

GREENWICH

ASTRONOMICAL OBSERVATIONS,

1870.

INTRODUCTION.

I. Personal Establishment and Arrangements.

At the beginning of the year 1870, the establishment of Assistants in the Astronomical Department of the Observatory consisted of the following persons:—Edward James Stone, Esq., M.A., F.R.S., Fellow of Queens' College, Cambridge, First Assistant; Mr. Edwin Dunkin, Mr. William Ellis, Mr. George Stickland Criswick, Mr. William Thynne Lynn, B.A. Univ. London, and Mr. James Carpenter. In the summer of 1870 Mr. Stone resigned the office of First Assistant on his appointment as Her Majesty's Astronomer at the Cape of Good Hope, and was succeeded by Mr. William Henry Mahony Christie, B.A., Fellow of Trinity College, Cambridge.

The duties of the establishment are distributed in the following manner:—

The First Assistant, in the absence of the Astronomer Royal, is empowered to act in all respects as his representative, and to conduct confidential as well as routine business. In the ordinary transactions, the First Assistant superintends the calculations generally; and observes, occasionally, with any of the instruments. The observations made by Mr. Stone are distinguished by the signature S. Those made by Mr. Christie are signed W. C.

Mr. Criswick is charged with the observations necessary for the determination of the errors of division, of the form of the pivots, and of the flexure of the telescope, of the Transit-Circle. Mr. Lynn has the superintendence of the Altazimuth, which is specially devoted to extrameridional observations of the Moon. The ordinary observations with both these instruments have been generally made by Mr. Ellis, Mr. Criswick, Mr. Lynn, and Mr. Carpenter; occasionally observations have been made by Mr. Dunkin. The initials of these observers are E., C., L., J.C., and D. Other persons who have occasionally observed with these instruments are:—Mr. Henry James Carpenter, Mr. Gabriel Keating, Mr. Joseph Pyle Potts, and Mr. Charles Augustus Jenkins, who are employed as computers in the Observatory; their signatures are H.C., K., P., and J.

The observations with the South-East, or Great Equatoreal, are generally made by Mr. Carpenter. Miscellaneous observations with the other Equatorials are not distinctly appropriated to any special observers.

The management of the Galvanic Apparatus for Chronographic Registry of Transits, movement of sympathetic clocks, and external distribution of time-signals; the receiving, issuing, and rating of Chronometers; the raising of the Time-Signal Ball at 1 o'clock; and the computations belonging to the same; are intrusted to Mr. Ellis.

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With regard to the Reduction of the Observations.—The First Assistant is always charged with the duty of making the examination of observations, as entered in the Books of First Calculations, in order to ascertain that no error has crept into the records of individual wire-transits or individual microscope-readings; and with the adoption of Clock-rates, instrumental zeros and instrumental errors. Mr. Dunkin superintends the reduction of the Transit-Observations, and the Results of the Meridional Observations, and the reading of the proof-sheets of these observations and reductions when printed. Mr. Dunkin is also charged with the general superintendence of the supernumerary computers of the astronomical department; by whom the great mass of calculations and of reading proof-sheets is effected. Mr. Criswick translates the chronograph-barrel-readings into figures. Mr. Criswick and Mr. Lynn respectively superintend the reduction of Circle-Observations and Altazimuth-Observations, and the reading of the proof-sheets of these observations and reductions when printed.

Mr. Ellis arranges the Money Accounts of the Observatory.

Mr. Carpenter has the general charge of the Observatory Library and Manuscripts.

The whole of these works are under the immediate direction of the Astronomer Royal, who is responsible for every part.

Correspondence relating to the affairs of the Observatory, not transacted by the Astronomer Royal himself, is managed under his general or special instructions.

The course of observations and the succession of observers are arranged every Monday by the First Assistant and sanctioned by the Astronomer Royal. In general, the Assistant who makes the observations with the Transit-Circle is charged with all the observations that may occur from 15^h mean time (3 o'clock in the morning) to the next 15^h; although it is sometimes found necessary (especially during the latter part of the Lunation, when the Moon passes the meridian in early morning) to appoint separate observers for the morning and the evening. It is established as a rule, to be adhered to as closely as circumstances permit, that no Assistant be occupied on two successive days with astronomical observations. And it is always arranged, if possible, when the Moon's time of transit passes 15^h, that the same Assistant should not be required to observe the Moon and accompanying stars late in the night when the Moon passes last before 15^h, and early in the morning when the Moon passes first after 15^h.

In October 1863, a convention was made with M. Le Verrier (since renewed with his successor M. Delaunay), under which the Observatory of Greenwich is charged with the meridional observations of the Asteroids from new moon to full moon, the Imperial Observatory of Paris being charged with their observation from full moon to new moon. Since this arrangement has come into effect, the aid of the additional observer, previously necessary for the evening observations, when the Moon passed the meridian in early morning, has not often been required; it is found at the same time that all requisite observations can be made without greatly increasing the labour of the observer.

For many particulars relating to the internal constitution of the Observatory, reference may be made to the "Regulations of the Royal Observatory," forming Appendix II. to the *Greenwich Observations*, 1852.

II. Instruments.

The principal Instruments used by Halley, Bradley, Bliss, and Maskelyne, are still preserved in the Royal Observatory: namely, Halley's Transit, with pivots unequally distant from the Telescope; Bradley's Transit; Bradley's small Equatoreal; the Zenith Sector of Bradley and Maskelyne; and the two Mural Quadrants, mounted on their pier, the Quadrant on the Western side of the pier being now included in the smaller fire-proof room of the Observatory. The ancient instruments first mentioned, together with the Telescopes for investigating the parallaxes of α Aquilæ and α Cygni, formerly attached respectively to the West side of the pier of Troughton's Mural Circle, and to the Quadrant pier, are now, with proper labels, suspended on brackets on the Western wall of the Transit-Circle Room.

Troughton's Transit Instrument and Mural Circle, used to the end of the year 1850, were dismantled in the year 1851, and are suspended, the one on the West and the other on the East wall of the Transit-Circle Room. The object-glass of the Transit Instrument is now inserted in the Reflex Zenith-Tube.

The 25-foot Zenith-Sector was dismantled, and its tube was divided (at its joints) into several parts, in May 1848; and the separate portions of the instrument are stored away in frames constructed to hold them. The object-glass, as will shortly be mentioned, was removed from the tube in 1850, to be used for the Collimator of the Altazimuth.

Jones's Cape Circle was transferred in November 1851 to the Observatory of Queen's College, Belfast.

The Instruments now in use are the following:—

The Transit-Circle, constructed by Messrs. Ransomes and May, as engineers, and by Mr. Simms, as optician, erected in the year 1850, and brought into use at the beginning of 1851.

The room in which this instrument is mounted occupies the site of the old Circle Room, but is extended to the south, so that its entire length is 36 feet. The ridge of the roof is in the north-and-south direction. The opening in the roof, along the ridge, is 3 feet wide, and is covered by four shutters: the vertical openings, in the north and south walls, are also 3 feet wide, and each is covered by a single shutter. Any one of the shutters can be opened without disturbing the others.

A detailed description of the instrument, illustrated by plates, is given in Appendix I. of the volume for 1852: a reprint of which, with some modifications, is attached to the volume for 1867. The following particulars may be given here. The center of the instrument is about $5\frac{1}{2}$ feet South and 19 feet East of the old transit-instrument. The length of its telescope is nearly 12 feet, and the clear aperture of the object-glass is about 8 inches. The length of the axis between

the extremities of the pivots is 6 feet. The axis of the instrument is of cast iron, in two similar pieces: each half includes half the central cube, one cone, and the pivot which terminates it. The mould of the pivot was made of iron, for the purpose of hardening it by the process technically called *chilling*; the moulds for the other parts were sand. The two halves are connected by bolts through flanges at the junction-plane in the middle of the cube. The two portions of the telescope-tube (also of cast iron, with the exception of the object-glass cell and the eyepiece-work) are bolted on the cube. The diameter of each pivot is 6 inches. For examination of the form of the pivots, each is perforated; within the hollow of the eastern pivot there is fixed a plate of metal perforated with a hole about 0.01 inch in diameter, behind which a light can be placed for illumination; at the distance of 6 inches from this hole is a lens of 1 inch focal length, producing an image of the hole about 0.002 inch diameter, which in fact is the real mark for collimation; and in the hollow of the western pivot there is fixed an object-glass at a distance from that image equal to its focal length. This combination forms a reversed telescope revolving with the instrument. It is viewed by a telescope of 7 feet focal length, which, when required, is placed on Y's, one of them planted in the opening of the western pier, and the other in a hole made for that purpose in the western wall of the room.

On 1866, June 28, observations were made for the determination of the relative errors of the form of the pivots of the Transit-Circle. The process employed is fully explained in Appendix I. of the volume of *Greenwich Observations* for 1852. The following table contains the residual errors, which define the apparent changes of position of a certain imaginary line in the material axis of the instrument.

N. P. D. Pointer Reading.	Error at Inclina- tion of 45°, Microme- ter Head Above and South.	Error at Inclina- tion of 45°, Microme- ter Head Above and North.	N. P. D. Pointer Reading.	Error at Inclina- tion of 45°, Microme- ter Head Above and South.	Error at Inclina- tion of 45°, Microme- ter Head Above and North.	N. P. D. Pointer Reading.	Error at Inclina- tion of 45°, Microme- ter Head Above and South.	Error at Inclina- tion of 45°, Microme- ter Head Above and North.	N. P. D. Pointer Reading.	Error at Inclina- tion of 45°, Microme- ter Head Above and South.	Error at Inclina- tion of 45°, Microme- ter Head Above and North.
0 /	"	"	0 /	"	"	0 /	"	"	0 /	"	"
2. 30	+0.09	+0.61	92. 30	+0.39	-0.74	182. 30	+0.20	-0.08	272. 30	+0.29	+0.60
7. 30	-0.28	+1.02	97. 30	+0.34	-0.54	187. 30	-0.36	-0.13	277. 30	+0.50	+0.36
12. 30	-0.60	+0.62	102. 30	+0.18	-0.43	192. 30	-0.35	-0.32	282. 30	+0.27	-0.38
17. 30	-0.26	+0.72	107. 30	+0.15	+0.18	197. 30	-0.48	-0.28	287. 30	+0.06	-0.14
22. 30	-0.02	+0.28	112. 30	-0.07	+0.44	202. 30	-0.09	-0.50	292. 30	0.00	+0.20
27. 30	+0.07	+0.73	117. 30	-0.22	+0.07	207. 30	+0.14	-0.29	297. 30	+0.02	+0.23
32. 30	-0.04	+0.25	122. 30	-0.19	-0.42	212. 30	+0.13	-0.07	302. 30	+0.01	+0.31
37. 30	-0.27	+0.01	127. 30	-0.16	-0.59	217. 30	-0.42	+0.19	307. 30	-0.01	+0.05
42. 30	-0.38	+0.01	132. 30	-0.08	-0.12	222. 30	-0.57	+0.22	312. 30	-0.08	-0.34
47. 30	-0.35	+0.23	137. 30	-0.17	+0.28	227. 30	-0.37	-0.18	317. 30	-0.28	-0.66
52. 30	+0.16	+0.18	142. 30	-0.23	+0.57	232. 30	+0.13	+0.20	322. 30	-0.11	-0.56
57. 30	+0.24	-0.08	147. 30	-0.01	+0.13	237. 30	+0.18	+0.06	327. 30	-0.01	+0.21
62. 30	+0.09	-0.09	152. 30	-0.03	-0.31	242. 30	+0.21	-0.19	332. 30	+0.20	+0.50
67. 30	0.00	-0.24	157. 30	-0.11	-0.49	247. 30	-0.17	-0.18	337. 30	+0.17	+0.30
72. 30	-0.35	-0.05	162. 30	+0.18	-0.62	252. 30	-0.45	-0.13	342. 30	+0.74	-0.66
77. 30	-0.49	-0.12	167. 30	+0.27	+0.20	257. 30	-0.43	+0.17	347. 30	+1.00	-0.82
82. 30	-0.03	-0.50	172. 30	+0.46	+0.30	262. 30	-0.13	+1.36	352. 30	+0.59	-0.57
87. 30	+0.07	-0.38	177. 30	+0.48	+0.55	267. 30	+0.25	+0.41	357. 30	+0.55	-0.56

These observations agree with those previously made, in not assigning any appreciable error to the form of the pivots.

The wire frame contained originally (besides the horizontal wire, to be noticed shortly) seven vertical wires, adapted to observations of transits by eye-and-ear; to which six were added in the spring of 1854, for more convenient use in the observations of transits by galvanic contact: the whole frame and whole system of vertical wires are moved horizontally by a micrometer-screw, whose graduated head is locked up in a small box attached to the eyepiece, to prevent inadvertent disturbance of the micrometer after it has been set to the reading which is adopted for the line of collimation. The micrometer-head is on the eastern side of the eyepiece, and the readings increase as the wire is moved towards the micrometer-head. The field of view is illuminated by the light from a central gas-light (to be mentioned hereafter), which enters the axis and is reflected by an internal annular reflector; by inclining the reflector, the illumination is diminished and finally destroyed; and by inclining it still more, the light is thrown in such a manner as to illuminate the wires, leaving the field dark. The intensity of illumination of the wires was, in the original construction of the apparatus, practically constant: but in 1865, October, an apparatus was introduced by which the intensity of the light is graduated with great delicacy.

For determining the error of collimation, two horizontal telescopes of about 6 feet 10 inches focal length and 7 inches aperture, with their object-glasses turned towards the center of the instrument, are mounted on Y's which are carried by massive brick piers, one on the north and one on the south side of the transit-circle. The height of the axes of these telescopes is as nearly as possible the same as that of the axis of the transit-circle. External reflectors are provided, by which the light of the sky is directed into the eye-ends of these reversed telescopes. Each telescope is furnished with wires in its principal focus, to be used as collimating marks; and each telescope may be used as presenting a distinct mark for the other, or for the transit-circle-telescope. The system of wires is the same in both, consisting of two parallel wires inclined to the vertical at an angle of about $2\frac{3}{4}^{\circ}$, two other parallel wires at right angles to the former, and therefore inclined to the horizontal line at the same angle (the intersection of this pair with the former producing a square), and a fifth wire parallel to the two last mentioned, and at a distance from the nearest of about ten times the side of the square. The middle of that portion of the nearly horizontal fifth wire which is included by the two nearly vertical wires, is in the same vertical with the middle of one of the nearly vertical sides of the square; and these middle points are the points adopted for observation. Those wires are finer than the others. For adjustment of these North and South Reversed Telescopes accurately on each other, the plates carrying the wires are moveable by micrometer-screws: that of the South Telescope in altitude only, and that of the North Telescope in azimuth only. Each micrometer-head, when not in use, is locked up in a box attached to the eyepiece. In order to view either telescope by the transit-circle-telescope, it is only necessary to direct the transit circle-telescope towards that telescope; but in order to view one telescope by the other

it is necessary to place the transit-telescope vertical, and to uncover the perforations in the opposite sides of its central cube, which permit one Reversed Telescope to view the other through eight holes of sector-form in those perforations. This apparatus was mounted and brought into use on 1866, December 17. To obtain a somewhat more perfect view of one Reversed Telescope by the other, it is necessary to raise the transit-circle so far that there shall be no impediment to a direct view. A mechanical apparatus is provided for the express purpose of sufficiently raising the transit-circle.

The process of adjusting the Reversed Telescopes, and of using them for determining the line of collimation of the Transit-Circle-Telescope, is as follows :—

The transit-telescope being placed in proper position, and illumination being given to the South Telescope, the eye is applied to the eyepiece of the North Telescope, and the systems of wires in both are distinctly seen: the nearly vertical wires of one being inclined about $5\frac{1}{2}^{\circ}$ to those of the other. By means of the micrometer screw of the North Telescope, the middle of one nearly vertical side (the fine-wire side) of the square of the North Telescope is made to coincide with the image of that of the South Telescope, and the micrometer-reading is taken. This operation is usually repeated six times, and, the mean of all the readings being found, the micrometer is left in the position indicated by that mean. The geometrical line in each telescope, passing through the focal center of its object-glass and through the adopted point of the delicate wire, being considered as the axis of the telescope, it is plain that, in the positions in which the wires are thus left, the axes of the two telescopes are in the same line, or at least are strictly parallel to each other: and, therefore, when the transit-telescope is employed to view the wires in the two telescopes, the images of the adopted points of their wires in all respects represent two objects at infinite distance and exactly opposed to each other.

This operation is performed whenever, for the purpose of cleaning the pivots, &c. (which is usually done on every Monday), the instrument is raised; and these opportunities are preferred, as the wires are then seen very sharply defined. On other days, however, upon placing the transit-telescope vertical and uncovering its apertures, the wires are very well seen; and the coincidence of the images of the wires of the two Reversed Telescopes is therefore examined every day.

The daily observation for collimation of the transit-telescope is then made by bringing, by means of its micrometer, the central vertical wire several times in succession upon the proper point of the image of the nearly vertical fine wire of the North Telescope, and several times upon the corresponding point of the South Telescope, and reading the micrometer for each coincidence. The mean of the readings for the North and South Telescopes gives the reading for the position of the line of collimation. The observation admits of extreme accuracy, since the eye can judge with great delicacy of the equality of the two acute-angled triangles formed by the central transit-wire and the collimator-wire in the process of observation.

Tables of the micrometer-readings of the South Telescope-wire for coincidence with North Telescope-wire, and of the daily readings of the Transit-Micrometer

for coincidence with the wires of both telescopes, are given at the end of the section of printed Transit Observations.

The instrument is not well adapted to the application of a spirit-level or other contrivance for determining the difference of level of the surfaces of the pivots. The error of level is ascertained by the use of a Bohnenberger's eyepiece, with three lenses, and a transparent glass reflector whose surface makes an angle of 45° with the axis of the eyepiece, and which is placed between the lowest lens and the wires of the telescope. A beam of light being thrown horizontally upon the reflector, and a trough of quick-silver being placed below the object-glass of the telescope, the image of the central wire is seen by reflexion at the same time as the wire itself; by means of the micrometer-screw the images are made to coincide, or to touch alternately on the two sides; the mean of the micrometer-readings is taken; and the difference between the mean reading and the reading corresponding to the line of collimation is the error of level. This process is perhaps in every case preferable to the use of a spirit-level.

The graduated vertical circle for zenith-distance-observations is fixed on the cylindrical basis of the axis-cone on the west side of the central cube. It is of cast iron, 6 feet in diameter, and has two sets of divisions: one set, on its western side, cut upon a band of silver, which is let into a dished or flat internal conical surface, is accurately divided to five-minute spaces, and is read by the microscopes; the other set, on its eastern side, is roughly divided by points to every $5'$, and is intended for setting the telescope to any object by means of two pointers reading respectively North Polar Distances and Zenith-Distances. The reading microscopes, six in number, are simply inclined perforations through the western pier; having their eyepieces at the back of the western pier arranged in a circle whose center is 5 feet 2 inches above the floor, and diameter about 21 inches; and their object-glasses on the inner or eastern side of the pier, arranged in a circle of about 5 feet in diameter, pointing to the graduations of the circle. The pointer-microscope is between the two lowest reading-microscopes, and is a similar inclined perforation through the pier: it has a large field of view, and is furnished with a single wire parallel to the graduations of the limb at which it is pointed. The divisions under the microscopes are illuminated by means of a central gas-light in the central opening at the external surface of the western pier, which throws light upon the proper divisions through seven illuminating holes (each furnished with a lens) corresponding to the seven microscopes; and this light is reflected from the graduated limb accurately into the microscopes without any need of illuminating-reflectors; the inclination of the graduated limb being that which causes the light, on the usual law of specular reflexion, to enter the microscopes parallel to their axes. A lining of double tin plates (fixed on 1860, November 26) is inserted in the central opening of the pier, which effectually screens, from the radiation of the gas flame, the stone pier, the micrometers and their eyepieces, and the brass plate which carries them.

The circle is completely shielded from the Sun's rays by the steps which are used by the observers for ascending to the upper part of the pier.

There are two clamps attached to the eastern pier, at the same height as the center of the circle (one on the north side, the other on the south side), which can take hold of the clamping circle of the instrument; but they have no slow motion. The eyepiece of the telescope contains only one horizontal wire, moveable by a micrometer, with which all observations of zenith-distance are made. For reducing every observation, therefore, it is necessary to combine the value of the reading of the telescope-micrometer with that of the mean of readings of the microscope-micrometers. When the telescope points vertically upwards, the head of the telescope-micrometer is on the north side; and the telescope-micrometer-readings increase as the wire is moved towards the head. The reading 20^{rev} corresponds nearly to the center of the field of view.

The reading (consisting of the combination of telescope-micrometer-reading and mean of microscope-readings), corresponding to the nadir-position of the telescope, is found by the use of the Bohnenberger's eyepiece and the trough of mercury; the direct and reflected images of the horizontal wire being made to coincide or to touch alternately on the two sides, and the mean of the readings of the micrometer being taken.

Other explanations necessary for the understanding of the process of reduction of the observations will be given under the proper heads. In this place it may be useful to explain briefly the methods employed in making the various classes of observations which are required.

For star-observing generally, the telescope is directed approximately towards the object by the indications of the N.P.D. pointer, and, the telescope being moved by hand till the star is brought near the horizontal micrometer-wire at or near the reading of 20^{rev} , the clamping circle is fastened. The transit of the star is then observed over the vertical wires in the usual way, either by galvanic touch or by eye and ear; and, during the transit, by means of the micrometer-screw which acts on the horizontal wire, that wire is made to bisect the star near the passage of the central vertical wire, if practicable. The telescope-micrometer, and the pointer and the six microscope-micrometers, are afterwards read, and the observation is complete. If the star be too faint to allow of illumination of the field, the wires are illuminated, and the observation is made in a field perfectly dark.

For observations of stars by reflexion, the telescope is placed, some minutes previously to the transit of the star, in the direction which is proper for viewing the reflected image of the star; and the mercury-trough is carefully placed in the requisite position, and the microscope-micrometers are read after the instrument is clamped. The observer then ascends to the eyepiece of the telescope, and, by means of the micrometer-screw which carries the horizontal wire, bisects the reflected image of the star near the passage of the first vertical wire (if the star has large polar-distance), or near the second or third wire (if the star is circumpolar), and reads the telescope-micrometer. He then descends rapidly into the pit, unclamps the instrument, turns the telescope to the position proper for direct view of the star, and fastens the clamping circle; bisects the star near its passage over one of the vertical wires by

means of the micrometer-screw, and completes the direct observation in the usual way by reading the telescope-micrometer and the microscope-micrometers.

In observing the Sun, the transits of both limbs are taken for Right Ascension, and observations are made both of the upper and lower limb for North Polar Distance, in the following manner. The observer at the telescope is aided by two assistants (usually two of the supernumerary computers), who are stationed in readiness to read the microscope-micrometers. After the transit of the first limb is completed, the telescope is moved by hand till one of the limbs (upper or lower) is brought near to the horizontal wire, when near the reading 20^{rev} ; then the instrument is clamped, and the horizontal wire is moved, by means of the micrometer-screw which carries it, to touch the limb while passing one of the vertical wires (the No. of which is registered). The telescope-micrometer is then read by the observer, and the microscope-micrometers by the assistants, who in fact had commenced to read the micrometers as soon as the instrument was clamped. The instrument is then unclamped, the telescope is directed to the other limb (lower or upper), the instrument is clamped, the telescope-micrometer is turned to place its wire upon the limb, and the micrometers are all read again. Finally, the instrument is unclamped, and the transit of the second limb over the vertical wires is taken. This operation requires readiness and expertness in the observers; but, when the transits are made by galvanic touch, it is found perfectly easy to take those of the first and the second limb over all the nine wires, still leaving time enough for the observations of both limbs in N.P.D.

For the Moon before opposition, (that is, when the transit of the first limb is observed,) after the transit is completed, the telescope is moved till the limb (upper or lower), which is to be observed in Zenith Distance, is brought near to the middle of the field; the instrument is clamped; and the horizontal telescope-micrometer-wire is brought repeatedly upon the limb (upper or lower) at its passage over the seven original vertical wires at wide intervals, the telescope-micrometer being read after each contact of the wire with the limb. The microscope-micrometers are afterwards read, and the observation is complete.

After the opposition in Right Ascension, the setting for the full limb (upper or lower) is accurately computed beforehand; the instrument is set with care, and is clamped; and the microscope-micrometers are read previously to the passage. The telescope-micrometer is then read for the contact of the wire with the limb at the passage of each of the vertical wires, as explained above; then the clamp is relaxed, and the telescope is turned by hand to a position proper for observing the transits of the second limb in Right Ascension; and, the transits over the vertical wires being taken, the observation is complete.

When both the upper and the lower limbs are so nearly full as to admit of observation, as also when the first and second limbs are very nearly full at the opposition of the Moon, another person is employed to read the microscope-micrometers as in the case of the Sun; and the mode of observation will be readily understood from the

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preceding explanations, applying to the observation of the Sun. In this case, however, the aid of one person is sufficient.

