morrison’s  $\Delta T$  determination.  $Z$  represents the observed lunar longitude drift in the absence of a tidal acceleration component.  $F$  represents the effect of Morrison’s  $\dot{n}_{\text{Moon}} = -26$  arcsec/cy<sup>2</sup> and  $T = Z - F$  represents the value of  $\Delta T$  for the given  $\dot{n}_{\text{Moon}}$ . All units in the ordinate are expressed in sec while the abscissa contains the year

case there is no intermingling of lunar tidal acceleration effects with determinations of  $\Delta T$ .

The resultant values of  $\Delta T$  are plotted in Fig. 3 using the Spencer-Jones model ( $\dot{n}_{\text{Moon}} = -22''.44$ ) of tidal acceleration of the Moon. In the Supplement paper I present plots of the Morrison versus Brouwer-Martin values reduced to a common lunar tidal acceleration. Essentially, the Morrison data are more smooth than the less-accurate Brouwer-Martin data. In Fig. 4 I present a plot of the difference in  $\Delta T$  values in the sense of  $\Delta T$  based upon the Spencer-Jones model of lunar acceleration ( $\dot{n}_{\text{Moon}} = -22''.44$ ) minus the value of  $\Delta T$  based upon the Morrison model of lunar acceleration ( $\dot{n}_{\text{Moon}} = -26''.0$ ). If the old Galilean eclipse observations clearly prefer one model over the other it should be evident in the residual plots which will be given later. If the Morrison value of  $\dot{n}_{\text{Moon}}$  for tidal acceleration of the Moon as it occurs in values of  $\Delta T$  is better than the Spencer-Jones value, then the satellite eclipse residuals ought to cluster about the curve given in Fig. 4 which would represent the zero-residual curve for the Morrison value of  $\dot{n}_{\text{Moon}}$ .

#### 4. Eclipse residuals

There are currently two accurate ephemerides which recently have been published in the literature and which are useful for analyzing and predicting the positions of the Galilean satellites based upon my 1977 improvement of Sampson’s (1921) theory of their motion. The first set of parameters labeled E-2 was published by Lieske (1980) and was based upon an analysis of 1753 eclipse observations from 1878–1972, together with 85 mutual events from 1973 and with 2964 photographic observations from 1967–78. The other commonly available set of parameters was published by Arlot (1982) and labeled G-5. It resulted from an analysis of 8656 photographic observations from 1891 to 1978.

Since numerous scientists have requested a listing of the series coefficients for ephemerides E-2 and for G-5 in an easily readable form similar to that presented for the original theory (Lieske,

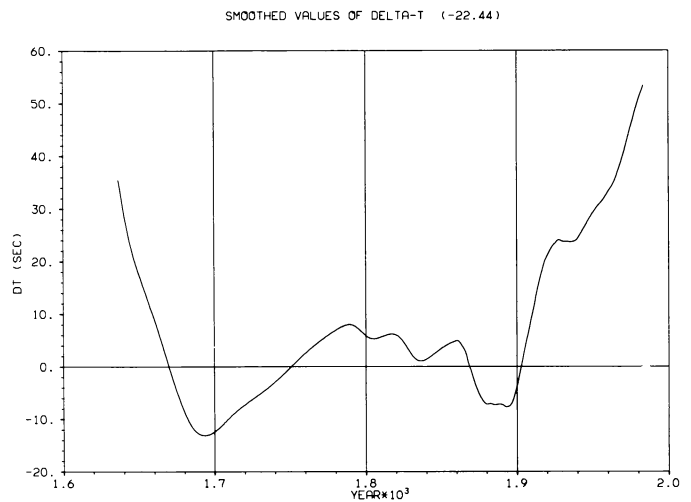
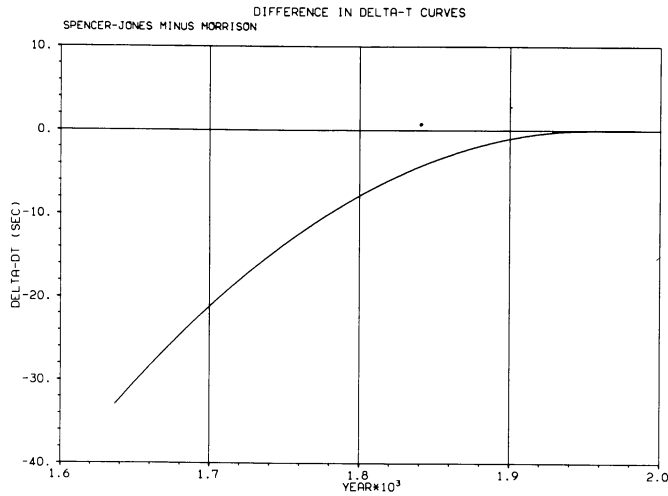


Fig. 3. Plot of  $\Delta T$  from Morrison’s data using the Spencer-Jones values of  $\dot{n}_{\text{Moon}} = -22.44$  arcsec/cy<sup>2</sup>. The curve represents the initially adopted value of  $\Delta T$  for calculation of residuals





**Fig. 4.** The difference between  $\Delta T$  values based upon Spencer-Jones'  $\dot{n}_{\text{moon}} = -22.44 \text{ arcsec/cy}^2$  versus that based upon Morrison's  $\dot{n}_{\text{moon}} = -26 \text{ arcsec/cy}^2$  is plotted as a function of the year. The curve is based upon Morrison's data

1977) in order that they more readily may program the ephemerides on diverse computers, I present the fundamental epsilon-beta parameters for E-2 and for G-5 in Table 3, along with the error estimates originally published by the two authors. See the subsequent discussion for the interpretation of the error estimates. In

Table 4 the series coefficients for the components in radial direction, longitude and latitude are presented for the two ephemerides for all four satellites. The application of these coefficients to the generation of ephemerides is described in the earlier paper by Lieske (1977).

