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No. 41. THE PROPER MOTION AND THE DISTANCE OF THE PRAESEPE CLUSTER,
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THE PROPER MOTION AND THE DISTANCE OF THE PRAESEPE CLUSTER.

Our knowledge of the structure of the Milky Way system is limited mainly on account of a lack of knowledge of the distances of the stars. This difficulty is caused by the position of the Sun within this system; it does not exist in an investigation of the local clusters: all objects are at the same distance from the Sun and it is thus possible to find out the relative frequencies of stars of determined absolute magnitude and spectral class etc., if we know which stars are members of the group.

1. Introduction and Summary.

This paper deals with the Praesepe-cluster ($\alpha = 8^{\text{h}}34^{\text{m}}39^{\text{s}}$, $\delta = +20^{\circ}1'$). This is a stargroup of 4° to 5° in diameter, probably cosmically related to the Hyades. The brightness of the stars varies between the limit of naked-eye visibility to at least the eighteenth magnitude. The first attempt to distinguish the fainter members of the group from the backgroundstars by means of the proper motions was made by VAN RHIJN¹⁾, ten years ago. The result was negative. The investigation is repeated in this paper with more material.

The photographic plates have been furnished at the request of Prof. Dr. P. J. VAN RHIJN by several observatories, summarised in the tables 1 and 2. The writer is greatly indebted to the Directors of these observatories for their kindness in repeating the early plates and sending them, together with the new ones, to the Kapteyn Laboratory for measurement.

The results in this paper may be summarised as follows:

The proper motions of about 600 stars have been derived with a probable error of $0''.0015$ to $m = 13$, but a magnitude error has weakened the result. 200 Stars belonging to the cluster have been found. Group stars occur to the limit of the plates ($m = 18.0$). The brighter stars are more concentrated towards the centre and they cover a smaller area than the fainter ones. The brighter part of the cluster is elongated in a direction parallel to the Milky Way.

The proper motion of the group is $0''.037$ in the position angle 249° . The distance is found to be 137 parsecs ($\pi = 0''.0073$).

The distribution of the absolute photographic magnitudes of the Praesepe stars has been compared with the distribution of the absolute photographic magnitudes in the neighbourhood of the Sun up to $M = m + 5 \log \pi = +7$. The two curves are similar except that the number of bright stars is larger in the cluster. The spectral types A, F, G and K have also been treated separately up to $M = +0.5$.

Finally the velocity of the cluster through space appears to be nearly equal and parallel to that of the Hyades, only the position angles of the proper motions being somewhat discordant ($8^{\circ} = 2\frac{1}{2} \times$ probable error).

¹⁾ *Groningen Publications* 26, 1916.

CHAPTER I.

2. The material. The material discussed in this paper has been summarised in table 1. The meaning of the columns will appear from their headings. Both the new plates of pair VI have been measured; similarly the two early plates of pair VIII. Table 2 gives a list of the plates which have been partly measured; they will be discussed in section 8.

TABLE I. LIST OF THE COMPLETELY MEASURED PLATES.

Pair	Observatory	Numb. of plate	Epoch	Mean. Sid. Time	Numb. of images	Exp Time	Lim. Ph. Magn.	Measured area. sq. degr.	1 mm ~
I	Pulkowo	F 3	11 Mar. 1894	h m 7 37	1	m 25	14	2.8	60
		C 78	11 Mar. 1923	7 23		28			
II	Greenwich	1972	10 Apr. 1894	9 52	1	40	14	2.8	60
		9266	23 Jan. 1923	9 26		40			
VI	Greenwich	1973	10 Apr. 1894	10 20	2	6, 3	11.5	2.8	60
		9277	8 Feb. 1923	8 41		4 $\frac{1}{2}$, 2			
		9280	17 Mar. 1923	8 44		6, 3			
VIII	Stockholm	331	13 Mar. 1899	9 8	1	24	12	2.2	87
		339	23 Mar. 1900	11 37		30			
		1915	9 Apr. 1923	12 15		15			
X	Helsingfors	2	3 Feb. 1891		1	20	12.5	2.8	60
		3	21 Feb. 1923			20			
XII	Radcliffe	235	26 Mar. 1909	9 44	2	20	14	1.5	29
		920	12 Mar. 1924	9 45		15			
XIII	Radcliffe	234	26 Mar. 1909	8 45	2	20	14	1.5	29
		918	4 Mar. 1924	8 48		15			
XIV	Radcliffe	231	19 Feb. 1909	7 38	2	20	13.5	1.5	29
		886	17 Mar. 1923	7 37		15			
XV	Radcliffe	68	31 Mar. 1905	9 49	3	5	13	1.5	29
		923	1 Apr. 1924	9 52		4			
XVI	Radcliffe	66	30 Mar. 1905	10 5	3	5	13	1.5	29
		922	31 Mar. 1924	10 5		4			
XVII	Lick	43	15 Jan. 1902	8 9	1	123	18	0.5	39
		4300	13 Apr. 1923	10 46		90			
A	Potsdam	55	17 Apr. 1893	11 20	1	60	14	2.8	60
		690	10 Apr. 1915	11 23		60			

The centre of the plates, Nr. XVII excepted, is $\alpha_{1900} = 8^{\text{h}}34^{\text{m}}39^{\text{s}}$, $\delta_{1900} = +20^{\circ}1'0''$; the centre of Nr. XVII is $8^{\text{h}}34^{\text{m}}19^{\text{s}}$, $+20^{\circ}15'5''$.

TABLE 2. LIST OF INCOMPLETELY MEASURED PLATES.

Pair	Observatory	Number of plate.	Epoch	Mean Sid. Time		Exp. Time	1 mm ~
				h m	m		
1	Radcliffe	114	22 Mar. 1906	9	16	10	"
		981	30 Mar. 1926	9	25	10	29
2	Radcliffe	119	29 Mar. 1906	9	29	5	29
		986	12 Apr. 1926	9	34	3	
3	Radcliffe	120	29 Mar. 1906	9	41	5	29
		982	30 Mar. 1926	9	41	3	
4	Radcliffe	121	29 Mar. 1906	9	56	5	29
		983	30 Mar. 1926	9	56	3	
5	Radcliffe	122	29 Mar. 1906	10	11	5	29
		984	9 Apr. 1926	10	10	3	
6	Yerkes	110	30 Nov. 1909	8	40	60	11
		6381	1 Apr. 1924	8	40	60	
7	Allegheny	1379	1 Mar. 1915	8	42	4, 4	15
		32302	15 Mar. 1924	8	50	4½, 1½	
8	Dearborn	A 31	5 Febr. 1913	0	50	12, 12	30
		A 5553	16 Mar. 1923	0	48		

All the plates except the pair A have been measured by the writer on the 3. The measurements. Repsold measuring machine. This instrument has been described at length by VAN DE SANDE BAKHUYZEN; I therefore refer to his paper ¹⁾ on the subject.

The measurements of the pair A have been taken from *Groningen Publications* 26 pages T1 to 11; they are rediscussed here.

If the plate of the new epoch has been exposed through the glass, the early and the new plate are put together, film against film, in the measuring machine. The distance between both images of the same star is then measured directly. This applies to the plates from the Radcliffe, Lick, Potsdam and Helsingfors observatories. In all other cases, the plate of the new epoch not being exposed through the glass, each plate has been measured separately with reference to the division lines of the scale.

The first method has been fully explained in *Gron. Publ.* 19 page 6, the second one in *Gron. Publ.* 25 page 7.

The plates are measured in two positions differing 90°. Only the plates X and A have been measured in four positions.

¹⁾ Bulletin de la Carte du Ciel 1, 169, 1892.

The rectangular coordinates of the stars, x and y , have been taken from *Gron. Publ. 26*; they are expressed in minutes of arc; x is the coordinate in the direction of increasing right ascension, y in the direction of increasing declination. A new Durchmusterung has been prepared for plate XVII, because it contains stars fainter than the limiting magnitude of *Gron. Publ. 26*.

- (1) The maximum measured area is a circle with a diameter 110' around the star BD + 20° 2166 = Boss 2310. The area of each plate separately has been given in table 1.

In the course of this investigation it appeared that the cluster covers a larger area than had been measured. The total area of the plates I and II has therefore been investigated after the regular measurements. The resulting proper motions are not printed in this paper; the group stars only have been picked out and are given in section 7.

The stability of the plate during the measurements has been tested by remeasuring two stars each morning. The differences in these measures can always be explained by a normal error of pointing.

The micrometer used has been described in *Gron. Publ. 19*, 10; the run of the screw is such that 1 revolution corresponds nearly to 0.1 mm on the plate.

4. The Reductions. The method of computing the annual proper motions from the measured quantities is well known. ¹⁾ I need not repeat it here in detail. The following may suffice:

The plate constants have been determined from a certain number of suitably chosen stars. These reduction-stars are the faintest stars with good images and small proper motion, uniformly distributed over the plate and not belonging to the Praesepe-cluster. Their number is at least 80 to 100. Six plate-constants have always been computed in both coordinates. They are a constant term and the coefficients of the terms x , y , x^2 , xy and y^2 . The reduction-stars have been chosen between the limits of magnitude and proper motion given in table 3.

I consider it necessary, if quadratic terms are taken into account, to have as large a number as 80 to 100 reduction-stars. Moreover the stars ought to be uniformly distributed over the plate. If for instance, to take an extreme case, all the stars lie at the same distance from the centre, or lie on a diagonal of the plate, it is impossible to compute 6 constants; the normal equations are not independent of one another in these cases. ²⁾

¹⁾ See e. g. *Groningen Publications* 26, 1917.

²⁾ Cf. JACKSON, *Monthly Notices* 84, 1924.

TABLE 3. LIMITS OF MAGNITUDE AND PROPER MOTION OF THE REDUCTION-STARS.

Plate.	Phot. magn.	μ_x and μ_y .
I and II	10.6 to 13.6	± 0.020
VI	8.0 to 10.8	group-stars
VIII and X	10.6 to 12.8	± 0.025
XII and XIV	10.8 to 13.7	± 0.020
XIII	10.8 to 13.5	± 0.025
XV and XVI	10.6 to 13.3	± 0.020
A	10.6 to 13.5	± 0.025
XVII	15.0 to 17.5	± 0.020

In the case of plate VI the constants have been determined from the group-stars, the other stars being too small in number.

A certain number of stars certainly not belonging to the cluster have been picked out by means of a preliminary reduction of plate I. They have been used for the reduction of all plates except nr. VI and nr. XVII. This latter plate contains much fainter stars than the other ones; a preliminary reduction with linear terms has been sufficient to choose a set of reduction-stars.

The right-ascension and declination of the stars, occurring in *Gron. Publ. 26* 5. Spherical Coordinates. have been taken from that publication; for the other stars, the coordinates have been computed by means of the same formulae as have been used there. The equinox is that of the year 1900.

Photographic magnitudes derived from estimates of the diameters of the star 6. The magnitudes. images are given in *Gron. Publ. 26*. The standard magnitudes were taken from an investigation by HERTZSPRUNG¹⁾.


Later on HERTZSPRUNG²⁾ has published more accurate values, the differences with the first set being however very small. The later magnitudes have been adopted. They have been determined by means of the Halbgitter and Objectivgitter methods, the zero point being taken in accordance with the Göttinger Actinometrie. The scale is therefore identical with that of Mt. Wilson³⁾.

¹⁾ *Astronomische Nachrichten* 203, 261, 1916.

²⁾ *Astronomische Nachrichten* 205, 71, 1917.

³⁾ Seares (*Transactions of the International Astronomical Union*, Vol. 1, 78, 1922) finds by a direct comparison of the Mt. Wilson and Göttingen magnitudes a possible zero-correction of $+0.05$ to the latter. An indirect comparison between the two scales by means of Harvard Circular 170 gives the value -0.03 .

The probable error of a magnitude, derived from the diameters amounts to ± 0.12 . SCHILT¹⁾ has developed a method, that gives a higher accuracy. The principle is as follows: the image of a small circular lens is formed on the photographic plate. The image of a star on the plate is brought to the centre of the circular bright spot projected on the plate by the illuminated lens; the darker the image of the star, the smaller will be the fraction of the light transmitted by the photographic plate. This fraction is measured by means of a thermocurrent. The reading of the galvanometer, which indicates the intensity of this current, is thus a measure of the photographic magnitude of the star.

SCHILT finds that the relation between the galvanometer values and the magnitudes is very nearly a linear one. The curves for the Praesepe plates are less straight, they have the form: . This means that the sensitiveness of the method increases from the brighter stars to a maximum and then decreases to practically zero for the very faintest stars.

I also find that there is a systematic correction depending on the distance from the centre of the plate. This is a serious difficulty, if the standard-magnitudes are not distributed over the whole plate. This is the reason why the magnitudes of the stars outside HERTZSPRUNG's field (distances 30' to 55') have less weight than the other stars (distance 0' to 30').

TABLE 4. PLATES MEASURED WITH THE MICRO-PHOTOMETER.

Nr. of Plate.	Observatory.	Date.
C 78	Pulkowo	11 — 3 — 1923
9266	Greenwich	23 — 1 — 1923
4300	Lick	13 — 4 — 1923

The plates have been pressed against a thick plate-glass in order to eliminate the influence of the curvature of the plate on the galvanometer readings, which are very sensitive to changes in focus.

The plates have been measured in the following way. The image of a star is brought into the field of the microscope; the light-beam is admitted and the galvanometer is read. Then the film near the star image is brought into the field and the galvanometer is read again. The quotient of the two readings is the galvanometer value so called.

Before and after the regular measurements the galvanometer values of the

¹⁾ *Groningen Publications* 32, 1924.

same eight stars have been determined to test the constancy of the measures. The galvanometer has been read also repeatedly for a definite point of the film.

It appeared that none of these quantities remained completely constant; especially if the measurements lasted more than one day. The variations of the reading of the film are of no consequence. From the galvanometer-values of the standard-stars corrections have been derived, by means of which the measurements of each day have been reduced to a common standard.

The corrected galvanometer-values have been plotted against HERTZSPRUNG's photographic magnitudes. Two curves have been derived in the case of plate C 78, one for the stars lying at distances $0'$ to $15'$, another for the stars at distances larger than $15'$ from the centre of the plate. In the case of the plates 9266 and 4300 three groups of stars have been formed, corresponding to the distances $0'$ to $10'$, $10'$ to $20'$, $> 20'$ and $0' - 15'$, $15' - 25'$, $> 25'$ respectively.

The two curves of plate C 78 are identical for the fainter part (galvanometer-values '600 to 1'000). The magnitudes of all stars, whatever their distance from the centre, have been read from this part of the curve. For the brighter stars a distance correction has been derived, amounting to $0^m.35$ as maximum. This correction has been applied only to the stars inside a circle of $30'$; the magnitudes of the stars outside HERTZSPRUNG's area have not been determined from this plate.

The three curves of plate 9266 are identical for all magnitudes. It has been assumed that the distance-correction is zero also for the stars at distances exceeding $30'$; the magnitudes of all the stars on the plate have been determined.

In the case of plate 4300, there is some difference between the three curves, depending on the distance. As however no stars occur on this plate at distances exceeding $35'$, no extrapolation is needed. The magnitudes of all stars are read from one of the curves.