The Chronograph.—In the year 1854 an apparatus was connected with the Transit-Circle for the purpose of registering transits according to the Chronographic method, by means of a galvanic circuit. A detailed account of this apparatus, illustrated by engravings, is given in the Appendix to the Volume for 1856:—in this place it may be desirable to give such a description of the chief parts of it as is necessary for explanation of the observations and of the notes appended to them.

In the ground-floor room of the North Dome, there is mounted a clock of peculiar construction, whose motion is governed by the conical rotation of a pendulum. (In the original construction of this instrument, the limitation of the radius of the conical arc depended only on the resistance of the air, or on contact with a light spring: in 1860 an apparatus was introduced which, as the radius of the arc increases, dips a revolving plate deeper into an annular trough of water, and thus supplies the required resistance, without affecting the centripetal force upon the pendulum.) One spindle of the clock gives motion to a revolving brass barrel, about 20 inches long and 12 inches in diameter; and, as the clock with conical pendulum moves without jerks, the brass barrel revolves without jerks, and with a motion sensibly uniform. The barrel revolves in two minutes of time; its cylindrical surface, therefore, moves through 0·3 inch nearly in one second of time. The barrel is covered with woollen cloth, and upon this a sheet of paper is folded; the ends of the sheet are cemented together; when the sheet is filled by the register about to be described, the cement is softened, the paper is removed, and another sheet of paper is put in its place.

Another spindle of the clock turns two long screws, both parallel to the axis of the barrel, which cause a travelling-frame to traverse the whole length of the barrel. In one revolution of the barrel, the frame moves through 0·1 inch. This travelling frame carries two levers, and each lever is armed at one end with a pricking point; the mounting of each lever being such that, when the opposite end of the lever is pulled away from the barrel, the pricking end is impressed upon the barrel, and makes a permanent puncture on the paper. The prickers are mounted in such a way that, when their points have entered the paper, they yield laterally to the motion of the revolving barrel, and do not scratch the paper. Two galvanic magnets are fixed on the travelling frame, so as to attract the lever-ends opposite to the pricking points. All that is required, therefore, to cause these points to make punctures upon the paper, is, to send galvanic currents through the galvanic magnets.

One of the prickers is devoted to the register of seconds of the transit-clock. For this purpose, the wires of its galvanic magnet (after passing through a galvanic battery) are led to the transit-clock, and the circuit is there completed at every second of time by the following mechanism. Upon the escape-wheel-arbor, a wheel of 60

teeth is mounted; and, at every second, the start of a tooth of this wheel presses together two springs, during a very small fraction of a second. (There is also another pair of springs driven into contact by the same wheel-teeth, used for the sympathetic system of chronometers, as will be mentioned hereafter, in the last paragraph of this section.) Thus a series of punctures is made upon the revolving barrel, one at every second of the transit-clock. Proper means are provided for breaking the circuit at pleasure, and at the same time stopping the movement of the travelling-frame, so as to avoid unnecessary consumption of paper upon the revolving barrel. In the month of November 1856, one of the teeth in the wheel before mentioned was cut away, so that once in each minute no contact of the two springs takes place. The omission of the corresponding puncture on the revolving barrel thus marks with certainty the commencement of each minute.

The other pricker is used for the register of the times of observations. The wires of its galvanic magnet, after passing through a battery, are led to the Transit-Circle-pier, and terminate in two large springs, which touch two large insulated brass rings upon the conical axis of the Transit-Circle. From these brass rings, wires are led within the Transit-Circle-Telescope, to a contact piece near the eye-end, where the observer, by a touch of the finger, can complete circuit, and thus make a puncture on the revolving barrel.

Branches of the same wires are led to the Altazimuth, and to the Great Equatoreal; on each of which there is a nearly similar apparatus for completing circuit.

The Altazimuth, constructed by Messrs. Ransomes and May (as engineers), and by Mr. Simms (as instrument-maker and optician), and erected in 1847.

This instrument is mounted in a tower (now called the South Dome), which is built on the walls of what was formerly called the Advanced Building (the same in which Flamsteed's Mural Arc and Equatoreal Sector were mounted), and is raised to such a height that the instrument commands the horizon in all directions above the buildings of the Observatory, except the East Dome, the new South-East Dome, and the Octagon Room. Its center is about 28 feet West and $34\frac{1}{2}$ feet South of the old Transit-Instrument, and about 47 feet West and 29 feet South of the new Transit-Circle. Within the Tower is built a three-rayed pier; the rays being carried up nearly to the floor of the Dome, and a central cylindrical mass, 3 feet in diameter, being carried through the floor. Upon this cylindrical mass is planted the Azimuthal Circle, on which the lower pivot for azimuthal rotation rests. For the support of the upper pivot, a horizontal iron triangle is carried by the three-rayed pier; on each side of this there is mounted a vertical iron triangle; and the three vertices of these are connected by an upper horizontal iron triangle: three radial iron bars, supported on its angles, carry, at their point of union, the Y in which the upper pivot of the vertical axis turns. The frame revolving in azimuth consists of a top, and a bottom, connected by two vertical cheeks, all of cast iron:

b 2

the microscopes for viewing the divisions of the horizontal circle are cast in the same flow of metal with the bottom piece, and those for viewing the divisions of the vertical circle are cast in the same flow with one of the vertical cheeks. The vertical circle and telescope are of gun-metal; the side of the circle which carries the graduated limb, the ends of the telescope, and one of the pivots, being cast in one flow; and the other side of the circle with its pivot being cast in another flow.

The diameter of each of the two circles (horizontal and vertical) is 3 feet; the length of the telescope is 5 feet; the aperture of its object-glass $3\frac{3}{4}$ inches. The top carries two spirit-levels and the bottom carries two spirit-levels, parallel to the axis of the vertical circle: the vertical cheek which carries the microscopes carries also two spirit-levels parallel to the plane of the vertical circle. No important parts are connected by small screws; and no part whatever admits of adjustment; except that the coarse screws on the ends of the upper radial bars are sometimes touched, to bring the vertical axis to a position conveniently near to exact verticality.

The instrument can be firmly clamped in azimuth; and the vertical circle can be firmly clamped; but neither clamp is furnished with a slow motion. For each movement, however, there is a moderately-slow motion, by rack and pinion.

For a detailed account of this instrument, illustrated by engravings, and for a description of the processes gone through in its adjustment, I refer to the volume of *Astronomical Observations for 1847*. The description, with some modifications, is reprinted, and attached to the volume for 1867.

As a fixed mark of reference, and as an object for facilitating the determination of the zenith-point of the vertical circle and the collimation-error for horizontal transits, a reversed-telescope or collimator is used. The object-glass of the telescope is the object-glass of 5 inches aperture and 24 feet 6 inches focal length, which was formerly used for the 25-foot Zenith Sector. It is planted in the north wall of the tower of the South Dome; a brass tube about 1 foot long is fixed by Roman cement in the wall, and the object-glass-cell is screwed to a flat bearing upon a ring within the tube; a small penthouse on the outside of the wall protects it from rain. The mark is the image of a small circular hole, as formed by a lens of short focus. The hole is a perforation $\frac{1}{30}$ inch in diameter, in a small circular piece of metal fixed in a larger circular piece of ivory which is attached to an opaque plate. At the distance of about 7 inches from this perforation is a lens of one inch focal length: and the image of the perforation therefore has a diameter of about $\frac{1}{30}$ inch; this image is in the focus of the $24\frac{1}{2}$ -foot object-glass, and is in fact the mark viewed with the telescope of the Altazimuth. The perforated plate and the lens are carried by a very strong brass tube about an inch in diameter (a piece cut from the tubular standard of the Royal Astronomical Society), and this is fixed by strong iron thumb-screws into an iron frame which is strongly bolted to the west side of the west wall of the Upper Computing-Room, below the ridge of the roof of the Passage-Room (part of the ancient Quadrant-

Room). The mounting of the mark is thus entirely protected from the Sun and from the weather: and although the separation of the mark and the collimator-object-glass on two unconnected buildings is not unobjectionable, yet the other circumstances of mounting are here as favourable as it is possible to find. The perforation is illuminated by a small gas-light: and its image as viewed through the telescope of the Altazimuth then appears as a very well-defined round point, admitting of most accurate bisection by a wire either in the horizontal or in the vertical direction, surrounded at a little distance by a fainter ring of light. For viewing this mark, the telescope of the Altazimuth is pointed downwards at an inclination of $12^{\circ}.18'$ below the horizon.

By means of the branches of the galvanic wires leading from the galvanic magnet of one pricker of the Chronographic Barrel to contact-pieces upon the Altazimuth, the observations of transits are registered on the same sheet of paper as those made with the Transit-Circle, in transit-clock-time; and thus all comparisons of clocks become unnecessary, and all errors arising from the transmission of time are avoided.

The wire-plate originally carried six horizontal and six vertical wires, at intervals adapted to eye-and-ear observation of transits; but in the spring of 1854, for more convenient use in the observations by galvanic contact, four additional horizontal wires were inserted at equal intervals between the two central horizontal wires, and four additional vertical wires at equal intervals between the two central vertical wires. On 1861, February 7, a new system of six horizontal wires for observation by galvanic contact was inserted, the middle interval of wires being much larger than either of the other four intervals. On 1864, August 5, another system was inserted by Mr. Simms, and the intervals were inadvertently made equal.

For observing an azimuth, the instrument is clamped in azimuth; and when the object enters the field of view with an oblique course, the moderately-slow motion of the vertical circle is used to make the course of the object apparently horizontal through the middle of the vertical wires; the times of transit over the wires are observed, and the azimuth-circle and the levels parallel to the horizontal axis are read. For observing a zenith-distance, the process is similar, *mutatis mutandis*. The two observations can never be made at the same time.

On 1864, September 30 and October 1, the pivots of the axis of the Vertical Circle of the Altazimuth were examined. The method employed is the same as that explained in detail in the Introduction to the *Greenwich Observations* for 1847, and in the Description of the Altazimuth attached to the volume for 1867, page 14. The residual errors, showing the movements of certain imaginary points on the ends of the two pivots, are given in the following tables:

Pivot on the opposite side to the Graduated Face.

Pointer Read- ing.	Horizontal Error, Micrometer Head to Right.	Vertical Error, Micrometer Head Below.	Pointer Read- ing.	Horizontal Error, Micrometer Head to Right.	Vertical Error, Micrometer Head Below.	Pointer Read- ing.	Horizontal Error, Micrometer Head to Right.	Vertical Error, Micrometer Head Below.	Pointer Read- ing.	Horizontal Error, Micrometer Head to Right.	Vertical Error, Micrometer Head Below.
0	r	r	0	r	r	0	r	r	0	r	r
5	- 0'041	+ 0'012	95	+ 0'010	- 0'022	185	- 0'007	+ 0'016	275	- 0'009	+ 0'003
15	- 0'026	- 0'020	105	- 0'004	- 0'008	195	- 0'039	- 0'005	285	- 0'011	- 0'008
25	- 0'026	- 0'016	115	+ 0'013	- 0'012	205	- 0'012	+ 0'028	295	+ 0'034	- 0'012
35	- 0'018	- 0'006	125	+ 0'023	- 0'018	215	0'000	+ 0'047	305	+ 0'028	+ 0'007
45	- 0'027	- 0'012	135	+ 0'041	- 0'029	225	- 0'001	+ 0'019	315	+ 0'006	+ 0'015
55	- 0'028	+ 0'003	145	+ 0'031	- 0'020	235	+ 0'008	- 0'010	325	+ 0'007	+ 0'021
65	- 0'024	+ 0'005	155	+ 0'015	- 0'021	245	+ 0'004	+ 0'007	335	+ 0'020	- 0'004
75	+ 0'008	+ 0'014	165	+ 0'021	- 0'003	255	- 0'003	+ 0'018	345	- 0'016	+ 0'005
85	+ 0'009	+ 0'006	175	+ 0'017	+ 0'013	265	- 0'006	+ 0'001	355	- 0'030	- 0'018

Pivot on the same side as the Graduated Face.

Pointer Read- ing.	Horizontal Error, Micrometer Head to Right.	Vertical Error, Micrometer Head Above.	Pointer Read- ing.	Horizontal Error, Micrometer Head to Right.	Vertical Error, Micrometer Head Above.	Pointer Read- ing.	Horizontal Error, Micrometer Head to Right.	Vertical Error, Micrometer Head Above.	Pointer Read- ing.	Horizontal Error, Micrometer Head to Right.	Vertical Error, Micrometer Head Above.
0	r	r	0	r	r	0	r	r	0	r	r
5	- 0'001	+ 0'009	95	+ 0'010	0'000	185	- 0'007	- 0'001	275	+ 0'003	- 0'032
15	- 0'004	+ 0'003	105	+ 0'012	+ 0'009	195	- 0'010	+ 0'003	285	- 0'003	- 0'023
25	+ 0'011	+ 0'019	115	- 0'005	+ 0'002	205	+ 0'003	+ 0'006	295	+ 0'008	- 0'019
35	+ 0'010	- 0'006	125	+ 0'001	+ 0'014	215	+ 0'015	+ 0'013	305	- 0'005	- 0'011
45	+ 0'004	- 0'017	135	+ 0'016	+ 0'004	225	- 0'004	+ 0'026	315	- 0'015	- 0'011
55	+ 0'012	- 0'024	145	- 0'004	+ 0'020	235	- 0'012	+ 0'004	325	+ 0'001	0'000
65	+ 0'028	- 0'030	155	- 0'006	+ 0'022	245	+ 0'006	- 0'012	335	- 0'001	+ 0'015
75	+ 0'009	- 0'008	165	- 0'002	+ 0'022	255	- 0'016	- 0'020	345	- 0'023	+ 0'016
85	+ 0'019	- 0'016	175	0'000	+ 0'003	265	- 0'012	- 0'015	355	- 0'015	+ 0'039

Value of one revolution of the Micrometer = 22".45.

The zero in azimuth of this instrument has sometimes undergone sudden changes, from some cause not yet ascertained. It appeared to me not improbable that the radii of the horizontal circle, which rest in three iron forks fixed on the top of the cylindrical pier, might be so strongly held by friction (being pressed down by the weight, not only of the horizontal circle but also of the whole rotating apparatus and its counterpoise, which were carried by the horizontal circle) that they could not obey the laws of thermal expansion, until the strain became so great that they jumped into a new position. In order to obviate this, Mr. Simms, in May 1865, under my instruction, placed the support of the counterpoise apparatus on the pier (leaving no pressure upon the horizontal circle except the unrelieved portion of the weight of the rotating instrument) and polished the rubbing surfaces of the three bearing radii and the forks in which they rest. It does not appear, however, that the steadiness of the circle has been materially improved.

The 5-foot Equatoreal in the North Dome, constructed by Ramsden.

This instrument was the property of Sir George Shuckburgh, and is fully described by him in the Philosophical Transactions for 1793. It was presented to the Observatory in the year 1811. It was intended to be mounted in what is now called the East Dome, as an Altitude and Azimuth Instrument; but the fixed supporting columns (similar to those of the Palermo Circle) were found so unsteady that it was never once used; and it was then mounted as an Equatoreal in the North Dome (formerly called the North-Eastern Dome), where it has since remained. The situation of this dome is most unfavourable, as the South-Western sky in every part to the altitude of 35° , and through a considerable horizontal extent to the altitude of 53° , is concealed by the Octagon Room. The position of the instrument is about 52 feet West and 90 feet North of the old Transit-Instrument, or 71 feet West and $97\frac{1}{2}$ feet North of the new Transit-Circle. This Equatoreal is one of that class, usually called the "English Equatoreal," in which the two pivots of the polar-axis are at the two extremities of the polar-axis, and the two pivots of the declination-axis are at the two extremities of the declination-axis: the telescope and declination-circle being between the pivots of the declination-axis, and the declination-axis being within the frame of the polar-axis, and the complete polar axis and hour-circle being between the polar supports. The whole length of the polar-axis, between the extremities of the pivots, is about 9 feet. These pivots turn in Y's (having proper adjustments), which are carried by two piers within the Dome, one being a lofty pier on the North side, the other a pier of small elevation on the South side. The North pivot is at the center of a circular frame; the South pivot is at the apex of a cone; and the polar frame consists of six pillars, connecting the base of this cone with the circular frame. Three pillars are united by intervening bars to form the Eastern side of the polar frame, and three to form the Western side: they carry the Y's for the declination-axis and the microscopes for reading the declination-circle. The length of the declination-axis between the extremities of its pivots is about 2 feet 2 inches; the diameter of the declination-circle is 4 feet, and the circle is divided to $5'$ of arc. The telescope is 5 feet 4 inches in length, and has an object-glass of 4.1 inches aperture. The hour-circle is connected with the cone; its diameter is 4 feet, and it is divided to $10'$ of arc: these divisions are read by fixed micrometer-microscopes. The graduations of the hour-circle had become very indistinct, and the circle was therefore redivided by Mr. James Simms in the month of November 1860.

The Equatoreal in the Eastern Dome (formerly called the South or South-Eastern Dome).

This instrument was erected in the year 1838. The aperture of the object-glass is about 6.7 inches, and its focal length about 8 feet 2 inches. The object-glass was made by M. Cauchoix, of Paris, and was presented to the Observatory by the late Rev. R. Sheepshanks. Its definition is good: a small quantity of colour from the secondary spectrum, and a diffusion of light from brilliant objects, being the principal defects.

It is mounted in the Eastern Dome, 38 feet East and 6 feet South of the old Transit-Instrument, or 19 feet East and $1\frac{1}{2}$ feet North of the Transit-Circle; with a mounting similar in general form to that known as the "German Equatoreal." A stone pier is erected, whose extreme breadth from East to West is 1 foot 4 inches, and from North to South 5 feet 4 inches: the southern or principal portion of the upper surface of this pier is sloped so that its plane produced passes through the celestial pole: upon the surface is fixed a cradle of cast iron, having the lower bearing of the polar-axis in a projection from its lower end, and the upper bearing at its upper end: the distance between the two bearings is 3 feet 7 inches. The axis is of cast iron; its form is nearly conical: the end which rests in the lower bearing is a more obtuse cone. The diameter of the axis, where it turns in the upper bearing, is 6 inches: it rests here in a Y upon two plates of gun-metal. At a small distance below the upper bearing, a strong circular plate parallel to the equator, 14 inches in diameter, is fixed to the axis: and close above it, another plate of the same size is mounted, parallel to the former, turning freely round the axis; in that surface of each of these two plates which is nearest to the other plate, a dovetailed groove is turned, and a moveable clamping-piece has one clamp in the groove of one plate, and the other clamp in the groove of the other plate. By means of this clamping-piece, the two circular plates can be fixed together at pleasure, in any relative position. The moveable circular plate is inseparably connected with a long flat arm, or sector, of 24 inches in length (measured from the circumference of the plate) in the plane of the equator: the edge of this sector is cut into teeth, in which works the endless screw carried by the clock, which is fixed to the North side of the pier. Therefore, if the clamping-piece above-mentioned is not fixed to either plate, or is fixed to only one, the action of the clock-work upon the sector, though it turns the moveable circular plate, does not turn the fixed circular plate; but if the clamping-piece is fixed to both plates, the action of the clock-work on the sector carries the moveable plate and the fixed plate (now connected with it), and therefore turns the polar axis, and the telescope, &c., which is supported by the polar axis. Between that part of the clamping-piece which is connected with the fixed plate, and that part which is connected with the moveable plate, there is a slow-motion screw, turned by means of a Hook's joint and a long handle. Immediately above the upper bearing, the polar axis carries the hour-circle, 12 inches in diameter; it is divided on its edge to 1^m of time, and is read off to 2^s by two verniers. Above this, a square box is firmly fixed to the axis; perforated in a direction parallel to the equator for the insertion of the declination-axis. The diameter of the declination-axis at each of its two bearings is about 4 inches; it is supported at each by a Y. To one end of the declination-axis is fixed the cradle, carrying the telescope; to the other is fixed the declination-circle, and the counterpoise. The diameter of the declination-circle is 11 inches; it is divided on its edge to $15'$ of arc, and is read off to $30''$ by two verniers attached to the square box. The telescope-tube is of wood; its form is square in the middle, chamfered off towards the ends so as to become octagonal: several stops, or transversal plates with holes of the proper magni-

tude, are fixed in it ; it is very firm, and free from tremors. Upon a large ring which is fixed to the square box there turns with stiff friction another ring, carrying two sector-arms, graduated at their extremities ; these graduations are read by micrometer-microscopes, carried, one by the eye-end of the telescope-tube and one by the object-end : the use of this graduated double sector is, to measure small differences of declination (not exceeding 10°) with great accuracy ; as, being brought by the hand under the telescope, it is then retained in its position by friction, and is not affected by the motion of the telescope. Upon another ring, which is fixed to the square box, there turns a ring-clamp, or brake, that admits of being fastened to it in any position ; with this ring-clamp the telescope-cradle is connected by means of a slow-motion screw, which fixes the telescope in declination, or gives the means of imparting to it a slow motion in declination. The speed of the clock is regulated by two balls, suspended to the ends of a horizontal arm of $4\frac{3}{4}$ inches in length, which is carried by a vertical spindle ; when the velocity is so great as to cause the suspending-rods to make a certain angle with the vertical, small projections, carried by the balls, are thereby made to rub against the lower surface of a fixed horizontal ring, and the friction thus caused prevents the weight which urges the clock from greatly increasing the velocity. This mounting was constructed by Mr. T. Grubb, of Dublin. Besides several negative eyepieces unfurnished with wires, this telescope has a wire-micrometer, a comet-eyepiece with thick wires, and a double-image micrometer constructed on the principles explained in the *Memoirs of the Royal Astronomical Society*, vol. xv, page 199, and *Monthly Notices*, vol. x, page 160 ; (and described in page xx, below).

The Great Equatoreal, constructed by Messrs. Ransomes and Sims as Engineers, and Mr. Simms as Instrument Maker and Optician.—A complete description of this instrument, with engravings, is attached as Appendix to the volume for 1868. The following account will give information on its principal peculiarities. It is to be premised that the form of the instrument is the “English Equatoreal ;” the polar-axis turning on pivots at its extreme ends, and including between its two sides the telescope and declination-circle attached to it ; the frame which carries the telescope and declination-circle having its pivots at opposite extremities of the declination-axis.

The “South-East Dome,” which contains this instrument, is in close proximity to the south-east corner of the Record Room, and occupies part of the isthmus which connects the Observatory Hill with the upper part of Greenwich Park. It is in form an octagon, with an attached projection on the north side, containing the staircase. The length of the line drawn perpendicularly through opposite sides of the octagon is 31 ft. 4 in. The building consists of three stories ; that of the ground floor contains the Water-Clock-Movement (to be mentioned below), and is used for other purposes unconnected with the Equatoreal ; the middle story has been used, in 1870, as a room

for chronometers; the upper story is properly the Equatoreal Room. To the top of the walls of that room, the building is fire-proof.

The walls are built to the height of 9 ft. 5 in. above the floor of the Equatoreal Room. Arches are turned across the angles of the octagon, so as to make the upper surface of the walls a polygon of sixteen sides. Upon this surface is planted a circular wooden ring or curb, upon which is fixed an iron curb, containing a channel in which cannon balls run, and containing also a circular rack or toothed wheel (its teeth pointing upwards), which surrounds the room. Upon the balls runs another curb with inverted iron channel, which curb is the foundation of the revolving dome. The dome is drum-shaped; its clear inner height above the floor being 25 ft. 8 in. It carries a toothed wheel which works in the fixed rack just mentioned, so that a rotation of the wheel causes the dome to revolve. This rotation is effected by winch-work, which is carried by an iron frame that is attached to the interior of the dome, and projects downwards to a convenient level. The person who turns the winch must follow the movement of the dome; his place is always opposite to the shutter-opening. The opening for observation is 3 feet wide; it extends, without interruption, from the curb of the dome to the top of the dome-wall, and along its nearly flat top about 2 feet beyond its center. One nearly horizontal shutter covers the whole opening in the flat top, and one vertical shutter covers the whole opening in the dome-wall; each of these parts can be opened independently of the other. An iron frame attached to the interior of the dome projects downwards to a convenient position, and carries the winch-machinery by which the shutters are opened and closed.

The South Pier, which supports the lower extremity of the polar-axis, is built from the ground through the lower and middle stories, nearly to the floor of the Equatoreal Room, where the iron foundation-frame is planted which carries the bearing-piece for the lower pivot and its antifriction wheels, the attachment for the slow-motion screw, and the fixed time-microscope. The North Pier is built to the same height in two massive trapezoidal pillars (upon one foundation), united by strong stones at each of the floors; the entrances of the lower and middle rooms pass between these pillars. Upon the upper surface of the pier is planted a lofty iron frame (cast in one piece by Messrs. Ransomes and Sims), the top of which carries the bearing piece for the upper pivot, the antifriction wheels, and the apparatus subservient to the transmission of gas and to galvanic communications. The entrance to the Equatoreal Room passes between the upright parts of this iron frame; they are, however, sufficiently distant from the wall to permit the passage of the irons, projecting downwards from the dome, which carry the winch-apparatus for moving the dome and opening its shutters.