In Arlot's analysis he compares the "error" estimates of E-2 and of G-5 and suggests that G-5 is more accurate than E-2, although the sum-of-squares of residuals for a common set of data which Arlot employs do not differ by much - indicating that the two published estimates for errors are not really comparable. In fact, Lieske's E-2 attempted to give "realistic errors" based upon consideration of non-estimated parameters such as the masses of the satellites and the pole of Jupiter [which had been obtained from Null (1976)] upon the 24 epsilon-beta orbital parameters (which correspond roughly to the 24 arbitrary constants of integration which one must determine in discussing the initial values for 4 satellites) which were estimated. Arlot's stated errors, on the other hand, were the formal errors obtained in estimating only the 24 orbital parameters from his data set. As is evidenced by the closeness in the sum-of-squares which either E-2 or G-5 yields in analyzing a common set of data (viz. that of Arlot), the real error estimates of the two parameter sets must be very similar. Arlot's Table 3 (Arlot, 1982 p. 309) suggests that they differ by less than 0.5%.

Whichever way one wishes to go (either using consideration covariance errors or the formal errors based upon the 24 orbital parameters) the two sets are related approximately by a factor of 3, so that Lieske's E-2 "realistic errors" are about 3 times the

**Table 3.** Theory parameters for E2 (Lieske) and G5 (Arlot)

Epsilon Parameter	E2 value (dimensionless)	G5 value (dimensionless)
1 $\delta m_1$	+0.041590 ± 0.0098	+0.041590
2 $\delta m_2$	-0.002461 ± 0.0200	-0.002461
3 $\delta m_3$	-0.023189 ± 0.0076	-0.023189
4 $\delta m_4$	+0.256938 ± 0.0084	+0.256938
5 $\delta S/J$	(+206.7082138 ± 9.5) · 10 <sup>-6</sup>	+206.7082138 · 10 <sup>-6</sup>
6 $\delta n_1$	(+5.6763 ± 3.69) · 10 <sup>-9</sup>	(-1.835945 ± 0.8513) · 10 <sup>-9</sup>
7 $\delta n_2$	(+10.9655 ± 5.79) · 10 <sup>-9</sup>	(+11.054947 ± 0.5523) · 10 <sup>-9</sup>
8 $\delta n_3$	(-2.44689 ± 2.87) · 10 <sup>-8</sup>	(-5.5560148 ± 0.15354) · 10 <sup>-8</sup>
9 $\lambda_A$	(+11.4663 ± 2.21) · 10 <sup>-4</sup>	(+14.9959 ± 0.86918) · 10 <sup>-4</sup>
10 $\delta n_J$	(+16.2 ± 6.3) · 10 <sup>-6</sup>	+16.2 · 10 <sup>-6</sup>
11 $\delta J_2$	-0.007778 ± 0.00054	-0.007778
12 $\delta J_4$	-0.275934 ± 0.024	-0.275934
13 $\delta R_J$	-0.000308 ± 0.00060	-0.000308
14 $\delta P_J$	(+0.095 ± 2.8) · 10 <sup>-4</sup>	+0.095 · 10 <sup>-4</sup>
15 $\delta S(C-A)/2C$	0. ± 0.15	0.
16 $\delta e_{11}$	-0.793261 ± 0.424	-0.473172 ± 0.098801
17 $\delta e_{22}$	+0.116719 ± 0.266	+0.463707 ± 0.108628
18 $\delta e_{33}$	-0.031160 ± 0.019	-0.043680 ± 0.004671
19 $\delta e_{44}$	-0.005380 ± 0.004	-0.003586 ± 0.000542
20 $\delta e_J$	+0.002781 ± 0.0005	+0.002781
21 $\delta c_{11}$	+0.479780 ± 0.409	+0.492066 ± 0.060640
22 $\delta c_{22}$	+0.001049 ± 0.025	-0.006578 ± 0.002110
23 $\delta c_{33}$	+0.041111 ± 0.049	+0.050194 ± 0.003248
24 $\delta c_{44}$	-0.066572 ± 0.109	-0.070668 ± 0.001315
25 $\delta J_J$	+0.005384 ± 0.011	+0.005384
26 $\delta J$	-0.000133 ± 0.00011	-0.000133
27 $\delta e$	0. ± 4.7 · 10 <sup>-6</sup>	0.
28 $\delta n_S$	0. ± 1.0 · 10 <sup>-6</sup>	0.
Beta Parameter	E2 value (deg)	G5 value (deg)
1 $\Delta \epsilon_1$	+0.048170 ± 0.0176	+0.046245 ± 0.004819
2 $\Delta \epsilon_2$	-0.013693 ± 0.0039	-0.014445 ± 0.000877
3 $\Delta \epsilon_3$	[-0.0446245	-0.0447900]
4 $\Delta \epsilon_4$	-0.062787 ± 0.0049	-0.066536 ± 0.000443
5 $\Delta \phi_1$	+184.415351 ± 20.3	+182.797225 ± 0.005084
6 $\Delta \pi_1$	+77.868511 ± 73.8	+62.231560 ± 7.608520
7 $\Delta \pi_2$	+54.429883 ± 15.5	+86.403965 ± 4.320290
8 $\Delta \pi_3$	+12.691861 ± 0.92	+14.181513 ± 0.236000
9 $\Delta \pi_4$	-0.717416 ± 0.13	-0.747260 ± 0.028121
10 $\Delta \Pi_J$	+0.166755 ± 0.05	+0.166755
11 $\Delta \omega_1$	+65.628689 ± 18.5	+60.834877 ± 3.490252
12 $\Delta \omega_2$	+8.153378 ± 1.1	+6.075500 ± 0.125467
13 $\Delta \omega_3$	-6.237802 ± 2.5	-5.450563 ± 0.210661
14 $\Delta \omega_4$	+4.854064 ± 2.4	+4.903778 ± 0.077832
15 $\Delta \psi$	-0.233589 ± 0.19	-0.233589
16 $\Delta G'$	0. ± 0.4	0.