The plates C 78 and 9266 cover the same magnitude interval. From the differences the probable error of one magnitude, derived from one plate, can therefore be computed. It is $0^m.06$.

There is also a systematic difference between the two plates. For the inner stars it is zero, as might be expected a priori, but for the stars lying at distances $30'$ to $55'$ it is about $0^m.23$; I therefore did not succeed in eliminating the distance-error for these larger distances.

The final magnitudes, printed in the catalogue are the mean of the magnitudes of *Gron. Publ. 26*, if found there, and those derived here; the weights being 1 and 3 respectively.

The cluster-stars are distinguished from the background-stars by means of 7a. Cluster-stars up to $m = 14$.
the proper motion. For this purpose the relative proper motions, as derived in

section 4, are plotted in a diagram for each plate separately, three or more groups being formed according to the magnitude. The motion of the cluster is clearly shown in each diagram. It consists in a condensation of points in the third quadrant (μ_x and μ_y negative), more or less separated from the other points. The stars, forming this condensation will be called the group-stars. They have been selected from the diagrams of each plate separately. A comparison of the different plates shows that the mutual agreement is very good; there are only 3 stars left, out of the 162, of which it is doubtful whether they belong to the cluster.

On two plates, nrs. I and II, cluster-stars have been sought for outside the regularly measured area (1) between the limits: $\alpha = 8^h 30^m 7^s$ and $8^h 39^m 11^s$, (2) $\delta = +18^\circ 52'5$ and $20^\circ 58'5$. The proper motions of this region have been treated in a similar way to the proper motions of the inner area. The results from both plates agree well. Twenty-six groupstars have been found up to the magnitude 13.0. Groupstars fainter than this limit could not to be distinguished from the backgroundstars. Seven stars of the twenty six are considered doubtful

Table 5 gives the cluster-stars; the doubtful cases are denoted by an asterisk. The numbers of the stars of the originally measured area, being always less than 532, are those of the catalogue, pages 42 to 47. The other 26 stars with numbers 532 to 557 are to be found in the catalogue on page 48.

The table is complete down to the photographic magnitude 13.0 within the limits (2). For the plenitude of the stars between 13.0 and 14.0, occurring within the area (1), see section 11.

A star, which really does not belong to Praesepe, may have nearly the same proper motion as the cluster-stars and may therefore have been inserted in table 5. The probability however, is very small. It is true that the angle between the direction towards the solar antapex and the direction of the groupmotion, amounts only to 40° , but the mean parallactic motion of the fainter stars ($m > 11$) is less than 25% of the group motion and the brighter stars do not occur in any considerable number. The table by SEARES and VAN RHIJN¹⁾ gives 9 backgroundstars per 2.8 square degrees, brighter than the tenth magnitude, whereas I have found 8 such stars.

Moreover it will be seen from figure 2, which represents a diagram of the proper motions of the catalogue, that there is a clear gap between the groupstars and the other objects. This also shows that non-cluster stars probably do not occur between the cluster stars.

I have estimated that, apart from the doubtful cases, the probability of a star of table 5 being in reality a backgroundstar, is of the order 10^{-2} .

¹⁾ *Mt. Wilson Contributions* 301, 1925.

TABLE 5. LIST OF 188 STARS BELONGING TO THE PRAESEPE-CLUSTER, BRIGHTER THAN THE FOURTEENTH MAGNITUDE.

No.	Phot. Magn.	Spec-trum.	No.	Phot. Magn.	Spec-trum.	No.	Phot. Magn.	Spec-trum.	No.	Phot. Magn.	Spec-trum.	No.	Phot. Magn.	No.	Phot. Magn.
300	6.33	A2	292	8.45	A6	250	9.91	F7	49	10.85		368	11.73	514	12.60
265	6.46	A0	143	8.51	A2	472	9.91	F3	508	10.87	G	336	11.81	52	12.62
204	6.70	F0	340	8.56	A4	31	9.92	F8	288	10.90	G0	304	11.84	474	12.64
284	6.76	F0	318	8.60	A3	268	9.92	F9	196	10.92	G	476	11.86	313	12.65
328	7.08	A5	350	8.67	A5	454	9.96	F8	392	10.92	G5	309	11.89	448	12.66
283	7.10	G5	124	8.76	A8	293	9.97	F8	*555	10.99		297	11.91	417	12.68
348	7.11	A3	271	8.77	A8	47	10.01	F8	322	11.04	G5	403	11.94	*347	12.73
50	7.14	A5	226	9.00	F0	*548	10.06	G5	399	11.06	G	498	11.98	48	12.76
253	7.25	K0	370	9.00	A5	549	10.06	F2	541	11.07	G0	32	11.99	*545	12.76
212	7.26	K0	538	9.14	A0	282	10.06	F7	127	11.10	G2	184	12.04	544	12.77
224	7.34	A0	218	9.19	F2	515	10.06	G0	432	11.14	G	537	12.06	363	12.81
229	7.50	A0	459	9.22	F0	275	10.08	G0	466	11.21	G2	546	12.06	*532	12.92
276	7.54	A0	411	9.33	A9	495	10.08	G2	257	11.27	G	70	12.13	535	12.92
428	7.54	K0	295	9.37	A8	371	10.14	F8	90	11.28		213	12.16	256	12.96
150	7.65	F0	16	9.38	F8	421	10.29	F9	335	11.28	G5	533	12.18	172	12.97
279	7.72	A0	232	9.38	F2	222	10.30	F8	554	11.29	K	542	12.18	141	13.00
286	7.81	A0	146	9.45	F2	238	10.36	F9	334	11.31	G3	263	12.30	183	13.16
207	7.85	A3	142	9.46	F8	258	10.39	G0	301	11.35		*547	12.30	198	13.17
323	8.00	A5	439	9.54	F7	217	10.40	F8	543	11.36		*530	12.32	209	13.22
385	8.01	A3	155	9.55	A7	244	10.42	F8	540	11.40		430	12.34	401	13.23
40	8.02	A0	416	9.58	F5	182	10.45	F8	23	11.43		460	12.40	272	13.31
203	8.02	A3	227	9.60	F5	557	10.46	G3	58	11.43		492	12.41	60	13.36
114	8.07	A5	332	9.63	F2	365	10.48	G2	425	11.43		471	12.43	390	13.38
445	8.10	A3	34	9.65	F6	341	10.49	F8	30	11.46		*550	12.44	237	13.42
449	8.12	A5	496	9.67	F8	287	10.56	F2	488	11.48		236	12.44	415	13.58
*534	8.22	A2	536	9.68	F5	418	10.59	G4	164	11.53		79	12.46	299	13.86
552	8.22	A0	478	9.72	F4	181	10.69	G2	9	11.56		353	12.46	267	13.90
45	8.23	A2	239	9.76	F5	100	10.71	A0	*539	11.58		246	12.47	*93a	14.00
375	8.24	A3	458	9.80	F7	208	10.80	G6	326	11.63		349	12.47		
429	8.34	F0	396	9.84	F5	325	10.81	G0	434	11.64		344	12.48		
154	8.36	A0	553	9.87	F6	162	10.82	G2	27	11.66		456	12.55		
38	8.42	A5	556	9.87	G0	367	10.84	G	55	11.72		551	12.59		

* doubtful.

TABLE 6. TWENTY STARS, BELONGING TO THE CLUSTER,
FAINTER THAN THE FOURTEENTH MAGNITUDE.

Nr.	Phot. magn.	Nr.	Phot. magn.
576	14.07	569	16.15
568	14.33	570	16.37
574	14.43	558	16.65
560	14.70	571	16.71
559	14.99	573	16.99
572	15.10	564	17.12
575	15.26	562	17.16
561	15.41	565	17.25
577	15.71	567	17.68
566	15.97	563	18.07

**7b. Cluster-stars
18 > m > 14.**

The proper motions of the stars fainter than the 14th magnitude have been derived with a larger probable error. Moreover the measured area is one fifth of the maximum area of the other plates (table 1, plate XVII).

The proper motions are again plotted in a diagram for each magnitude separately. It is a little more difficult to distinguish the cluster-stars from the background-stars than in the case of section 7a but the presence of a group motion cannot well be doubted (figure 3). The 20 stars, lying within the dotted line of figure 3, are contained in table 6. The six cluster-stars in common with the other plates ($m = 13.0$ to 14.0) have been found also on this plate.

The absolute proper motion of these faint Praesepe-stars, derived in section 9, is practically identical with that of the stars brighter than the magnitude 14.

**8. The Magnitude
Error.**

The accuracy of the proper motions, derived in this paper is high as far as the accidental errors are concerned. The probable error of the mean of the plates is $0''.0015$ or less, up to the magnitude 12 or 13. It is therefore disappointing to find that a systematic error, of several times the value of this probable error, has vitiated the results. This error depends on the magnitude and will therefore be called magnitude error; this implies however no indication of its cause.

The value of this magnitude error can be determined by three different methods:

First method: the relative proper motions are compared with known meridian proper motions.

Second method: the differences are computed between the theoretical parallax motion of the stars of determined magnitude and the mean relative proper motion of stars of the same magnitude.

Third method: the supposition is made that the mean proper motion of the cluster stars is independent of the magnitude.

The first method is useless in our case. Absolute proper motions of non-group stars are unknown because they are too faint and the range in brightness of the group-stars with known meridian proper motion is too small for the derivation of the magnitude error.

The second method gives better results for the stars fainter than the tenth magnitude. Table 7 contains the quantities: $\Delta\mu_x$ and $\Delta\mu_y$ under the heading: background-stars.

$$\Delta\mu_x = \frac{h}{\varrho} \sin \lambda \sin \chi - \bar{\mu}_x$$

$$\Delta\mu_y = \frac{h}{\varrho} \sin \lambda \cos \chi - \bar{\mu}_y$$

$\bar{\mu}_x$ and $\bar{\mu}_y$ = mean relative proper motion of the background-stars of determined magnitude in the x and y direction respectively.

$\frac{h}{\varrho}$ = parallactic motion taken from table 26 of *Gron Publ.* 29. 1)

λ is the angular distance from the solar antapex

χ is the position angle of the direction towards the solar antapex.

TABLE 7. MAGNITUDE ERROR, DERIVED FROM CLUSTER-STARS AND BACKGROUND-STARS RESPECTIVELY.

Plate-Group.	I, II						VI					
	Group-stars			Background-stars			Group-stars			Background-stars		
Phot. magn.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.
6.0 — 7.0	+ 0"011	+ 0"006	4	- 0"011	- 0"004	8	- 0"034	- 0"005	4	- 0"041	- 0"022	9
7.0 — 8.0	+ 0"007	+ 0"008	14				- 0"034	- 0"007	14			
8.0 — 9.0	0"000	+ 0"008	17				- 0"034	- 0"012	19			
9.0 — 10.0	0"000	0"000	31				- 0"034	- 0"014	30			
10.0 — 11.0	+ 0"001	- 0"002	22	- 0"005	- 0"004	24	- 0"032	- 0"013	23	- 0"041	- 0"010	21
11.0 — 12.0	0"000	- 0"004	27	- 0"003	- 0"004	60	- 0"032	- 0"014	10	- 0"049	- 0"020	13
12.0 — 13.0	- 0"001	- 0"006	25	- 0"004	- 0"004	100						
13.0 — 14.0	0"000	- 0"003	10	- 0"005	- 0"003	156						

1) The parallactic motion used here, is changed very little by applying the correction $+ 0"006 \cos \delta$ to the μ_δ .

TABLE 7. (Continued).

Plate-Group.	VIII						X					
	Group-stars			Background-stars			Group-stars			Background-stars		
	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.
6'0 — 7'0	+ 0"003	+ 0"014	4	} — 0"011 — 0"013 5	} — 0"002 — 0"010 4	} — 0"018 — 0"031 8	+ 0"007	+ 0"018	14	+ 0"002	— 0"008	14
7'0 — 8'0	+ 0"005	+ 0"007	19				— 0"002	— 0"012	19			
8'0 — 9'0	0"000	— 0"008	30				— 0"005	— 0"011	31			
9'0 — 10'0	— 0"001	— 0"008	24				— 0"002	— 0"009	23	— 0"004	— 0"005	24
10'0 — 11'0	— 0"002	— 0"003	25	— 0"001	— 0"007	52	— 0"004	— 0"005	27	— 0"006	— 0"005	57
11'0 — 12'0	— 0"003	— 0"007	18	— 0"007	— 0"003	55	— 0"003	— 0"008	16	— 0"006	— 0"005	59
12'0 — 13'0												
13'0 — 14'0												

TABLE 7. (Continued).

Plate-Group.	XII, XIII, XIV						XV, XVI					
	Group-stars			Background-stars			Group-stars			Background-stars		
	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.
6'0 — 7'0	— 0"018	+ 0"021	4	} — 0"018 + 0"009 12	} — 0"016 + 0"025 4	} — 0"010 + 0"005 11	— 0"023	+ 0"024	13	— 0"015	+ 0"023	13
7'0 — 8'0	— 0"017	+ 0"022	14				— 0"014	+ 0"012	14			
8'0 — 9'0	— 0"011	+ 0"012	21				— 0"006	+ 0"003	21			
9'0 — 10'0	— 0"006	+ 0"004	16				— 0"004	— 0"001	16	— 0"004	— 0"005	28
10'0 — 11'0	— 0"004	— 0"002	15	— 0"004	— 0"004	30	— 0"005	— 0"003	16	— 0"003	— 0"001	43
11'0 — 12'0	— 0"003	— 0"004	14	— 0"004	— 0"005	42	— 0"002	— 0"006	13	— 0"003	— 0"004	17
12'0 — 13'0	— 0"002	— 0"006	10	— 0"003	— 0"008	64	0"000	— 0"008	6			
13'0 — 14'0												

TABLE 7. (Continued).

Plate-Group.	A						All plates, VI excepted.					
	Group-stars			Background-stars			Group-stars			Background-stars		
	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$	Nr.	$\Delta\mu_x$	$\Delta\mu_y$		$\Delta\mu_x$	$\Delta\mu_y$	
6'0 — 7'0	+ 0"036	+ 0"007	4	} + 0"006 — 0"013 8	} — 0"005 + 0"014	} — 0"012 — 0"004	+ 0"026	+ 0"006	14	— 0"007	+ 0"015	
7'0 — 8'0	+ 0"020	+ 0"002	19				— 0"007	+ 0"010				
8'0 — 9'0	+ 0"011	— 0"002	29				— 0"005	+ 0"003				
9'0 — 10'0	+ 0"002	— 0"004	23				+ 0"001	— 0"004	24	— 0"003	— 0"001	
10'0 — 11'0	0"000	— 0"006	27	— 0"002	— 0"007	59	— 0"002	— 0"003		— 0"004	— 0"004	
11'0 — 12'0	— 0"004	— 0"005	25	— 0"007	— 0"003	107	— 0"002	— 0"006		— 0"004	— 0"003	
12'0 — 13'0	— 0"009	0"000	11	— 0"007	— 0"001	157	— 0"002	— 0"005		— 0"004	— 0"004	
13'0 — 14'0												

The result of the third method is given in table 7 under the heading: groupstars.

$$\begin{aligned}\Delta\mu_x &= -0''.034 - \bar{\mu}_x \\ \Delta\mu_y &= -0''.013 - \bar{\mu}_y.\end{aligned}$$

$\bar{\mu}_x$ and $\bar{\mu}_y$ are the mean proper motion of the clusterstars in the x and y direction respectively. The adopted value of the group motion is $-0''.034$ in the x and $-0''.013$ in the y coordinate (section 9).