The polar-axis consists of two braced skeleton-prisms, each about 22 feet long, 2 feet apart, united at the bottom and at the top by ovals about 8 feet long (in the direction parallel to the declination-axis), and 5 feet broad (in the transverse direction). The pivot of the lower oval, projecting downwards, is long enough to carry the Hour-

Circle, which is a cast-iron circle 6 feet in diameter, revolving freely on the long pivot, but admitting of being connected with the lower oval by clamp and slow-motion-screw. The circumference of this circle is racked, and the worm or endless screw, to which motion is given by the clock-movement, acts in it. The circle bears two graduations: one which is viewed by a fixed microscope (attached to the iron foundation-frame), whose reading, when the circle has been properly placed and the clock-movement is properly adjusted, always gives True Sidereal Time; another, which is viewed by two microscopes carried by the lower oval, and whose reading (when the clock-movement, &c., are adjusted) always gives the Right Ascension of the object under view. There are also independent means of fixing the lower oval, when the use of the clock-movement is not desired. The upper oval is cut through on one side as far as its pivot, to allow the telescope to view the pole. Its pivot is perforated to allow the passage of a gas pipe, by which lights on various parts of the instrument are supplied; and it carries four insulated galvanic rings (connected, as will presently be mentioned, with four wires that lead to springs which touch rings upon the declination-axis), touched by four springs which are attached to the lofty iron frame, and to which are attached four wires; one pair of these wires communicates with the galvanic magnets of one pricker upon the chronographic barrel, and one pair with the eastern contact-springs of the transit-clock.

The declination-axis is supported on brackets, which are carried nearly at the middle of the prisms' length, in such a position that the telescope, when parallel to the earth's axis, is so far removed from the imaginary axis joining the two pivots of the polar-axis, that it can view the pole through the cutting of the upper oval already mentioned.

The telescope in its declination-axis nearly represents a transit-instrument. It carries on one side a graduated circle 5 feet in diameter, which is viewed by two microscopes attached to one of the prisms of the polar-axis. On the other side it carries a clamp and slow-motion screw, which connects it with a circle affixed to the other prism. One pivot is perforated for a gas pipe: it also carries four rings which are touched by four springs that are connected by wires with the rings on the declination-axis; two wires are led from these rings through the telescope-tube to a touching-piece at the eye-end, and a contact made there produces a puncture upon the chronographic-barrel; and the other two wires are led to a galvanic chronometer on the eye-end of the telescope, which is thus regulated to synchronism with the transit-clock. The telescope-tube is of mahogany; it is square in the middle of its length, and octagonal at the ends. The focal length of the object-glass, made by Messrs. Merz and Son, of Munich, is about 16 ft. 6 in. Messrs. Merz originally contemplated the supply of an object-glass of greater focal length, in consequence of which the whole frame of the instrument is made in larger dimensions than are necessary for the object-glass actually supplied. The clear aperture of the object-glass is about $12\frac{1}{2}$ inches. Its definition, as shown by examination of close double stars, is very fine; the components of the

small star of γ Andromedæ being widely separated; and there is very little stray colour.

The clock-movement is fixed in the ground-floor story, upon a frame which is attached to the South Pier. The power is given by the flow of water, received from the water pipes which supply the Observatory under a pressure of 100 feet, acting through a reaction-machine, which is made to revolve four times in one sidereal second. The spindle of this reaction-machine rises through the lower and middle rooms, and acts by an endless screw in a wheel of 480 teeth, which revolves in two minutes and whose axis carries an endless screw which acts in the rack of the hour-circle. Very great care was taken in the preparation and examination of this large endless screw. The supply of water to the reaction-machine is determined by the construction called "Siemens' Chronometric Governor," in which the first of three wheels of a train is connected with the machine, the third maintains the motion of a conical pendulum (so arranged by water-resistance that its arc is sensibly invariable), and the axis-frame of the second or intermediate wheel is moveable, and is connected with the throttle-valve of the water-supply. If the supply accelerates the machine too much, its excess of motion is immediately impressed on the frame of the second wheel, and the supply of water is diminished.

The Double-Image Micrometer.—The general form of the double-image eyepiece, together with the mode of use, and the advantages and disadvantages attending the use of it, are described fully in the preceding volumes, for 1840 and for 1843 to 1844 to which it is sufficient in this place to refer.

The special arrangement of this double-image eyepiece is described in vol. xv. of the *Memoirs of the Royal Astronomical Society*. The characteristic of this construction is, that the colour produced by the prismatic dispersion, which is occasioned by the passage of the rays through each half of the divided lens where the images are separated, is corrected by a new arrangement of the lenses. In this construction the focal length of the first lens, or that nearest to the object-glass, is arbitrary; so that the power is changed by change of this first lens instead of the fourth, as in the original construction. The eyepiece now used is the same as that which was first used in 1851, and was made on the principles above explained, adopting, among the various admissible relations of the focal lengths and intervals of lenses, one which was suggested by Mr. B. Valz, of Marseilles, and which is described in the *Monthly Notices of the Royal Astronomical Society*, 1850, June 14. The principal difference between this eyepiece and that used in 1850 consists in the circumstance that the divided lens is concave, instead of being convex, as in the former case. By this means much less light is lost from the central portions of the pencil in its passage past the divided surfaces of the lenses, and the construction is undoubtedly preferable to that used before.

The numbers defining the construction of this eye-piece are as follows:—

Focal length of 1 st lens, or that nearest the object-glass, arbitrary, or a ;	
Distance from 1 st lens to 2 nd lens, the same as focal length of 1 st lens,	
or	a ;
Focal length of 2 nd or divided lens, which is concave	1;
Distance from 2 nd lens to 3 rd	1;
Focal length of 3 rd or field-glass	1;
Distance from 3 rd to 4 th	3;
Focal length of 4 th or eye-glass	1;

Where the numbers 1 and 3 may be applied to any scale of linear measure.

And the forms of the lenses should be the following:—

1 st lens	equi-convex.
2 nd or divided lens	equi-concave.
3 rd or field-glass	plano-convex, with its plane side next the divided lens.
4 th or eye-glass	equi-convex.

The same double-image micrometer which in preceding years was used with the Sheepshanks Equatoreal in the Eastern Dome was in the year 1861 mounted (by use of an adapting-tube) on the South-East Equatoreal; the value of its micrometer is thereby necessarily altered.

The Reflex Zenith-Tube, constructed under my direction by Mr. Simms.—A detailed account of this instrument is given in Appendix I. to the volume for 1854; in this place the following account will suffice: The object-glass (formerly the object-glass of Troughton's Transit-Instrument) is mounted upon a fixed tube, which is in a vertical position; upon this tube it can be turned in azimuth. To the cell of the object-glass is firmly fixed the micrometer-frame, revolving with the object-glass when the object-glass is turned. The point of the screw of the micrometer A rests upon the fixed micrometer-frame. The moving frame of the micrometer A carries the resting-point of the micrometer-screw of the micrometer B. The micrometer B carries the wires by which the star's image is bisected. The eyepiece is a 4-glass diagonal eyepiece bent at right angles between its third lens and its fourth lens (counting from the eye), and having a diagonal-prism-reflector at the place where it is bent; and so placed that the fourth lens can receive rays of light from the direction of the nadir, and can, by means of the diagonal prism, transmit them horizontally to the eye. The fourth lens (which looks vertically downwards), and the diagonal prism, are placed nearly over the center of the object-glass, being carried by arms which are fixed to the large tube; the small horizontal tube which carries the remaining lenses of the eyepiece is supported by the large tube of the telescope, and does not project over any part of the object-glass. Below the object-glass, at a distance nearly equal to half its focal length, is a trough of quicksilver. The image of the star, as it passes near to the

zenith, is formed in the plane of the micrometer wires. These particulars will probably suffice for enabling the reader to understand the reductions. It will easily be seen that, to ensure accuracy of result, no firmness of construction is requisite in this instrument, except in the connection between the micrometer and the object-glass. The instrument is mounted in a new building erected for it in the Middle Garden, in the angle between the passage behind the Astronomer Royal's Official Room and the south projection of the Transit-Circle-Room.

For the support of the quicksilver, the following method has, after several trials, been adopted:—A well was dug to the depth of ten feet below the surface, or seven feet below the deepest foundation of the walls of the Observatory, and was filled with incoherent rubbish. When a stage was placed upon it, the tremor (which had been intolerable while the quicksilver-trough rested on the solid ground) was sensibly diminished. Afterwards from this stage, No. 1, there was suspended by straps of vulcanized caoutchouc, a stage, No. 2, and from this, in like manner, a stage, No. 3, on which the quicksilver was placed. The habitual tremor was now destroyed, but the image slowly floated or oscillated. Finally, this last defect was corrected by connecting the trough horizontally in two directions by shreds of vulcanized caoutchouc with stage No. 1, and by this means the floating was nearly destroyed, leaving the image practically almost perfect. The experiments were concluded in May 1856, and from that time the use of the instrument has been continuous, and no difficulty has been experienced in making observations of γ Draconis at its meridian transit, at any hour of the day or night.

The theory of the caoutchouc-suspension may be thus stated:—If the length of a pendulum is such that it will naturally vibrate in a long time; and if a rapid vibration, or a vibration of short period, be given by some external force to the point of suspension; then the disturbance of the pendulum consequent on that movement of the point of suspension will be very much less than that movement itself. Thus, if the equation to the pendulum's motion be $\frac{d^2 x}{dt^2} = m^2 (y - x)$, where m is small; and if $y = a \cdot \cosine n t$, where n is large; the corresponding term in x will be $\frac{-m^2}{n^2 - m^2} \times a \cdot \cosine n t$, which is much smaller than that in y . Now, the caoutchouc-suspension permits a horizontal oscillation, which is naturally one of long period; and the elasticity of extension of the caoutchouc permits a vertical oscillation, which is also naturally one of long period; but the disturbing tremor of the earth is one of exceedingly short period; and therefore the disturbances, horizontal and vertical, given to the suspended stages are exceedingly small. The duplication of the apparatus again diminishes the disturbance the second time in nearly the same proportion as at the first time.

Two detached telescopes, one of which is 46 inches in focal length, and the other 30 inches; the former is usually kept in the Octagon Room, and the other in the

Magnetic Observatory. The diameters of the object-glasses of these telescopes are 3·6 inches and 2·7 inches respectively. The telescope formerly belonging to the Western Equatorial has also been mounted for use as a detached telescope ; its focal length is 36 inches, and the aperture of its object-glass 3·6 inches. The 62-inch telescope mentioned in former years, and that of the transit-instrument formerly used as a collimator to Troughton's transit, are now mounted on tripod stands, for general use. The other achromatic telescope, mentioned in former years, has been given to the Quebec Observatory.

Finally, there are two Newtonian reflecting telescopes, the largest being one of 10 feet, by Sir W. Herschel.

The Transit-Clock, constructed by Hardy, and originally furnished with Hardy's escapement. A dead-beat escapement was substituted for this by Dent in the year 1829. The jewelled holes were removed by Dent in 1836, and the pivots now turn in brass holes. This clock was transferred from the Old Transit-Room to the Transit-Circle-Room in December 1850. Mention has already been made (page xi) of the apparatus now connected with the escape-wheel-arbor for the purpose of completing a galvanic circuit at every second of the transit-clock (omitting only the 60th second of every minute), by which a puncture is impressed at every second (except one in each minute) on the chronograph-barrel.

A clock in the North Dome, marked "Arnold 1," having contact apparatus similar to that in the transit-clock (as described at page xi), in order that the clock may, if required, be used as a temporary transit-clock ; one in the East Dome, marked "Earnshaw ;" one in the South Dome (the place of the Altazimuth), marked "Graham 1 ;" one in the Reflex-Zenith-Tube-Apartment, marked "Mudge and Dutton," which was presented in the year 1846 to the Observatory by the Rev. Charles Turnor ; one marked "Arnold 2," placed in the Second Computing Room ; one marked "Graham 2," usually preserved in the passage that was formerly part of the Quadrant Room, now placed in the occasional observatory ; and one marked "Graham 3," formerly used for the daily dropping of the Time-Signal-Ball at 1^h, but now occasionally employed for facilitating the regulation of the galvanic motor-clock. There is a clock marked "Dent" placed in the Chronometer-Room, and used occasionally for comparisons of chronometers in case of accidental failure of the galvanic clock placed there ; also a chronometer, "Brockbanks," generally kept in the Computing-Room, but occasionally used for extra-meridional observations. Besides these, there are some journeyman or assistant clocks, two of which, occasionally used in longitude operations, are fitted with contact springs, for the purpose of giving galvanic signals ; and a watchman's clock.

The transit-clock is wound up every Monday and Thursday, and the other ordinary clocks in daily use, every Monday.

The galvanic Normal Mean time or "motor" clock is placed in the lobby at the

foot of the Octagon-Room staircase, near to the trigger of the ball-apparatus. It is a clock of Shepherd's construction, in which the swing of the pendulum completes three galvanic circuits: by one of these the movement of the pendulum is maintained, independently of any train of wheels; by the other two a frame of magnets is made to oscillate, and thus to give motion to the seconds-wheel, and, through it, to the other wheels. The wire which carries the current that produces that oscillation is led through corresponding parts of six similar clocks, and the current, by relay action, animates a seventh clock, and regulates another. The movements of the whole of these clocks are therefore necessarily synchronous with those of the motor-clock. One of the clocks has a large dial exposed to public view on the east boundary wall of the Observatory; three are in the Chronometer-Room, and are used in the daily comparisons of chronometers; one is in the Computing-Room; one (of the dimensions of a chronometer) is upon the desk of the Superintendent of the Time Department; one is in the hall of the Astronomer Royal's dwelling house; and one (the regulated clock) is at the London Bridge Station of the South-Eastern Railway. The regulation of the last-mentioned clock is effected by the method (slightly modified) of Mr. R. L. Jones, and the clock is used for automatic alteration of galvanic contacts which determine the direction of hourly galvanic signal-currents sent from the Royal Observatory. The arrangement for giving hourly signals is as follows. The motor clock closes a circuit precisely at each hour: that at 1^h, by the intervention of electro-magnets, pulls automatically the ball-trigger and drops the Signal-Ball at Greenwich. At every hour also the primary clock current by relay action causes galvanic currents to pass, on one line of wire to the central station of the Post Office Telegraphs, Telegraph Street, London, and on another line to the London Bridge Station of the South-Eastern Railway. The currents received in Telegraph Street are distributed daily, by automatic action, on some of the principal lines of railway and to important provincial towns. The current at 1^h is used to fire signal guns at Newcastle and North Shields. The hourly currents pass also to the clock tower of the Westminster Palace for the guidance of the superintendent of the clock, which is not regulated or corrected by any direct galvanic action. And return currents are received at definite times from the Westminster clock and from a clock in the Post Office, which show daily at Greenwich the deviation of the clocks from true time. The hourly currents which pass from Greenwich on the wire to London Bridge are there distributed at different hours in different directions, by the regulated clock before spoken of, principally to places on the South-Eastern lines of railway. At 1^h the current drops a Signal Ball at Deal, the property of the Admiralty; and from this ball a return galvanic current is automatically communicated to Greenwich at the instant that the ball has completed its descent.

A sympathetic system of chronometers is also connected with the transit-clock. By means of the wheel on the escape-wheel-arbor (described in page xi), 59 currents are sent through an additional pair of springs every minute, and are used to regulate the

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pendulum of a half-seconds-clock placed on the foundation frame upon the South Pier of the Great Equatoreal, near to the Time-Microscope; to regulate also a half-seconds-chronometer fixed to the eye-end of the telescope of the Great Equatoreal, near to the eye-piece, and always in view of the observer; and to drive a galvanic chronometer placed in the Computing Room on the desk of the Superintendent of the Time Department. The half-seconds-clock is regulated in the manner introduced by Mr. R. L. Jones, excepting that the galvanic coil is fixed to the clock-case and the bar-magnet attached to the pendulum. A similar principle is used for regulation of the chronometer on the eye-end of the Great Equatoreal: upon the axis of its balance a small magnet is fixed (its center being pierced by the balance-staff); a fixed coil embraces the magnet as in the ordinary galvanometer, and through this coil pass the currents received from the transit-clock. The omission of one current in each minute is unimportant as concerns the regulated clock and chronometer, but not so as regards the chronometer which is driven by the current. For this chronometer, therefore, the seconds circle on its dial plate is divided into 59 equal parts (instead of 60), so that one particular division corresponds to two consecutive seconds, and at this division the seconds hand of the transit-clock advances once, whilst that of the chronometer remains at rest. A comparison of this chronometer with the chronometer on the same desk, synchronous with the motor-clock (as mentioned in the last paragraph), is, in fact, a comparison of the transit-clock with the motor-clock. The error of the motor-clock is thus ascertained; and then, by means of a turn-plate on the same desk, the superintendent of clocks completes the circuit of a galvanic current, which, passing through a galvanic coil (with no iron core) in the clock-case, can be made either to attract or to repel a magnet attached to the pendulum, and thus to accelerate or retard the motor-clock as long as may be necessary for its correction. The clocks connected with the motor-clock necessarily receive the same correction.

III. *Subjects of Observation in the Year 1870.*

The Sun has been observed on the meridian at every practicable opportunity, except on Sundays: the Moon and Moon-culminating stars have been observed at every opportunity without exception.

With regard to the Planets, the following rules have been observed: The inferior Planets, Mercury and Venus, have been observed on the meridian at every practicable opportunity, excepting Sundays. The superior large Planets, Mars, Jupiter, Saturn, Uranus, and Neptune, have not generally been observed when their solar time of meridian passage is greater than 15^h, excepting at times when the Moon passes the meridian later than 15^h. The small Planets have been observed only when the time of meridian passage is earlier than 13^h, and only in the first part of each Luration from New Moon to Full Moon (the observations from Full Moon to New Moon being undertaken by M. Delaunay, as is mentioned above, page ii). The observations of all Planets are intermitted on Sundays.

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In the meridional observations of the stars, it has been considered as the first object to establish with indisputable accuracy the places of those included in the Nautical Almanac list (as far as they are visible in this latitude). For this purpose the number of observations of each star made in the two preceding years was ascertained, and the additional number necessary to make up this to fifteen was in 1870 considered to be the number due from that year. In far the greater number of instances this number is exceeded: in a few (especially of stars too near the pole to be used for clock-error), the just number is not completed.

The other stars observed are principally: A list of 92 stars whose right ascensions have been well determined, and which are used, in connection with the Nautical Almanac Stars, for determining clock-error; Stars remaining from former years, including stars to complete previous catalogues; Moon-culminating Stars to the end of the list in the Nautical Almanac 1873; Stars whose occultations by the Moon have been observed at Greenwich; variable Stars; Stars which pass near the North and South Horizon; Stars suspected or known to have large Proper Motions; Stars to be used in future, for the determination of Azimuthal Errors; Stars of which observations have been requested by Astronomers for special purposes.

The Altazimuth has been used for observations of the Moon on every day when she could be seen, without exception; and for the observations of Stars necessary for instrumental adjustments, and of the collimator for the same purpose. Its telescope has also been occasionally used for observing Occultations of Stars by the Moon, and for the phenomena of Jupiter's Satellites.

The Reflex Zenith-Tube has been used throughout the year 1870 for observations of γ Draconis. The observations are made at every opportunity (Sundays excepted) unless when γ Draconis passes the meridian very early in the morning. In these cases the observation is only made when the Moon also passes in the early morning.

The North Equatoreal, the East Equatoreal, and the South-East or Great Equatoreal, have been used for observing Occultations of Stars by the Moon, and for the phenomena of Jupiter's Satellites.

IV. *Explanation of the Printed Observations.*

§ 1. *Transits observed with the Transit-Circle, and Computations of Apparent Right Ascension*, page [1] to [84].

The *first* column on each page contains the day, which is always supposed to commence with the transit of the Sun.

The *second* column contains the numbers for convenience of reference.

The *third* column contains the name of the object observed. With respect to the Sun, Moon, and Planets, the limb whose transit is observed is always mentioned. If no limb is mentioned it is to be understood that the estimated center was observed. The center is observed only when the planet's disc is so small and so round as to

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make it easier to estimate the center than to determine with accuracy the place of the limb. With regard to the stars, the proper names which have commonly been used in the Greenwich Observations and the Nautical Almanac are adopted in preference to other names. For other stars, the names have been taken in the following order of preference :—

1. Flamsteed's constellation-N° and constellation, with Bayer's letter ; taken from Baily's edition of Flamsteed. When the description thus found differs from that in the British Association Catalogue, the difference is mentioned in the notes.
2. The N° in Bessel's Fundamenta, &c., deduced from Bradley's Observations.
3. The hour and N° in Piazzi's Catalogue, edition 1814.
4. The N° in Groombridge's Catalogue.
5. The N° in Baily's edition of Flamsteed's Catalogue.
6. The N° in Santini's Catalogue of 1677 Stars (Memoirs of the Royal Astronomical Society, vol. xii.)
7. The hour and N° in Weisse's Catalogues of the Stars in Bessel's Zones.
8. The N° in Lalande's Catalogue, published by the British Association, or in that edited by Fedorenko.
9. The N° in Lacaille's Catalogue of Southern Stars, published by the British Association.
10. The N° in Rümker's Catalogue of 12,000 Stars.
11. The N° in Oeltzen's Catalogues of Argelander's Zone Observations.
12. The N° in the Radcliffe Catalogues.
13. The N° in Carrington's Red Hill Catalogue.
14. The N° in the Greenwich Catalogues ; or in the British Association Catalogue ; or in the First Cambridge Catalogue.

In observing a double star, the brighter star (if it is not otherwise expressed) is always observed.

When no mark is attached to the name of the object observed, it is to be understood that the observations were made by the galvanic or chronographic method, which was generally in use throughout the year. In any exceptional case where the eye-and-ear method is employed, the observation is distinguished by having the initials (E & E) prefixed to it.

The *fourth* column contains the initials of the observer's name.

The next *nine* columns contain the clock-times (seconds and decimals of a second only) at which the object was observed to pass each of the wires. For eye-and-ear transits, the wires used are those which were in use before the commencement of the galvanic observations, and they are denoted by the letters N, O, P, T, X, Y, Z. Polaris and other stars very near the pole are, however, observed by eye-and-ear over the wires intended for the galvanic transits. The wires used for galvanic transits are denoted by the letters P, Q, R, S, T, U, V, W, X ; P, T, and X, being wires of the original system, and Q, R, S, U, V, W, being new wires inserted between P, T, and X. The intervals P-Q, Q-R, R-S, U-V, V-W, W-X, are nearly equal ;

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the intervals, S-T, T-U, are nearly double of the former, for convenience of easily distinguishing the central wire.

In observing by galvanic contact, the observer merely makes contact of the galvanic spring at the instant of the object passing the wire. Occasionally, when no object is under observation, he makes contacts in any arbitrary number, recording in his book their number and the time by the transit-clock; and thus the numeration of hours and minutes on the punctured sheets is easily established. The punctured sheets are examined the next day, the numeration of minutes and seconds is written upon them, and the transits are read into the transit-book.

In observing by eye-and-ear, it is the practice to take a second from the clock-face before the transit over the first wire, and to preserve the counting by listening to the beats of the clock, and not to look again at the clock-face till the transit is completed. The fraction of the second is estimated by remarking the place at which the object is seen at the successive beats of the clock. Errors in the hours and minutes are seldom alluded to in the notes of the printed observations; but every alteration of the seconds is carefully recorded.

The *fourteenth* column contains the Concluded Transits, giving the hour and minute of the time of meridian passage (which have not been given in the preceding columns), as well as the mean of seconds.

When transits have not been observed over all the wires, a correction is applied to the mean of those actually observed, in order to give the mean of the transits as it would have resulted if each had been reduced separately to the center wire. When transits have been observed over all the wires, the same process of correction is used, but the amount of correction for the mean is very small.

The equatoreal intervals of the wires were determined by observations of stars. From the nature of the process, these intervals are necessarily corrected for the mean effects of refraction. The following are the intervals which were in use during the year 1870:—

For wire N	+	41·509
O	+	27·623
P	+	13·815
Q	+	10·962
R	+	8·246
S	+	5·465
T		0·000
U	—	5·580
V	—	8·363
W	—	11·097
X	—	13·852
Y	—	27·716
Z	—	41·535

INTERVALS OF THE TRANSIT WIRES.