**Table 8.** Continued

Beta Parameter	E2 value (deg)	G5 value (deg)			
17 $\Delta G$	-0.140391 ± 0.03	-0.140391			
18 $\Delta \phi_1$	+15.610 ± 3.1	+15.610			
19 $\Delta \phi_2$	+5.135 ± 4.2	+5.135			
20 $\Delta \phi_3$	-1.719 ± 2.1	-1.719			
21 $\Delta \phi_4$	-7.784 ± 1.8	-7.784			
22 $\Delta \Omega_J$	+0.044280 ± 0.007	+0.044280			
Index	E2 angle (deg)	G5 Angle (deg)	E2 rate (deg/day)	G5 rate (deg/day)	
1 $\epsilon_1$	106.078590000	106.076665000	203.4889553630643	203.4889538344055	
2 $\epsilon_2$	175.733787000	175.733035000	101.3747245566245	101.3747245669222	
3 $\epsilon_3$	120.561385500	120.561220000	50.31760915340462	50.31760993133556	
4 $\epsilon_4$	84.455823000	84.452074000	21.57107087517961	21.57107020450808	
5 $\phi_1$	184.415351000	182.797225000	0.17356902	0.17354439	
6 $\pi_1$	82.380231000	66.743280000	0.16102275	0.16075291	
7 $\pi_2$	128.960393000	160.934475000	0.04645644	0.04681876	
8 $\pi_3$	187.550171000	189.039823000	0.00712408	0.00712296	
9 $\pi_4$	335.309254000	335.279410000	0.00183939	0.00183940	
10 $\Pi_J$	13.470395000	13.470395000	0.	0.	
11 $\omega_1$	308.365749000	303.571937000	-0.13280610	-0.13280633	
12 $\omega_2$	100.438938000	101.361060000	-0.03261535	-0.03261574	
13 $\omega_3$	118.908928000	119.696167000	-0.00717678	-0.00717675	
14 $\omega_4$	322.746564000	322.796278000	-0.00176018	-0.00176018	
15 $\psi$	316.500101000	316.500101000	-2.480 · 10 <sup>-6</sup>	-2.480 · 10 <sup>-6</sup>	
16 $G'$	31.9785280244	31.9785280244	0.033459733896	0.033459733896	
17 $G$	30.2380210168	30.2380210168	0.08309256178969453	0.08309256178969453	
18 $\phi_1$	188.443270647	188.443270647	0.	0.	
19 $\phi_2$	52.1445966929	52.1445966929	0.	0.	
20 $\phi_3$	257.461000000	257.461000000	0.	0.	
21 $\phi_4$	149.336611731	149.336611731	0.	0.	
22 $\Omega_J$	99.997540000	99.997540000	0.	0.	
$a_1$	2.819347 · 10 <sup>-3</sup> a.u.	2.819347 · 10 <sup>-3</sup> a.u.			
$a_2$	4.485872 · 10 <sup>-3</sup> a.u.	4.485873 · 10 <sup>-3</sup> a.u.			
$a_3$	7.155352 · 10 <sup>-3</sup> a.u.	7.155352 · 10 <sup>-3</sup> a.u.			
$a_4$	1.2585436 · 10 <sup>-2</sup> a.u.	1.2585438 · 10 <sup>-2</sup> a.u.			
Substitution Values for E2+. [Otherwise identical with E2]					
Parameter	Value for E2+	Parameter	Value for E2+	Parameter	Value for E2+
$\epsilon_8$	-7.8066 · 10 <sup>-9</sup>	$\epsilon_{10}$	-5.417 · 10 <sup>-9</sup>	$\beta_4$	-0.06449
$\epsilon_4$	84.45412	$n_4$	21.57107123460327	$a_4$	1.2585435 · 10 <sup>-2</sup> a.u.
$v_1$	#14 -5595	$\pi_3 - \pi_4$			
$v_2$	#35 +3450	$\epsilon_2 - \pi_4$			
$\epsilon_3$	#7 -7893	$\epsilon_3 - \pi_4$	$v_3$	#35 +15799	$\epsilon_3 - \pi_4$
$\epsilon_4$	#9 -73326	$\epsilon_4 - \pi_4$	$v_4$	#41 +146668	$\epsilon_4 - \pi_4$