The agreement between the results of the second and third method is satisfactory except in the case of the stars brighter than the magnitude 10, the number of which is however very small. Some plates have a pretty large magnitude error both in μ_x and in μ_y . The magnitude error in the x coordinate practically disappears, if the mean of the different plates is taken. This is not the case in the y coordinate; nearly all the plates have an error in the same direction; this is more clearly shown in table 8 containing the mean relative proper motion of the group stars. All the plates but Nr. X, indicate that the brighter stars move more rapidly to the south than the fainter ones.

TABLE 8. MEAN RELATIVE PROPER MOTION OF THE GROUP-STARS AS A FUNCTION OF THE MAGNITUDE.

Plate Phot. Magn.	I			II			VI			VIII		
	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.
6 — 7	$-0''.041$	$-0''.024$	4	$-0''.049$	$-0''.014$	4	$0''.000$	$-0''.008$	4	$-0''.036$	$-0''.027$	4
7 — 8	$-0''.039$	$-0''.023$	14	$-0''.043$	$-0''.020$	14	$0''.000$	$-0''.006$	14	$-0''.041$	$-0''.029$	14
8 — 9	$-0''.032$	$-0''.021$	18	$-0''.038$	$-0''.020$	18	$0''.000$	$-0''.001$	19	$-0''.038$	$-0''.020$	19
9 — 9.5	$-0''.028$	$-0''.014$	12	$-0''.038$	$-0''.013$	12	$0''.000$	$+0''.001$	12	$-0''.038$	$-0''.006$	10
9.5 — 10	$-0''.031$	$-0''.010$	19	$-0''.039$	$-0''.015$	19	$0''.000$	$0''.000$	19	$-0''.031$	$-0''.005$	18
10 — 10.5	$-0''.033$	$-0''.011$	10	$-0''.040$	$-0''.015$	10	$-0''.001$	$0''.000$	10	$-0''.032$	$-0''.005$	9
10.5 — 11	$-0''.032$	$-0''.008$	12	$-0''.037$	$-0''.010$	12	$-0''.002$	$+0''.001$	12	$-0''.033$	$-0''.005$	12
11 — 11.5	$-0''.032$	$-0''.008$	17	$-0''.037$	$-0''.010$	17	$-0''.000$	$+0''.002$	11	$-0''.033$	$-0''.009$	15
11.5 — 12	$-0''.035$	$-0''.009$	10	$-0''.032$	$-0''.007$	10	—	—	—	$-0''.032$	$-0''.012$	10
12 — 12.5	$-0''.036$	$-0''.007$	14	$-0''.031$	$-0''.007$	14	—	—	—	$-0''.029$	$-0''.005$	17
12.5 — 13	$-0''.035$	$-0''.008$	11	$-0''.031$	$-0''.006$	11	—	—	—	$-0''.032$	$-0''.007$	5
13 — 13.5	$-0''.035$	$-0''.008$	8	$-0''.034$	$-0''.006$	7	—	—	—	—	—	—
> 13.5	$-0''.033$	$-0''.008$	2	$-0''.034$	$-0''.018$	3	—	—	—	—	—	—

TABLE 8. (Continued).

Plate Phot. Magn.	X			XII			XIII			XIV		
	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.
6 — 7	— 0"031	— 0"003	4	— 0"020	— 0"024	4	— 0"008	— 0"032	4	— 0"020	— 0"047	4
7 — 8	— 036	— 005	14	— 011	— 027	13	— 007	— 037	13	— 015	— 051	13
8 — 9	— 032	— 001	19	— 018	— 027	14	— 010	— 039	14	— 023	— 040	14
9 — 9.5	— 028	— 001	12	— 024	— 021	7	— 019	— 035	6	— 024	— 031	6
9.5 — 10	— 031	— 003	18	— 025	— 018	14	— 022	— 028	14	— 024	— 025	14
10 — 10.5	— 033	— 006	10	— 026	— 018	7	— 027	— 026	7	— 027	— 020	7
10.5 — 11	— 031	— 003	13	— 029	— 011	9	— 031	— 017	9	— 028	— 013	9
11 — 11.5	— 030	— 007	17	— 031	— 008	11	— 032	— 015	11	— 030	— 013	11
11.5 — 12	— 030	— 009	10	— 030	— 012	4	— 033	— 010	4	— 029	— 014	4
12 — 12.5	— 030	— 005	11	— 029	— 008	7	— 031	— 013	7	— 031	— 010	8
12.5 — 13	— 033	— 006	5	— 032	— 009	5	— 034	— 009	5	— 035	— 005	6
13 — 13.5	—	—		— 033	— 006	8	— 034	— 006	8	— 028	— 007	6
> 13.5	—	—		— 030	— 011	2	— 030	— 004	2	—	—	

TABLE 8. (Continued).

Plate Phot. Magn.	XV			XVI			A			Mean of all plates	
	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.	$\bar{\mu}_x$	$\bar{\mu}_y$	Nr.	$\bar{\mu}_x$	$\bar{\mu}_y$
6 — 7	— 0"020	— 0"062	4	— 0"017	— 0"012	4	— 0"071	— 0"020	4	— 0"029	— 0"027
7 — 8	— 021	— 055	13	— 018	— 017	13	— 060	— 019	14	— 027	— 028
8 — 9	— 023	— 036	14	— 019	— 015	13	— 055	— 016	19	— 027	— 023
9 — 9.5	— 027	— 021	6	— 023	— 013	6	— 049	— 011	11	— 028	— 018
9.5 — 10	— 029	— 020	14	— 029	— 013	14	— 042	— 012	18	— 030	— 014
10 — 10.5	— 031	— 016	7	— 027	— 016	7	— 037	— 009	10	— 031	— 015
10.5 — 11	— 031	— 009	9	— 031	— 007	9	— 034	— 008	13	— 032	— 009
11 — 11.5	— 031	— 010	10	— 029	— 011	11	— 034	— 008	17	— 032	— 010
11.5 — 12	— 032	— 009	4	— 029	— 010	4	— 034	— 006	10	— 031 ^b	— 010
12 — 12.5	— 034	— 007	6	— 031	— 008	6	— 032	— 008	14	— 032	— 008
12.5 — 13	— 034	— 005	6	— 034	— 006	5	— 028	— 008	11	— 033	— 007 ^b
13 — 13.5	— 030	— 005	5	— 038	— 006	5	— 024	— 011	8	— 032	— 006 ^b
> 13.5	—	—		—	—		— 027	— 015	3	— 026 3/	— 011

Is this actually the case? I think not, for the following reasons:

1⁰. The magnitude effect is very different for different plates. Take for instance the magnitude 6—7. The mean μ_y varies from — 0"003 to — 0"062, whereas according to Boss' proper motions we should expect something like

— $0''.020$. Part of the magnitude effect at least must therefore be a real error.

2°. Suppose the bright stars have a μ_x differing as much from that of the fainter ones as shown in table 8. The result will be that the cluster cannot exist at all. The fainter stars would have been outdistanced by the brighter ones at a rate of something like 5° in 10^8 years, the proper motion in declination of the bright and faint stars being $-0''.028$ and $-0''.008$ respectively. I find on the contrary in table 17, section 11, that the centre of the cluster is independent of the magnitude.

3°. There are several binaries belonging to the cluster, whose components differ considerably in magnitude. Now let us assume that the sum of the masses of the components $\cong 10 \odot$, the parallax of the cluster = $0''.007$ and the mean distance of the components = d'' ; then the relative proper motion of the two components cannot exceed $0''.016 \cdot d^{-1/2}$. The mean distance d of the binaries of table 9 is about $30''$. Therefore, their mean relative motion must be smaller than $0''.003$.

The relative proper motions actually found are much larger than $0''.003$, and agree almost exactly with the difference between the proper motions of the bright and faint cluster stars of the same brightness. I have investigated this point for each plate separately; in all cases the agreement is very good. See table 9.

TABLE 9. THE MEAN RELATIVE PROPER MOTION OF THE COMPONENTS OF A FEW BINARIES, BELONGING TO THE CLUSTER, COMPARED WITH THE MEAN GROUP MOTION AS DERIVED FROM THE SAME PLATE.

Plate.	Binaries.	$\overline{m}_{\text{phot.}}$	Binaries		Group motion, table 8	
			$\overline{\mu}_x$	$\overline{\mu}_y$	$\overline{\mu}_x$	$\overline{\mu}_y$
I	<i>a, b, c, d, e</i>	7.9	— $0''.039$	— $0''.023$	— $0''.036$	— $0''.022$
		11.8	— $0''.032$	— $0''.008$	— $0''.035$	— $0''.009$
II	<i>a, b, c, d, e</i>	7.9	— $0''.040$	— $0''.021$	— $0''.041$	— $0''.020$
		11.8	— $0''.032$	— $0''.006$	— $0''.032$	— $0''.007$
X	<i>a, b, c, d, e</i>	7.9	— $0''.035$	— $0''.002$	— $0''.034$	— $0''.003$
		11.8	— $0''.035$	— $0''.004$	— $0''.030$	— $0''.009$
XII	<i>a, c, d, e</i>	7.7	— $0''.015$	— $0''.025$	— $0''.012$	— $0''.027$
		11.6	— $0''.032$	— $0''.009$	— $0''.030$	— $0''.011$
XIII	<i>a, c, d, e</i>	7.7	— $0''.004$	— $0''.044$	— $0''.008$	— $0''.037$
		11.6	— $0''.028$	— $0''.015$	— $0''.033$	— $0''.012$
XIV	<i>a, b, c, d</i>	8.0	— $0''.019$	— $0''.048$	— $0''.019$	— $0''.045$
		11.7	— $0''.028$	— $0''.016$	— $0''.029$	— $0''.014$
XV	<i>a, b, c</i>	8.4	— $0''.022$	— $0''.039$	— $0''.023$	— $0''.038$
		12.0	— $0''.034$	— $0''.007$	— $0''.033$	— $0''.008$
XVI	<i>c, d</i>	8.0	— $0''.016$	— $0''.016$	— $0''.019$	— $0''.016$
		11.0	— $0''.031$	— $0''.008$	— $0''.030$	— $0''.009$
A	<i>a, b, c, d, e</i>	7.9	— $0''.056$	— $0''.009$	— $0''.058$	— $0''.017$
		11.8	— $0''.037$	— $0''.009$	— $0''.034$	— $0''.007$
$a = 429,430$; $b = 344,350$; $c = 323,325$; $d = 287,283$; $e = 212,213$.						

The objection may be raised, that the binary character of these stars is not very well established, as the distances between the stars in a cluster are always small. The distances of the binaries of table 9, however, are only one tenth or less of the mean distance between the cluster stars.

4^o. The results of the second and third method, tabulated in table 7, agree pretty well as far as they overlap. For the fainter magnitudes the magnitude errors found here, are not at all exceptionnally large. See for instance table IX of *Gron. Publ.* 19. The brighter stars on our plates show the larger deviations, but usually the number of these stars is too small for the determination of the magnitude error according to the second method ¹).

5^o. It will be shown below that the proper motion in declination of the cluster according to Boss' catalogue ²) is $-0''\cdot011$. The mean of the plates of this paper gives $-0''\cdot032$ for the brightest stars, the correction to absolute proper motion being derived in accordance with the second method (see above)³). The difference between these two values cannot be explained by accidental errors. A systematic error in the corrected ²) Boss' system of this amount, seems very improbable. It must, therefore, be a systematic error in the photographic plates.

These circumstances indicate, that the cause of the magnitude error is not a cosmical one but that the phenomenon is due to the photographic plates. In order to test this conclusion, I have partly measured some more plates. They are given in table 2. Three pairs of plates are from the Allegheny, Dearborn and Yerkes observatories respectively. The other five pairs of plates are another set taken with the Radcliffe refractor.

On each plate about ten bright and some fifteen faint cluster stars were measured. The following table 10 gives the result.

TABLE 10. MEASURES OF BRIGHT PRAESEPE STARS RELATIVE TO FAINT ONES.
MEAN PROPER MOTION IN DECLINATION.

Plates.	Brighter stars.	Magn.	Fainter stars.	Magn.
1	$-0''\cdot018$	8.3	$0''\cdot000$	12.9
2	$-0''\cdot021$	8.3	$0''\cdot000$	12.2
3	$-0''\cdot027$	7.4	$0''\cdot000$	11.0
4	$-0''\cdot022$	7.6	$0''\cdot000$	11.0
5	$-0''\cdot022$	7.9	$0''\cdot000$	11.6
6	$0''\cdot000$	7.2	$0''\cdot000$	12.2
7	$-0''\cdot008$	7.2	$0''\cdot000$	11.0
8	$-0''\cdot013$	7.7	$0''\cdot000$	11.0

¹) Kreiken has measured plates, containing the Pleiades (*Bulletin of the Astronomical Institutes of the Netherlands* Vol. II, 55, 1924); he also finds pretty large magnitude corrections.

²) A correction of $-0''\cdot007$ has been applied to the catalogue values.

³) See also section 9.

Seven of the eight plates once more indicate, that the brighter stars move faster to the south than the fainter ones! The plates taken with the Allegheny and Yerkes telescopes (6 and 7), having a large focal length show a small relative shift. On the Radcliffe plates the discrepancy is largest and again in the same direction as on the regularly measured plates. The values of this relative shift are almost identical on these five plates but they are, perhaps, not independent of one another as four of the five early plates have been taken in the same night with a time interval of a few minutes.

The error cannot be due to the method of measurement or to the computing devices. Mr. EBELS, observer at the KAPTEYN Laboratory has made revised measurements of some twenty bright stars, relative to the fainter ones. These revisions give exactly the same values as the original measurements. Moreover the measurements in the x and y direction have been performed in exactly the same way, and it is difficult to see why the $\bar{\mu}_y$ should be erroneous, whereas the $\bar{\mu}_x$ is free from magnitude error.

If a plate contains more than one image, the error is almost the same for each image.

The fainter cluster stars have a systematically later spectral type than the brighter ones (section 12). One might think therefore that it is due to atmospheric dispersion. Table 1 shows however that the hour angles of the new and early epoch are almost the same in most cases. Moreover on this supposition the four bright giants of the type G — K should give the same values of the proper motions as the faint stars of this type. This is not the case. Their proper motion is equal to that of the A stars of the same brightness (table 11).

TABLE 11. RELATIVE, UNCORRECTED PROPER MOTIONS OF THE FOUR GIANT CLUSTER STARS OF TYPE G AND K, COMPARED WITH OTHER BRIGHT AND FAINT CLUSTERSTARS. MEAN OF ALL PLATES.

Nr.	Phot. magn.	μ_x giant	μ_y groupstars	Phot. magn.	μ_x all groupstars;	μ_y table 8
212	7.3	— 0"027	— 0"026	7.3 (A)	— 0"027	— 0"028
253	7.2	— 0.028	— 0.036	12. (G and K)	— 0.032	— 0.009
283	7.1	— 0.030	— 0.034			
428	7.5	— 0.030	— 0.034			
mean	7.3	— 0.029	— 0.032			

It must be concluded that the error is due to the plates, but I have no explanation to offer of its real cause, unless it should be a guiding error, which seems highly improbable ¹⁾).