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Hence for the usual circumpolar stars, and for the nine wires usually employed in their observation, the intervals in time from each wire to the center wire are,—

For λ Ursæ Minoris, assuming its declination = $88^{\circ}.54' + n''$:

Wire P	=	+	^m 11.59 ^s .96 + $n \times 0^{\circ}.185$
Q	=	+	9.31 .18 + $n \times 0^{\circ}.148$
R	=	+	7. 9 .61 + $n \times 0^{\circ}.110$
S	=	+	4.44 .69 + $n \times 0^{\circ}.074$
T			0 .00
U	=	—	4.50 .69 — $n \times 0^{\circ}.074$
V	=	—	7.15 .71 — $n \times 0^{\circ}.110$
W	=	—	9.38 .22 — $n \times 0^{\circ}.148$
X	=	—	12. 1 .89 — $n \times 0^{\circ}.185$

For Polaris, assuming its declination = $88^{\circ}.36' + n''$:

Wire P	=	+	^m 9.25 ^s .60 + $n \times 0^{\circ}.111$
Q	=	+	7.28 .75 + $n \times 0^{\circ}.088$
R	=	+	5.37 .54 + $n \times 0^{\circ}.066$
S	=	+	3.43 .69 + $n \times 0^{\circ}.045$
T			0 .00
U	=	—	3.48 .40 — $n \times 0^{\circ}.045$
V	=	—	5.42 .35 — $n \times 0^{\circ}.066$
W	=	—	7.34 .28 — $n \times 0^{\circ}.088$
X	=	—	9.27 .12 — $n \times 0^{\circ}.111$

For Cephei 51, assuming its declination = $87^{\circ}.14' + n''$:

Wire P	=	+	^m 4.46 ^s .23 + $n \times 0^{\circ}.029$
Q	=	+	3.47 .11 + $n \times 0^{\circ}.023$
R	=	+	2.50 .84 + $n \times 0^{\circ}.017$
S	=	+	1.53 .22 + $n \times 0^{\circ}.011$
T			0 .00
U	=	—	1.55 .60 — $n \times 0^{\circ}.011$
V	=	—	2.53 .26 — $n \times 0^{\circ}.017$
W	=	—	3.49 .91 — $n \times 0^{\circ}.023$
X	=	—	4.47 .00 — $n \times 0^{\circ}.029$

For δ Ursæ Minoris, assuming its declination = $86^{\circ}.36' + n''$:

		m		s
Wire	P	=	+	3.52.95 + $n \times 0.019$
	Q	=	+	3.4.84 + $n \times 0.015$
	R	=	+	2.19.04 + $n \times 0.011$
	S	=	+	1.32.15 + $n \times 0.008$
	T			0.00
	U	=	-	1.34.09 - $n \times 0.008$
	V	=	-	2.21.02 - $n \times 0.011$
	W	=	-	3.7.12 - $n \times 0.015$
	X	=	-	3.53.58 - $n \times 0.019$

For stars above the pole, the designations of wires I., II., III., &c., at the heads of the columns of printed transits, correspond to P, Q, R, &c., (or to N, O, P, &c., when the object is observed by eye and ear (E & E), in all cases excepting Polaris, &c.) For stars below the pole, the designations I., II., III., &c., correspond to X, W, V, &c., or to Z, Y, X, &c.

The signs of the numbers must be changed when the star is below the pole.

The correction to the imperfect transit of a star can be found by adding together the equatoreal numbers from one of the tables given above for the wires observed, then dividing by the number of wires, and multiplying by the secant of the star's declination.

For a planet, the correction, computed as for a star, is to be multiplied by

$$1 + \frac{\text{daily increase of R.A. in seconds of time}}{24 \times 60 \times 60};$$

or by $1 + \frac{\text{hourly increase of R.A. in seconds of time}}{60 \times 60}:$

but it has generally been found easier to add, to the computed interval between the mean of wires and the center wire, the amount of the planet's increase of Right Ascension for that interval, which is very readily determined from the numbers given in the Nautical Almanac.

For the Moon, the equatoreal numbers for the wires observed are added together, and the sum is divided by the number of wires; this quotient is then multiplied by,

$$\frac{3600 + I}{3600} \times \frac{\sin \text{Moon's geocentric } Z.D.}{\sin \text{Moon's apparent } Z.D.} \times \text{secant of Moon's geocentric declination,}$$

where I is the increase (in seconds of time) of the Moon's R.A., for the transit over a meridian upon the Earth distant by 1^h of terrestrial longitude, as given in the section *Moon-culminating Stars* in the Nautical Almanac.

CORRECTION OF IMPERFECT TRANSITS.

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For the easy computation of this formula, the following small Table (including the limits of the values of I) of the natural numbers and logarithms of $\frac{3600 + I}{3600}$, is used :—

I = Var. in R. A. for 1 ^h of Longitude.	$\frac{3600 + I}{3600}$		I = Var. in R. A. for 1 ^h of Longitude.	$\frac{3600 + I}{3600}$	
	Nat. Number.	Log.		Nat. Number.	Log.
100 ^s	1.02778	0.01190	145 ^s	1.04028	0.01715
101	.02806	.01202	146	.04056	.01727
102	.02834	.01213	147	.04083	.01738
103	.02861	.01225	148	.04111	.01750
104	.02889	.01237	149	.04139	.01761
105	.02917	.01249	150	.04166	.01773
106	.02945	.01260	151	.04195	.01784
107	.02972	.01272	152	.04222	.01796
108	.03000	.01284	153	.04250	.01808
109	.03028	.01296	154	.04278	.01819
110	.03055	.01307	155	.04306	.01831
111	.03084	.01319	156	.04333	.01842
112	.03111	.01330	157	.04361	.01854
113	.03139	.01342	158	.04389	.01866
114	.03167	.01354	159	.04417	.01877
115	.03195	.01366	160	.04444	.01888
116	.03222	.01377	161	.04472	.01900
117	.03250	.01389	162	.04500	.01912
118	.03278	.01401	163	.04528	.01923
119	.03306	.01413	164	.04556	.01935
120	.03333	.01424	165	.04583	.01946
121	.03361	.01436	166	.04611	.01958
122	.03389	.01447	167	.04639	.01969
123	.03417	.01459	168	.04667	.01981
124	.03444	.01471	169	.04694	.01992
125	.03472	.01482	170	.04722	.02004
126	.03500	.01494	171	.04750	.02015
127	.03528	.01506	172	.04778	.02027
128	.03556	.01518	173	.04806	.02039
129	.03583	.01529	174	.04833	.02050
130	.03611	.01541	175	.04861	.02061
131	.03639	.01552	176	.04889	.02073
132	.03667	.01564	177	.04916	.02084
133	.03694	.01575	178	.04944	.02096
134	.03722	.01587	179	.04972	.02107
135	.03750	.01599	180	.05000	.02119
136	.03778	.01611	181	.05028	.02130
137	.03806	.01622	182	.05056	.02142
138	.03833	.01634	183	.05083	.02153
139	.03861	.01645	184	.05111	.02165
140	.03889	.01657	185	.05139	.02176
141	.03917	.01669	186	.05167	.02188
142	.03945	.01680	187	.05194	.02199
143	.03972	.01692	188	.05222	.02211
144	.04000	.01703	189	.05250	.02222
145	.04028	.01715	190	.05278	.02234

The *fifteenth* column contains the numerical values, in seconds of arc, of the errors of collimation, level, and azimuth ; the two last being distinguished from the first by a round and a square bracket respectively. These errors will be treated separately, as follows :—

Error of Collimation.

The value of this error is given in seconds of arc. The sign of the error is considered positive when it implies an additive correction to the time of observed transits of stars above the pole.

The method of determining the position of the line of collimation by means of the north and south reversed telescopes has been so fully explained above in the description of the instrument, that it is unnecessary to repeat the explanation here. It is only necessary to state that the reading of the micrometer of the south telescope, for coincidence of its nearly vertical wire with the image of that of the north telescope, is frequently ascertained (the results of which will be found on pages [86] to [90]), and that the micrometer-wire of the south telescope is then left in the position so ascertained. And that every day the reading of the transit-telescope-micrometer, for coincidence with the image of the wire of each reversed telescope, is found (the results of which are given in pages [91] to [93]); that the mean of these gives the reading for the line of collimation for that day; and that the mean of these determinations, usually for a week, is adopted as the true reading for the geometrical line of collimation of the transit-telescope.

During the year 1851 the observations of the reversed telescopes with the transit-telescope were usually made twice in every day. Upon examination of the results it did not appear that there was any discoverable difference at different hours of the day, and therefore generally, since that time, the observations have been made only once in every day.

The micrometer of the transit-telescope is left at some convenient reading, near to that of the geometrical collimation, but not necessarily coinciding with it. This reading is given at the foot of every page of transits. The algebraical excess of the reading for geometrical collimation above this is the geometrical error of collimation, with the sign as explained above. This excess is converted into arc at the rate of $14''.78$ for one revolution of the micrometer. (This determination of the value of a revolution was made at the end of the year 1850, as is explained in the description of the Transit Circle, page {22}, Appendix I., of the Volume for 1852, or in the reprint attached to the volume for 1867, page 25: a new investigation for verification of the value was made on 1854, June 27, the resulting value of a revolution being $14''.76$, which is essentially identical with the preceding.) To the excess thus converted into arc is then applied $-0''.19$ for diurnal aberration; and the result is the quantity which is given in the fifteenth column of the *Transits* as the Error of Collimation, and which is adopted for correction of the observed transits.

The numerical correction to the time of observed transit, in seconds of time, is,

$$\text{Error of Collimation} \times \frac{1}{15 \sin \text{N.P.D.}}$$

Error of Level.

The error of level of the axis of revolution is considered positive when the western end of the axis is too high.

The process of determining the error of level consists in taking the reading of the transit-telescope-micrometer which makes the image of the wire as seen by reflexion from the surface of quicksilver to coincide with the wire as seen directly, as is explained in the description of the instrument above, and comparing this reading with the reading for the geometrical line of collimation. The excess of the reading for the line of collimation, above the reading for coincidence of direct and reflected images, gives the error of level, with the sign mentioned above. It is converted into arc at the rate of $14''.78$ for one revolution of the micrometer. The mean of the results is adopted sometimes for a week, sometimes for a shorter time, as the instrument appears to have been more or less steady in level.

The details of these operations are given in pages [94] to [96].

The result adopted for the error of level is given in the fifteenth column of the *Transits*.

The numerical correction to the time of observed transit, in seconds of time, is,

$$\text{Error of level} \times \frac{\text{cosine zenith distance}}{15 \sin \text{N.P.D.}}.$$

During the year 1851 observations for the error of level were usually made twice every day; but on examination there appeared to be no discoverable difference between the results for different hours of the day; and since that time the observation has been made in general only once each day. Subsequently, however, there appeared reason for believing that the variations of level have a close connexion with the variations of temperature, any sudden change of temperature being almost invariably accompanied by an abrupt change of the error of level. To verify this fact, observations of the level were made for a short period, in 1858 (see *Greenwich Observations*, 1858, Introduction, page xxiv), at the end of long night-watches, as well as at the commencement, so as to obtain a great change of temperature; and it appeared that every notable rise of temperature was accompanied with a diminution of error of level. There appears to be nothing whatever in the metallic structure of the instrument, or its mounting, which can explain this thermal change. The qualities of the stones of which the two piers are built are different; but I can scarcely imagine that such masses can so quickly receive the influence of change of temperature. In the observations of a single evening, something might be attributed to the radiation from the illuminating lamp; but this cannot explain the changes whose periods are long.

Error of Azimuth.

This error is considered positive when the Eastern pivot is too far North. It is generally determined from observations of Polaris or of δ Ursæ Minoris, at consecutive passages above and below the pole; or from one observation of Polaris combined with

one observation of another star; or occasionally, from observations of δ Ursæ Minoris combined with those of other stars. The stars Cephei 51 (Hev.) and λ Ursæ Minoris have also frequently been employed. The stars used are, however, always mentioned in the Notes; the method of using them is as follows:—

If two consecutive passages of Polaris have been observed, the first transit (as corrected for the error of collimation and level-error) is altered by the change of the star's R.A. and by the estimated clock-rate through 12^h ; and the difference, in seconds of time, between the altered first transit and the second transit (rejecting 12^h) is divided by 3.438 to obtain the azimuthal error in seconds of space.

If three transits have been observed, the difference between the first and second is taken (rejecting 12^h), and the difference between the second and third in like manner: and the mean between these is supposed to be independent of the change of R.A. and of the clock's rate, and is then divided by 3.438.

If several transits have been observed, the same process is used for every successive set of three, and the results are used separately, or the mean of the results is taken, accordingly as there appears reason to think that the position of the instrument has or has not undergone a change.

When only one observation of a circumpolar star can be obtained, the following process is used:—The letter z being put for the azimuthal error; the time of true transit of any star consists of an observed time with an additional term multiplied by z ; and, therefore, the clock-error as given by comparison of that transit with the star's tabular R.A., contains a term multiplied by z . The clock-error given thus by a star near the pole contains a large multiple of z . The clock-error given by a star far from the pole contains a small multiple of z . Equating these, with proper allowance for the rate of clock, z is found. The combination of two stars, both near the pole, but one above and the other below the pole, is very favourable, as both factors of z are large, but have opposite signs.

The error is positive when the transit of the northern star above the pole is too late. The numerical correction to the observed transit, in seconds of time, is,

$$\text{Azimuthal error} \times \frac{\sin \text{zenith distance south}}{15 \sin \text{N.P.D.}}$$

The numerical values of the three corrections for the errors of collimation, level, and azimuth, have been obtained throughout the year 1870 by means of sliding scales (one for each error) constructed by Mr. Simms, according to my directions. These scales give by simple inspection the numerical corrections in seconds of time for each transit; in the case of the stars in the Nautical Almanac, by means of their names which are written on cards attached to the scales; and, in the case of all other stars, by the North Polar Distances engraved on the scales. The value of the error in collimation, level, or azimuth, on the slider, is set to a brass pin which is let into the scale; and the value of the correction to transits, with its proper sign, is then taken out very readily at sight.

NUMERICAL CORRECTION OF TRANSITS FOR THE THREE INSTRUMENTAL ERRORS. xxxv

The following table of factors, however, for the three errors, having for argument the N.P.D. of the object, may be found convenient for the verification of the computed corrections.

N.P.D.	Collimation.	Level.	Azimuth.	N.P.D.	Collimation.	Level.	Azimuth.
	$\frac{1}{15 \sin \text{N.P.D.}}$	$\frac{\cos Z. D.}{15 \sin \text{N.P.D.}}$	$\frac{\sin Z. D.}{15 \sin \text{N.P.D.}}$		$\frac{1}{15 \sin \text{N.P.D.}}$	$\frac{\cos Z. D.}{15 \sin \text{N.P.D.}}$	$\frac{\sin Z. D.}{15 \sin \text{N.P.D.}}$
—45. 0	—0.094	—0.011	+0.094	—7. 30	—0.511	—0.355	+0.368
—44. 0	—0.096	—0.013	+0.095	—7. 0	—0.547	—0.383	+0.390
—43. 0	—0.098	—0.014	+0.096	—6. 30	—0.589	—0.416	+0.417
—42. 0	—0.100	—0.016	+0.098	—6. 0	—0.638	—0.455	+0.447
—41. 0	—0.102	—0.018	+0.100				
—40. 0	—0.104	—0.021	+0.102	6. 0	+0.638	+0.538	—0.343
—39. 0	—0.106	—0.023	+0.104	6. 30	+0.589	+0.499	—0.312
—38. 0	—0.108	—0.025	+0.105	7. 0	+0.547	+0.466	—0.286
—37. 0	—0.111	—0.027	+0.107	7. 30	+0.511	+0.438	—0.263
—36. 0	—0.113	—0.030	+0.109	8. 0	+0.479	+0.413	—0.243
—35. 0	—0.116	—0.033	+0.111	8. 30	+0.451	+0.391	—0.226
—34. 0	—0.119	—0.036	+0.114	9. 0	+0.426	+0.371	—0.210
—33. 0	—0.122	—0.039	+0.116	9. 30	+0.404	+0.353	—0.196
—32. 0	—0.126	—0.042	+0.119	10. 0	+0.384	+0.337	—0.183
—31. 0	—0.129	—0.045	+0.121	10. 30	+0.366	+0.323	—0.172
—30. 0	—0.133	—0.049	+0.124	11. 0	+0.349	+0.310	—0.161
—29. 0	—0.138	—0.053	+0.127	11. 30	+0.334	+0.298	—0.152
—28. 0	—0.142	—0.057	+0.130	12. 0	+0.321	+0.287	—0.143
—27. 0	—0.147	—0.061	+0.133	12. 30	+0.308	+0.277	—0.135
—26. 0	—0.152	—0.065	+0.137	13. 0	+0.296	+0.267	—0.128
—25. 0	—0.158	—0.070	+0.141	13. 30	+0.286	+0.259	—0.122
—24. 0	—0.164	—0.076	+0.145	14. 0	+0.276	+0.251	—0.116
—23. 0	—0.171	—0.082	+0.150	14. 30	+0.266	+0.244	—0.111
—22. 0	—0.178	—0.088	+0.155	15. 0	+0.257	+0.236	—0.105
—21. 0	—0.186	—0.094	+0.160	15. 30	+0.249	+0.230	—0.099
—20. 0	—0.195	—0.102	+0.166	16. 0	+0.242	+0.224	—0.093
—19. 30	—0.200	—0.106	+0.170	16. 30	+0.235	+0.218	—0.088
—19. 0	—0.205	—0.110	+0.173	17. 0	+0.228	+0.212	—0.084
—18. 30	—0.210	—0.114	+0.176	17. 30	+0.222	+0.207	—0.080
—18. 0	—0.216	—0.119	+0.180	18. 0	+0.216	+0.202	—0.076
—17. 30	—0.222	—0.124	+0.184	18. 30	+0.210	+0.197	—0.072
—17. 0	—0.228	—0.129	+0.188	19. 0	+0.205	+0.193	—0.068
—16. 30	—0.235	—0.134	+0.192	19. 30	+0.200	+0.189	—0.065
—16. 0	—0.242	—0.140	+0.197	20. 0	+0.195	+0.185	—0.062
—15. 30	—0.249	—0.146	+0.202	21. 0	+0.186	+0.177	—0.056
—15. 0	—0.257	—0.153	+0.207	22. 0	+0.178	+0.171	—0.051
—14. 30	—0.266	—0.160	+0.213	23. 0	+0.171	+0.164	—0.046
—14. 0	—0.276	—0.168	+0.219	24. 0	+0.164	+0.159	—0.041
—13. 30	—0.286	—0.176	+0.225	25. 0	+0.158	+0.153	—0.037
—13. 0	—0.296	—0.184	+0.232	26. 0	+0.152	+0.148	—0.033
—12. 30	—0.308	—0.194	+0.240	27. 0	+0.147	+0.144	—0.029
—12. 0	—0.321	—0.204	+0.248	28. 0	+0.142	+0.140	—0.026
—11. 30	—0.334	—0.214	+0.256	29. 0	+0.138	+0.136	—0.023
—11. 0	—0.349	—0.227	+0.266	30. 0	+0.133	+0.131	—0.020
—10. 30	—0.366	—0.240	+0.276	31. 0	+0.129	+0.128	—0.017
—10. 0	—0.384	—0.254	+0.288	32. 0	+0.126	+0.125	—0.014
—9. 30	—0.404	—0.270	+0.300	33. 0	+0.122	+0.122	—0.012
—9. 0	—0.426	—0.288	+0.314	34. 0	+0.119	+0.119	—0.009
—8. 30	—0.451	—0.308	+0.330	35. 0	+0.116	+0.116	—0.007
—8. 0	—0.479	—0.330	+0.348	36. 0	+0.113	+0.113	—0.005
—7. 30	—0.511	—0.355	+0.368	37. 0	+0.111	+0.111	—0.003

xxxvi INTRODUCTION TO GREENWICH ASTRONOMICAL OBSERVATIONS, 1870.

N.P.D.	Collimation.	Level.	Azimuth.	N.P.D.	Collimation.	Level.	Azimuth.
	$\frac{1}{15 \sin N.P.D.}$	$\frac{\cos Z. D.}{15 \sin N.P.D.}$	$\frac{\sin Z. D.}{15 \sin N.P.D.}$		$\frac{1}{15 \sin N.P.D.}$	$\frac{\cos Z. D.}{15 \sin N.P.D.}$	$\frac{\sin Z. D.}{15 \sin N.P.D.}$
37. °	+0.111	+0.111	-0.003	82. °	+0.067	+0.049	+0.046
38. °	+0.108	+0.108	-0.001	83. °	+0.067	+0.048	+0.047
39. °	+0.106	+0.106	+0.001	84. °	+0.067	+0.047	+0.048
40. °	+0.104	+0.104	+0.003	85. °	+0.067	+0.046	+0.048
41. °	+0.102	+0.101	+0.004	86. °	+0.067	+0.045	+0.049
42. °	+0.100	+0.099	+0.006	87. °	+0.067	+0.044	+0.050
43. °	+0.098	+0.097	+0.007	88. °	+0.067	+0.043	+0.051
44. °	+0.096	+0.096	+0.009	89. °	+0.067	+0.042	+0.052
45. °	+0.094	+0.094	+0.011	90. °	+0.067	+0.041	+0.052
46. °	+0.093	+0.092	+0.012	91. °	+0.067	+0.040	+0.053
47. °	+0.091	+0.090	+0.013	92. °	+0.067	+0.040	+0.054
48. °	+0.090	+0.088	+0.015	93. °	+0.067	+0.039	+0.054
49. °	+0.088	+0.087	+0.016	94. °	+0.067	+0.038	+0.055
50. °	+0.087	+0.085	+0.017	95. °	+0.067	+0.037	+0.056
51. °	+0.086	+0.084	+0.018	96. °	+0.067	+0.036	+0.057
52. °	+0.085	+0.082	+0.020	97. °	+0.067	+0.035	+0.057
53. °	+0.083	+0.081	+0.021	98. °	+0.067	+0.034	+0.058
54. °	+0.082	+0.080	+0.022	99. °	+0.067	+0.033	+0.059
55. °	+0.081	+0.078	+0.023	100. °	+0.068	+0.032	+0.060
56. °	+0.080	+0.077	+0.024	101. °	+0.068	+0.031	+0.060
57. °	+0.080	+0.075	+0.025	102. °	+0.068	+0.030	+0.061
58. °	+0.079	+0.074	+0.026	103. °	+0.068	+0.029	+0.062
59. °	+0.078	+0.073	+0.027	104. °	+0.069	+0.028	+0.063
60. °	+0.077	+0.072	+0.028	105. °	+0.069	+0.027	+0.063
61. °	+0.076	+0.070	+0.029	106. °	+0.069	+0.027	+0.064
62. °	+0.076	+0.069	+0.030	107. °	+0.070	+0.026	+0.065
63. °	+0.075	+0.068	+0.031	108. °	+0.070	+0.025	+0.066
64. °	+0.074	+0.067	+0.032	109. °	+0.071	+0.024	+0.066
65. °	+0.073	+0.066	+0.033	110. °	+0.071	+0.023	+0.067
66. °	+0.073	+0.065	+0.034	111. °	+0.072	+0.022	+0.068
67. °	+0.072	+0.064	+0.035	112. °	+0.072	+0.021	+0.069
68. °	+0.072	+0.063	+0.035	113. °	+0.073	+0.020	+0.070
69. °	+0.071	+0.061	+0.036	114. °	+0.073	+0.018	+0.071
70. °	+0.071	+0.060	+0.037	115. °	+0.074	+0.017	+0.072
71. °	+0.071	+0.059	+0.038	116. °	+0.075	+0.016	+0.072
72. °	+0.070	+0.058	+0.039	117. °	+0.075	+0.015	+0.073
73. °	+0.070	+0.057	+0.039	118. °	+0.076	+0.014	+0.074
74. °	+0.069	+0.056	+0.040	119. °	+0.076	+0.013	+0.075
75. °	+0.069	+0.055	+0.041	120. °	+0.077	+0.012	+0.076
76. °	+0.069	+0.054	+0.042	121. °	+0.078	+0.011	+0.077
77. °	+0.068	+0.053	+0.043	122. °	+0.079	+0.009	+0.078
78. °	+0.068	+0.053	+0.043	123. °	+0.080	+0.008	+0.079
79. °	+0.068	+0.052	+0.044	124. °	+0.080	+0.007	+0.080
80. °	+0.068	+0.051	+0.045	125. °	+0.081	+0.005	+0.081
81. °	+0.067	+0.050	+0.045	126. °	+0.082	+0.004	+0.082
82. °	+0.067	+0.049	+0.046				

The *sixteenth* column contains the seconds of every transit, as affected with the three preceding corrections; and is conceived to represent the clock-time at which each body passed the true astronomical meridian of Greenwich. The numbers to which a bracket is annexed are those resulting from the mean of the two limbs of the Sun or a planet.