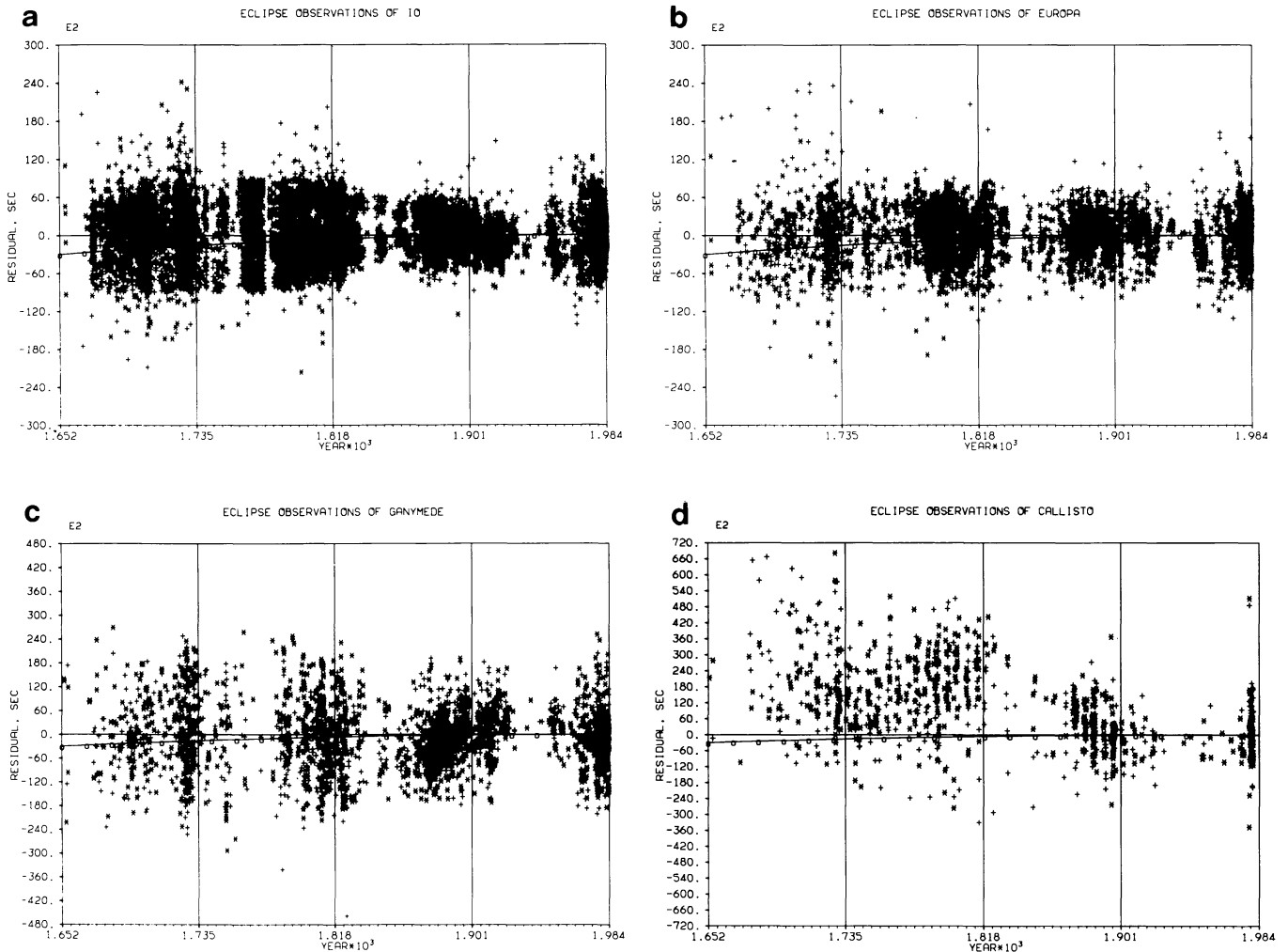
“formal” error in Arlot’s G-5. It should be pointed out, however, that the formal error given by Arlot for the phase of the libration ( $\Delta\beta_5$  in the theory) almost certainly is incorrect and should probably be interpreted as the error in  $\varepsilon_9 \Delta\beta_5$ , since Arlot (using Lieske’s software) undoubtedly employed the partial derivative with respect to  $\varepsilon_9 \Delta\beta_5$  rather than simply the partial derivative with respect to  $\Delta\beta_5$  alone.

At any rate, the only reliable way to compare two sets of predictions is to evaluate them with a common set of data. Arlot has performed such a comparison using photographic data and, as noted above, there is very little difference between the two ephemerides if one ignores Arlot’s “error estimate” comparison and relies on the more meaningful difference in sum-of-squares of residuals for the common set of data.

In order to demonstrate the long-term comparison of the two sets of parameters E-2 and G-5, I have calculated the Observed minus Calculated times of observation for the collection of eclipses which is the subject of this paper. I have adopted the Spencer-Jones value for lunar tidal acceleration of  $\dot{n}_{\text{Moon}} =$

$-22''.44$  in reducing Morrison’s values of  $\Delta T$  to the Spencer-Jones standard in relating ET for the predictions and UT for the observations. In the plots I also show the reference line for zero residuals if one adopts Morrison’s value of  $\dot{n}_{\text{Moon}} = -26''.0$  for the lunar acceleration. It should be noted that no adjustment of either the E-2 or of the G-5 parameters has been made, but I have merely “extrapolated” the two ephemerides into epochs where neither had contained any data in the analyses which originally produced E-2 and G-5. In this comparison for the sake of consistency I have employed the same satellite radii as employed in the paper on eclipse predictions (Lieske, 1981) based upon the work of O’Leary and van Flandern (1972) for the radius of Io (1820 km) and that of Aksnes and Franklin (1976) for the other satellites (1533 km, 2608 km, and 2445 km). Future studies will of course utilize the IAU radii as given by Davies et al. (1983) or its successor.

The residuals for ephemeris E-2 are presented in Fig. 5 for the four satellites. In calculating the positions of Jupiter and of the Earth I have employed the JPL ephemeris DE-102 (Newhall et al.,