The error might, perhaps, be due to either the early plates or the new plates exclusively. I have investigated this point in the case of the plates XIV, XV, 1, 3 and 4. For this purpose the distances in the y direction of a few binaries have been measured, on the plates of the new and of the early epoch separately. The same binaries were measured on both plates of the pair X, which, according to table 8, yielded proper motions practically free from magnitude equation. I assumed therefore that the distances, derived from the latter pair of plates, were correct. The differences between these two measurements (fourth column of table 12) will be due to observational errors for the most part.

The result has been tabulated in the following table 12; the upper number for each binary in the first column represents the northern component. The last five columns contain the corrections to be applied to the measurements of the plates XV, XIV, 1, 3 and 4; the sign being positive, if the declination of the brighter component is too large.

TABLE 12. MEASUREMENTS OF THE DISTANCES IN THE y DIRECTION OF 5 BINARIES. DIFFERENCES BETWEEN THE MEASUREMENTS OF DIFFERENT PLATES.

Pair of Plates.				X—XV	X—XIV	X—1	X—3	X—4
Binary	Phot. magn.	Early plate and new plate	Distance in y on X					
283	7.10	E	11.75	+0.69	+0.11	+0.14	-0.12	+0.12
287	10.56	N	11.99	-0.40	-0.31	+0.02	-0.15	-0.30
212	7.26	E	35.44	+1.09	+0.56	+0.47	+0.65	+0.49
213	12.16	N	35.48	+0.08	-0.18	+0.34	+0.01	+0.14
150	7.65	E	5.95	+0.35	+0.33	+0.35	+0.38	+0.10
155	9.55	N	6.22	-0.32	+0.11	+0.11	+0.29	+0.21
325	10.81	E	16.12	+0.32	+0.34	+0.32	+0.34	—
323	8.00	N	16.12	-0.63	-0.33	+0.07	-0.30	—
350	8.67	E	0.98	+0.24	+0.15	+0.11	+0.23	-0.02
344	12.48	N	0.83	-0.36	-0.67	-0.69	-0.28	-0.11
Mean magn. bright: 7.7 faint: 11.1			mean	+0.54 -0.33	+0.30 -0.28	+0.28 -0.11	+0.30 -0.09	+0.17 -0.02
			Diff.	+0.87	+0.58	+0.39	+0.39	+0.19
Diff. between μ_{δ} (table 8 and 10) $m = 7.7$ and 11.1, multiplied by Δ Epoch.				+0.79	+0.50	+0.30	+0.38	+0.44

¹⁾ In a recent letter to Prof. VAN RIJN, Prof. KNOX-SHAW states that he has traced the cause of the error of the Radcliffe plates to the object-glass of the refractor. As however experiments are still going on, the definite result will be published later by the Radcliffe astronomer.

It will be seen from these figures, that the cause of the magnitude error of the proper motions cannot be ascribed either to the early plates, or to the new plates exclusively, although the latter plates need a smaller correction.

A value of the magnitude error of the annual proper motions can be derived from table 12, by dividing the difference between the corrections of the early and new plate by the epoch difference. This value is in good agreement with the magnitude error as derived above, as may be seen from the last two lines of the table. Thus the reality of this error is confirmed once more, but no more light is thrown on its cause.

I have applied corrections to the proper motions, which make the proper motions of the cluster stars independent of the magnitude. The corrected proper motions are printed in the catalogue. These corrections are the $\Delta\mu_x$ and $\Delta\mu_y$ of table 7 under the heading: group-stars. They have been read from a smooth curve for each star separately.

Even if it were not true that the bright and faint cluster stars have exactly the same proper motion, this procedure would have to be followed. It is quite impossible, with the data of this paper, to distinguish between a magnitude error and a real dependence on the brightness.

The proper motions of the stars fainter than the 14th magnitude have been derived from plate XVII. The number of group stars of each magnitude is very small. The magnitude error has therefore been derived according to the second method described on page 14. Table 13 contains the result.

TABLE 13. DIFFERENCE BETWEEN PARALLACTIC MOTION AND MEAN PROPER MOTION OF THE STARS OF PLATE XVII.

Phot. magn.	$\bar{\mu}_x$	$\bar{\mu}_y$	$\left(\frac{h}{\varrho}\right)_x - \bar{\mu}_x$	$\left(\frac{h}{\varrho}\right)_y - \bar{\mu}_y$	Nr.
13 — 14	+ 0"012	+ 0"010	— 0"014	— 0"013	47
14 — 15	+ '009	+ '003	— '011	— '005	63
15 — 16	+ '003	— '005	— '004	+ '003	99
16 — 17	+ '001	— '002	— '002	'000	143
17 — 18	— '002	— 003	+ '001	+ '002	78

If these corrections are applied to the cluster stars, they yield proper motions which are practically independent of the magnitude (table 14).

TABLE 14. MEAN ABSOLUTE PROPER MOTIONS OF CLUSTER STARS, DERIVED FROM PLATE XVII.

Phot. magn.	Numb.	$\bar{\mu}_x$	$\bar{\mu}_y$
13 ^o — 14 ^o	6	— 0 ^o 034	— 0 ^o 005
14 ^o — 15 ^o	5	— 0 ^o 041	— 0 ^o 012
15 ^o — 16 ^o	5	— 0 ^o 038	— 0 ^o 009
16 ^o — 17 ^o	5	— 0 ^o 052	— 0 ^o 009
17 ^o — 18 ^o	4	— 0 ^o 042	— 0 ^o 014
mean		— 0 ^o 041	— 0 ^o 010

9a. Reduction to absolute proper motions, $m \angle 14$.
Proper motion of the Cluster.

The proper motions derived from photographic plates are relative to the faint stars of small motion. A correction must therefore be applied to reduce them to absolute proper motions. If the proper motions are absolute ones, the background stars ought to move towards the solar antapex, except for the peculiar motions. The correction is therefore equal to the parallactic motion minus the mean relative proper motion¹⁾. This quantity has already been computed for each magnitude separately in table 7, section 8, under the heading: $\Delta\mu_x$ and $\Delta\mu_y$, background stars.

The absolute proper motion of Praesepe can be found from the members of the cluster, which have the same magnitude as the reduction stars, by applying the correction which holds for the magnitude of the latter stars. Table 15 contains the result for different plates.

TABLE 15. ABSOLUTE PROPER MOTION OF THE PRAESEPE CLUSTER AS DERIVED FROM DIFFERENT PLATES.

Plates.	Mean magn. of reduction stars.	Relative prop. mot. groupstars		From table 7 background-stars		Absolute prop. mot.	
		μ_x	μ_y	$\Delta\mu_x$	$\Delta\mu_y$	μ_x	μ_y
I, II	12.5	— 0 ^o 033	— 0 ^o 008	— 0 ^o 004 ^b	— 0 ^o 004	— 0 ^o 038	— 0 ^o 012
X	11.7	— 0 ^o 031	— 0 ^o 005 ^b	— 0 ^o 005 ^b	— 0 ^o 005 ^b	— 0 ^o 037	— 0 ^o 011
XII, XIII, XIV	12.4	— 0 ^o 030 ^b	— 0 ^o 009 ^b	— 0 ^o 004	— 0 ^o 006	— 0 ^o 034	— 0 ^o 016
XV, XVI	12.1	— 0 ^o 031	— 0 ^o 008	— 0 ^o 004	— 0 ^o 004	— 0 ^o 035	— 0 ^o 012
(3) mean						— 0 ^o 036	— 0 ^o 013

¹⁾ C. f. *Groningen Publications*, 28, 12—15, 1918.

The correction to absolute proper motions can be determined also by means of known absolute proper motions of Praesepe stars.

HECKMANN ¹⁾ has determined the group motion from 9 BOSS' stars and 6 unpublished stars investigated by KÜSTNER. He finds for the proper motion of the cluster, reduced to BOSS' system: $\mu_\alpha \cos \delta = -0''.031$, $\mu_\delta = -0''.020$. The BOSS' proper motions in declination however need a correction. KAPTEYN ²⁾ estimated this correction to be $+0''.013 \cos \delta$. Other investigators ³⁾ find a value which is half this amount. Recently RAYMOND ⁴⁾ has derived corrections to the BOSS' system by means of 34 catalogues not used by BOSS. At the declination $+20^\circ$ the correction to the μ_δ is $+0''.004$.

After having applied RAYMOND's corrections, VAN RHIJN has determined a residual correction of the form $G \cos \delta$, using the method described in B. A. N. 36. The preliminary result, not yet published, is $G = +0''.0033$.

I have therefore applied a correction of $+0''.007$ to the BOSS' proper motions in declination and find the following result:

$$\begin{array}{rcl}
 \text{BOSS} & (8 \text{ stars}) & \overline{\mu_\alpha \cos \delta} = -0''.032 & \overline{\mu_\delta} = -0''.011 \pm .001^5 \\
 \text{KÜSTNER} & (6 \text{ stars}) & \overline{\mu_\alpha \cos \delta} = -0''.033 & \overline{\mu_\delta} = -0''.019 \pm .002^5 \\
 \text{mean} & & \overline{\mu_\alpha \cos \delta} = -0''.032^5 & \overline{\mu_\delta} = -0''.013.
 \end{array} \tag{4}$$

The agreement between the values (3) and (4) is good; their mean is

$$\mu_\alpha \cos \delta = -0''.034 \quad \mu_\delta = -0''.013. \tag{5}$$

The reduction to absolute proper motion and the corrections for magnitude error have been applied simultaneously, so as to make the mean group motion of stars of each magnitude identical with the value (5).

Table 13 contains the corrections to absolute proper motions in the case of the stars of plate XVII. This correction is equal to the difference between the parallactic motion and the mean relative proper motion.

9b. Reduction to absolute proper motions, $m > 14$.

The corrected group motion of these fainter cluster stars becomes $-0''.041$, $-0''.010$ (table 14). A glance at figure 3 at the end of this paper shows, that this value has a relatively large probable error. The agreement with the value (5) is therefore quite satisfactory.

¹⁾ *Astronomische Nachrichten* 225, 49, 1925.

²⁾ *Bull. Astron. Instit. Netherlands I*, 69, 1922.

³⁾ VAN RHIJN and VAN DE KAMP, *Bull. Astron. Instit. Netherlands I*, 209, 1923.
ALDEN and VAN DE KAMP, *Astronomical Journal* XXXVI, 17, 1924.

OORT and MARSH, *Popular Astronomy* 32, 559, 1924.

⁴⁾ *Astronomical Journal* XXXVI, 129, 1926.

O. Final Values of the Proper Motions and their Probable Errors.

The proper motions as derived from different plates have been compared with one another, the corrections of sections 8 and 9 having been applied.

The probable error of one plate ϱ is computed according to the formula

$$(6) \quad \left(0.845 \frac{\text{sum differences}}{\text{number}}\right)^2 = \varrho_1^2 + \varrho_2^2.$$

I have compared plates for which the probable errors, according to the formula (6),⁷ are equal: $\varrho_1 = \varrho_2$.

The result is summarised in table 16. The second column contains the probable error computed according to the formula:

$$(7) \quad \varrho = \frac{r}{\Delta T \sqrt{n}}$$

ΔT = epoch difference

n = number of images of each star.

r = prob. error of one distance of two single images.

I have adopted:

$$r = 0''.18 \text{ if } 1 \text{ mm. } \sim 90''$$

$$= 0''.14 \text{ " " " } \sim 60''$$

$$= 0''.11 \text{ " " " } \sim 30''.$$

TABLE 16. LIST OF PROBABLE ERRORS.

Plate.	ϱ (form. (7))	Assumed weight.	Plates.	ϱ (form. (6))
I	0.0048	5 ¹ / ₂	I, II	0.0033
II	.0048	5 ¹ / ₂	I, II, X	.0035
VI	.0034	6	I, II, A	.0047
VIII	.0068	2	XII, XIII, XIV	.0035
X	.0044	5	XV, XVI	.0034
XII	.0052	3 ² / ₈		
XIII	.0052	3 ² / ₈		
XIV	.0052	3 ² / ₈		
XV	.0034	7		
XVI	.0034	7		
XVII	.0060	3		
A	.0064	2		

It appears from the table that the probable errors computed according to the formula (6) are, in general, smaller than those of formula (7). It does not follow from this that the accuracy of measurement is higher than usual. The explanation is that all systematic differences depending on the magnitude, have been eliminated and that similar plates had practically the same reduction stars.

The weights in the third column of table 16 have been assumed nearly in accordance with the probable errors (7). The unit of weight corresponds with a probable error of $0''.010$. The sum of the weights is given in the catalogue for each star. These weights refer of course to the accidental errors only. The mean weights are about 50—40 for magnitudes 6 to 11 and 40—20 for magn. 11 to 13.5.

It appears from a consideration of the cluster stars that the weights assumed are not too large. The cluster stars should all have exactly the same proper motion but for the accidental errors and the internal motion. The latter probably is not negligible. The Hyades, for instance, the distance of which is about one fourth of that of Praesepe, have a mean internal motion of $0''.006$ ¹⁾.

The arithmetical mean of the differences $(\bar{\mu}_x - \mu_x)$ and $(\bar{\mu}_y - \mu_y)$ for the Praesepe stars is $0''.0021$, whereas the average accidental error, according to the above is:

$$\frac{0''.010}{0.845 \sqrt{\text{mean weight}}} = 0''.0019.$$

These two values are practically identical. The cluster stars therefore even point to somewhat smaller accidental errors than those adopted in table 16. An independent value of the internal motion of the cluster stars cannot be found from the present material, the accidental errors being too large.

¹⁾ VAN RHIJN and KLEIN WASSINK, *Groningen Publications* 35, 1924.

CHAPTER II.

11. The figure of the cluster, as projected on the sphere. The centre of the cluster is independent of the magnitude. This appears from table 17, where the mean has been taken of the right-ascension and declination of the stars of table 5 and 6.

TABLE 17. MEAN POSITION OF THE GROUPSTARS.

Phot. magn.	α_{1900}	δ_{1900}	Numb.
	8 ^h	+	
6.0 — 8.0	34 ^m 23 ^s	19° 59'.3	18
8.0 — 10.0	34 38	20 2.1	52
10.0 — 12.0	34 24	19 59.7	64
12.0 — 14.0	34 47	19 58.7	55
14.0 — 16.0	(34 20)	(20 14.6)	10
16.0 — 18.0	(33 52)	(20 13.6)	10

- The centre of the brighter stars ($m = 6$ to 14) lies very near the adopted (8) centre $\alpha_{1900} = 8^h 34^m 39^s$, $\delta_{1900} = +20^\circ 1'.0$. The mean position of the fainter stars does not coincide with this centre. As these stars occur, however, only on plate XVII, this being a very small plate, they do not give the centre of the cluster at all, but they actually give the centre of this plate: $\alpha = 8^h 34^m 19^s$, $\delta = +20^\circ 15'.5$ (table 1). It seems safe to assume the same centre (8) for all magnitudes.