The *seventeenth* column contains the seconds of the tabular R.A. of the stars which are used for determining clock-errors. In addition to the list of stars taken from the

TRUE TRANSIT: ASSUMED RIGHT ASCENSIONS OF CLOCK STARS. xxxvii

Nautical Almanac, whose North Polar Distances exceed 50° , there has been used, as in preceding years, another list, consisting in the year 1870 of 92 stars, selected and observed for this purpose, and lying within the same limit of Polar Distance. The apparent clock-errors given by the observations of Polaris, Cephei 51 (Hev.), δ Ursæ Minoris, and λ Ursæ Minoris, are set down, whenever they have been actually used in determining the azimuthal error, to enable the reader to judge of the general state of adjustment of the instrument.

For the Nautical-Almanac-stars, the Right Ascensions are computed by applying, to the numbers given in the Nautical Almanac, corrections fundamentally deduced from the "New Seven-Year Catalogue of 2760 Stars, deduced from Observations, extending from 1861 to 1867, at the Royal Observatory, Greenwich, and reduced to the "Epoch 1864," which is printed as an Appendix to the volume for 1868. To bring up the Mean Right Ascensions from the epoch of the Catalogue, viz., 1864, to the year 1870, use has been made of the precessions of that Catalogue, and of the proper motions given by Mr. Main or by Mr. Stone. The corrections necessary to bring up the stars' Right Ascensions to the day of observation are computed by the formula $E e + F f + G g + H h + L + l - 300^s + \mu t$, to which further allusion will be made below. For stars near the pole, the additional correction depending on the place of the Moon is also taken into account. The following table gives the Mean Right Ascensions for 1870, January 1, of all the stars which have been used in 1870 for determining clock-errors, together with the constant corrections to the Right Ascensions of the Nautical-Almanac-stars; it gives also, in addition, the Right Ascensions of Polaris and other stars very near the pole, which have been observed for the determination of azimuthal error throughout the year 1870.

ASSUMED MEAN RIGHT ASCENSIONS OF CLOCK STARS AND CIRCUMPOLAR STARS, WITH THE CORRECTIONS TO THE NAUTICAL ALMANAC, FOR 1870, JANUARY 1.

Star's Name.	Assumed Mean R. A. 1870, Jan. 1.	Correction to N.A.	Star's Name.	Assumed Mean R. A. 1870, Jan. 1.	Correction to N.A.
α Andromedæ.....	^h 0. ^m 1. ^s 40.27	+ 0.03	α Arietis.....	^h 1. ^m 59. ^s 50.92	+ 0.01
γ Pegasi.....	0. 6. 32.58	+ 0.03	ξ^1 Ceti.....	2. 6. 6.72	
ϵ Ceti.....	0. 12. 48.17		67 Ceti.....	2. 10. 29.96	+ 0.04
44 Piscium.....	0. 18. 44.31		ξ^2 Ceti.....	2. 21. 14.93	0.00
12 Ceti.....	0. 23. 24.20	- 0.07	ν Ceti.....	2. 29. 3.17	
ϵ Andromedæ.....	0. 31. 41.41		δ Ceti.....	2. 32. 49.24	
β Ceti.....	0. 37. 3.75	+ 0.10	γ^2 Ceti.....	2. 36. 33.94	+ 0.03
δ Piscium.....	0. 41. 56.28		σ Arietis.....	2. 44. 19.04	
μ Andromedæ.....	0. 49. 32.62		α Ceti.....	2. 55. 29.12	+ 0.08
ϵ Piscium.....	0. 56. 11.86	- 0.03	δ Arietis.....	3. 4. 11.91	+ 0.01
β Andromedæ.....	1. 2. 27.56		τ Arietis.....	3. 13. 43.49	
ζ Piscium.....	1. 6. 56.43		σ Tauri.....	3. 17. 49.17	
Polaris.....	1. 11. 16.83	- 0.16	f Tauri.....	3. 23. 41.87	
θ Ceti.....	1. 17. 31.50	+ 0.03	ϵ Eridani.....	3. 26. 48.36	
η Piscium.....	1. 24. 31.76	+ 0.06	11 Tauri.....	3. 33. 0.60	
ν Piscium.....	1. 34. 40.02	+ 0.02	δ Eridani.....	3. 37. 1.27	
σ Piscium.....	1. 38. 31.81		η Tauri.....	3. 39. 45.60	+ 0.06
β Arietis.....	1. 47. 27.69	+ 0.03	γ Eridani.....	3. 51. 57.84	+ 0.04

xxxviii INTRODUCTION TO GREENWICH ASTRONOMICAL OBSERVATIONS, 1870.

ASSUMED MEAN RIGHT ASCENSIONS OF CLOCK STARS AND CIRCUMPOLAR STARS,
WITH THE CORRECTIONS TO THE NAUTICAL ALMANAC, FOR 1870, JANUARY 1—*cont.*

Star's Name.	Assumed Mean R.A. 1870, Jan. 1.	Correction to N.A.	Star's Name.	Assumed Mean R.A. 1870, Jan. 1.	Correction to N.A.
ω^1 Tauri.....	^h 4. ^m 1. ^s 35.69		34 Sextantis.....	^h 10. ^m 35. ^s 54.63	
ϕ^1 Eridani.....	4. 5. 31.21	+ 0.01	ι Leonis.....	10. 42. 25.34	+ 0.05
γ Tauri.....	4. 12. 23.81		d Leonis.....	10. 53. 50.73	
ϵ Tauri.....	4. 21. 1.62	0.00	χ Leonis.....	10. 58. 18.58	- 0.02
Aldebaran.....	4. 28. 27.75	- 0.03	δ Leonis.....	11. 7. 11.49	- 0.02
τ Tauri.....	4. 34. 26.62		δ Crateris.....	11. 12. 50.55	+ 0.05
μ Eridani.....	4. 39. 0.17		τ Leonis.....	11. 21. 15.05	
ι Aurigæ.....	4. 48. 31.79	- 0.02	ν Leonis.....	11. 30. 17.54	- 0.02
ϵ Leporis.....	4. 59. 57.50	+ 0.09	β Leonis.....	11. 42. 25.62	+ 0.04
Rigel.....	5. 8. 17.43	+ 0.02	π Virginis.....	11. 54. 12.65	
β Tauri.....	5. 18. 4.51	+ 0.02	ϵ Corvi.....	12. 3. 26.51	+ 0.01
δ Orionis.....	5. 25. 21.91	- 0.07	η Virginis.....	12. 13. 15.29	+ 0.05
α Leporis.....	5. 26. 59.81	- 0.05	δ^2 Corvi.....	12. 23. 8.46	
ϵ Orionis.....	5. 29. 37.01	- 0.01	β Corvi.....	12. 27. 33.68	+ 0.17
α Columbæ.....	5. 34. 56.57	- 0.15	ρ Virginis.....	12. 35. 18.28	
κ Orionis.....	5. 41. 35.43		35 Virginis.....	12. 41. 14.26	
α Orionis.....	5. 48. 8.04	+ 0.01	δ Virginis.....	12. 49. 3.33	
ι Geminorum.....	5. 56. 13.07		ϵ Virginis.....	12. 55. 42.33	
ν Orionis.....	6. 0. 8.96	- 0.03	θ Virginis.....	13. 3. 13.20	+ 0.01
η Geminorum.....	6. 7. 1.82		Spica.....	13. 18. 20.76	+ 0.02
μ Geminorum.....	6. 15. 5.72	- 0.02	ζ Virginis.....	13. 28. 4.19	- 0.04
β Canis Majoris.....	6. 16. 58.49		m Virginis.....	13. 34. 47.42	
ν Geminorum.....	6. 21. 14.60		τ Boötis.....	13. 41. 5.07	
γ Geminorum.....	6. 30. 12.04	- 0.06	η Boötis.....	13. 48. 29.69	+ 0.02
Cephei 51.....	6. 38. 43.55	+ 2.73	τ Virginis.....	13. 55. 1.88	+ 0.03
θ Canis Majoris.....	6. 48. 8.99		κ Virginis.....	14. 5. 57.78	
ϵ Canis Majoris.....	6. 53. 30.99	- 0.04	Areturus.....	14. 9. 43.92	+ 0.02
ζ Geminorum.....	6. 56. 23.85		f Boötis.....	14. 20. 24.61	
γ Canis Majoris.....	6. 57. 52.62	- 0.04	ρ Boötis.....	14. 26. 13.62	- 0.03
51 Geminorum.....	7. 5. 54.32		ϵ^2 Boötis.....	14. 39. 18.57	+ 0.07
δ Geminorum.....	7. 12. 21.44	- 0.04	α Libræ.....	14. 43. 41.38	+ 0.04
β Canis Minoris.....	7. 20. 5.99		ϵ^2 Libræ.....	14. 49. 42.99	
Castor.....	7. 26. 18.12	- 0.03	ψ Boötis.....	14. 58. 52.52	- 0.06
Procyon.....	7. 32. 29.73	+ 0.04	β Libræ.....	15. 10. 0.77	+ 0.01
Pollux.....	7. 37. 21.47	0.00	ϕ^2 Libræ.....	15. 15. 46.87	
ξ Navis.....	7. 43. 49.62		ζ^1 Libræ.....	15. 20. 55.69	
6 Cancri.....	7. 55. 31.84	- 0.06	α Coronæ.....	15. 29. 11.04	+ 0.05
15 Argûs.....	8. 2. 0.43	- 0.05	α Serpentis.....	15. 37. 51.93	+ 0.07
β Cancri.....	8. 9. 27.80		ϵ Serpentis.....	15. 44. 20.18	
d^1 Cancri.....	8. 15. 55.04		γ Serpentis.....	15. 50. 26.96	
η Cancri.....	8. 25. 11.28	+ 0.04	β Scorpii.....	15. 57. 52.83	+ 0.03
γ Cancri.....	8. 35. 45.58		δ Ophiuchi.....	16. 7. 32.02	+ 0.03
ϵ Hydræ.....	8. 39. 53.39	- 0.04	γ Herculis.....	16. 16. 11.14	
α Cancri.....	8. 51. 22.49		Antares.....	16. 21. 26.35	+ 0.02
κ Cancri.....	9. 0. 42.23		λ Ophiuchi.....	16. 24. 21.46	
83 Cancri.....	9. 11. 43.34	+ 0.10	ζ Ophiuchi.....	16. 30. 0.10	
α Hydræ.....	9. 21. 11.90	+ 0.01	ζ Herculis.....	16. 36. 23.19	+ 0.03
ξ Leonis.....	9. 24. 56.19		κ Ophiuchi.....	16. 51. 30.92	- 0.02
ϕ Leonis.....	9. 34. 12.61		ϵ Herculis.....	16. 55. 18.99	
ϵ Leonis.....	9. 38. 28.08	0.00	η Ophiuchi.....	17. 2. 55.40	
μ Leonis.....	9. 45. 21.94		α Herculis.....	17. 8. 43.21	+ 0.07
π Leonis.....	9. 53. 20.51	- 0.01	θ Ophiuchi.....	17. 14. 1.62	+ 0.06
Regulus.....	10. 1. 26.76	- 0.02	σ Ophiuchi.....	17. 20. 3.88	
γ Leonis.....	10. 12. 48.10	- 0.02	α Ophiuchi.....	17. 28. 54.00	+ 0.05
μ Hydræ.....	10. 19. 48.23		β Ophiuchi.....	17. 37. 3.02	
ρ Leonis.....	10. 25. 57.86	- 0.03	μ Herculis.....	17. 41. 22.30	+ 0.08

ASSUMED RIGHT ASCENSIONS OF CLOCK STARS; CLOCK RATES AND ERRORS. xxxix

ASSUMED MEAN RIGHT ASCENSIONS OF CLOCK STARS AND CIRCUMPOLAR STARS,
WITH THE CORRECTIONS TO THE NAUTICAL ALMANAC, FOR 1870, JANUARY 1—*concl.*

Star's Name.	Assumed Mean R.A. 1870, Jan. 1.	Correction to N.A.	Star's Name.	Assumed Mean R.A. 1870, Jan. 1.	Correction to N.A.
89 Herculis	^h ^m ^s 17. 50. 10.53	^s	32 Vulpeculæ.....	^h ^m ^s 20. 49. 1.18	+ 0.03
72 Ophiuchi.....	18. 1. 11.17		θ Capricorni.....	20. 58. 38.19	
μ Sagittarii	18. 5. 59.29	+ 0.06	ζ Cygni	21. 7. 24.23	+ 0.08
δ Ursæ Minoris....	18. 14. 16.45	- 0.22	α Equulei.....	21. 9. 19.46	
η Serpentis.....	18. 14. 34.98		ι Capricorni.....	21. 15. 0.29	
λ Sagittarii	18. 19. 56.83		β Aquarii.....	21. 24. 42.78	+ 0.04
α Lyræ.....	18. 32. 32.20	+ 0.04	ξ Aquarii.....	21. 30. 49.73	
β Lyræ.....	18. 45. 16.81	+ 0.10	ε Pegasi.....	21. 37. 48.05	0.00
ε Aquilæ.....	18. 53. 43.29		δ Capricorni.....	21. 39. 51.75	
ζ Aquilæ.....	18. 59. 26.05	+ 0.14	16 Pegasi.....	21. 47. 8.87	0.00
ψ Sagittarii	19. 7. 34.00		α Aquarii.....	21. 59. 6.31	+ 0.03
ω Aquilæ.....	19. 11. 42.82	+ 0.03	ι Pegasi.....	22. 0. 57.60	
δ Aquilæ.....	19. 18. 56.56	+ 0.04	θ Aquarii.....	22. 9. 58.29	0.00
α Vulpeculæ.....	19. 23. 17.76		γ Aquarii.....	22. 14. 56.42	
μ Aquilæ.....	19. 27. 44.28		σ Aquarii.....	22. 23. 45.91	
ε ¹ Sagittarii	19. 33. 16.43		η Aquarii.....	22. 28. 40.49	+ 0.03
γ Aquilæ.....	19. 40. 4.71	+ 0.05	ζ Pegasi.....	22. 34. 58.69	+ 0.09
α Aquilæ.....	19. 44. 26.38	+ 0.04	μ Pegasi.....	22. 43. 43.81	
β Aquilæ.....	19. 48. 55.61	+ 0.06	λ Aquarii.....	22. 45. 49.81	
λ Ursæ Minoris....	19. 54. 16.12	- 1.70	Fomalhaut.....	22. 50. 27.68	+ 0.04
c Sagittarii	19. 54. 39.64		α Pegasi.....	22. 58. 17.16	+ 0.02
θ Aquilæ.....	20. 4. 35.75		γ Piscium.....	23. 10. 25.52	0.00
α ² Capricorni.....	20. 10. 50.37	+ 0.07	κ Piscium.....	23. 20. 16.05	- 0.03
β Capricorni.....	20. 13. 42.28		ι Piscium.....	23. 33. 15.82	- 0.04
ρ Capricorni.....	20. 21. 26.55	+ 0.17	δ Sculptoris.....	23. 42. 9.00	- 0.01
ε Delphini.....	20. 27. 0.09		ω Piscium.....	23. 52. 38.16	- 0.04
α Delphini.....	20. 33. 35.97		2 Ceti.....	23. 57. 4.68	
ε Aquarii.....	20. 40. 38.18				

The *eighteenth* column contains the error of the clock, found by subtracting the numbers in the sixteenth column from those in the seventeenth. The error is therefore positive when the clock is slow.

The *nineteenth* column contains the adopted losing rate, and the adopted error of the clock at 0^h sidereal, as found by the following process. The observations are divided into groups, defined by bars across this column (in all instances the same as the limits of the observations of each observer). The mean of the clock-errors given by all the clock-stars in each group is then taken, and this is considered to be the clock-error corresponding to the mean of all the times of transit of those stars. The next step is to investigate the clock-rate, making allowance for personal equation between the transits of successive observers; and it will be sufficient to explain the personal equation existing between any two observers, but more especially between Mr. Dunkin and some other observer; for example, between Mr. Dunkin and Mr. Ellis; since it was the practice until the end of 1870 to reduce all the clock-times of observation with the Altazimuth to sidereal time by means of errors of the transit-clock referred to Mr. Dunkin as the standard. Suppose then that transits have been observed on suc-

cessive days by Mr. Dunkin and Mr. Ellis, and that, for the set of observations on each day, the mean is taken as described above. It will be seen by one of the tables in the Introduction to the *Greenwich Observations*, 1869, page xlvii, that the clock-error given by Mr. Ellis's observations is greater than that given by Mr. Dunkin's observations by $0^s.20$, as deduced from observations suitable for the determination of this quantity in the year 1869; and this is the last determination of personal equation which is available for the daily reduction of observations in 1870. The quantity $0^s.20$ is therefore subtracted from Mr. Ellis's clock-errors, and it is then considered that we have two sets of clock-errors (namely, Mr. Dunkin's as unaltered, and Mr. Ellis's as modified) justly comparable. Each mean clock-error, properly modified, is now compared with that which precedes and with that which follows; a preceding rate and a following rate are thus found, and by these the computer is guided in adopting the clock-rate to be used through the group of observations: this adopted clock-rate is set down in the nineteenth column. For facility of calculation, the proportional part of this rate, corresponding to the mean sidereal time or mean of all the times of transit for the group, is applied with changed sign to the mean clock-error; and thus the clock-error at 0^h sidereal is found. If it happen that any observations included in the same group are made in the sidereal day preceding or following that for which the mean error has been found, the whole adopted daily rate is subtracted from or added to the error found for 0^h ; and thus the error for 0^h of the preceding or the following sidereal day is obtained. These errors at 0^h for all the different sidereal days are also set down in the nineteenth column. It is to be remarked that, in the application of these errors, if the observations of small stars and planets have been made by the same person as the observations of the clock-stars (whether it be Mr. Dunkin or Mr. Ellis), no further computation is necessary for obtaining the right ascensions of those objects than the application, to the time of transit, of the clock-error at 0^h , and of a proportional part of the clock-rate corresponding to the right ascension of the object: but, if the clock-stars are observed by Mr. Ellis, and the other object by Mr. Dunkin, a further correction $-0^s.20$ must be applied: if the clock-stars are observed by Mr. Dunkin, and the object by Mr. Ellis, $+0^s.20$ must be applied. The personal equations are *not* applied in the column of *Apparent Right Ascensions from the Observations* in this Section.

In the preceding years, observations were exhibited which gave the relative personal equations of the different observers of transits, as far as means existed for determining them. In the year 1870 the following sets of observations have been found available for determining personal equations in the use of the galvanic method of recording transits. They have been treated in the same manner as in preceding years, by comparing the clock-error at the same sidereal hour given by two different groups of stars observed by different persons, but are referred to Mr. Criswick instead of Mr. Dunkin as standard.

PERSONAL EQUATIONS IN CHRONOGRAPHIC TRANSITS.

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OBSERVATIONS FOR THE DETERMINATION OF THE PERSONAL EQUATIONS OF
THE VARIOUS TRANSIT-OBSERVERS USING THE GALVANIC METHOD OF
OBSERVING TRANSITS.

Day, 1870.	Observers in order of Seniority.	Interval of nearest Stars.	Order of Observations.	Clock Slow at 0^h Sidereal by Senior Observer.	Clock Slow at 0^h Sidereal by Junior Observer.	Excess of Clock Slow by Junior Observer.
April 21	S and C	0^h	C S	$30^s.86$	$30^s.62$	$- 0^s.24$
April 21	S and H C	3	S H C	$30^s.86$	$30^s.54$	$- 0^s.32$
October 11	W C and C	0	W C C	$50^s.30$	$50^s.23$	$- 0^s.07$
November 2		0	C W C	$20^s.16$	$20^s.03$	$- 0^s.13$
December 12		4	C W C	$50^s.13$	$50^s.09$	$- 0^s.04$
October 3	W C and J C	0	W C J C	$37^s.12$	$37^s.00$	$- 0^s.12$
„ 27		0	W C J C	$12^s.16$	$12^s.04$	$- 0^s.12$
October 31	W C and H C	0	H C W C	$17^s.06$	$16^s.95$	$- 0^s.11$
December 12	W C and J	2	W C J	$50^s.13$	$50^s.05$	$- 0^s.08$
June 18	D and E	3	D E	$37^s.20$	$37^s.39$	$+ 0^s.19$
August 15		1	D E	$30^s.71$	$30^s.89$	$+ 0^s.18$
February 5	D and C	0	C D	$57^s.33$	$57^s.21$	$- 0^s.12$
„ 9		2	C D	$61^s.17$	$61^s.11$	$- 0^s.06$
August 17		5	D C	$38^s.63$	$38^s.61$	$- 0^s.02$
January 8	D and J C	2	J C D	$38^s.70$	$38^s.50$	$- 0^s.20$
„ 10		1	D J C	$40^s.95$	$40^s.90$	$- 0^s.05$
„ 12		0	J C D	$42^s.51$	$42^s.43$	$- 0^s.08$
August 17	D and J	4	J D	$38^s.63$	$38^s.56$	$- 0^s.07$
January 3	E and C	0	E C	$32^s.28$	$32^s.05$	$- 0^s.23$
„ 5		0	C E	$35^s.25$	$35^s.01$	$- 0^s.24$
„ 11		0	E C	$42^s.06$	$41^s.69$	$- 0^s.37$
February 21		1	C E	$9^s.26$	$8^s.96$	$- 0^s.30$
April 4		0	E C	$50^s.06$	$49^s.81$	$- 0^s.25$
„ 6		0	C E	$47^s.78$	$47^s.50$	$- 0^s.28$
„ 8		0	C E	$45^s.36$	$45^s.10$	$- 0^s.26$
„ 10		0	E C	$42^s.94$	$42^s.67$	$- 0^s.27$
„ 12		0	C E	$40^s.53$	$40^s.22$	$- 0^s.31$
August 29		0	C E	$24^s.88$	$24^s.63$	$- 0^s.25$
„ 31		0	E C	$30^s.14$	$29^s.82$	$- 0^s.32$
September 2		0	E C	$34^s.78$	$34^s.51$	$- 0^s.27$
„ 28		0	E C	$27^s.87$	$27^s.57$	$- 0^s.30$

GREENWICH OBSERVATIONS 1870.

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OBSERVATIONS FOR PERSONAL EQUATIONS—continued.

Day, 1870.	Observers in order of Seniority.	Interval of nearest Stars.	Order of Observations.		Clock Slow at 0 ^h Sidereal by Senior Observer.	Clock Slow at 0 ^h Sidereal by Junior Observer.	Excess of Clock Slow by Junior Observer.
October 2	E and C <i>cont.</i>	0	C	E	35.23	34.96	— 0.27
November 26		1	C	E	49.18	48.90	— 0.28
December 4		0	E	C	52.37	52.15	— 0.22
May 17	E and L	0	E	L	15.01	14.52	— 0.59
„ 19		1	L	E	16.22	15.82	— 0.40
„ 21		5	E	L	17.18	16.76	— 0.42
August 6		0	E	L	11.78	11.36	— 0.42
„ 8		0	L	E	12.67	12.22	— 0.45
October 4		1	L	E	39.06	38.57	— 0.49
„ 8		0	L	E	45.36	44.90	— 0.46
„ 10		0	L	E	48.89	48.46	— 0.43
„ 12		0	E	L	51.48	51.00	— 0.48
„ 26		2	L	E	10.95	10.45	— 0.50
November 1		0	L	E	18.90	18.54	— 0.36
February 10	E and J C	0	E	J C	2.30	2.07	— 0.23
March 24		2	E	J C	63.28	63.02	— 0.26
April 19		0	J C	E	33.09	32.86	— 0.23
May 19		1	E	J C	16.22	16.06	— 0.16
June 6		0	J C	E	27.27	27.09	— 0.18
„ 8		0	E	J C	28.97	28.81	— 0.16
„ 9		0	E	J C	30.44	30.22	— 0.22
„ 12		0	J C	E	32.25	32.02	— 0.23
„ 14		0	J C	E	34.15	33.84	— 0.31
July 7		0	E	J C	49.85	49.72	— 0.13
„ 13		0	J C	E	54.34	54.13	— 0.21
„ 15		0	E	J C	55.87	55.55	— 0.32
„ 21		4	J C	E	60.98	60.76	— 0.22
„ 23		5	E	J C	3.98	3.68	— 0.30
August 15		4	E	J C	32.63	32.52	— 0.11
September 4		0	J C	E	39.47	39.23	— 0.24
„ 6		0	E	J C	43.82	43.60	— 0.22
„ 20		1	E	J C	14.21	13.95	— 0.26
October 18		2	E	J C	59.22	59.01	— 0.21
November 12		1	J C	E	34.18	33.97	— 0.21

PERSONAL EQUATIONS IN CHRONOGRAPHIC TRANSITS.