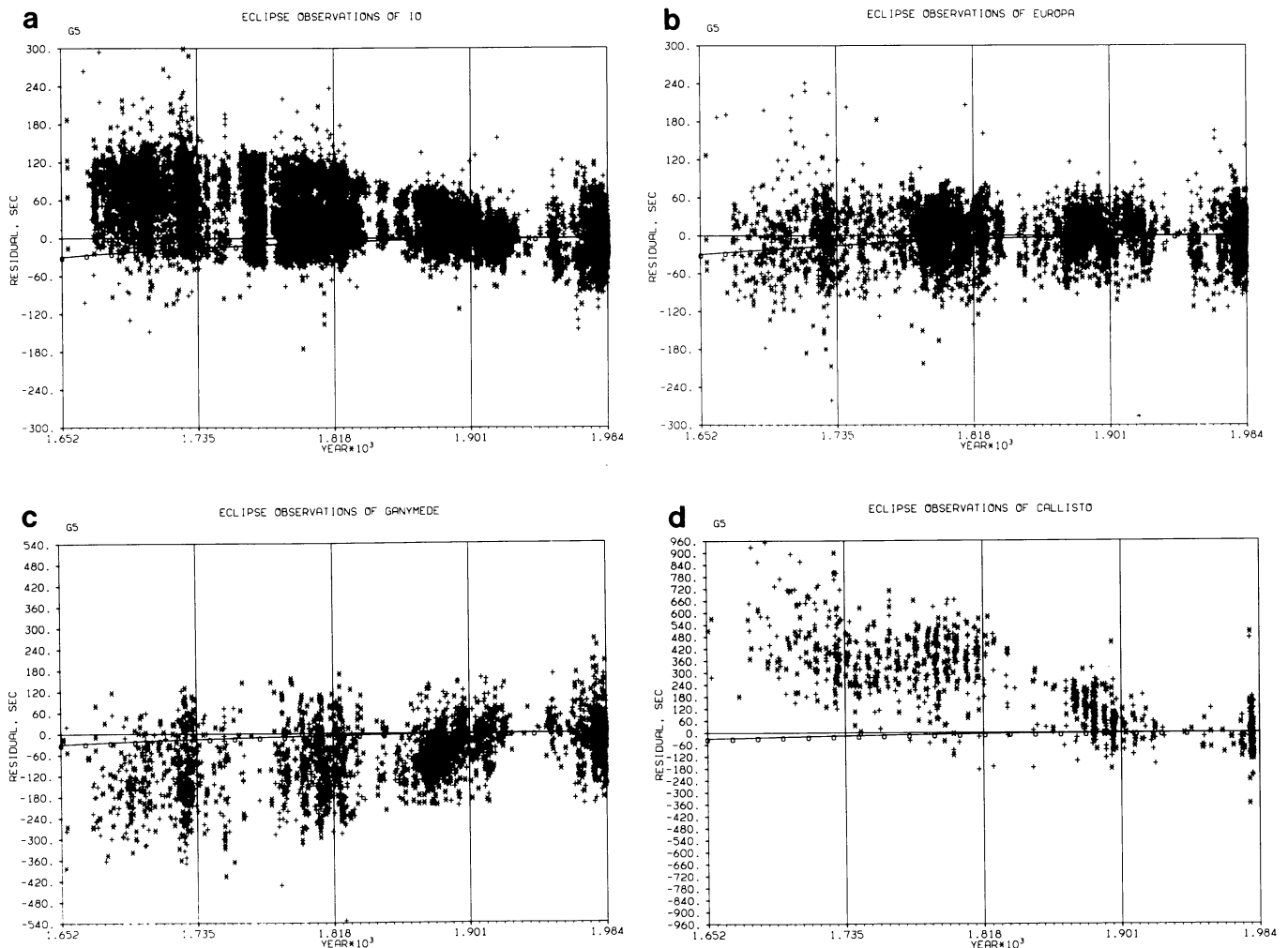


**Fig. 5a–d.** Extrapolated O-C eclipse residuals (for the data contained in the present collection) for Io (a), Europa (b), Ganymede (c), and Callisto (d) in sec as a function of year of observation is plotted for Ephemeris E-2 (Lieske, 1980). The abscissa is based upon Spencer-Jones’  $\dot{n}_{\text{moon}} = -22.44$  in the calculation of  $\Delta T$ . The analogues x-axis of zero residuals for Morrison’s  $\dot{n}_{\text{moon}} = -26$  arcsec/cy<sup>2</sup> is represented by the solid line  $\circ-\circ-\circ$ . No adjustment to the E-2 parameters have been made

1983). The O-C residuals are expressed in seconds of time, and disappearances are represented by an asterisk (\*) while reappearances are represented by a plus sign (+). The reference axis for the ordinate is based upon the Spencer-Jones lunar tidal term of  $\dot{n}_{\text{Moon}} = -22''.44$  in  $\Delta T$ , while the reference axis for zero-residuals for the Morrison and Ward lunar acceleration of  $\dot{n}_{\text{Moon}} = -26''.0$  is depicted as the reference value labeled as a  $\circ-\circ-\circ$  curve. There is some evidence for Satellites I through III that a value for the lunar tidal acceleration should be between the Spencer-Jones (horizontal axis) and the Morrison and Ward ( $\circ-\circ-\circ$ ) values, although the residuals are remarkably flat for over three centuries without any adjustments to the orbital parameters. Satellite IV suggests evidence of a drift in the time prior to the 20th century where no data were employed in generating E-2. The residuals in seconds of time can be converted to approximate longitude residuals (measured in km) by multiplying the time-residuals by the negative of the velocity for each satellite:  $18 \text{ km s}^{-1}$  for Io,  $14 \text{ km s}^{-1}$  for Europa,  $11 \text{ km s}^{-1}$  for Ganymede and  $8 \text{ km s}^{-1}$  for Callisto.

Similar plots for Arlot's G-5 ephemeris (Arlot 1982), whose constants are given in Tables 3 and 4, are presented in Fig. 6. There are more pronounced drifts for the inner three satellites for ephemeris G-5.

The detailed analysis of the data contained in the present collection will be presented in a subsequent paper in which the satellite masses and Jupiter's pole will be estimated with an accuracy comparable to that of the spacecraft-based results of Campbell and Synnott (1985), but for the present study I made an initial investigation of the Satellite IV data and adjusted only the longitude ( $\beta_4$ ), mean motion ( $\varepsilon_8$ ) and eccentricity ( $\varepsilon_{19}$ ) of Satellite IV in order to demonstrate how much of the drift present in Fig. 5 could be attributed to simple orbital effects. The resultant residuals for "E2+" for Callisto are depicted in Fig. 7 with the three changed parameters listed in Table 3. The other satellite residuals do not perceptibly change. Statistics of the graphical representations are given in Table 5. Again, it should be noted (with the exception of E2+) that no adjustments to the E-2 or the G-5 parameters have been made. In the table the maximum, minimum