The figure of the cluster, as projected on the sphere, can be easily derived from the groupstars of table 5. The data of the following table were obtained by counting the stars in 12 sectors, each 30° wide; ψ denotes the position angle with respect to the centre (8). Stars whose distance from the centre exceeds $60'$ are not included in the counts.

TABLE 18. NUMBER OF GROUPSTARS IN DIFFERENT DIRECTIONS FROM THE CENTRE.

Phot. Man. ψ	6.0 — 9.0	9.0 — 11.0	11.0 — 13.0	Phot. Magn. ψ	6.0 — 9.0	9.0 — 11.0	11.0 — 13.0
0° — 30°	3	3	5	180° — 210°	3	7	2
30 — 60	4	6	10	210 — 240	4	3	7
60 — 90	0	4	4	240 — 270	3	5	4
90 — 120	0	4	5	270 — 300	3	2	5
120 — 150	3	4	9	300 — 330	4	4	6
150 — 180	4	6	4	330 — 360	6	9	2

The numbers of magnitudes 6.0 — 9.0 and 9.0 — 11.0 show two maxima at $\psi = 180^\circ$ and 345° approximately and two minima at $\psi = 90^\circ$ and 285° . The figures in the fourth column of the table do not show these maxima and minima. This is due to the figure of the brighter part of the cluster being elongated in the directions $\psi = 180^\circ$ and 345° and shortened in the other two directions. The general aspect resembles an ellipse with maior axis in the direction $\psi = 172^\circ$, which is nearly parallel to the plane of the Milky Way: $\psi = 162^\circ$. The same phenomenon has been observed in other clusters¹⁾. The fainter stars of the cluster seem to be distributed more equally in all directions.

The diameter of the group cannot be found directly from the data of tables 5 and 6, because the cluster extends beyond the limits of this paper. The counted numbers, however, may be extrapolated without introducing too much uncertainty.

In the first place it is necessary to investigate the limit of completeness of the observed stars. For this purpose I have compared the numbers of non-group stars with the numbers of SEARES and VAN RHIJN²⁾ (table 19).

The Durchmusterung contains stars of the magnitude 14.1; the limit of completeness therefore is $\angle 14.1$. In the case of plate XVII it is $\angle 18.7$. It appears from the last column of table 19, that the plates are complete down to the magnitude 13.0, but that the logarithm of the numbers between 13.0 and 14.0 requires a correction of $+0.18$. The last column shows that plate XVII is probably complete down to the magnitude 18.0.

The logarithm 0.18 corresponds with a factor 1.5. Actually I have multiplied the counted numbers of magnitude 13.0 to 14.0 by 1.3 for distances from the centre less than 30' and by 2.0 for the distances 30' to 56'.

The counts of the groupstars have been inserted in table 20. This table contains also the logarithm of the star-density, *i. e.* the number of stars per square minute.

¹⁾ RASMUSON, *Meddelanden Lund* II, 26, 1921.

²⁾ *Proceedings Nat. Ac. Sciences* Vol. 11, 358, 1925.

TABLE 19. LOG. NUMBERS OF NON-GROUP STARS PER SQUARE DEGREE, COMPARED WITH THE CORRESPONDING NUMBERS OF SEARES AND VAN RHIJN.

Phot. magn.	Log. numb. backgroundstars		Log. numb. S. and V. R.	Difference.
	all plates	plate XVII		
10.0			0.30	+0.15
10.5	0.45		0.50	+0.20
11.0	0.70		0.69	+0.12
11.5	1.13		0.88	+0.25
12.0	1.29		1.06	+0.23
12.5	1.41		1.24	+0.17
13.0	1.50	} 1.97	1.41	+0.09
13.5	1.48		1.58	-0.10
14.0		2.23	2.12	+0.11
15.0		2.23	2.41	-0.18
16.0		2.46	2.66	-0.20
17.0		2.73	2.89	-0.16

TABLE 20. NUMBER OF CLUSTER-STARS AND LOGARITHM OF STAR-DENSITY, ACCORDING TO PHOTOGRAPHIC MAGNITUDE AND DISTANCE FROM THE CENTRE.

Phot. Magn. Distance	6.0 — 9.0	9.0 — 11.0	11.0 — 13.0	13.0 — 14.0
	0' — 12'	11 8.39	8 8.25	10 8.34
12 — 24	9 7.82	15 8.04	11 7.91	5 7.57
24 — 36	10 7.64	14 7.79	10 7.64	4.5 7.30
36 — 48	6 7.28	11 7.54	17 7.73	4 7.10
48 — 60	1 6.36	9.1 7.34	14.3 7.54	3 6.87
60 — 72	1.6 6.50	6.9 7.15	7.6 7.18	— —

The figures of the distances 48' to 60' and 60' to 72' need some more explanation. These distances partly fall outside the limits of the plates. The counted numbers have therefore been multiplied by the factors 1.03, 1.19 and 1.74 in the case of the distances 54' to 60', 60' to 66' and 66' to 72' respectively.

For the purpose of extrapolating the numbers of table 20, I assumed 1⁰ that the number of stars in each ring from the distance 12' on outwards, falls off proportionately to the distance; 2⁰ that the logarithm of the surface-density is a linear function of the distance.

TABLE 21. NUMBER OF CLUSTERSTARS, ACCORDING TO PHOTOGRAPHIC MAGNITUDE AND DISTANCE FROM THE CENTRE.
EXTRAPOLATED NUMBERS ARE IN ITALICS.

Phot. magn. Distance.	6'—7'	7'—8'	8'—9'	9'—10'	10'—11'	11'—12'	12'—13'	13'—14'	13'—14'	14'—15'	15'—16'	16'—17'	17'—18'
0'—12'	2	9	0	4	4	4	6	4	3.2	2.6	2.2	3.1	4.4
12—24	2	3	4	7	8	6	5	5	5.8	4.6	3.9	5.5	7.8
24—36	0	1	9	9	5	7	3	4.5	5.8	4.6	3.9	5.5	7.8
36—48	0	1	5	3	8	8	9	4	5.0	4.0	3.4	4.8	6.7
48—60	0	0	1	4.8	4.3	6.5	7.8	3	3.9	3.1	2.6	3.7	5.2
60—72	0	0	1.6	4.7	2.2	2.5	5.1	2.3	3.0	2.3	2.0	2.8	4.0
72—84	0	0	0.2	2.6	2.5	3.1	3.2	1.8	2.1	1.7	1.4	2.0	2.8
84—96	0	0	0	1.7	1.6	2.3	2.3	1.3	1.4	1.2	1.0	1.4	1.9
96—108	0	0	0	1.0	1.0	1.6	1.6	0.8	0.9	0.7	0.6	0.9	1.3
108—120	0	0	0	0.5	0.5	1.0	1.0	0.4	0.6	0.4	0.4	0.5	0.8
120—132	0	0	0	0.4	0.3	0.7	0.6	0.1	0.4	0.3	0.2	0.3	0.5
132—144	0	0	0	0.3	0.2	0.4	0.5	0.0	0.1	0.1	0.1	0.2	0.3
144—156	0	0	0	0.2	0.1	0.3	0.3	0.0	0.0	0.0	0.0	0.0	0.1
156—168	0	0	0	0.1	0.0	0.2	0.2	0.0	0.0	0.0	0.0	0.0	0.0
Total number	4.0	14.0	20.8	39.3	37.7	43.6	45.6	27.2	32.2	25.6	21.7	30.7	43.6
Extrapolated number	0.0	0.0	0.2	6.8	6.2	9.6	9.7	6.7	23.2	18.4	15.6	22.1	31.4

The numbers, computed according to these hypotheses, have been averaged with weights 1 and 2; the result for magnitudes 6 to 14 is contained in table 21. The extrapolated numbers are printed in italics.

The counted numbers of stars fainter than magnitude 14.0 (table 6) have been treated in the way shown in table 22. The third column of the table contains a factor to allow for the missing stars, that could not be measured on account of bad images etc. The fifth column contains the logarithm of the number of stars per square minute.

TABLE 22. FAINTER CLUSTER-STARS, DERIVED FROM PLATE XVII.

Phot. Magn.	Counted number	factor	product	Log. Density
13.0 — 14.0	6	1.19	7.1	7.59
14.0 — 15.0	5	1.08	5.4	7.48
15.0 — 16.0	5	1.00	5.0	7.43
16.0 — 17.0	5	1.20	6.0	7.52
17.0 — 18.0	4	2.38	9.6	7.72

The centre of the cluster lies near the edge of plate XVII. The numbers of clusterstars could be counted for distances up to 30' as maximum. In order to extrapolate the numbers to larger distances, I assumed, that $\frac{d \log. dens.}{d \text{ dist.}}$ has the same value as for the brighter magnitudes. An inspection of table 20 shows that this differential quotient is

$$\begin{aligned} & - 0.018 \quad m = 9 - 11 \\ & - 0.016 \quad m = 11 - 13 \\ & - 0.020 \quad m = 13 - 14. \\ & \text{mean} - 0.018 \end{aligned}$$

With this number and the data of table 22, the numbers of table 21 for magnitudes 13.0—18.0 have been computed. The agreement between the numbers, derived from plate XVII, and the data of the other plates may be judged from the overlapping magnitude 13.0 to 14.0.

Table 21 shows at once the diameter of the cluster. The distance, where the number of stars in a ring, 12' wide, becomes less than $\frac{1}{2}$, is given in table 23.

The area covered by the very brightest stars, is far less than the area of the stars of magnitude 9 and fainter, partly because the former are fewer in number and partly because they are more strongly concentrated towards the centre of the group. The higher concentration of the brighter stars has been found also in other clusters¹⁾ (e. g. the Pleiades, $\frac{1}{2}$ Persei, Messier 11 and 13, and others).

¹⁾ TRÜMLER, *Lick Bulletin* 361, 1925. *Publ. Allegheny Obs.*, Vol. 6, 45, 1922.
SHAPLEY, *Mt. Wilson Contributions* 116, 69, 1915.

The diameter of the Praesepe group seems to lie between 4° and 5° .

TABLE 23. DISTANCE WHERE THE NUMBER OF STARS IN A RING OF $12'$ BECOMES LESS THAN 0.5.

Phot. Magn.	Radius.	Phot. Magn.	Radius
6.5	25'	12.5	125'
7.5	45	13.5	110
8.5	70	14.5	(110)
9.5	110	15.5	(110)
10.5	110	16.5	(110)
11.5	125	17.5	(110)

In the preceding section the numbers of groupstars of each magnitude have been derived, as completely as can be done at present. They are found in table 21. The following table 24 contains the logarithms of these numbers (third column). For the sake of comparison I have added in the fourth column the frequencies of the stars in the neighbourhood of the Sun, as derived by VAN RHIJN¹⁾. The assumed parallax of the cluster is $0''.0073$. The table is illustrated by figure 1.

12. Frequency of the Luminosities.

TABLE 24. FREQUENCY OF THE LUMINOSITIES OF THE PRAESEPE-STARS. COMPARISON WITH FREQUENCY OF NEAR-SUN STARS (*Gron. Publ* 38, table 71).

Phot. Magn.	Abs. magn. $m + 5 \log 0.0073$	Logarithm number		Difference 4 th and 3 ^d col.
		Clusterstars.	Near-Sun stars per 15140 cubic parsecs.	
< 6.0		$-\infty$	9.66	
6.0 — 7.0	-4.1	0.60	0.34	-0.26
7.0 — 8.0	-3.3	1.15	0.71	-0.44
8.0 — 9.0	-2.3	1.32	1.02	-0.30
9.0 — 10.0	-1.2	1.59	1.27	-0.32
10.0 — 11.0	-0.2	1.58	1.49	-0.09
11.0 — 12.0	+0.8	1.64	1.73	+0.09
12.0 — 13.0	+1.8	1.66	1.73	+0.07
13.0 — 14.0	+2.8	1.44	1.60	+0.16
14.0 — 15.0	+3.8	1.41	1.57	+0.16
15.0 — 16.0	+4.8	1.34	1.68	+0.34
16.0 — 17.0	+5.8	1.49	1.78	+0.29
17.0 — 18.0	+6.8	1.64	1.88	+0.24

¹⁾ *Groningen Publications* 38, 1926.

It appears that the number of bright stars is relatively larger in the Praesepe-cluster than in the galactic system generally. The general features of both curves are, for the rest, very similar. In both cases there is a maximum at the absolute magnitude +2 and a minimum two or three magnitudes after the maximum. The slopes for the brighter and the fainter ends are practically identical.

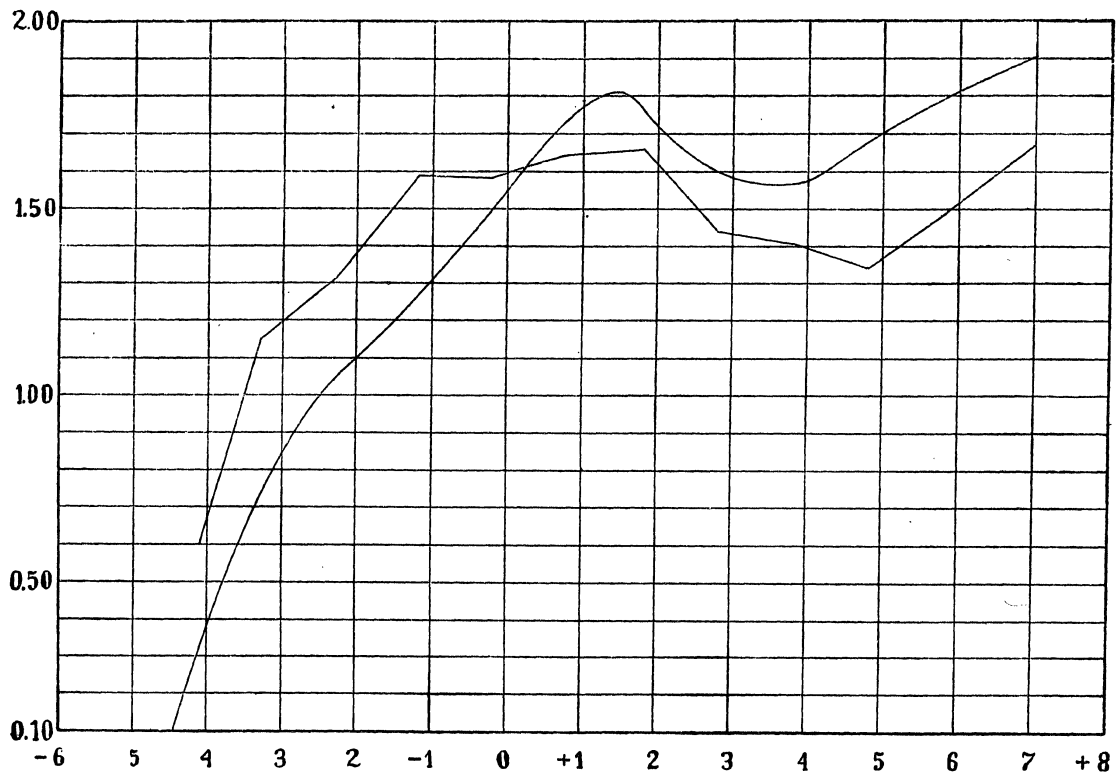


Figure 1. The abscissae are absolute photographic magnitudes; the ordinates represent the logarithms of the numbers of stars in the cluster and in the neighbourhood of the Sun; broken line = Praesepe stars, smooth curve = Near Sun stars per 15140 cubic parsecs.