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OBSERVATIONS FOR PERSONAL EQUATIONS—*continued.*

Day, 1870.	Observers in order of Seniority.	Interval of nearest Stars.	Order of Observations.	Clock Slow at 0 ^h Sidereal by Senior Observer.	Clock Slow at 0 ^h Sidereal by Junior Observer.	Excess of Clock slow by Junior Observer.
January 25	E and H C	^h 1	E H C	50.98	50.79	— 0.19
March 10		0	H C E	13.07	12.85	— 0.22
„ 14		0	H C E	12.28	11.99	— 0.29
April 16		0	E H C	36.21	36.02	— 0.19
„ 18		2	E H C	34.25	33.97	— 0.28
May 3		0	H C E	14.79	14.53	— 0.26
„ 9		0	E H C	12.15	11.99	— 0.16
„ 20		4	H C E	17.18	16.98	— 0.20
June 21		3	H C E	39.60	39.26	— 0.34
November 15		0	H C E	38.36	38.11	— 0.25
December 24		0	H C E	33.03	32.83	— 0.20
February 24	E and K	1	E K	10.18	10.05	— 0.13
March 24		5	K E	63.28	63.19	— 0.09
April 14		0	K E	38.13	38.01	— 0.12
„ 18		1	K E	34.25	34.15	— 0.10
May 13		0	K E	13.45	13.31	— 0.14
August 11		1	E K	15.95	15.71	— 0.24
May 7	E and P	0	E P	10.50	10.37	— 0.13
„ 11		0	P E	13.13	13.04	— 0.09
August 19		1	P E	53.65	53.58	— 0.07
September 22		6	E P	18.20	17.99	— 0.21
August 17	E and J	0	E J	36.61	36.46	— 0.15
October 14		0	E J	53.62	53.40	— 0.22
December 29		0	J E	34.27	34.12	— 0.15
February 15	C and L	0	C L	5.45	5.16	— 0.29
June 9		0	C L	29.34	29.26	— 0.08
„ 11		1	C L	31.08	30.87	— 0.21
„ 22		3	C L	39.95	39.86	— 0.09
July 10		0	C L	52.00	51.80	— 0.20
„ 12		0	L C	53.49	53.26	— 0.23
„ 14		0	C L	54.90	54.81	— 0.09
„ 16		1	L C	56.31	56.20	— 0.11
„ 20		2	L C	59.75	59.64	— 0.11
„ 22		4	C L	61.53	61.35	— 0.18

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OBSERVATIONS FOR PERSONAL EQUATIONS—*continued*.

Day, 1870.	Observers in order of Seniority.	Interval of nearest Stars.	Order of Observations.		Clock Slow at 0 ^h Sidereal by Senior Observer.	Clock Slow at 0 ^h Sidereal by Junior Observer.	Excess of Clock Slow by Junior Observer.
August 10	C and L <i>cont.</i>	^h 0	L	C	13 ^s ·21	13 ^s ·09	— 0 ^s ·12
September 7		0	L	C	45·80	45·63	— 0·17
„ 9		0	C	L	49·92	49·72	— 0·20
„ 15		0	C	L	1·92	1·76	— 0·16
„ 19		0	C	L	9·65	9·43	— 0·22
November 13		6	C	L	35·25	35·11	— 0·14
January 24	C and J C	4	J C	C	49·89	49·93	+ 0·04
March 5		0	J C	C	11·90	11·91	+ 0·01
„ 13		1	C	J C	12·29	12·34	+ 0·05
„ 19		2	C	J C	8·00	8·06	+ 0·06
April 15		3	J C	C	36·75	36·91	+ 0·16
„ 19		4	C	J C	32·91	32·86	— 0·05
„ 23		5	C	J C	28·12	28·23	+ 0·11
May 4		1	J C	C	13·01	13·16	+ 0·15
„ 6		0	C	J C	9·64	9·68	+ 0·04
„ 8		1	J C	C	11·03	11·14	+ 0·11
„ 10		0	C	J C	12·45	12·52	+ 0·07
„ 12		0	J C	C	13·05	13·07	+ 0·02
„ 14		0	J C	C	13·50	13·56	+ 0·06
„ 16		0	J C	C	14·17	14·20	+ 0·03
„ 18		0	C	J C	15·31	15·28	— 0·03
July 2		0	J C	C	46·93	46·93	0·00
„ 16		5	C	J C	56·31	56·36	+ 0·05
August 5		0	J C	C	10·91	10·94	+ 0·03
„ 12		0	J C	C	23·37	23·42	+ 0·05
„ 20		2	J C	C	56·62	56·71	+ 0·09
October 9		2	J C	C	48·56	48·50	— 0·06
February 11	C and H C	2	H C	C	2·93	2·88	— 0·05
May 20		5	C	H C	17·14	16·98	— 0·16
June 15		0	H C	C	34·64	34·67	+ 0·03
December 30		0	H C	C	34·14	34·14	0·00
May 20	C and P	2	P	C	16·68	16·73	+ 0·05
August 16		0	P	C	33·94	34·13	+ 0·19
October 15		0	P	C	54·62	54·73	+ 0·11
December 12		0	P	C	50·09	50·21	+ 0·12
April 5	L and J C	0	J C	L	48·44	48·64	+ 0·20
„ 13		0	J C	L	38·93	39·26	+ 0·33
„ 20		2	L	J C	31·61	31·85	+ 0·24
May 24		3	L	J C	19·04	19·14	+ 0·10
June 1		0	L	J C	23·71	23·90	+ 0·19
„ 3		0	L	J C	23·94	24·14	+ 0·20

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OBSERVATIONS FOR PERSONAL EQUATIONS—continued.

Day, 1870.	Observers in order of Seniority.	Interval of nearest Stars.	Order of Observations.	Clock Slow at 0^h Sidereal by Senior Observer.	Clock Slow at 0^h Sidereal by Junior Observer.	Excess of Clock Slow by Junior Observer.
July 19	L and J C <i>cont.</i>	^h 3	J C L	59.55	59.83	+ 0.28
September 29		4	L J C	29.17	29.27	+ 0.10
October 1		0	J C L	32.69	33.02	+ 0.33
November 3		1	L J C	21.11	21.30	+ 0.19
„ 12		0	L J C	32.24	32.57	+ 0.33
„ 25		0	L J C	48.71	48.95	+ 0.24
March 22	L and H C	4	H C L	4.61	4.74	+ 0.13
July 1		2	L H C	46.13	46.32	+ 0.19
May 19	L and K	5	K L	15.82	16.02	+ 0.20
August 30		0	L K	27.08	27.32	+ 0.24
April 20	L and P	3	P L	31.61	31.86	+ 0.25
October 17		6	P L	57.64	57.97	+ 0.33
December 14		3	P L	46.49	46.85	+ 0.36
September 3	L and J	1	J L	36.55	36.97	+ 0.42
November 16		1	J L	37.93	38.15	+ 0.22
December 14		1	L J	46.49	46.73	+ 0.24
January 6	J C and H C	0	J C H C	36.46	36.41	— 0.05
„ 14		0	H C J C	43.40	43.31	— 0.09
February 4		0	H C J C	56.12	56.09	— 0.03
„ 24		4	H C J C	9.97	9.87	— 0.10
April 7		0	H C J C	46.37	46.32	— 0.05
„ 11		0	H C J C	41.29	41.39	+ 0.10
June 20		3	J C H C	38.63	38.56	— 0.07
August 9		2	J C H C	12.82	12.75	— 0.07
September 8		1	H C J C	48.22	48.16	— 0.06
„ 14		4	J C H C	60.05	60.03	— 0.02
April 9	J C and K	0	J C K	43.95	44.04	+ 0.09
May 18		1	J C K	15.23	15.41	+ 0.13
June 20	J C and P	4	P J C	38.65	38.75	+ 0.10
July 19		1	P J C	58.93	59.08	+ 0.15
November 14		0	P J C	36.72	36.81	+ 0.09
September 10	J C and J	0	J J C	51.83	51.85	+ 0.02
„ 14		0	J J C	60.05	60.13	+ 0.08
„ 16		0	J J C	4.07	4.15	+ 0.08
November 15		4	J C J	38.24	38.20	— 0.04

OBSERVATIONS FOR PERSONAL EQUATIONS—*continued.*

Day, 1870.	Observers in order of Seniority.	Interval of nearest Stars.	Order of Observations.	Clock Slow at 0 ^h Sidereal by Senior Observer.	Clock Slow at 0 ^h Sidereal by Junior Observer.	Excess of Clock Slow by Junior Observer.
February 25	H C and K	^h 4	K H C	10 ^s 27	10 ^s 45	+ 0 ^s 18
June 17	H C and P	1	P H C	36 47	36 68	+ 0 21
October 17		0	P H C	57 86	57 97	+ 0 11
November 11		1	H C P	32 50	32 67	+ 0 17
September 14	H C and J	3	J H C	60 03	60 13	+ 0 10
September 3	P and J	1	P J	36 83	36 97	+ 0 14

From these differences, if we form equations in which each observer's initial shall successively stand first, we obtain the following groups of equations:—

For S.

$$\begin{aligned} S - C &= + 0^s \cdot 24 \\ S - H C &= + 0^s \cdot 32 \end{aligned}$$

For W C.

$$\begin{aligned} 3 (W C - C) &= + 0^s \cdot 24 \\ 2 (W C - J C) &= + 0^s \cdot 24 \\ W C - H C &= + 0^s \cdot 11 \\ W C - J &= + 0^s \cdot 08 \end{aligned}$$

For D.

$$\begin{aligned} 2 (D - E) &= - 0^s \cdot 37 \\ 3 (D - C) &= + 0^s \cdot 20 \\ 3 (D - J C) &= + 0^s \cdot 33 \\ D - J &= + 0^s \cdot 07 \end{aligned}$$

For E.

$$\begin{aligned} 2 (E - D) &= + 0^s \cdot 37 \\ 16 (E - C) &= + 4^s \cdot 42 \\ 11 E - L &= + 5^s \cdot 00 \\ 20 (E - J C) &= + 4^s \cdot 41 \\ 11 (E - H C) &= + 2^s \cdot 58 \\ 6 (E - K) &= + 0^s \cdot 82 \\ 4 (E - P) &= + 0^s \cdot 50 \\ 3 (E - J) &= + 0^s \cdot 52 \end{aligned}$$

For C.

$$\begin{aligned} C - S &= - 0^s \cdot 24 \\ 3 (C - W C) &= - 0^s \cdot 24 \\ 3 (C - D) &= - 0^s \cdot 20 \\ 16 (C - E) &= - 4^s \cdot 42 \\ 16 (C - L) &= + 2^s \cdot 60 \\ 21 (C - J C) &= - 0^s \cdot 99 \\ 4 (C - H C) &= + 0^s \cdot 18 \\ 4 (C - P) &= - 0^s \cdot 47 \end{aligned}$$

For L.

$$\begin{aligned} 11 (L - E) &= - 5^s \cdot 00 \\ 16 (L - C) &= - 2^s \cdot 60 \\ 12 (L - J C) &= - 2^s \cdot 73 \\ 2 (L - H C) &= - 0^s \cdot 32 \\ 2 (L - K) &= - 0^s \cdot 44 \\ 3 (L - P) &= - 0^s \cdot 94 \\ 3 (L - J) &= - 0^s \cdot 88 \end{aligned}$$

For J C.

$$\begin{aligned} 2 (J C - W C) &= - 0^s \cdot 24 \\ 3 (J C - D) &= - 0^s \cdot 33 \\ 20 (J C - E) &= - 0^s \cdot 41 \\ 21 (J C - C) &= + 0^s \cdot 99 \\ 12 (J C - L) &= + 2^s \cdot 73 \\ 10 (J C - H C) &= + 0^s \cdot 44 \\ 2 (J C - K) &= - 0^s \cdot 22 \\ 3 (J C - P) &= - 0^s \cdot 34 \\ 4 (J C - J) &= - 0^s \cdot 14 \end{aligned}$$

PERSONAL EQUATIONS IN CHRONOGRAPHIC TRANSITS.

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For H C.		For P.	
H C - S	= - 0.32	4 (P - E)	= - 0.50
H C - W C	= - 0.11	4 (P - C)	= + 0.47
11 (H C - E)	= - 2.58	3 (P - L)	= + 0.94
4 (H C - C)	= - 0.18	3 (P - J C)	= + 0.34
2 (H C - L)	= + 0.32	3 (P - H C)	= + 0.49
10 (H C - J C)	= - 0.44	P - J	= - 0.14
H C - K	= - 0.18		
3 (H C - P)	= - 0.49		
H C - J	= - 0.10		

For K.		For J.	
6 (K - E)	= - 0.82	J - W C	= - 0.08
2 (K - L)	= + 0.44	J - D	= - 0.07
2 (K - J C)	= + 0.22	3 (J - E)	= - 0.52
K - H C	= + 0.18	3 (J - L)	= + 0.88
		4 (J - J C)	= + 0.14
		J - H C	= + 0.10
		J - P	= + 0.14

Now, since one of the quantities denoted by S, W C, D, E, &c. must evidently remain indeterminate, we will refer all the rest to C as a standard; and, putting $C = 0$, the initials S, W C, D, E, &c. will represent the values of "clock slow," which would be given by the observations of Mr. Stone, Mr. Christie, Mr. Dunkin, Mr. Ellis, &c., when that given by the observations of Mr. Criswick = 0.

Then, adding all the equations in each group, we get the following equations, in which each observer's personal equation is successively affected by a large co-efficient; the equation for C is omitted as being included in the others:—

2 S - H C	= + 0.56
7 W C - 2 J C - H C - J	= + 0.67
9 D - 2 E - 3 J C - J	= + 0.23
73 E - 2 D - 11 L - 20 J C - 11 H C - 6 K - 4 P - 3 J	= + 18.62
49 L - 11 E - 12 J C - 2 H C - 2 K - 3 P - 3 J	= - 12.91
77 J C - 2 W C - 3 D - 20 E - 12 L - 10 H C - 2 K - 3 P - 4 J	= - 1.52
34 H C - S - W C - 11 E - 2 L - 10 J C - K - 3 P - J	= - 4.08
11 K - 6 E - 2 L - 2 J C - H C	= + 0.02
18 P - 4 E - 3 L - 3 J C - 3 H C - J	= - 0.14
14 J - W C - D - 3 E - 3 L - 4 J C - H C - P	= + 0.59

Solving these equations by successive approximations, that is, by first substituting in each equation the approximately known values of all the personal equations, except that which has the largest co-efficient; thence deducing the value of that one personal equation; then using that deduced value for substitution in the other equations, and repeating the process, we get finally the following values:—

S = + 0.28	W C = + 0.13	D = + 0.11	E = + 0.27
L = - 0.17	J C = + 0.05	H C = 0.00	K = + 0.14
P = + 0.13	J = + 0.10		

or, restoring C:—

C - S = - 0.28	C - W C = - 0.13	C - D = - 0.11	C - E = - 0.27
C - L = + 0.17	C - J C = - 0.05	C - H C = 0.00	C - K = - 0.14
C - P = - 0.13	C - J = - 0.10		

The observations by eye and ear since 1859 are insufficient in number to give a trustworthy determination of the personal equations observed by that method. Those determined in 1858 and 1859 (Introduction to *Greenwich Observations*, 1858, page xl, and 1859, page xlii,) were the following:—

$$\begin{array}{rcl} D - E & = & + \overset{s}{0} \cdot 03 \\ D - C & = & + \overset{s}{0} \cdot 01 \end{array} \quad \left| \quad \begin{array}{rcl} D - L & = & + \overset{s}{0} \cdot 38 \\ D - J C & = & + \overset{s}{0} \cdot 14 \end{array}$$

None of these, however, have been applied in 1870.

The above personal equations, as applicable to the chronographic method of observing, deduced from the observations made in 1870 and referred to Mr. Criswick as Standard Observer, have been applied to the collected results of transits for the Sun, Moon, and Planets, whenever they were needed throughout the year 1870.

But those used in the adoption of clock-rate as explained above, page xl, and in the reduction of Altazimuth Observations, have been deduced from the observations in 1869, and are referred to Mr. Dunkin as Standard. The investigation of these is given in the *Introduction to the Greenwich Astronomical Observations*, 1869, page xlii.

In the standing foot-note on each page is given the duration of passage for the semidiameter of a planet when only one limb has been observed. It is found as follows:—

For the Sun, a correction of $- 0^s \cdot 04$, derived from the observations of several preceding years, is applied to the Nautical Almanac semidiameter.

For the Moon and Mercury, the duration is taken without alteration from the Nautical Almanac.

For Venus, a correction is applied to the Nautical-Almanac-semidiameter, determined from observations made with the Transit-Circle from 1851 to 1862. The investigation by Mr. Stone will be found in the *Monthly Notices of the Royal Astronomical Society*, Vol. XXV. No. 3. The correction which has been applied additively to the Nautical-Almanac-semidiameter during the year 1870, is

$$+ 0^s \cdot 026 + 0 \cdot 027 \times \text{tabular duration of passage of semidiameter.}$$

For Jupiter and Saturn, both limbs are always observed, if possible; but if, through accident or necessity, only one limb is observed, the duration of passage of the semidiameter is obtained by applying to the value given in the Nautical Almanac a correction derived from a few of the neighbouring observations. The elements of computation are given in the notes.

The *twentieth* column contains the right ascension of the center of the body observed: it is formed by adding the time from the sixteenth column, the clock-error at 0^h next preceding from the nineteenth column, the proportional part of the rate in the same column corresponding to the right ascension, and the duration of the passage of the semidiameter from the foot-notes. No result is set down for a clock-star, unless at least four clock-stars, distributed over several hours of right ascension, have been observed; no result is set down for Polaris, δ Ursæ Minoris,

Cephei 51, or λ Ursæ Minoris, unless Polaris, δ Ursæ Minoris, or Cephei 51, has been observed at opposite passages; and no result is set down for other close circumpolar stars, unless there has been a good determination of the azimuthal error on the day of observation.

The *twenty-first* column contains the correction with its proper sign, as it is to be applied for reducing the apparent right ascension of each star at the time of observation to the mean right ascension on the 1st of January, 1870. It is computed in the following manner.

For stars in the list of the Nautical Almanac, the mean R. A. of the Nautical Almanac is subtracted from the apparent R. A. of the Nautical Almanac (corrected, in the cases of Polaris, Cephei 51 (Hev.), δ Ursæ Minoris, and λ Ursæ Minoris, for the Moon's longitude): the sign of the quantity so found is changed.

For other stars, the corrections are computed by the formula

$$E e + F f + G g + H h + L + l - 300^s + \mu t;$$

(where μ is the annual proper motion in R.A. taken from Mr. Main's or Mr. Stone's papers in the *Memoirs of the Royal Astronomical Society*, or from the *British Association Catalogue*, and t is the fraction of a year corresponding to the day of observation) which is derived from the well-known formula,

$$A a + B b + C c + D d + \mu t,$$

or its equivalent,

$$\frac{A}{15} \cos R.A. \operatorname{cosec} N.P.D. + \frac{B}{15} \sin R.A. \operatorname{cosec} N.P.D. + C \sin R.A. \cotan N.P.D. \times \text{numb. log. } 0.1259 + \frac{D}{15} \cos R.A. \cot N.P.D. + C \times \text{numb. log. } 0.4869 + \mu t,$$

by a process which is explained with sufficient detail in the Introduction to the Twelve-Year-Catalogue appended to the volume for 1847, in the Introduction to the Six-Year Catalogue of 1576 Stars for 1850, appended to the volume for 1854, in the Introduction to the Seven-Year Catalogue of 2022 Stars for 1860, appended to the volume for 1862; and in that of the New Seven-Year Catalogue for 1864, attached to the volume for 1868. It will be sufficient here to state that $E = A + 25$, $F = B + 25$, $G = C + 1.2$, $H = D + 25$, $e = a + 1.2$, $f = b + 1.2$, $g = c + 25$, $h = d + 1.2$, $L = 210 - 1.2 \times E - 1.2 \times F - 25 \times G - 1.2 \times H$, $l = 210 - 25 \times e - 25 \times f - 1.2 \times g - 25 \times h$. The values of the day-constants $\log. E$, $\log. F$, $\log. G$, $\log. H$, and L , are given in the Nautical Almanac. The values of the star-constants, $\log. e$, $\log. f$, $\log. g$, $\log. h$, and l , for stars contained in the Seven-Year Catalogue for 1860, and in the New Seven-Year Catalogue for 1864, are printed in those Catalogues. For other stars, the star-constants will be found in the annual Catalogues for the years 1868 and 1869, or in that included in the present volume.

The sign of the computed quantity is changed before application.

§ 2. *Observations of the Collimators, and of the Reflected Image of the Central Vertical Wire of the Transit-Circle, for the Determination of the Errors of Collimation, and Level, page [86] to [96].*

With regard to these tables, the following remarks, in addition to the explanation which has been given, in the description of the instrument, and in the account of the methods of determining the errors of collimation and level, will be sufficient.

OBSERVATIONS FOR COINCIDENCE OF COLLIMATORS.

These observations are made on every week day. For those made on Monday, the Transit-Circle is raised to admit an uninterrupted view of the South Collimator or Reversed Telescope by the North Collimator. On other days, the view is taken through the pierced cube of the Transit-Circle Telescope.

By means of the micrometer of the North Collimator, the nearly vertical sides of the squares formed by the intersecting wires are made to cross at their middle points, and the readings of the micrometer-head of the North Collimator are taken six times. The wire is then left at a reading corresponding to the mean of the six. These means are printed in the table, and will give a satisfactory idea of the firmness of the collimators.

OBSERVATIONS OF THE COLLIMATORS FOR DETERMINATION OF THE ERROR OF COLLIMATION.

The way in which these observations are made has been fully explained (pages v and xxxii). The mean of the readings for the separate collimators, and the resulting reading for the line of collimation, are set down in consecutive columns, and the last column gives the reading which has been adopted for the period of time limited by the bars above and below. By comparing the numbers in this column with the *Readings of Transit-Micrometer* given in the foot-notes of the section *Transits observed, &c.*, and applying $-0''.19$ for diurnal aberration, the errors of collimation actually used will be deduced. For determination of the sign of the error, it must be observed that the micrometer-head is East, and that the readings of the micrometer increase as the wire moves towards the head.

DETERMINATION OF THE LEVEL ERROR.

The method of making these observations has been described (pages vii and xxxiii). A comparison of the transit-micrometer-reading for coincidence of the direct and reflected images of the central wire, with the adopted reading for the line of collimation set down in the contiguous column, gives the error of level in terms of revolutions of the micrometer; and the numbers in the next column exhibit the errors of level in arc. The last column gives the adopted values of the error, and the limits of time during which they have been used. The determination of the sign of the errors has been previously explained.

DETERMINATION OF ERRORS OF COLLIMATION AND LEVEL;
ZENITH DISTANCE OBSERVATIONS.

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§ 3. *Observations of Zenith Distance with the Transit-Circle*, page (1) to (106).

In order to include the whole of the reductions belonging to a single observation on one page, the elements for those reductions which are not frequently changed, and which do not require tabular arrangement, are given in the foot-notes: these are;— correction for runs; formulæ used in computing micrometer-corrections, corrections for curvature of path, and inclination of wire; and Zenith-Point-corrections.

The corrections for planets, including change of N. P. D. for reduction to the meridian, parallax, and semidiameter, and also the corrections for reducing the apparent places of stars to mean places, are exhibited in tabular arrangement at the lower part of each page, opposite to the reference-numbers which correspond to the observations in the upper part of the page.

DAY.—The day of observation always begins with the Sun's transit.

NO. FOR REFERENCE.—This column requires no explanation.

NAME OF OBJECT.—The nomenclature of stars follows the same general rule as in the section of *Transits observed*, &c., except that, as a last resource, the place of the star is defined by its right ascension, which is generally accurate to 1^s. The letters N.L. and S.L. denote north and south limbs of planets, and N.C. and S.C. the north and south cusps of Mercury or Venus. The words *Nadir Observation* indicate an observation of the image of the horizontal or zenith-distance wire as seen by reflexion in a trough of mercury, as is described in page viii. For other objects, the letter R. denotes that the object is observed by reflexion in the trough of mercury.

READINGS OF THE SIX MICROSCOPE-MICROMETERS.—The application of the letters is the same as in the Observations of preceding years from 1836: the observer, beginning with the northern horizontal microscope, and passing the upper microscopes, the southern horizontal, and the lower ones, in the direction of the circle's circumference, reads them in the order A, C, E, B, D, F. These readings in the observing books are placed in the order $\begin{smallmatrix} A, C, E \\ B, D, F \end{smallmatrix}$; from which form they are easily changed into the order of printing. Each pair of adjacent readings, therefore, is the pair of readings at the opposite ends of a diameter. The number of integral revolutions is given in the fifth column only. Occasionally the number of revolutions expressed in this column does not apply unchanged to all the microscopes, on account of the difference of their readings; but since the readings never differ by more than four or five tenths of a revolution, and the order of the more conspicuous differences is noted at the bottom of the page, this will occasion no ambiguity. The reading of the pointer-microscope is omitted for the sake of economy of space, but it may be inferred from the Zenith-Point given in full at the bottom of each page, and from the deduced Zenith-Distance.

It is proper now to explain how the revolutions and parts of revolutions of the microscope-micrometers are converted into arc.