**Fig. 6a-d.** Extrapolated O-C residuals for the observations contained in the present collection are plotted for Ephemeris G-5 (Arlot, 1982). No adjustment of Arlot's G-5 parameters have been made. As in Fig. 5 the solid curve represents the zero-residual axis for Morrison's  $\dot{n}_{\text{moon}}$  in the calculation of  $\Delta T$ . Time-residuals may be converted to longitude residuals by multiplication of each satellite's speed ( $18 \text{ km s}^{-1}$ ,  $14 \text{ km s}^{-1}$ ,  $11 \text{ km s}^{-1}$ ,  $8 \text{ km s}^{-1}$  for Io through Callisto, respectively)

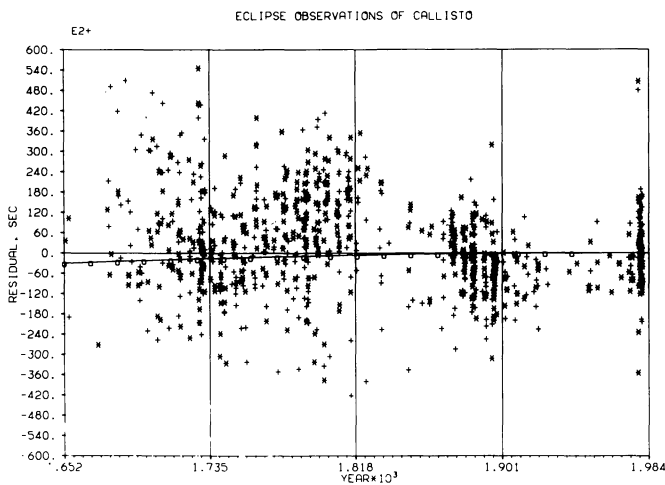


Fig. 7. Graph of Callisto O-C eclipse is plotted in sec of time as a function of year for Ephemeris E2+, which was derived from E-2 by adjusting only the longitude, mean motion and eccentricity of Callisto

Table 5. Statistics for ephemerides E2 (Lieske), G5 (Arlot) and E2+

Satellite	Max	Min	Mean	$\sigma_o$	$\sigma$	N	$\sigma_a$
<b>Io</b>							
E2	242*	-216*	-1*1	44*4	44*4	8502	43*2
G5	299	-175	+31.0	58.0	49.0	8502	43.2
E2+	242	-216	-1.1	44.4	44.4	8502	43.2
<b>Europa</b>							
E2	239	-254	+0.8	42.4	42.4	3966	44.2
G5	241	-261	-1.8	43.0	43.0	3966	44.2
E2+	239	-254	+0.8	42.4	42.4	3966	44.2
<b>Ganymede</b>							
E2	269	-458	-7.0	86.1	85.8	2394	78.4
G5	267	-534	-62.7	115.8	97.3	2394	78.4
E2+	269	-458	-7.0	86.1	85.8	2394	78.4
<b>Callisto</b>							
E2	682	-347	112.1	197.0	162.0	849	124.8
G5	952	-355	247.4	327.9	215.3	849	124.8
E2+	545	-422	24.9	148.8	146.7	849	124.8
<b>All</b>							
E2	682	-458	4.6	68.9	68.7	15711	53.2
G5	952	-534	20.1	100.7	98.6	15711	53.2
E2+	545	-458	-0.1	62.0	62.0	15711	53.2

and mean residuals are given, along with the standard deviation  $\sigma$ , the standard deviation from zero mean  $\sigma_o$ , the number of observations  $N$  and the average apriori uncertainty  $\sigma_a$  (discussed subsequently) for each satellite. The residual plot for Callisto depicted in Fig. 7 still suggests that some of the physical parameters of E-2 (e.g., the pole of Jupiter, the satellite masses, etc.) may need revision – or perhaps that the theory lacks a periodic term or perhaps that it contains one which it should not [such as Term 35 in  $v_4$  of Table 4:  $-6112 \cdot 10^{-7} \sin(\pi_3 - \pi_4)$  with a period of 186 yr].

## 5. Catalog of eclipse observations

The collection of eclipse observations 1652–1983 is more thoroughly described in the Supplement paper, but a sample page from the collection is presented here in Table 6. Each observation is assigned a reference number (NUMBER) and the Gregorian data of observation in a proleptic UT scale is given as YEAR, MONTH, DAY. The apriori uncertainty  $\sigma_a$  of the observation

(SIGMA) is given in Field 5 in sec and is intended to be employed for weighting the individual observations in future analyses. It is to some extent arbitrary and is generally based upon a long series of observations by a given observer so that the weighted sum-of-squares is approximately equal to the number of observations. If a given observer normally observes “last speck” (at the beginning B of an eclipse) or “first speck” (at the end E of an eclipse) for disappearances (D) and reappearances (R), then often if he describes the observing conditions as being poor, his disappearances will be interpreted as D-times (half-brightness or mid-event for disappearance) and his reappearances will be R-times (half-brightness for reappearance). The suffix to the SIGMA field is either a V (for visual observation) or a P (for photometric). In the sixth field (SAT) the satellite number and type of event (e.g. 1D for a disappearance of Satellite I or 3R for a reappearance of Satellite III) is given.

All observations are reduced to the mid-event or half-brightness time of observation (see Peters, 1975, or Thuillot, 1983) using the  $T_Q$  values given in column 10 and described in an earlier paper (Lieske, 1981).  $T_Q$  represents the amount of time required for a satellite to move a distance equal to its radius in a direction normal to the eclipse cone and is thus approximately the difference in time between the “last speck” (B) and half-brightness time for a disappearance (D) or the difference between the “first speck” (E) and half-brightness time for a reappearance (R). There is some arbitrariness in my allocation: I assumed that an observer observed either the mid-event (D or R) or that he observed the last/first speck (B or E) rather than trying to interpolate to some ideal standard for each observer. If an observer determined the last/first speck at the beginning (B) or end (E) of an eclipse, then I reduced the observed times to the comparable mid-event times for disappearance (D) or reappearance (R). If he observed a mid-event D or R then I made no change in the observed time but inserted in the NOTES column of Field 9 the letter ‘S’ (for “switched”) so that another analyst would be free to apply his own correction if desired.