It is true that the counted numbers, on which the frequencies of the faint Praesepe stars are based, are rather small and I think, that the agreement between the two curves is partly accidental; yet the general result will be near to the truth: the frequencies of the luminosities in the Praesepe-cluster do not differ very much from the frequencies of the stars in general.

The frequencies of the separate spectral types show clearly the well known form of RUSSEL'S diagram (see for instance: *Astron. Nachr.* 211, 289, 1920; *B. A. N.* I, 79, 1922; *Astron. Journ.* 34, 1, 1921).

Several giant stars exist of which four are of the type G—K. The dwarf stars change from the A class to the later types with decreasing brightness.

The available data are collected in table 25. The spectral types have been

taken from the HENRY DRAPER Catalogue up to $m = 8.5$ and from unpublished data, kindly furnished by Prof. Dr. SCHWAZSMANN from $m = 8.5$ to $m = 11.3$. The limit of completeness of the stars of table 25 is $M = +0.6$.

TABLE 25. NUMBER OF CLUSTERSTARS AND OF NEAR-SUN STARS, ACCORDING TO PHOTOGRAPHIC MAGNITUDE AND SPECTRAL TYPE.

Abs. Magn. $m + 5 \log 0.0073$	A type		F type		G type		K type	
	Praesepe	Near-Sun	Praesepe	Near-Sun	Praesepe	Near-Sun	Praesepe	Near-Sun
≤ -4.4	0	2.4	0	0.0	0	0.0	0	0.0
$-4.4 - -3.4$	5	7.0	2	0.2	1	0.2	2	0.3
$-3.4 - -2.4$	17	11.9	1	1.0	0	0.6	1	1.1
$-2.4 - -1.4$	11	10.1	4	4.9	0	0.9	0	1.2
$-1.4 - -0.4$	3	4.5	28	17.4	5	3.8	0	0.5
$-0.4 - +0.6$	1	—	6	18.6	21	22.4	1	0.7

The number of near Sun stars has been derived from the frequencies given by VAN RHIJN¹⁾, so as to make the total number of near-Sun stars equal to the number of cluster stars.

It will be seen that the agreement is not bad, except in the case of the F-stars.

The division into giants and dwarfs in clusters has been one of the grounds for assuming a similar division for the stars in general. VAN RHIJN (l. c.) however has shown that the existence of the latter is not beyond doubt, for the missing stars, if they really exist, occur among objects of an apparent magnitude and proper motion, which have not yet been sufficiently investigated.

In the Praesepe cluster they certainly do not exist, but the frequency is perhaps not high enough to form a single star, as is indicated by the seventh and last column of table 25.

SCHWARZSCHILD and HERTZSPRUNG²⁾ have raised the hypothesis that the Hyades and the Praesepe cluster move together through space in the same direction with identical velocities. As the convergent and the radial velocity of the Hyades are known, the parallax of Praesepe can be computed by means of the proper motion. SCHWARZSCHILD finds $\pi = 0''.0063$.

KOHLSCHÜTTER³⁾ assumes equal absolute magnitudes of stars of the same

1) loco citato, table 71.

2) *Astronomische Nachrichten* 196, 9, 1913.

3) *Astronomische Nachrichten* 211, 289, 1920.

13. On the Parallax of Praesepe.

spectral type in the two clusters and gets $\pi = 0''.0072$. VAN DEN BOS¹⁾ finds, by means of the same hypothesis for the giants $\pi = 0''.0078$. SITTERLY²⁾ makes use of the magnitudes and spectral types of the HENRY DRAPER Catalogue and gets $\pi = 0''.0055$. HERTZSPRUNG³⁾ applied the KAPTEYN correction to the proper motions in declination of BOSS' catalogue; he computes a parallax $\pi = 0''.0060$ from the proper motion of Praesepe and the parallax, proper motion and convergent of the Hyades.

(16) As however this correction of $+0''.013 \cos \delta$ is too large, I have computed the convergent etc. of the Hyades, assuming a correction of $+0''.007$ to BOSS' proper motions in declination (see section 9). The result is:

(9)	Centre of the Hyades	$\alpha = 65^\circ.5$	$\delta = +15^\circ.5$
(10)	Point of convergence (39 BOSS' stars)	$\alpha = 92^\circ.0$	$\delta = +8^\circ.6 \pm 1.8$
(11)	Total proper motion in the centre	$\mu_2 = 0''.110$	± 0.0015
(12)	Position angle of the proper motion	$\psi_2 = 101^\circ.8$	± 3.8
(13)	Radial velocity (23 stars)	$R_2 = +39.0$ K.M. sec. ⁻¹	± 0.5
(14)	Space-velocity from (10) and (13)	$V_2 = +43.7$ K.M. sec. ⁻¹	± 0.7
(15)	Parallax from (4) ⁴⁾ , (5) ⁴⁾ , (6) ⁴⁾ and (9) ⁴⁾	$\pi_2 = 0''.027$	± 0.0016

The values (10)⁴⁾ and (11) have been computed from the data given by BOSS⁴⁾ and the correction (16). The radial velocities have been taken from several authorities⁵⁾. The formulae for the space-velocity and the parallax are:

$$(17) \quad V = R \sec \lambda$$

$$(18) \quad \pi = 4.74 \mu (V \sin \lambda)^{-1}$$

$\lambda =$ angular distance from point of convergence.

If we assume, that the point of convergence and the space-velocity of the Praesepe-cluster are identical with those of the Hyades, the radial velocity of the former, according to formula (17), is found to be ± 34.8 K.M. sec.⁻¹ ± 1.1 ;

(19) the observed radial velocity is $+33.0$ K.M. sec.⁻¹ ± 0.6 (24 stars⁶⁾). The position

(20) angle of the proper motion should be $257^\circ.5 \pm 3$; the observed angle is $249^\circ \pm 2.5$.

(21) The centre of the cluster is $\alpha = 128^\circ.6$, $\delta = +20^\circ.1'$; the total proper

(22) motion is $\mu_1 = 0''.037 \pm 0.001^5$.

Applying formula (18) to the Hyades and to the Praesepe-group and eliminating the space velocity V , we get

$$(23) \quad \pi_1 = \pi_2 \mu_1 \sin \lambda_2 \mu_2^{-1} \sin^{-1} \lambda_1 = 0''.0067 \pm 0.0007.$$

¹⁾ *Bull. Astron. Instit. Netherlands* I, 79, 1922.

²⁾ *Astronomical Journal* XXXIV, 1, 1921.

³⁾ *Bull. Astron. Instit. Netherlands* I, 150, 1922.

⁴⁾ *Astronomical Journal* XXVI, 31, 1908.

⁵⁾ The same as were used by VOÛTE in his catalogue of radial velocities and also from: *Mt. Wilson Contributions* 258 and *Publications of the Dominion Observatory* II, 1.

⁶⁾ Most of these radial velocities have been kindly furnished by Dr. W. ADAMS (see also: *Annual Report of the Director of the Mt. Wilson Observatory* 1923 page 200).

The uncertainty in the underlying data is large enough to explain the observed differences. The two clusters move along almost parallel lines through space; a real difference between the velocities at least cannot yet be shown. Neither can it be settled at present whether other star clusters, for instance Messier 67¹⁾ and the Monoceros group²⁾, share this motion.

¹⁾ *Groningen Publications* 33.

²⁾ *Astronomical Journal* XXXIV, 1, 1921.

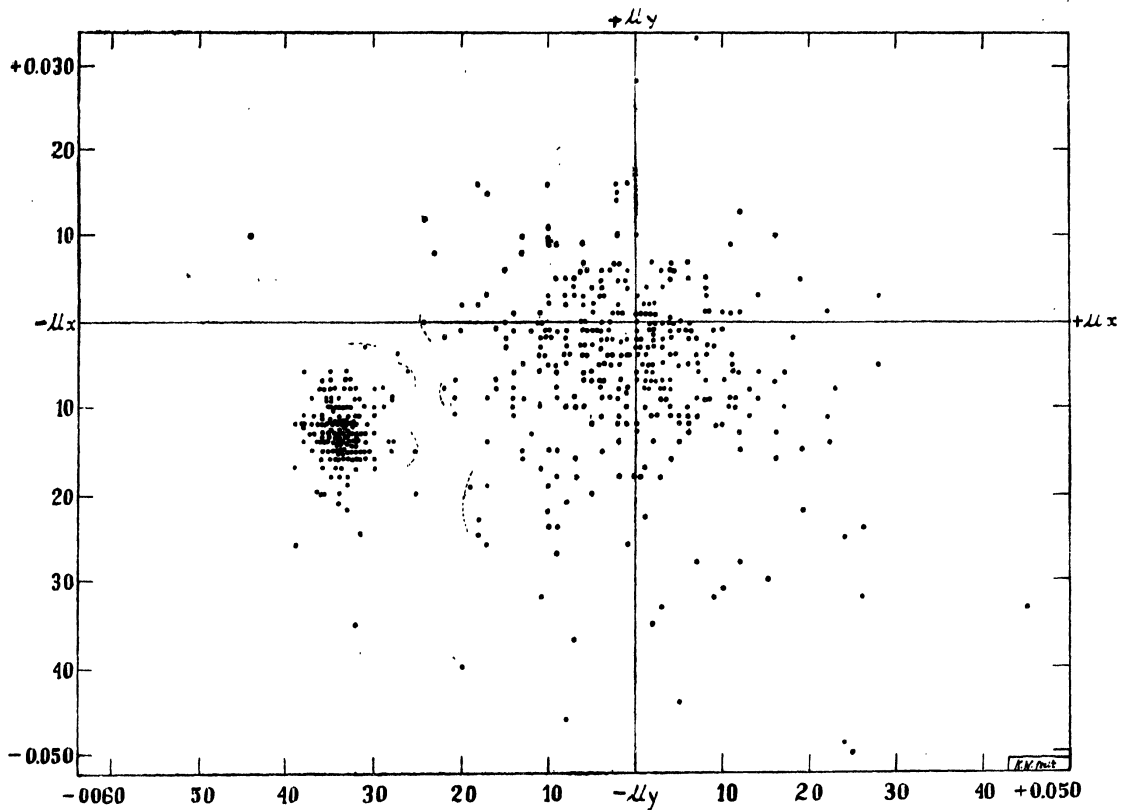


Figure 2. Diagram of the absolute proper motions of the Catalogue; photographic magnitude 6 to 14.0, numbers 1 to 531. The dotted lines separate the Praesepe stars from the backgroundstars.

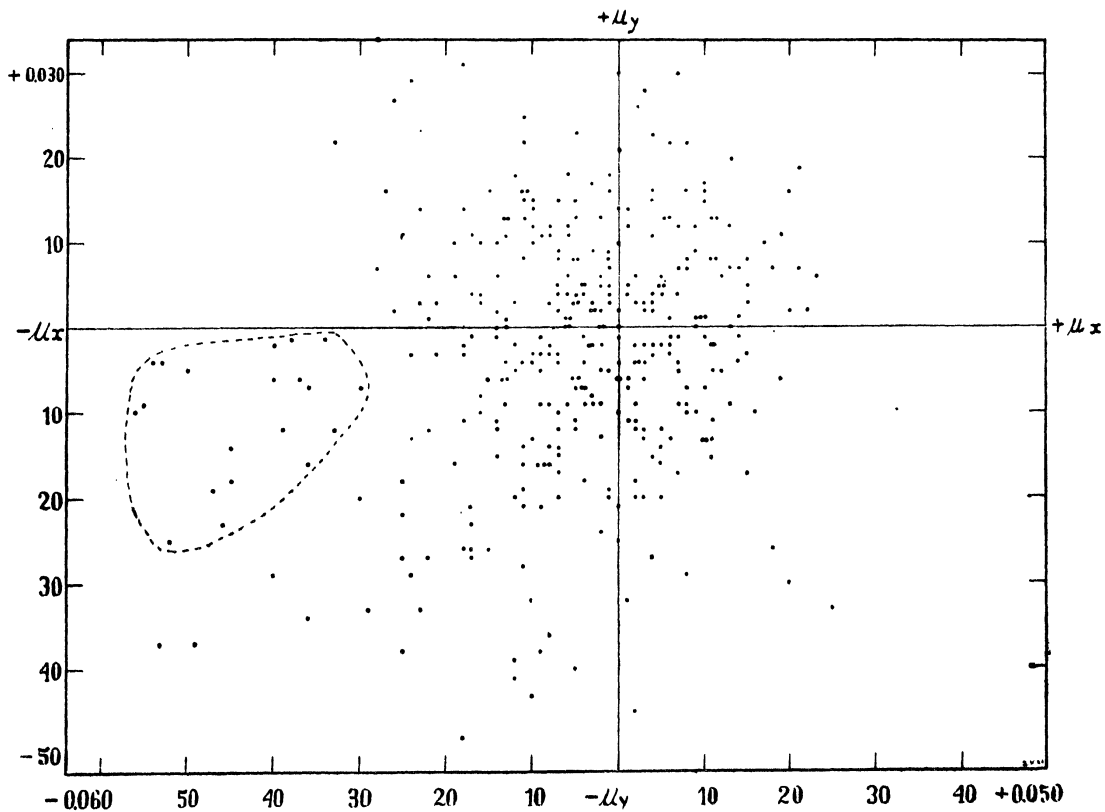


Figure 3. Diagram of the absolute proper motions derived from plate XVII. Phot. magn. 14.0 to 18.0. The stars within the dotted line are given in the Catalogue, nrs. 558 to 577.

EXPLANATION OF THE CATALOGUE.

The catalogue is divided into three parts: no. 1 to 531 containing all stars brighter than magnitude 13.0 and most stars between 13.0 and 14.0 inside a circle of 56' radius (section 3); the second part (numbers 532 to 557) contains the groupstars brighter than the magnitude 14, outside the circle of 56' radius; the third part contains the groupstars fainter than the magnitude 14.0 (section 7).

The *second column* contains the photographic magnitude on the scale of HERTZSPRUNG (*Astr. Nachr.* Bd 205, 71, 1917) (section 6).

The *third and fourth column* contain the right-ascension and declination, derived from the measured coordinates.

The total absolute proper motion μ and its position angle ψ are contained in the *fifth and sixth column*. The proper motion is the mean of all plates, corrected for magnitude error (sections 8 and 9).

The weight in the *last column* is the weight of μ_x or μ_y ; weight = $1 \propto$ probable error = 0".010.

THE CATALOGUE.