First, it may be premised that, as one revolution of each microscope-micrometer

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does not differ extravagantly from 1' on the limb of the circle, we may consider each revolution as a nominal minute. Next, supposing the number of integral revolutions, as shown by each microscope, to be the same for all, we ought, in order to obtain the mean of the fractions of a revolution, to add together the subdivisions as shown by the different micrometer-heads, and divide the sum by 6. Thirdly, as the subdivisions are in the decimal scale, we should then multiply this mean by 60, to reduce it to sexagesimal seconds. It is evident thus that the number of nominal seconds to be attached to the nominal minute will be found by simply adding together the subdivisions on the micrometer-heads, and shifting the decimal point.

From the ordinary observations of runs (those for the year 1870 being given at page (108) &c. of the present volume), it is known that the screws of the micrometers are so sensibly equal that, in the reduction of the observations, it is sufficient to take the mean of the six readings, and to apply to it the mean correction for runs. To do this, the following process is employed. The sum of the runs for the six microscopes never differs materially from 29·3. Now, if the correction, by which each revolution of a micrometer may be converted into a minute of arc, were exactly $\frac{1}{50}$ part of the reading, then the sum of the runs would be $\frac{50}{51} \times 30\cdot000$, or 29·4118. It is not likely that the sum of the runs will ever amount to this quantity; and the variable correction, after adding $\frac{1}{50}$ part to the mean of the readings of the microscopes, will therefore always be additive. To determine this quantity, let the sum of the runs be $29\cdot412 - x$. Then the true reading in seconds of space, corresponding to a nominal reading of r'' (including the value both of the nominal minutes and of the subdivisions of the nominal minute) will be

$$r'' \times \frac{30\cdot000}{29\cdot412 - x}$$

or
$$r'' \left\{ 1 + \frac{1}{50} + 0\cdot03468 \times x \right\}$$

Hence the correction, after adding $\frac{1}{50}$ part of the mean of readings, will be $+ r x \times 0\cdot03468$. For the purpose of calculating this quantity easily by the ordinary proportional scale, it is convenient, in the first place, to compute its value when $r = 100''$. This value, which is evidently $+ 3\cdot468 \times x$, is tabulated for different values of x . Let X be the number taken from this table; then, for any actual reading r , the correction will be $\frac{rX}{100}$: a quantity which can easily be taken from the ordinary sliding-rule.

On a few occasions the cross-wires of one or more of the microscopes have fallen on the negative side of the micrometer zero: these cases are always mentioned in the notes.

READING OF TELESCOPE-MICROMETER.—This column contains the reading of the micrometer in the eyepiece of the telescope. The instrument is furnished with two clamps, one north and the other south, for fixing the instrument, but with no slow-motion screw; the object must therefore be bisected by means of the micrometer-screw,

CORRECTION FOR RUNS;
EXAMINATION OF TELESCOPE-MICROMETER.

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and the micrometer must be read, for every observation. The reading of 20^r corresponds pretty nearly to the middle of the range of the screw, and the wire is then tolerably near the center of the field of view; observations are, therefore, generally made with a position of the wire not greatly different from this.

A new telescope-micrometer, prepared by Mr. Simms, has been in use since 1867, July 10.

To determine the value of the micrometer-revolution; on 1867, July 12, the telescope was directed to the nearly horizontal wire of the southern Reversed Telescope, and was placed so as to give Circle Readings (approximately) alternately of $89^\circ.29'$ and $89^\circ.34'$; the microscope-micrometers were read and corrected as usual; and the reading of the telescope-micrometer was taken, which was required to produce coincidence of its wire with the image of the wire of the Reversed Telescope. The observations were made under the direction of Mr. Dunkin. The mean of 42 intervals thus measured gave one revolution of telescope-micrometer = $34''.526$.

On 1867, July 31, after relieving the micrometer from a very slight constraint, observations were made by Mr. Stone for ascertaining the validity of this revolution-value through several revolutions. It appeared that, with different indexes of micrometer-revolutions, the following corrections were necessary, to refer the complete results (in the form of Results of Zenith Distance Observations) to the same mean:—

	r		''	
Micrometer-reading	14,	correction required appeared to be	— 0.19	
"	"	19,	"	0.00
"	"	22,	"	— 0.16
"	"	27,	"	+ 0.35

The corrections apparently required are too small to be adopted for use.

On 1868, March 11, observations were made by Mr. Dunkin to determine whether there is any appreciable difference of results, according as the screw is turned to increase readings or to diminish readings. The following are the results:—

Micrometer-head turned so that readings increase.		Micrometer-head turned so that readings diminish.	
r		r	
Separate readings	$20^r.423$		$20^r.421$
	$.420$		$.420$
	$.420$		$.415$
	$.417$		$.418$
	$.419$		$.417$
	$.414$		$.413$
	$.411$		$.412$
	$.409$		$.412$
	$.409$		$.410$
	$.410$		$.412$
Means..	$20^r.415$		$20^r.415$

Observations were also made by Mr. Dunkin to determine whether the separate portions of the screw's revolution are sensibly different. The means of the readings are as follows :—

Readings of Collimator- micrometer.	Readings of Telescope- micrometer.	Intervals.	Readings of Collimator- micrometer.	Readings of Telescope- micrometer.	Intervals.
	r	r		r	r
{ '000	17'998 }	0'501	{ '000	18'295 }	0'501
{ '720	18'499 }		{ '720	18'796 }	
{ '000	18'505 }	0'504	{ '000	18'781 }	0'501
{ '720	19'009 }		{ '720	19'282 }	
{ '000	19'028 }	0'504	{ '000	19'289 }	0'501
{ '720	19'532 }		{ '720	19'790 }	
{ '000	19'548 }	0'502	{ '000	19'791 }	0'504
{ '720	20'050 }		{ '720	20'295 }	
{ '000	20'036 }	0'502	{ '000	20'297 }	0'501
{ '720	20'538 }		{ '720	20'798 }	
{ '000	20'563 }	0'501	{ '000	20'802 }	0'505
{ '720	21'064 }		{ '720	21'307 }	
{ '000	21'046 }	0'500	{ '000	21'277 }	0'502
{ '720	21'546 }		{ '720	21'779 }	
{ '000	21'560 }	0'503	{ '000	21'799 }	0'500
{ '720	22'063 }		{ '720	22'299 }	
{ '000	21'998 }	0'502	{ '000	22'303 }	0'504
{ '720	22'500 }		{ '720	22'807 }	
{ '000	22'555 }	0'506	{ '000	22'791 }	0'503
{ '720	23'061 }		{ '720	23'294 }	
{ '000	23'061 }	0'505	{ '000	23'307 }	0'504
{ '720	23'566 }		{ '720	23'811 }	

The evidence against any appreciable drunkenness of screw is very strong.

VERTICAL WIRE AT WHICH OBSERVATION IS MADE.—Omitting, in this Section, all reference to the wires Q, R, S, U, V, W, (page xxvii) adapted to galvanic observation of transits, the telescope contains seven vertical or transit wires N, O, P, T, X, Y, Z, here called 1, 2, 3, 4, 5, 6, 7, placed at sensibly equal intervals of about 14° for transit of an equatoreal star; and the central or 4th wire is so nearly in the meridian as to prevent the necessity of any correction to the observed circle-reading when the body is observed at the passage over that wire. In that case, the only corrections which are required to the mean of the microscope-micrometer-readings (when converted into arc and combined with the equivalent for the telescope-micrometer-reading) are those arising from errors of division of the graduated circle, and from astronomical flexure of the telescope. When the body is not observed at the central wire, additional corrections are required, to be mentioned on page lix.

CORRECTIONS FOR ERROR OF DIVISION AND FOR FLEXURE OF TELESCOPE.—The errors due to these causes were elaborately investigated in 1851 and 1852, and a full account

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On 1867, April 25 and May 13, the following Observations were made for the determination of the Horizontal Astronomical Flexure of the Telescope of the Transit-Circle.

The nearly horizontal wire of the South Collimator, used in these observations, was brought upon the image of the corresponding wire of the North Collimator, by looking through the cube of the Transit-Circle; and the micrometer-head was set at the mean of 20 successive readings. After each complete set of 10 observations of the collimating wires the coincidence of these wires was again tested.

OBSERVATIONS FOR THE DETERMINATION OF THE ASTRONOMICAL FLEXURE OF THE TELESCOPE OF THE TRANSIT-CIRCLE.

Month and Day, 1867.	Order of Observa- tion.	Concluded Circle Reading at bisection of Wire of North Collimator.	Mean Concluded Circle Reading, North Collimator.	Order of Observa- tion.	Concluded Circle Reading at bisection of Wire of South Collimator.	Mean Concluded Circle Reading, South Collimator.
April 25		° ' "	° ' "		° ' "	° ' "
	1	269. 34. 52.68		2	89. 34. 53.45	
	3	53.37		4	53.52	
	5	52.67		6	53.53	
	7	52.75		8	53.45	
	9	52.77	269. 34. 52.71	10	53.71	89. 34. 53.49
	11	52.45		12	53.07	
	13	52.72		14	53.58	
	15	52.56		16	53.50	
	17	52.59		18	53.41	
	19	52.51		20	53.70	
	22	269. 34. 52.87		21	89. 34. 53.38	
	24	52.75		23	53.10	
	26	52.44		25	52.83	
	28	52.10		27	53.18	
	30	52.39	269. 34. 52.50	29	53.34	89. 34. 53.23
	32	52.54		31	53.42	
	34	52.44		33	53.18	
	36	52.18		35	53.46	
	38	52.52		37	53.10	
	40	52.75		39	53.30	
	41	269. 34. 52.77		42	89. 34. 52.70	
	43	52.81		44	52.89	
	45	52.27		46	52.90	
	47	52.55		48	53.09	
	49	52.53	269. 43. 52.40	50	52.93	89. 34. 52.94
	51	52.27		52	52.96	
	53	52.37		54	52.99	
	55	52.12		56	52.74	
	57	52.36		58	53.07	
	59	51.95		60	53.20	

CORRECTIONS FOR ERRORS OF DIVISION AND FLEXURE OF TELESCOPE. lvii

OBSERVATIONS FOR THE DETERMINATION OF THE ASTRONOMICAL FLEXURE OF THE TELESCOPE OF THE TRANSIT-CIRCLE—*continued.*

Month and Day, 1867.	Order of Observa- tion.	Concluded Circle Reading at bisection of Wire of North Collimator.	Mean Concluded Circle Reading, North Collimator.	Order of Observa- tion.	Concluded Circle Reading at bisection of Wire of South Collimator.	Mean Concluded Circle Reading, South Collimator.
May 13		° ' "	° ' "		° ' "	° ' "
	1	269. 34. 49'86		2	89. 34. 50'47	
	3	49'78		4	50'66	
	5	49'83		6	50'27	
	7	49'60		8	50'37	
	9	49'41	269. 34. 49'59	10	50'34	89. 34. 50'30
	11	49'41		12	50'28	
	13	49'53		14	50'47	
	15	49'40		16	50'42	
	17	49'63		18	50'31	
	19	49'45		20	50'73	
	21	269. 34. 49'41		22	89. 34. 50'06	
	23	49'50		24	50'24	
	25	49'04		26	50'57	
	27	48'76		28	49'93	
	29	49'29	269. 34. 49'09	30	50'51	89. 34. 50'09
	31	48'88		32	50'23	
	33	48'90		34	50'46	
	35	49'25		36	50'68	
	37	48'88		38	50'35	
	39	48'95		40	60'34	
	41	269. 34. 48'89		42	89. 34. 49'81	
	43	48'91		44	50'04	
	45	49'36		46	50'19	
	47	49'39		48	49'76	
	49	48'82	269. 34. 49'06	50	49'97	89. 34. 49'82
	51	48'88		52	50'23	
	53	48'93		54	50'08	
	55	49'20		56	49'89	
	57	48'98		58	49'99	
	59	49'26		60	50'10	

The Observations of April 25 give for the bisection of the wire of—

North Collimator . . 269°. 34'. 52''·54.

South Collimator . . 89°. 34'. 53''·22.

And the correction for Astronomical Horizontal Flexure = $-0''\cdot34$.

The Observations of May 13 give for the bisection of the wire of—

North Collimator . . 269°. 34'. 49''·25.

South Collimator . . 89°. 34'. 50''·07.

And the correction for Astronomical Horizontal Flexure = $-0''\cdot41$.

The mean of these results, $-0''\cdot37$, has been adopted for use during the year 1870.

GREENWICH OBSERVATIONS, 1870.

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The product of this quantity by the sine of the zenith-distance south has been incorporated with the mean of those numbers in the preceding table which apply to the six divisions that are viewed simultaneously under the six microscopes. The resulting corrections, which are contained in the following table, have been applied additively to all circle-readings throughout the year 1870. The argument in this table is the Zenith Distance South.

DIVISION CORRECTION + FLEXURE CORRECTION.

(Always Additive.)

Pointer Reading.	Corr.	Pointer Reading.	Corr.	Pointer Reading.	Corr.	Pointer Reading.	Corr.	Pointer Reading.	Corr.	Pointer Reading.	Corr.	Pointer Reading.	Corr.	Pointer Reading.	Corr.	Pointer Reading.	Corr.
0	0.51	36	0.45	72	0.39	108	0.46	144	0.72	180	0.51	216	0.89	252	1.09	288	1.16
1	0.53	37	0.54	73	0.43	109	0.44	145	0.73	181	0.55	217	0.98	253	1.13	289	1.15
2	0.56	38	0.62	74	0.54	110	0.37	146	0.69	182	0.58	218	1.08	254	1.26	290	1.11
3	0.53	39	0.70	75	0.60	111	0.29	147	0.61	183	0.57	219	1.16	255	1.32	291	1.01
4	0.51	40	0.72	76	0.62	112	0.16	148	0.53	184	0.57	220	1.20	256	1.34	292	0.93
5	0.55	41	0.73	77	0.65	113	0.00	149	0.45	185	0.61	221	1.21	257	1.37	293	0.83
6	0.62	42	0.78	78	0.62	114	0.03	150	0.33	186	0.70	222	1.28	258	1.34	294	0.71
7	0.71	43	0.78	79	0.65	115	0.13	151	0.30	187	0.79	223	1.28	259	1.37	295	0.66
8	0.71	44	0.70	80	0.81	116	0.16	152	0.32	188	0.81	224	1.22	260	1.53	296	0.82
9	0.66	45	0.62	81	0.86	117	0.14	153	0.24	189	0.78	225	1.14	261	1.58	297	0.80
10	0.67	46	0.54	82	0.71	118	0.15	154	0.21	190	0.79	226	1.08	262	1.45	298	0.81
11	0.69	47	0.51	83	0.59	119	0.18	155	0.36	191	0.83	227	1.05	263	1.33	299	0.82
12	0.66	48	0.54	84	0.57	120	0.19	156	0.52	192	0.82	228	1.08	264	1.31	300	0.83
13	0.70	49	0.51	85	0.57	121	0.22	157	0.62	193	0.86	229	1.07	265	1.31	301	0.86
14	0.81	50	0.44	86	0.53	122	0.26	158	0.71	194	0.99	230	1.00	266	1.27	302	0.88
15	0.86	51	0.35	87	0.44	123	0.24	159	0.80	195	1.06	231	0.93	267	1.18	303	0.86
16	0.88	52	0.21	88	0.36	124	0.23	160	0.86	196	1.08	232	0.79	268	1.10	304	0.85
17	0.90	53	0.04	89	0.27	125	0.28	161	0.85	197	1.12	233	0.64	269	1.01	305	0.88
18	0.87	54	0.07	90	0.15	126	0.36	162	0.92	198	1.09	234	0.67	270	0.89	306	0.96
19	0.89	55	0.17	91	0.11	127	0.45	163	0.92	199	1.13	235	0.77	271	0.85	307	1.05
20	1.04	56	0.18	92	0.12	128	0.47	164	0.86	200	1.30	236	0.80	272	0.86	308	1.05
21	1.09	57	0.16	93	0.04	129	0.43	165	0.78	201	1.35	237	0.78	273	0.78	309	1.01
22	0.94	58	0.17	94	0.00	130	0.45	166	0.72	202	1.22	238	0.79	274	0.74	310	1.01
23	0.82	59	0.18	95	0.15	131	0.48	167	0.70	203	1.10	239	0.82	275	0.89	311	1.04
24	0.79	60	0.19	96	0.30	132	0.47	168	0.73	204	1.09	240	0.83	276	1.04	312	1.01
25	0.78	61	0.22	97	0.39	133	0.51	169	0.72	205	1.10	241	0.86	277	1.13	313	1.05
26	0.74	62	0.24	98	0.48	134	0.63	170	0.66	206	1.06	242	0.90	278	1.22	314	1.17
27	0.64	63	0.22	99	0.57	135	0.70	171	0.58	207	0.98	243	0.88	279	1.29	315	1.22
28	0.56	64	0.21	100	0.60	136	0.72	172	0.45	208	0.90	244	0.87	280	1.32	316	1.24
29	0.46	65	0.24	101	0.61	137	0.76	173	0.30	209	0.82	245	0.92	281	1.33	317	1.26
30	0.33	66	0.32	102	0.67	138	0.73	174	0.33	210	0.61	246	1.00	282	1.39	318	1.23
31	0.29	67	0.41	103	0.67	139	0.77	175	0.44	211	0.67	247	1.09	283	1.39	319	1.25
32	0.29	68	0.42	104	0.60	140	0.93	176	0.46	212	0.69	248	1.10	284	1.32	320	1.41
33	0.21	69	0.37	105	0.52	141	0.99	177	0.45	213	0.61	249	1.07	285	1.24	321	1.45
34	0.16	70	0.38	106	0.45	142	0.85	178	0.47	214	0.58	250	1.08	286	1.17	322	1.31
35	0.31	71	0.41	107	1.43	143	0.74	179	0.49	215	0.73	251	1.11	287	1.13	323	1.18

In pages {22} and {25} of the detailed accounts of the Transit-Circle before cited mention is made of an apparatus for the investigation of the errors of every 5' of each degree of the circle. The apparatus itself consists simply of the insertion, in the micrometer with which the spaces of 1° were compared, of two wire-crosses at an interval corresponding nearly to 5' on the graduated circle. By a small motion

SPECIAL CORRECTIONS FOR ERRORS OF DIVISION AND FLEXURE OF TELESCOPE; lix
REDUCTION TO MERIDIAN.

of the micrometer, these crosses can be used conveniently for the measure of every space of 5', and after every twelve measures the divisions of the series of 1° (whose errors are known from the preceding operations) will be brought under the microscope, and the errors of the intermediate divisions can be ascertained. This investigation was in preceding years esteemed unnecessary; but on repeating the general investigation of the errors of divisions of single degrees of the circle at the end of the year 1856, it was thought prudent to examine the 5' divisions of those degrees of the circle which are under the microscopes in the observations of the Nadir Point, Polaris, and Polaris S.P. This examination was made between 1857, June 30 and July 3; and, for the method employed, the formulæ of reduction, and the details of the results, reference may be made to the volume for 1857.

In this place it is sufficient to state that the corrections to circle-readings for the Nadir Point, for Polaris, and for Polaris S.P., are as follows:—

For Nadir Point, the division under Microscope A being	$\begin{cases} 90^{\circ}. 5, \\ 90. 10, \end{cases}$	the correction is	$\begin{cases} +0''.60 \\ +0''.75 \end{cases}$
For Polaris,	,, , 233. 5,	,,	+1''.21
For Polaris S.P.	,, , 230. 10,	,,	+1''.58

In 1865, July, an examination was made of the 5' divisions employed in the observations of δ Ursæ Minoris and Cephei 51 above and below the pole. The following are the resulting corrections:—

For Cephei 51, the division under Microscope A being	234. 20,	the correction is	+1''.29
For Cephei 51 S.P.	,, , 228. 50,	,,	+1''.08
For δ Ursæ Minoris	,, , 235. 0,	,,	+1''.18
For δ Ursæ Minoris S.P.	,, , 228. 15,	,,	+1''.16

These corrections have been applied additively to the circle-readings whenever they were needed throughout the year 1870.

The differences between these numbers and those adopted before 1868 arise partly from the use of a different constant of flexure, and partly from the circumstance that in former years the adopted errors of division for each degree were those given by the examination of 1856 only, whereas from 1868 the mean of the errors for each degree found in 1851–1852 and in 1856 is adopted.

When the object has not been observed at the central wire, corrections are required for reduction to the meridian. These consist of three, viz.:—First, for want of horizontality of the micrometer-wire; secondly, for curvature of path of the object, or for difference between the small circle described by the body and the great circle of which the horizontal wire forms a part; and thirdly, in the case of the Sun, Moon, and Planets, for the change of N.P.D. in the interval between the time of observation and the meridian passage.

The correction due to inclination of wire was found by bisections of stars (by the telescope-declination-micrometer) at the first and seventh vertical wires. Its numerical value, additive before transit and subtractive after transit, for stars above the pole, is given in the foot-notes.

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The general formula for the correction for curvature is given also in the foot-notes ; its value is easily interpolated from a table constructed for convenient intervals of N.P.D. In the case of stars very near the Pole, when the place of observation does not coincide with a vertical wire, the correction for curvature is computed from the formula, "correction for curvature = number ($\log = 6.43569$) $\times \sin 2$ N. P. D. $\times t^2$," t being the interval between the time of meridian passage and the time of transit expressed in seconds of time.

The formulæ for correction for motion are the following. In the case of the Moon, the correction for the change of N.P.D. in passing from one wire to the next is computed from the formula, "Change of declination for one hour of terrestrial longitude (from the section of Moon-culminating stars in the Nautical Almanac) $\times$ sec. declination $\times \frac{\sin. \text{Geoc. Z.D.}}{\sin. \text{App. Z.D.}} \times \frac{14}{3600}$ (the logarithm of the last factor being 7.58983)"; this formula supposes the equatoreal interval of the wires to be $14''$. In the case of the other planets, the correction for motion is deduced immediately from the hourly motion in declination given in the Nautical Almanac ; or, in the case of newly discovered planets, from their peculiar Ephemerides.

SECONDS OF CONCLUDED MERIDIONAL CIRCLE-READING.—The numbers in this column are found by adding together the mean of the microscope-readings corrected for runs, the equivalent for telescope-micrometer-reading, and the corrections above mentioned. The degrees and minutes may be ascertained, when required, by subtracting the "Correction for Zenith Point" given in the notes, from the Apparent Zenith Distance.

ZENITH-POINT-CORRECTION.—The observations for this purpose are those of the reflected image of the horizontal wire, and those of the direct and reflected images of stars made at the same transit (see page viii). The zenith-points deduced from the reflected image of the wire are combined with those deduced from observations of stars, in the following manner:—It has been the practice to observe when possible two stars to the north and two to the south of the zenith on every evening, and, in combining them for zenith-point, to allow to each star-observation twice the weight of a nadir-point observation, lest too great weight should be given to the readings of those divisions of the circle which correspond to the nadir-point observations.

If D denote the circle-reading for a direct observation of a star, and R that for a reflexion observation, then the reading of the circle corresponding to the zenith, or the zenith-point, will be $\frac{R + D}{2} + 90^\circ$.

The details of the computation of zenith-point are given in a subsequent table, page (117) to (125). The adopted correction for zenith-point is given in the foot notes to this Section.

APPARENT ZENITH-DISTANCE.—The numbers in this column are found by adding the Zenith-Point-Correction to the Concluded Meridional Circle-Reading ; when the sum

CONCLUDED MERIDIONAL CIRCLE-READING : ZENITH-POINT CORRECTION ; lxi
CORRECTION FOR DEFECTIVE ILLUMINATION.

exceeds 270° (denoting that the object is between the zenith and the north horizon), the complement to 360° is taken, and the negative sign is attached to it; for stars observed by reflexion, the sum is subtracted from 180° , and the remainder, with its algebraical sign, is the apparent zenith-distance. When the object has been observed at several wires, the mean of all the concluded circle-readings is used to form the Zenith-Distance.

When both limbs of the Moon are observed, it usually happens that one of them is slightly defective from the failure of illumination by the Sun. The necessary correction (which is not applied in this column, but which must be applied with others in order to form the numbers in the column of *Geocentric N. P. D. of Center*) is ascertained by computation in the following manner:—When the Moon is horned, let θ be the angle which the circle joining the cusps makes with the meridian; δ_s the Sun's declination, and δ_m the Moon's declination as seen at Greenwich: P the Sun's hour angle at the Moon's Transit: then

$$\tan \theta = \operatorname{Cosec} P \cdot \cos \delta_m \cdot \tan \delta_s - \cot P \cdot \sin \delta_m ;$$

and the correction required will be

$$\text{Moon's semidiameter} \times \operatorname{versin} \theta.$$

For Mercury and Venus, when horned, the investigation of the correction for defective illumination assumes the same form as for the Moon.