The seventh field PUB of the table contains the index to the publication reference (see Table 1) and the eighth field LOC contains the index for the observatory site (see Table 2). The 9th field NOTES contains an ‘S’ if the original data were D/R rather than last(B)/first(E) speck reduced to mid-event. It usually is the result of use of a small-aperture telescope or the presence of adverse observing conditions. The NOTES field contains an asterisk (\*) if the data should not be employed in an analysis and is probably due to its being a duplicate (in which case it is marked with an @ symbol) or from the abnormally large residual which probably is a result of a recording error or an misinterpretation of the observing site or method of recording time. If several observations were made for the same event at a single observing site, then they are combined into one pseudo-observation (the letter V plus the number of observations that went into the calculation of the “normal” point appears in Field 9) while the original data are marked as “duplicates” with the notation \*@. The tenth field contains  $T_Q$ , the time in sec required for a satellite to traverse a distance equal to its radius into the eclipse cone. The “last speck” time of observation  $t_B$  at the beginning of an eclipse (B) is related to the half-brightness time of disappearance  $t_D$  by

$$t_B = t_D + T_Q \quad (2)$$

where  $T_Q$  is positive, while the reappearance (R) time of half-brightness  $t_R$  is related to the first speck (E) at the end of an

**Table 6.** Sample page from collection of eclipses  
Galilean satellite data and residuals for ephemerides E2 (Lieske), G5 (Arlot), and E2+

NUMBER	YEAR	MONTH	DAY	SIGMA	PUB	NOTES	T <sub>Q</sub>	E2	G5	E2+	NUMBER	YEAR	MONTH	DAY	SIGMA	PUB	NOTES	T <sub>Q</sub>	E2	G5	E2+	
1	1652	6	27.96845	50V	10	BC RL *S	108	-1641	-1563	-1641	!	51	1668	10	22.92826	50V	10	BA LN S	113	12	85	12
2	1652	9	24.84074	50V	2R	BC RL *S	-120	1401	1397	1401	!	52	1668	10	24.93140	50V	1R	CY TA **	-113	12272	12346	12272
3	1652	10	4.71094	150V	4D	BC RL	349	214	510	36	!	53	1668	10	29.90338	50V	1R	CY TA **	113	-9001	-6928	-9001
4	1652	10	25.71205	150V	3R	BC RL *S	-253	-3491	-3640	-3491	!	54	1668	11	12.92737	105V	3D	AZ LN S	367	83	-70	83
5	1653	4	30.12432	105V	3R	BC RL *S	-241	2743	2547	2743	!	55	1668	11	12.92737	105V	3D	BC PX S	367	83	-70	83
6	1653	5	7.10851	105V	3D	BC RL	241	139	-15	139	!	56	1668	11	20.09403	105V	3D	BC PX S	364	84	-68	84
7	1653	6	13.06137	150V	4D	BC RL *	300	1656	1951	1479	!	57	1668	11	20.09403	105V	3D	AZ LN S	364	84	-68	84
8	1653	6	19.10670	105V	3D	BC RL *	240	135	-19	135	!	58	1669	11	26.92051	50V	1D	AZ LN S	109	28	100	28
9	1653	6	30.02288	150V	4R	BC RL *S	-300	1725	2019	1547	!	59	1669	11	26.92051	50V	1D	BC PX S	109	28	100	28
10	1653	7	17.01353	150V	4R	BC RL *S	-300	21892	22186	21715	!	60	1670	5	31.85989	50V	1R	CY PX	-106	-40	30	-40

eclipse by

$$t_E = t_R + T_Q \tag{3}$$

where  $T_Q$  is negative. The eleventh through thirteenth fields labeled E2, G5 and E2+ contain the O-C residuals (in sec) for ephemerides E-2 (Lieske, 1980), G-5 (Arlot, 1982) and E2+ (noted at the end of Table 3 of this paper).

**6. Conclusions**

The collection of eclipse observations presented here represents the most thoroughly documented series of observations of Jupiter's Galilean satellites extant. The 332-yr series of eclipse observations represents a fairly uniform set of data from which present and future generations of astronomers can draw inferences which could not be derived from any highly accurate local series of data. Although they by themselves do not represent the greatest accuracy currently available, the eclipse observations, by their uniform accuracy and sheer length of time covered, provide one of the most valuable sources of data for studies in the long-term

motion of the satellites. It is hoped that this collection will provide a vital link to the past that will be required of future theories and analyses. Future analyses of these data should provide accuracies for the satellite masses and Jupiter pole parameters which are independent of and rival in accuracy the results of spacecraft-based studies.

*Acknowledgements.* This paper represents the results of one phase of research conducted at the Jet Propulsion Laboratory, California Institute of Technology under contract with the National Aeronautics and Space Administration. The work was initiated while the author was an Alexander von Humboldt Preisträger in Heidelberg in 1980. Most calculations were performed on the Univac 1100/81 at JPL. The data contained in Tables 1-5 were maintained on a microcomputer and typeset on a VAX 11/780 at JPL using the TeX typesetting system developed by D.E. Knuth of Stanford.

I am indebted to L. Morrison of Greenwich who introduced me to the Pingré volume, to A-M. de Narbonne of the Paris Observatory Library who located the Delisle manuscripts for me,

to Joan Gantz of the Mt. Wilson and Las Campanas Library in Pasadena who allowed me to peruse the wealth of astronomical literature in that location, to A. Wittmann of Göttingen who guided me through the University Library in Göttingen and located many old volumes of the Philosophical Transactions and other astronomical works, to L.K. Kristensen of Aarhus who provided me with Danish material on Ole Roemer's observations, to W. Fricke who was my Alexander von Humboldt host in Heidelberg and who provided me with access to the Berliner Astronomisches Jahrbuch, and to D. Pierce of El Camino College in California who in 1974 initially surveyed the literature for observations of the Galilean satellites.