No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.			No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.		
				μ	ψ	Weight					μ	ψ	Weight
1	13'16	30 ^m 49 ^s	19 56'6	0'013	219	6	51	12'53	32 ^m 3 ^s	19 32'0	0'014	51	19
2	13'23	30 49	19 59'6	0'014	352	6	*52	12'62	32 4	19 27'4	0'034	242	13
3	10'90	30 50	19 51'1	0'012	138	18	53	13'06	32 4	19 24'8	0'016	308	13
4	12'01	30 50	20 6'9	0'009	302	20	54	10'98	32 5	20 39'2	0'006	351	23
5	12'40	30 51	20 5'1	0'013	203	18	55	11'72	32 5	20 14'4	0'035	243	20
6	12'38	30 54	19 53'2	0'015	228	13	56	11'95	32 6	20 0'0	0'005	158	20
7	12'95	30 54	20 2'9	0'017	177	13	57	13'51	32 7	20 28'0	0'008	300	8
8	12'77	30 57	20 12'5	0'056	126	13	*58	11'43	32 7	20 20'2	0'039	249	20
9	11'56	31 1	20 6'8	0'040	236	18	59	13'82	32 8	20 10'1	0'012	149	6
10	12'83	31 2	19 45'1	0'011	260	10	60	13'36	32 8	19 45'9	0'022	251	11
11	12'28	31 5	20 18'0	0'018	276	18	61	12'67	32 8	19 18'1	0'008	263	13
12	12'79	31 9	20 14'2	0'015	352	13	62	13'60	32 10	20 29'0	0'020	75	11
13	12'56	31 13	19 54'1	0'011	218	13	63	11'94	32 10	19 37'9	0'028	84	20
14	11'66	31 14	19 48'0	0'009	160	18	64	11'30	32 11	19 20'2	0'009	108	23
15	11'22	31 14	19 42'7	0'005	259	18	65	13'08	32 12	20 30'5	0'023	178	11
16	9'38	31 17	19 57'1	0'027	257	22	66	12'55:	32 12	20 26'1	0'008	225	18
17	12'85	31 17	19 51'0	0'004	14	13	67	13'73	32 12	20 8'9	0'002	27	6
18	12'22	31 18	20 25'8	0'023	250	19	68	11'94	32 12	19 54'0	0'045	283	20
19	13'50	31 20	20 11'1	0'011	85	8	69	12'47	32 13	20 16'3	0'006	211	19
20	11'40	31 23	20 30'9	0'026	203	18	*70	12'13	32 13	19 35'1	0'036	250	20
21	12'99	31 24	20 8'4	0'011	131	11	71	13'78	32 16	19 29'6	0'022	208	6
22	12'06	31 24	19 41'2	0'004	117	19	72	13'52	32 17	19 52'2	0'011	170	11
23	11'43	31 26	20 9'2	0'033	249	19	73	12'39:	32 18	20 28'9	0'098	167	11
24	13'19	31 26	19 38'8	0'006	39	13	74	12'85	32 18	20 15'2	0'011	190	19
25	13'36	31 28	19 44'1	0'008	50	11	75	10'54	32 19	20 28'9	0'010	204	23
26	12'24	31 30	19 54'9	0'007	236	19	76	11'74	32 20	20 43'8	0'007	333	11
27	11'66	31 33	20 2'9	0'035	255	19	77	12'83	32 20	20 44'1	0'006	108	13
28	12'58	31 35	20 32'9	0'018	171	13	78	12'57	32 21	19 32'0	0'012	250	21
29	13'25	31 36	19 44'2	0'028	198	11	*79	12'46	32 22	20 20'2	0'034	258	34
30	11'46	31 36	20 31'7	0'036	255	20	80	13'60	32 22	20 26'9	0'006	309	15
31	9'92	31 43	19 54'8	0'033	256	26	81	12'64	32 26	19 44'1	0'009	216	38
*32	11'99	31 43	19 58'0	0'036	258	20	82	13'64	32 26	19 46'1	0'005	292	15
33	12'86	31 44	20 4'8	0'012	151	11	83	11'71	32 28	20 7'5	0'022	265	45
34	9'65	31 45	19 30'8	0'030	254	26	84	12'93	32 28	20 20'8	0'009	193	38
35	12'29	31 45	20 29'8	0'024	312	19	85	12'34	32 28	20 24'9	0'020	139	44
36	11'86	31 47	19 43'4	0'007	164	22	86	11'09	32 29	19 15'8	0'009	111	23
37	12'70	31 47	20 24'2	0'015	160	13	87	13'34	32 29	19 37'0	0'005	90	21
38	8'42	31 48	20 21'9	0'038	256	23	88	12'63	32 29	19 43'5	0'018	243	44
39	12'32	31 49	19 27'5	0'027	225	19	89	11'25	32 30	19 54'1	0'008	210	45
40	8'02	31 52	20 4'9	0'031	243	26	*90	11'28	32 31	19 42'9	0'039	253	48
41	13'29	31 53	20 20'0	0'164	171	11	91	11'39	32 32	19 20'3	0'014	172	23
42	12'30	31 53	19 52'1	0'020	207	16	92	13'28	32 33	19 33'9	0'015	262	19
43	10'76	31 55	20 6'2	0'004	146	23	93	13'11	32 33	20 32'9	0'018	223	17
44	10'60	31 56	20 6'7	0'002	90	26	93 ^a	14'00	32 36	19 45'2	0'039	282	4
*45	8'23	31 56	19 52'0	0'033	247	26	94	8'48	32 37	20 33'5	0'013	117	37
46	13'52	31 58	20 40'2	0'024	270	3	95	13'70	32 38	20 21'9	0'024	128	11
47	10'01	31 59	19 29'0	0'033	261	24	96	12'24	32 38	20 40'1	0'009	264	16
48	12'76	32 2	19 56'9	0'037	247	13	97	13'06	32 39	19 58'0	0'001	0	38
49	10'85	32 2	19 47'2	0'033	254	26	98	12'58	32 39	19 59'2	0'006	315	44
*50	7'14	32 3	19 37'0	0'029	252	26	99	11'88	32 39	20 24'7	0'010	287	42

25 prec. + 86 sec. — 5'1

25 prec. + 86 sec. — 5'1

No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.			No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.		
				μ	ψ	Weight					μ	ψ	Weight
*100	10'71	32 ^m 39 ^s	20 27'3	0'038	261	51	149	12'28	33 ^m 21 ^s	19 39'3	0'008	130	42
101	13'36	32 41	20 13'2	'015	113	22	*150	7'65	33 21	20 1 8	'032	250	50
102	12'41	32 45	20 24'6	'009	117	44	151	12'77	33 22	20 19'9	'001	45	38
103	13'30	32 45	19 44'0	'009	207	22	152	14'12	33 23	19 41'5	'038	171	6
104	11'50	32 45	19 27'4	'012	215	23	153	13'28	33 24	20 27'0	'013	315	24
105	12'28	32 46	20 28'9	'020	120	44	*154	8'36	33 25	19 56'6	'036	255	51
106	12'44	32 47	20 1'3	'008	83	38	*155	9'55	33 25	20 1'9	'036	248	50
107	11'63	32 47	19 44'7	'002	63	48	156	8'98	33 26	19 18'1	'027	297	26
108	10'84	32 48	19 48'9	'012	228	48	157	11'84	33 27	19 16'9	'012	211	20
109	10'02	32 49	20 12'8	'029	218	51	158	13'67	33 28	19 51'9	'010	264	19
110	13'76	32 49	20 0'2	'012	160	19	159	12'28	33 28	20 41'9	'009	69	19
111	12'95	32 50	20 4'2	'014	129	38	160	13'74	33 28	20 45'5	'014	249	3
112	12'12	32 51	20 3'8	'004	194	44	161	11'78	33 29	19 17'2	'085	246	20
113	13'57	32 52	20 36'1	'017	114	6	*162	10'82	33 29	19 28'0	'037	251	26
*114	8'07	32 52	20 20'4	'035	246	51	163	13'64	33 29	19 54'4	'010	259	19
115	13'79	32 52	20 15'0	'002	117	15	164	11'53	33 29	20 33'9	'035	240	20
116	12'55	32 52	19 51'8	'029	139	43	165	13'48	33 31	19 24'4	'018	180	13
117	10'77	32 53	19 59'9	'044	174	51	166	13'13	33 32	19 32'4	'007	180	21
118	13'48	32 54	19 39'5	'007	326	19	167	9'90	33 34	20 24'3	'035	136	51
119	13'44	32 54	19 29'0	'016	195	13	168	13'05	33 35	20 44'2	'007	297	13
120	13'15	32 56	19 16'8	'006	135	13	169	12'51	33 35	19 41'3	'006	239	38
121	11'38	32 59	20 23'1	'012	110	48	170	12'89	33 35	19 25'2	'017	128	13
122	12'35	33 1	19 55'6	'016	140	42	171	13'09	33 37	20 48'4	'011	326	10
123	13'01	33 2	20 46'8	'009	249	12	172	12'97	33 37	20 12'8	'035	250	38
124	8'76	33 2	19 51'1	'036	254	51	173	12'83	33 37	19 28'7	'012	115	11
125	13'83	33 3	20 17'2	'013	225	19	174	11'54	33 37	19 20'3	'003	180	23
126	13'46	33 3	19 55'1	'017	237	19	175	12'96	33 38	19 23'2	'008	194	11
*127	11'10	33 4	20 25'1	'036	249	48	176	13'21	33 39	20 25'8	'012	185	28
128	13'99	33 4	20 1'2	'011	326	11	177	13'55	33 40	19 30'9	'004	180	21
128a	13'74	33 6	19 38'1	'007	34	5	178	13'49	33 41	20 45'4	'003	45	10
129	12'01	33 6	19 55'9	'024	289	45	179	12'23	33 41	20 26'2	'007	164	45
130	11'46	33 7	20 22'2	'008	187	48	180	13'86	33 41	20 21'0	'004	90	15
131	12'81	33 7	19 25'0	'026	200	13	181	10'69	33 41	19 48'8	'037	247	51
132	13'63	33 8	19 32'4	'006	321	19	182	10'45	33 45	20 25'2	'035	253	50
133	12'59	33 8	19 26'1	'002	90	13	183	13'16	33 45	20 8'2	'036	245	38
134	10'57	33 11	19 33'0	'010	259	47	184	12'04	33 45	19 49'5	'037	246	44
135	11'87	33 13	20 3'0	'009	238	45	185	12'78	33 46	20 33'9	'007	236	18
136	12'68	33 14	19 36'4	'009	243	19	186	13'60	33 47	20 18'3	'006	270	22
137	13'16	33 15	19 23'2	'041	141	13	187	12'36	33 47	20 00'0	'005	281	44
138	11'07	33 15	19 46'5	'004	236	51	188	13'28	33 48	20 47'9	'033	164	10
139	12'73	33 16	20 21'5	'056	153	11	189	13'69	33 48	20 43'0	'023	247	8
140	13'10	33 17	20 8'8	'009	160	19	190	10'05	33 48	20 31'4	'017	280	51
141	13'00	33 18	19 40'7	'036	254	24	191	13'04	33 48	19 36'1	'033	162	38
*142	9'46	33 18	20 4'6	'036	243	50	192	10'78	33 49	19 38'9	'004	236	51
*143	8'51	33 18	20 21'1	'036	245	51	192a	13'68	33 50	19 15'9	'016	353	5
144	13'86	33 20	19 44'8	'009	96	8	193	12'96	33 50	20 21'7	'004	90	22
145	13'52	33 20	20 26'7	'017	123	8	194	12 88	33 50	20 21'6	'011	170	24
*146	9'45	33 20	20 28'2	'037	251	51	195	12 79	33 51	19 51'8	'015	302	44
147	13'13	33 21	19 16'4	'011	270	13	196	10'92	33 52	19 13'8	'034	256	23
148	11'49	33 21	19 23'8	'010	349	23	197	13'19	33 53	19 56'9	'018	180	31

25 prec. + 86 sec. — 5'1

25 prec. + 86 sec. — 5'1

1927PGro...41...1K

No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.			No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.		
				μ	ψ	Weight					μ	ψ	Weight
198	13'17	8 ^h 33 ^m 54 ^s	+ 19 47'6	0'037	257	26	245	13'06	8 ^h 34 ^m 19 ^s	+ 19 21'6	0'017	246	13
199	13'48	33 55	20 17'9	0'008	315	19	246	12'47	34 19	20 8'2	0'035	246	44
200	13'35	33 55	19 15'4	0'024	242	13	247	12'88	34 19	20 32'3	0'055	154	13
201	12'95	33 57	20 0'2	0'045	207	18	248	11'53	34 19	20 32'8	0'022	231	36
202	13'86	33 58	20 30'9	0'008	30	12	249	13'90	34 20	19 20'5	0'009	40	11
203	8'02	33 58	20 26'2	0'038	243	51	250	9'91	34 20	20 5'0	0'034	244	51
204	6'70	33 58	20 7'8	0'037	246	51	251	13'98	34 21	19 56'2	0'006	270	8
205	13'45	33 58	19 25'1	0'002	297	11	252	13'12	34 21	20 0'6	0'014	266	31
206	12'41	33 59	19 46'7	0'174	195	39	253	7'25	34 21	20 21'9	0'040	238	51
207	7'85	34 1	19 37'9	0'034	251	51	254	13'80	34 21	20 27'9	0'009	162	19
208	10'80	34 2	19 43'2	0'036	247	44	255	11'61	34 21	20 44'0	0'005	169	20
209	13'22	34 2	20 10'9	0'037	246	38	256	12'96	34 22	19 22'8	0'031	251	13
210	13'70	34 5	20 13'5	0'031	213	19	257	11'27	34 22	19 39'8	0'039	247	48
211	13'90	34 7	19 40'2	0'036	133	6	258	10'39	34 22	19 48'6	0'047	236	51
212	7'26	34 7	19 53'9	0'035	250	51	259	12'80	34 22	20 43'7	0'023	135	10
213	12'16	34 7	19 54'2	0'039	249	44	260	13'42	34 23	20 43'8	0'022	87	3
214	13'64	34 7	19 55'0	0'007	34	22	261	13'90	34 25	19 23'2	0'005	37	8
215	11'34	34 7	20 18'1	0'015	143	48	262	13'67	34 25	19 53'1	0'021	219	11
216	10'22	34 7	20 53'6	0'018	232	21	263	12'30	34 25	19 58'5	0'035	245	45
217	10'40	34 8	19 40'0	0'037	251	51	264	12'59	34 26	20 49'7	0'016	235	18
218	9'19	34 8	20 54'9	0'037	249	22	265	6'46	34 26	20 19'8	0'037	250	51
219	12'65	34 9	19 16'5	0'008	315	13	266	11'68	34 26	19 47'8	0'009	153	45
220	13'94	34 9	19 30'8	0'006	90	19	267	13'90	34 28	20 7'9	0'040	239	14
221	Var. ¹⁾	34 10	20 10'5	0'011	275	36	268	9'92	34 28	19 59'7	0'038	245	51
222	10'30	34 10	20 25'1	0'036	250	51	269	12'90	34 28	19 31'1	0'009	305	35
223	13'37	34 12	19 46'9	0'004	124	22	270	11'74	34 30	20 55'2	0'003	135	18
224	7'34	34 12	19 54'6	0'038	251	51	271	8'77	34 30	20 20'9	0'035	245	51
225	13'34	34 13	19 17'3	0'007	16	11	272	13'31	34 30	20 16'1	0'035	246	31
226	9'00	34 13	20 30'9	0'036	243	51	273	12'06	34 32	20 25'9	0'004	258	44
227	9'60	34 14	19 33'2	0'036	250	51	274	11'56	34 32	20 17'5	0'004	258	51
228	13'62	34 14	19 42'1	0'021	129	19	275	10'08	34 33	20 8'6	0'036	242	51
229	7'50	34 14	19 53'9	0'037	247	48	276	7'54	34 33	19 53'2	0'034	253	51
230	9'74	34 14	20 1'3	0'006	100	51	277	12'72	34 33	19 38'8	0'010	281	44
231	12'10	34 14	20 8'9	0'003	315	45	278	13'24	34 33	19 5'9	0'008	293	8
232	9'38	34 14	20 23'2	0'037	244	51	279	7'72	34 36	20 2'7	0'034	249	51
233	13'81	34 15	19 30'6	0'014	155	15	280	13'86	34 36	19 53'3	0'019	328	6
233a	14'19	34 15	19 41'9	0'030	100	5	281	12'53	34 36	19 23'2	0'018	204	19
234	9'94	34 16	19 17'9	0'020	267	26	282	10'06	34 37	20 27'8	0'036	255	51
235	12'59	34 16	19 41'3	0'033	175	44	283	7'10	34 37	20 1'6	0'041	241	51
236	12'44	34 16	19 55'2	0'035	248	44	284	6'76	34 37	19 42'2	0'033	252	51
237	13'42	34 16	19 55'9	0'034	248	38	285	13'14	34 38	20 46'0	0'005	307	51
238	10'36	34 16	20 9'7	0'036	250	51	286	7'81	34 39	20 11'5	0'038	247	51
239	9'76	34 16	20 29'4	0'035	248	51	287	10'56	34 39	20 1'8	0'036	243	48
239a	13'81	34 17	19 17'5	0'048	222	6	288	10'90	34 39	19 49'1	0'037	246	48
239b	14'08	34 17	19 40'7	0'012	9	6	290	12'79	34 41	20 53'4	0'069	203	13
240	13'06	34 17	20 8'4	0'011	270	38	291	10'38	34 41	20 44'4	0'093	180	26
241	12'82	34 17	20 16'1	0'017	234	44	292	8'45	34 41	20 32'2	0'039	242	51
242	12'70	34 18	19 14'2	0'020	213	13	293	9'97	34 41	19 49'9	0'036	250	50
243	12'63	34 18	20 52'1	0'016	166	10	294	13'48	34 41	19 23'1	0'004	346	13
244	10'42	34 19	19 21'2	0'036	254	26	295	9'37	34 42	20 2'5	0'036	247	51