I am grateful for advice and assistance in interpreting various aspects of this research to P. Ahnert of E. Germany, P. Gregorio of Italy, B. Kálmán of Hungary, J. Meeus of Belgium, M. Walch of France, and J.E. Westfall of the Association of Lunar and Planetary Observers. The contributions of amateur astronomers to the modern continuation of observations of eclipses of Jupiter's satellites are immense. Through the coordination of observers by Westfall's ALPO organization and its counterparts in Australia (G. McNamara), New Zealand (B. Loader), Denmark (N. Wieth-Knudsen), E. Germany (D. Büttner), France (S. Debarbat), and Japan (I. Hasegawa), a wealth of modern eclipse observations have been obtained. Additional contributions by U. Bezerra, P. Bretones, O. Correa, and C. Martins of Brazil and W. Owen in California are gratefully acknowledged.

## References

- Aksnes, K., Franklin, F.A.: 1976, *Astron. J.* **81**, 464  
 Arlot, J.-E. 1982, *Astron. Astrophys.* **107**, 305  
 Arlot, J.-E., Morando, B., Thuillot, W.: 1984, *Astron. Astrophys.* **136**, 142  
 Bigourdan, G.: 1897, "Inventaire général et sommaire des manuscrits de la bibliothèque de l'observatoire Paris *Ann. Obs. Paris*" **21**, F1–F60  
 Bigourdan, G.: 1901, *A.-G. Pingré: Annales Célestes du dix-septième siècle*, Gauthier-Villars, Paris  
 Brouwer, D.: 1952, *Astron. J.* **57**, 125–146  
 Campbell, J.K. Synnott, S.P.: 1985, *Astron. J.* **90**, 364–372  
 Davies, M.E., Abalakin, V.K., Lieske, J.H., Seidelmann, P.K., Sinclair, A.T., Sinzi, A.M., Smith, B.A., Tjufflin, Y.S.: 1983, "Report of the IAU Working Group on Cartographic Coordinates and Rotational Elements of the Planets and Satellites: 1982" *Celest. Mech.* **29**, 309  
 Delambre, J.-B.: 1817, *Tables Éliptiques des Satellites de Jupiter*, Paris  
 Goldstein, S.J. Jr: 1975, *Astron. J.* **80**, 532  
 de Lalande, J.J.F.: 1792, *Astronomie*, 3rd ed., Paris  
 Lieske, J.H.: 1977, *Astron. Astrophys.* **56**, 333 [Theory]  
 Lieske, J.H.: 1978, *Astron. Astrophys.* **65**, 83  
 Lieske, J.H.: 1980, *Astron. Astrophys.* **82**, 340 [E-2 ephemeris]  
 Lieske, J.H.: 1981, *Astron. Astrophys. Suppl. Ser.* **44**, 209  
 Lieske, J.H.: 1982, *Celest. Mech.* **26**, 257  
 Lieske, J.H.: 1983, in *Dynamical Trapping and Evolution in the Solar System*, eds. V.V. Markellos, Y. Kozai, Dordrecht: D. Reidel, pp. 51–59  
 Martin, C.F.: 1969, "A Study of the Rate of Rotation of the Earth from Occultations of Stars by the Moon, 1627–1860," Ph.D. Diss. Yale Univ.  
 Morrison, L.V.: 1979a *Monthly Notices Roy. Astron. Soc.* **187**, 41  
 Morrison, L.V.: 1979b *Geophys. J. Roy. Astron. Soc.* **58**, 349  
 Morrison, L.V.: 1980, Personal Communication  
 Morrison, L.V., Stephenson, F.R.: 1981, in *Reference Coordinate Systems for Earth Dynamics*, eds. E. M. Gaposchkin, B. Kolaczek, Dordrecht: D. Reidel, pp. 181–185  
 Morrison, L.V., Ward, C.G.: 1975, *Monthly Notices Roy. Astron. Soc.* **173**, 183  
 Newhall, XX, Standish E.M., Williams, J.G.: 1983, *Astron. Astrophys.* **125**, 150  
 Nielsen, A.V.: 1944, *Ole Romer, en skildring af hans liv or gerning*, Aarhus Observatory  
 Null, G.W.: 1976, *Astron. J.* **81**, 1153  
 O'Leary, B., van Flandern, T.C.: 1972, *Icarus* **19**, 209  
 Peters, C.F.: 1975, *Celes. Mech.* **12**, 99  
 Pierce, D.A.: 1974a, Observations of Jupiter's Satellites EM900-672, JPL  
 Pierce, D.A.: 1974b, *Publ. Astron. Soc. Pacific* **86**, 990  
 Sampson, R.A.: 1909 *Harvard Ann.* **52**, Part 2, 153  
 Sampson, R.A.: 1910, *Mem. Roy. Astron. Soc.* **58**  
 Sampson, R.A.: 1921, *Mem. Roy. Astron. Soc.* **63** [Sampson Theory]  
 Smart, W.M.: 1931, *Textbook on Spherical Astronomy* (5th Ed. 1962), Cambridge U. Press  
 Spencer Jones, H.: 1939, *Monthly Notices Roy. Astron. Soc.* **99**, 541–558  
 Tisserand, F.: 1896, *Traité de Mécanique Céleste*, Gauthier-Villars, Paris 4  
 Thuillot, W.: 1983, *Astron. Astrophys.* **127**, 63  
 Yoder, C.F., Peale, S.J.: 1981, *Icarus* **47**, 1  
 ———: 1980, *The Times Atlas of the World*, Comprehensive Edition, London: Times Books