¹⁾ HERTZSPRUNG, *Astronomische Nachrichten* 205, 33, 1917.

25 prec. + 86 sec. — 5'1

25 prec. + 86 sec. — 5'2

No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.			No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.		
				μ	ψ	Weight					μ	ψ	Weight
296	13 ^m 85	34 ^m 43 ^s	20 41.3	0.011	158	3	346	13 ^m 25	35 ^m 11 ^s	19 59.4	0.004	104	38
297	11 91	34 43	20 40.0	.037	247	20	347	12 ^m 73	35 11	20 13.1	.027	261	44
298	14 ^m 00	34 43	20 31.8	.008	263	6	348	7 ^m 11	35 12	19 56.0	.036	247	50
299	13 ^m 86	34 43	20 0.7	.041	241	16	349	12 ^m 47	35 12	20 5.2	.038	251	44
*300	6 ^m 33	34 43	19 54.1	.040	252	51	350	8 ^m 67	35 12	20 17.2	.039	246	51
*301	11 ^m 35	34 44	19 38.0	.036	254	48	351	13 ^m 78	35 14	19 50.1	.006	135	16
302	11 ^m 89	34 44	19 5.9	.021	194	18	352	13 ^m 30	35 16	20 13.9	.013	153	22
303	12 43	34 45	19 24.3	.031	216	20	353	12 ^m 46	35 16	20 48.8	.041	253	13
*304	11 ^m 84	34 46	20 33.3	.038	240	35	354	13 ^m 27	35 20	20 31.3	.002	27	16
305	12 ^m 06	34 46	20 16.4	.010	264	44	355	13 ^m 66	35 20	20 6.0	.034	12	14
306	13 ^m 75	34 46	19 45.8	.003	270	19	356	11 ^m 43	35 20	19 52.7	.009	291	45
307	13 ^m 37	34 46	19 22.9	.008	284	13	357	12 ^m 73	35 20	19 38.4	.016	266	44
308	13 ^m 26	34 46	19 21.9	.057	176	11	358	12 ^m 72	35 22	19 52.0	.002	27	44
*309	11 ^m 89	34 47	20 12.2	.035	245	45	359	13 ^m 78	35 23	19 57.7	.007	27	16
310	12 ^m 98	34 47	19 42.6	.012	138	38	360	11 ^m 76	35 23	19 43.5	.029	166	45
*311	10 ^m 71	34 47	19 18.5	.007	172	23	361	11 ^m 91	35 24	20 15.7	.023	311	45
312	13 ^m 01	34 47	19 16.2	.026	123	8	362	13 ^m 93	35 24	20 13.7	.018	137	18
*313	12 65	34 49	19 59.2	.040	248	44	363	12 81	35 24	19 48.0	.039	251	38
314	13 ^m 17	34 49	19 9.9	.002	180	13	364	13 ^m 42	35 24	19 32.8	.025	117	15
315	12 ^m 22	34 50	20 43.2	.012	156	19	365	10 ^m 48	35 24	19 25.6	.037	250	26
316	13 ^m 43	34 50	20 7.7	.005	169	22	366	13 ^m 48	35 25	20 25.9	.006	162	19
317	13 ^m 08	34 50	19 53.2	.010	174	38	367	10 ^m 84	35 25	20 12.6	.037	247	51
*318	8 ^m 60	34 50	19 33.0	.037	259	45	368	11 ^m 73	35 25	20 10.3	.036	248	45
319	14 ^m 04	34 50	19 30.0	.011	49	11	369	14 ^m 01	35 26	20 22.9	.004	225	11
320	12 ^m 48	34 52	19 32.4	.000	—	44	370	9 ^m 00	35 26	20 11.0	.038	248	51
321	11 ^m 48	34 53	20 15.4	.003	0	48	371	10 ^m 14	35 26	19 51.8	.036	249	51
*322	11 ^m 04	34 55	20 1.3	.037	250	48	372	13 ^m 03	35 27	20 28.3	.009	243	31
*323	8 ^m 00	34 56	19 34.9	.036	252	48	373	12 ^m 56	35 27	19 21.5	.010	186	19
324	10 ^m 80	34 57	20 55.4	.026	182	20	374	13 ^m 74	35 28	20 29.9	.014	78	19
*325	10 ^m 81	34 58	19 34.8	.037	257	51	375	8 ^m 24	35 28	20 16.6	.038	251	51
*326	11 ^m 63	34 58	19 55.2	.039	245	45	376	12 ^m 97	35 28	19 49.9	.013	148	38
327	11 ^m 84	34 58	20 22.1	.034	199	38	377	7 ^m 19	35 29	20 49.9	.004	166	21
328	7 ^m 08	34 59	20 4.3	.038	251	51	378	13 ^m 85	35 30	19 16.3	.010	96	11
329	13 ^m 62	34 59	20 19.2	.002	117	19	379	11 ^m 88	35 30	19 9.9	.012	265	12
330	13 ^m 55	34 59	20 52.1	.010	0	8	380	13 ^m 66	35 32	19 57.0	.004	194	12
331	13 ^m 76	35 1	20 8.0	.003	90	19	381	13 ^m 76	35 32	19 49.9	.023	239	19
*332	9 ^m 63	35 2	19 39.9	.037	247	51	382	13 ^m 27	35 32	19 29.8	.006	288	17
333	10 ^m 86	35 3	19 53.9	.002	207	51	383	13 ^m 78	35 32	19 22.8	.028	0	6
*334	11 ^m 31	35 3	20 0.9	.038	245	48	384	13 ^m 03	35 32	19 10.0	.007	106	13
*335	11 ^m 28	35 3	20 16.6	.034	251	48	385	8 ^m 01	35 35	19 36.9	.037	247	50
336	11 ^m 81	35 4	19 15.4	.037	247	20	386	11 ^m 54	35 35	19 9.3	.002	180	18
337	12 ^m 73	35 6	19 11.0	.007	236	13	387	11 ^m 88	35 37	20 20.1	.005	217	45
338	11 ^m 56	35 6	19 29.0	.018	96	20	388	13 ^m 12	35 38	19 21.8	.012	119	13
339	13 ^m 76	35 6	20 10.9	.003	225	19	389	13 ^m 64	35 39	20 37.2	.013	157	11
*340	8 ^m 56	35 7	20 37.1	.032	242	26	390	13 ^m 38	35 40	19 17.2	.040	254	8
*341	10 ^m 49	35 8	19 50.2	.038	247	51	391	13 ^m 28	35 41	20 45.9	.010	84	11
342	13 ^m 02	35 9	20 13.8	.008	120	42	392	10 ^m 92	35 41	20 17.9	.035	250	51
343	13 ^m 43	35 10	19 32.2	.007	344	11	393	14 ^m 06	35 41	19 55.2	.005	90	10
344	12 ^m 48	35 10	20 17.3	.037	246	35	394	12 ^m 91	35 41	19 10.8	.105	199	13
345	13 ^m 58	35 11	19 50.0	.014	188	18	395	13 ^m 58	35 42	20 35.9	.009	220	6

25 prec. + 86 sec. — 5'2

25 prec. + 86 sec. — 5'2

No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.			No.	Phot. Magn.	α_{1900}	δ_{1900}	Abs. Prop. Mot.		
				μ	ψ	Weight					μ	ψ	Weight
396	9.84	35 ^m 43 ^s	19 53.9	0.038	248	51	446	12.26	36 ^m 26 ^s	20 30.1	0.015	259	44
397	11.70	35 44	19 43.6	.019	242	42	447	12.44	36 27	20 30.9	.022	201	44
398	11.77	35 44	20 32.6	.002	297	38	448	12.66	36 28	19 38.0	.040	252	44
399	11.06	35 45	20 6.1	.041	250	46	449	8.12	36 28	19 17.5	.031	255	24
400	11.50	35 47	19 52.9	.012	241	48	450	12.43	36 31	20 31.7	.028	100	44
401	13.23	35 48	19 13.6	.038	241	13	451	13.82	36 31	20 24.5	.005	259	19
402	13.28	35 48	19 21.9	.003	180	13	452	12.41	36 31	20 5.2	.024	109	44
403	11.94	35 49	20 19.4	.039	251	45	453	13.72	36 31	20 4.0	.011	255	11
404	12.64	35 50	20 5.2	.006	180	44	454	9.96	36 31	20 2.7	.039	252	51
405	12.21	35 51	19 17.4	.008	173	20	455	13.17	36 32	19 58.4	.016	240	31
406	12.90	35 51	19 53.5	.006	171	38	456	12.55	36 33	20 46.1	.033	250	19
407	9.26	35 51	20 1.0	.025	222	51	457	11.26	36 33	20 4.9	.015	247	48
408	11.94	35 51	20 3.4	.011	142	44	458	9.80	36 35	20 23.7	.036	255	50
409	13.07	35 51	20 39.4	.006	219	13	459	9.22	36 36	20 32.2	.035	254	38
410	12.46	35 51	20 47.0	.003	135	19	460	12.40	36 37	20 28.5	.029	239	35
411	9.33	35 53	19 29.9	.040	252	40	461	11.43	36 37	20 38.6	.009	198	20
412	12.08	35 53	20 45.8	.015	222	20	462	11.09	36 40	19 56.8	.047	190	46
413	12.52	35 54	19 24.3	.015	132	19	463	12.06	36 42	20 37.8	.003	252	19
414	13.05	35 54	20 33.8	.012	189	13	464	13.62	36 47	19 21.0	.009	58	11
415	13.58	35 55	19 37.2	.036	260	18	465	14.20	36 47	20 6.8	.014	231	1
416	9.58	35 58	20 0.9	.039	249	51	466	11.21	36 49	19 45.2	.043	246	40
417	12.68	35 58	20 19.0	.037	257	44	467	13.13	36 49	20 16.8	.015	122	19
418	10.59	35 58	20 34.9	.038	243	26	468	13.16	36 50	19 52.2	.013	312	6
419	13.04	36 0	19 37.6	.016	356	38	469	12.61	36 52	19 20.0	.009	167	13
420	12.80	36 0	20 1.9	.012	180	43	470	12.50	36 54	19 32.0	.002	297	19
421	10.29	36 2	19 37.4	.038	253	51	471	12.43	36 57	19 29.3	.036	248	19
422	13.76	36 2	19 55.7	.005	202	14	472	9.91	36 57	19 54.0	.038	250	26
423	11.36	36 3	19 29.2	.018	186	23	473	13.63	36 58	19 57.2	.014	274	11
424	12.08	36 4	19 42.1	.008	210	45	474	12.64	36 59	19 58.9	.038	245	19
425	11.43	36 4	19 46.0	.029	252	48	475	12.98	36 59	20 3.2	.006	219	13
426	13.19	36 5	19 12.5	.009	125	13	476	11.86	36 59	19 27.4	.039	243	20
427	11.94	36 5	19 39.9	.015	270	44	477	12.22	37 1	20 21.5	.024	204	20
428	7.54	36 6	20 13.8	.041	241	50	478	9.72	37 1	19 56.2	.036	249	26
429	8.34	36 7	20 30.9	.036	259	48	479	13.17	37 1	19 40.7	.034	153	13
430	12.34	36 7	20 31.3	.036	258	40	480	11.58	37 1	19 24.2	.012	125	17
431	13.09	36 10	19 37.1	.007	135	31	481	13.57	37 2	19 59.9	.007	344	11
432	11.14	36 11	20 2.8	.036	250	51	482	12.32	37 3	20 42.8	.001	180	13
433	10.99	36 11	19 59.4	.008	187	48	483	13.84	37 4	19 58.1	.019	141	6
434	11.64	36 11	19 36.8	.036	254	45	484	11.98	37 4	19 49.5	.004	194	20
435	11.98	36 11	19 35.2	.011	236	44	485	12.22	37 6	19 41.9	.011	243	19
436	12.93	36 14	20 42.9	.010	241	11	486	13.52	37 10	20 12.6	.013	312	11
437	14.06	36 14	20 21.6	.014	295	6	487	13.72	37 13	20 2.3	.008	256	11
438	12.66	36 15	20 16.2	.016	292	35	488	11.48	37 15	20 41.8	.034	260	17
439	9.54	36 15	19 16.0	.034	256	26	489	11.86	37 17	20 1.2	.031	157	19
440	12.32	36 17	19 47.0	.003	162	45	490	13.07	37 17	19 53.6	.010	299	13
441	13.98	36 18	20 9.2	.005	217	6	491	12.46	37 19	19 48.7	.004	90	19
442	14.09	36 19	19 51.2	.018	311	8	492	12.41	37 19	19 31.6	.034	246	14
443	11.13	36 21	19 57.4	.038	191	51	493	10.94	37 21	19 57.2	.001	0	26
444	13.13	36 22	19 35.3	.004	135	38	494	12.12	37 21	19 39.0	.020	276	20
445	8.10	36 23	19 46.0	.040	245	48	495	10.08	37 22	19 47.8	.035	251	20

+ 25 prec. + 86 sec - 5.2

25 prec. + 86 sec. - 5.3