If the Moon be gibbous, as is the case in the greater number of instances, draw a great circle through the center of the Moon, at right angles to the meridian passing through the Moon, and let it meet the meridian passing through the Sun; then the intersection of this circle with the Sun's meridian will determine the place of a fictitious Sun, which would equally illuminate both limbs of the Moon when on the meridian; and the elevation or depression of the true Sun above or below the great circle joining the Moon and fictitious Sun, measured in a plane at right angles to that circle, will represent the angle by which the lowest or highest part of the illuminated hemisphere is distant from the limb, and therefore the angle whose versed sine multiplied into the Moon's semidiameter is the correction required.

Let then P be the North Pole of the heavens, M the Moon on the meridian of Greenwich, and S and S_1 the true and fictitious Suns, and imagine the triangles formed by great circles joining these. Let also δ_1 be the declination of the fictitious Sun, θ_1 the arc joining the true and fictitious Suns, and θ the perpendicular arc before mentioned.

Then $\tan \delta_1 = \tan \delta_m \cdot \cos MP S_1 .$

And $\theta_1 = \delta_s - \delta_1 .$

Also $\sin \theta = \sin \theta_1 \cdot \sin MS_1 P$

$$= \sin \theta_1 \frac{\sin MP}{\sin S_1 P}$$

$$= \sin \theta_1 \frac{\cos \delta_m}{\cos \delta} .$$

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Whence θ is found ; and the correction required is

$$\text{Moon's semidiameter} \times \text{versin } \theta.$$

In either case the North limb is fully illuminated if θ is positive, and the South limb if θ is negative.

In the cases of Mercury and Venus when gibbous, or of Mars and other planets sensibly gibbous, the investigation takes the following form. The angle θ being found as above, the length of the straight line drawn from the Sun perpendicular to the plane represented by the great circle above mentioned, is equal to Distance of Earth from Sun $\times \sin \theta$; and therefore if ϕ be the apparent angular distance of the Sun from that plane as seen from the planet, the value of ϕ is determined by the equation

$$\sin \phi = \frac{\text{Length of perpendicular line}}{\text{Dist. of Planet from Sun}} = \frac{\text{Dist. of Earth from Sun}}{\text{Dist. of Planet from Sun}} \times \sin \theta.$$

The angle ϕ represents in this case the angle by which the lowest or highest point of the illuminated hemisphere is distant from the limb as viewed by an observer anywhere in the plane of this great circle, and the correction therefore will be

$$\text{Planet's semidiameter} \times \text{versin } \phi.$$

BAROMETER.—The barometer is by Newman. Its scale is divided by vernier to 0·002 inch ; but it is not usually necessary to read it to a smaller quantity than 0·01 inch for the computation of refraction. The movement of the vernier displaces a plunger which enters into the cistern of mercury, and thus maintains it constantly at the same level. This construction is not well adapted to a merely meteorological instrument, which constantly requires a visible reference to the lower surface of the mercury, but it is exceedingly convenient for the barometer as an astronomical auxiliary, and entirely avoids the risk of error from inadvertent omission of the lower verification, or from friction of a floating index ; and is, on the whole, the best that can be employed. From careful comparisons made between 1863, February 6 and 11, the reading of this barometer appears to be greater than that of the Standard Barometer by 0·02 inch. The readings of the barometer have been corrected by this quantity throughout the year.

EXTERIOR THERMOMETER.—This thermometer is by Troughton and Simms. It is mounted on the north front of the Observatory, where it is carried by an arm projecting from the wall to a distance of 4½ feet, at a height of nearly seven feet from the ground.

The following are the results of comparisons with the Standard Thermometer, made on 1861, January 31 :—

Temperatures.	Excess of Reading of Circle Thermometer.
—	—
32·0	0·0
34·0	0·0
36·3	0·0
40·0	0·0

Temperatures.	Excess of Reading of Circle Thermometer.
42°1	—0°1
45°1	—0°1
48°4	0°0
53°5	0°0
57°0	0°0
60°0	0°0
63°1	—0°1
67°7	+0°1
72°0	0°0
76°6	0°0
83°6	0°0
88°6	0°0
94°7	0°0

INTERIOR THERMOMETER.—On 1868, July 14, the small interior thermometer which had been in use for many years was replaced by a thermometer, No. 12,264, by Negretti and Zambra. The readings of this thermometer are now regularly taken for comparison with those of the exterior thermometer.

REFRACTION.—The refraction is computed as in former years fundamentally from Bessel's Tables in the *Tabulæ Regiomontanæ*. These Tables, altered in form (but so as to give in all cases the same result) and expanded, are given in the Appendix to the volume for 1836, and they are also given in a still more expanded form, including the Supplementary Table for Zenith Distances greater than 85°, in an Appendix to the volume for 1853. The exterior thermometer only is used in the computation, excepting in cases when the Zenith Distance exceeds 85°.

The mean refractions used are the mean refractions of Bessel's Fundamenta, diminished in the proportion of—

$$1 : 0.99797.$$

This has been done on the authority of an investigation by Mr. Stone, in the *Monthly Notices of the Royal Astronomical Society*, 1867, November 8.

PARALLAX.—The parallaxes of the Sun, Moon, and Planets actually employed are given in the lower part of the page, as previously stated; the assumed ellipticity of the Earth being $\frac{1}{300}$.

For the planets the formula is, $\log. \text{parallax} = \log. \sin. (\text{zen. dist.} - 11'. 12'') + \text{ar. co. log. distance} + 0.95045$.

For the Moon, the horizontal equatoreal parallaxes are interpolated, without alteration, from the Nautical Almanac, for the time of observation. The formula employed

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for the computation of the parallax to be applied to the observed zenith distance, is—

$$\text{Parallax} = \text{Hor. Equat. Par. from N.A.} \times \text{Sin Dist. from Geoc. Zenith} \times \text{Geocentric Radius} \\ (\text{Log} = 9.9991136) + \text{Corr. derived from the following table :—}$$

Z. D.	Correction for South Limb.	Z. D.	Correction for South Limb.	Z. D.	Correction for North Limb.	Z. D.	Correction for North Limb.
30	— 0.01	60	+ 0.10	30	— 0.08	60	— 0.10
35	0.00	65	+ 0.11	35	— 0.09	65	— 0.10
40	+ 0.02	70	+ 0.13	40	— 0.09	70	— 0.10
45	+ 0.03	75	+ 0.15	45	— 0.10	75	— 0.10
50	+ 0.05	80	+ 0.16	50	— 0.10	80	— 0.09
55	+ 0.07			55	— 0.10		

The correction tabulated above is the sum of two corrections, viz. : of one peculiar to the Moon's limbs, for which the numbers may be inferred from the table of corrections given in a subsequent part of this Introduction for the Moon's parallax in occultations, by supposing V (the angle, from the vertical, of the point of the Moon's limb under observation) = 0° or 180° ; and of another due to the employment of the arc of equatoreal parallax instead of its sine, for which the formula is,

$$\frac{(\text{Seconds of hor. parallax})^2}{6} \times \text{Sin Z. D.} \times \text{Cos}^2 \text{ Z. D.} \times \text{Sin}^2 1''.$$

For the computation of the parallaxes of the small planets, the distances are taken from the Supplement to the Nautical Almanac, or from the *Berliner Jahrbuch*, for planets given in those works. For other planets they are usually taken from the *Astronomische Nachrichten*.

SEMIDIAMETER.—The semidiameters of the Sun, Moon, and Planets are given in the lower part of the page. For the Moon, Mercury, and Uranus, they are taken unchanged from the Nautical Almanac. For the Sun, Venus, Mars, Jupiter, and Saturn, the semidiameters are also taken unchanged from the Nautical Almanac, except in cases where only one limb has been observed; when, for the Sun, the correction — $0''.53$, derived from the observations of several preceding years, has been applied to the tabular semidiameter; for Venus, the correction $+ 0''.392 + 0.027 \times \text{tabular semidiameter}$, derived from an investigation mentioned at page xlviii above, has been applied to the semidiameter given in the Nautical Almanac; and, for Mars, Jupiter and Saturn, a correction usually derived from neighbouring observations, and specified in the notes, has been similarly applied.

GEOCENTRIC N. P. D. OF CENTER.—The numbers in this column are found by combining the Apparent Zenith Distance with the Refraction, Parallax, Semidiameter, and Assumed Colatitude $38^\circ.31'.21''-60$.

CORRECTION TO MEAN N. P. D. OF STARS.—The corrections for reducing the Apparent N.P.D. of the stars to the Mean North Polar Distances for the beginning of 1870, are

SEMIDIAMETERS OF PLANETS;
STAR CORRECTIONS IN N. P. D. ; RUNS OF MICROSCOPE-MICROMETERS.

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given at the lower part of the page. For the stars in the list of the Nautical Almanac, the correction is found by subtracting the mean declination of the Nautical Almanac from the apparent declination of the same. For stars not in the Nautical Almanac, the numbers required to change Mean N.P.D. to Apparent N.P.D. are computed by the formula,

$$E e' + F f' + G g' + H h' + L + l' - 300'' + \mu' t$$

(where μ' is the annual proper motion in N.P.D. taken from Mr. Main's or Mr. Stone's papers in the *Memoirs of the Royal Astronomical Society*, or from the *British Association Catalogue*, and t is the fraction of a year corresponding to the day of observation) which is derived from the well-known formula

$$A a' + B b' + C c' + D d' + \mu' t$$

or its equivalent

$$A. \sin N. P. D. \times \text{numb. (log} = 9.6376) - A. \sin R. A. \cos N. P. D. + B. \cos R. A. \cos N. P. D. + C. \cos R. A. \times \text{numb. (log} = 1.3020) - D. \sin R. A. + \mu' t.$$

The formulæ for E, F, G, H, L, have been already given (page xlix) : $e' = a' + 1.2$, $f' = b' + 1.2$, $g' = c' + 25$, $h' = d' + 1.2$, $l' = 210 - 25 \times e' - 25 \times f' - 1.2 \times g' - 25 \times h'$. The values of the day-constants log. E, log. F, log. G, log. H, and L, are given in the Nautical Almanac. The values of the star-constants log. e' , log. f' , log. g' , log. h' , and l' , for the stars contained in the Seven-Year Catalogue for 1860, and in the New Seven-Year Catalogue for 1864, are printed in those Catalogues. For other stars the star-constants will be found in the annual Catalogues for the years 1868 and 1869, or in that included in the present volume.

The sign of the computed quantity is changed before application.

§ 4. *Runs of each Microscope-Micrometer of the Transit-Circle ; and Zenith Points of the Transit-Circle, in the Year 1870 ; page (108) to (125).*

With regard to the *Runs of the Microscopes*, the columns under A, B, C, D, E, F, contain respectively the number of revolutions of each micrometer which measures an arc of 5' on the circle ; and the last column gives the sum of these numbers, and exhibits the number of revolutions which, for the mean of the microscopes, measures an arc of 30', on the supposition that the screws of the micrometers have sensibly equal values. In the first calculations for the reduction of the observations it is assumed that the space of 30' corresponds approximately to $\frac{50}{51} \times 30''000$, or to 29''.4118 ; and, the fiftieth part of the micrometer-reading for the mean of the microscopes being added to the micrometer-reading, the remaining correction, depending on the difference between the values in the last column of the table in question and 29''.4118, is computed in the way that has been explained (page lii).

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With regard to the Table of *Zenith Points*, the following explanation will be sufficient.

Whenever observations of stars have been made by reflexion, the results for zenith point derived from them have been combined with those derived from the observations of the reflected image of the wire. The results are always divided into three groups, viz.: those resulting from north stars, those from south stars, and those from wire-observations; and, to prevent too much weight being given to those divisions of the circle which are always under the microscopes for the wire-observations, to each result derived from a star-observation there is attributed twice the weight which is attributed to the result of a wire-observation. From the pains taken to equalize the number of observations of stars north and south of the Zenith, no undue weight is, on the average, given to either of these positions; and, on the whole, it is presumed that, by this method of combination, the best possible average result is obtained.

§ 5. *Apparent Right Ascensions of Polaris and δ Ursæ Minoris; and Mean Right Ascensions, and Mean North Polar Distances of Stars deduced from each day's observation in the Year 1870, page {1} to {62}.*

The observations of Right Ascension and North Polar Distance of Stars are made so frequently on the same days that it has been thought convenient in the present volume to combine them under one general arrangement.

The apparent right ascensions of Polaris and δ Ursæ Minoris are extracted without alteration from the *twentieth* column of the *Transits observed*, &c.

The mean right ascensions of stars are found by applying to the apparent right ascensions in the *twentieth* column the corrections in the *twenty-first* column.

The corrections for personal equation have been invariably applied in this section when the observations of stars for clock-error have been made by one observer, and those of any other object requiring reduction, on the same day, by another observer.

The rules for the nomenclature of stars are the same as those in the section of the *Transits observed*, detailed in page xxvii, but they are more rigorously followed. The stars in Weisse's Catalogues are referred to under the initials W.B., which stand for "Weisse's Bessel." The stars in Oeltzen's Catalogue of Argelander's Zones are referred to under the abbreviation Oeltz. Arg.

The Mean North Polar Distances are found by applying to the North Polar Distances in Section 4 the corrections given for each star in the lower part of the page.

SEPARATE RESULTS FOR STARS' R.A. AND N.P.D. ;
DISCORDANCE OF DIRECT AND REFLEXION RESULTS.

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§ 6. *Investigation of the Correction to North Polar Distance depending on the discordance between the results of Direct Observation and Reflexion Observation, and Investigation of the Apparent Correction to Assumed Latitude of the Observatory.*

The results of the direct and reflexion observations have been kept separate, with a view of ascertaining whether there is discordance between them, as has been frequently observed in the results of other circles; and the results of observations above and below the pole have been kept separate, in order to ascertain whether there is any sensible error in the assumed colatitude.

With regard to the first of these points, the means of the groups of Direct-results and Reflexion-results have been taken for all the stars observed: and the algebraical excess of the Reflexion-result over the Direct-result is given in the subjoined table. The weight is a number proportional to the fraction, whose numerator is the product of the numbers of direct and of reflexion observations, and whose denominator is their sum.

EXCESS OF REFLEXION-RESULTS ABOVE DIRECT-RESULTS, FOR OBSERVATIONS
OF ZENITH DISTANCES WITH THE TRANSIT-CIRCLE, 1870.

Name of Star.	Approximate N. P. D.	Seconds of R.	Seconds of D.	R. — D.	Number of Obs.		Weight.
					R.	D.	
Groombridge 2196	6. 57	21.72	23.16	— 1.44	2	2	4
Ursæ Minoris	7. 45	10.23	11.39	— 1.16	1	3	3
76 Draconis	7. 57	9.38	9.68	— 0.30	1	1	2
Groombridge 1845	8. 25	17.24	20.35	— 3.11	1	1	2
Piazzi VI. 285	8. 30	52.64	52.37	+ 0.27	1	1	2
Bradley 1439	8. 50	14.35	14.27	+ 0.08	1	1	2
Piazzi II. 60	8. 56	3.12	5.50	— 2.38	1	1	2
Groombridge 779	9. 29	34.85	35.28	— 0.43	2	2	4
Piazzi III. 160	9. 39	55.87	56.58	— 0.71	2	2	4
Piazzi VII. 155	9. 48	23.13	24.16	— 1.03	1	1	2
Bradley 2749	9. 56	12.21	12.79	— 0.58	1	1	2
41 Draconis	10. 0	57.94	58.08	— 0.14	3	3	6
40 Draconis	10. 1	9.59	10.11	— 0.52	4	4	8
Bradley 24	10. 40	4.14	5.81	— 1.67	2	2	4
Piazzi IV. 269	10. 55	30.03	32.89	— 2.86	1	1	2
Bradley 1634	11. 39	40.09	39.98	+ 0.11	2	5	6
Piazzi IV. 317	12. 8	57.73	57.67	+ 0.06	3	3	6
Bradley 1431	12. 44	50.13	50.45	— 0.32	1	1	2
Bradley 2440	13. 8	11.82	11.11	+ 0.71	2	2	4
Bradley 1446	13. 37	7.53	7.89	— 0.36	3	4	7
Bradley 6	13. 46	17.82	18.95	— 1.13	2	2	4
19 Ursæ Minoris	13. 47	45.66	45.57	+ 0.09	1	1	2
7 Ursæ Minoris	13. 56	46.06	47.30	— 1.24	1	1	2
Bradley 1650	14. 7	2.56	3.57	— 1.01	3	7	8
Groombridge 3508	14. 10	5.25	5.99	— 0.74	1	1	2

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EXCESS OF REFLEXION-RESULTS ABOVE DIRECT-RESULTS, FOR OBSERVATIONS
OF ZENITH DISTANCES WITH THE TRANSIT-CIRCLE, 1870—continued.

Name of Star.	Approximate N. P. D.	Seconds of R.	Seconds of D.	R.—D.	Number of Obs.		Weight.
					R.	D.	
Piazzi IV. 112	14. 18	3.65	4.43	— 0.78	1	1	2
50 Draconis	14. 43	15.19	14.63	+ 0.56	2	2	4
β Ursæ Majoris	15. 18	47.16	47.30	— 0.14	6	7	13
π Cephei	15. 18	54.86	54.74	+ 0.12	1	1	2
73 Draconis	15. 29	29.80	29.08	+ 0.72	2	3	5
23 Cassiopeiæ	15. 51	48.03	46.48	+ 1.55	1	1	2
B. F. 2577	16. 3	57.38	58.34	— 0.96	2	2	4
Groombridge 215	16. 19	37.42	36.34	+ 1.08	1	1	2
Bradley 3085	16. 28	38.89	38.88	+ 0.01	1	1	2
Piazzi XIII. 109	16. 55	58.14	58.05	+ 0.09	2	2	4
31 Cephei	17. 1	54.96	53.21	+ 1.75	1	1	2
Bradley 471	17. 5	50.73	49.61	+ 1.12	1	1	2
27 Ursæ Majoris	17. 9	32.52	31.52	+ 1.00	3	3	6
χ Draconis	17. 19	28.65	27.55	+ 1.10	1	2	3
16 Cephei	17. 26	18.81	19.78	— 0.97	2	2	4
Groombridge 3946	17. 33	40.46	39.81	+ 0.65	3	3	6
ψ Draconis	17. 47	17.53	17.36	+ 0.17	1	1	2
Groombridge 2437	18. 4	24.08	23.85	+ 0.23	5	5	10
54 Cassiopeiæ	19. 3	38.27	38.99	— 0.72	1	1	2
Groombridge 3409	19. 5	21.67	21.73	— 0.06	4	4	8
Bradley 2854	19. 16	39.71	40.95	— 1.24	1	2	3
κ Draconis	19. 29	42.07	40.99	+ 1.08	1	1	2
λ Draconis	19. 57	5.78	5.75	+ 0.03	6	6	12
β Cephei	20. 0	35.07	34.97	+ 0.10	4	7	11
42 Cassiopeiæ	20. 2	9.11	8.53	+ 0.58	2	2	4
4 Draconis	20. 4	41.82	41.44	+ 0.38	5	5	10
Bradley 3125	20. 21	18.56	19.95	— 1.39	1	1	2
Groombridge 3590	20. 27	4.72	6.02	— 1.30	1	1	2
σ Draconis	20. 33	36.39	35.95	+ 0.44	3	3	6
Piazzi V. 335	20. 38	21.71	21.46	+ 0.25	2	3	5
Groombridge 2952	20. 58	49.91	50.04	— 0.13	1	1	2
55 Camelopardali	21. 8	48.73	49.04	— 0.31	1	1	2
ω Draconis	21. 10	55.97	57.45	— 1.48	1	1	2
Bradley 2636	21. 32	8.77	9.33	— 0.56	2	2	4
ρ Ursæ Majoris	21. 51	59.88	61.06	— 1.18	1	1	2
46 Cassiopeiæ	21. 57	18.49	17.33	+ 1.16	1	1	2
Piazzi I. 88	22. 15	37.98	39.14	— 1.16	1	1	2
7 Draconis	22. 29	58.19	58.33	— 0.14	4	4	8
3 Draconis	22. 32	8.15	8.84	— 0.69	1	1	2
ψ Cassiopeiæ	22. 32	58.75	58.20	+ 0.55	1	1	2
δ Draconis	22. 34	1.25	0.70	+ 0.50	3	3	6
θ Cephei	22. 35	58.81	58.02	+ 0.79	1	1	2
9 Draconis	22. 42	4.50	5.18	— 0.68	2	2	4
Bradley 366	22. 43	49.08	48.32	+ 0.76	1	1	2
Piazzi V. 246	23. 0	12.78	14.31	— 1.53	1	1	2
Bradley 332	23. 11	3.15	3.85	— 0.70	1	4	3
Groombridge 3760	23. 56	60.13	58.04	+ 2.09	1	1	2
16 Cassiopeiæ	23. 58	1.08	1.12	— 0.04	1	1	2
55 Cassiopeiæ	24. 5	15.49	13.25	+ 2.24	1	1	2
ζ Draconis	24. 7	31.08	30.14	+ 0.94	1	1	2
55 Draconis	24. 14	20.40	20.33	+ 0.07	1	1	2
A Ursæ Majoris	24. 24	54.76	54.28	+ 0.48	2	2	4

DISCORDANCE OF DIRECT AND REFLEXION RESULTS.

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EXCESS OF REFLEXION-RESULTS ABOVE DIRECT-RESULTS FOR OBSERVATIONS
OF ZENITH DISTANCES WITH THE TRANSIT-CIRCLE, 1870—*continued.*

Name of Star.	Approximate N. P. D.	Seconds of R.	Seconds of D.	R.—D.	Number of Obs.		Weight.
					R.	D.	
ϵ Cephei.....	24. 28	58.72	58.30	+ 0.42	2	2	4
Groombridge 3739.....	24. 31	16.94	16.05	+ 0.89	1	1	2
π Draconis.....	24. 32	8.64	8.20	+ 0.44	5	10	13
δ Draconis.....	24. 38	1.84	2.38	- 0.54	3	3	6
Bradley 448.....	24. 49	37.35	34.46	+ 2.89	2	2	4
Piazzi XI. 43.....	24. 57	29.93	30.67	- 0.74	2	2	4
α Draconis.....	25. 0	7.93	7.40	+ 0.53	7	11	17
g Draconis.....	25. 9	52.12	50.55	+ 1.57	1	2	3
e Draconis.....	25. 32	32.10	33.89	- 1.79	1	1	2
36 Draconis.....	25. 38	47.69	47.91	- 0.22	1	1	2
28 Ursæ Majoris.....	25. 45	1.11	1.19	- 0.08	1	1	2
ξ^2 Cephei.....	26. 0	17.04	16.03	+ 1.01	1	1	2
h Ursæ Majoris.....	26. 22	18.95	18.63	+ 0.32	2	2	4
Piazzi XXI. 360.....	26. 59	33.97	34.30	- 0.33	3	3	6
Piazzi XXII. 115.....	27. 19	60.03	59.84	+ 0.19	1	1	2
θ Cephei.....	27. 26	31.65	32.47	- 0.82	1	1	2
α Ursæ Majoris.....	27. 32	51.18	51.87	- 0.69	5	8	12
Groombridge 2742.....	27. 46	44.20	44.41	- 0.21	2	2	4
α Cephei.....	27. 57	52.71	52.70	+ 0.01	2	6	6
68 Draconis.....	28. 18	51.92	52.11	- 0.19	1	1	2
Bradley 2370.....	29. 5	22.12	21.02	+ 1.10	1	1	2
ν Cephei.....	29. 28	42.72	42.46	+ 0.26	2	5	6
20 Ursæ Majoris.....	29. 40	22.92	23.52	- 0.60	2	2	4
β Camelopardali.....	29. 45	7.12	5.95	+ 1.17	1	3	3
τ Andromedæ.....	50. 4	57.10	55.42	+ 1.68	1	2	3
γ Cygni.....	50. 9	30.28	30.21	+ 0.07	1	1	2
Groombridge 3357.....	50. 15	16.39	17.44	- 1.05	2	3	5
12 Canum Venaticum..	50. 58	44.15	43.75	+ 0.40	4	5	9
η Lyræ.....	51. 4	35.54	34.59	+ 0.95	5	5	10
Groombridge 2530.....	51. 15	40.45	41.28	- 0.83	1	1	2
α Lyræ.....	51. 20	9.91	8.53	+ 1.38	5	22	17
Groombridge 1830.....	51. 20	56.28	55.07	+ 1.21	1	3	3
10 Lacertæ.....	51. 37	32.30	33.95	- 1.65	2	2	4
μ Aurigæ.....	51. 40	21.31	21.40	- 0.09	1	1	2
22 Cygni.....	51. 51	27.57	27.78	- 0.21	1	1	2
72 Cygni.....	52. 2	53.57	52.26	+ 1.31	2	4	5
μ Andromedæ.....	52. 12	23.32	22.16	+ 1.16	1	3	3
Piazzi I. 170.....	52. 41	43.86	44.84	- 0.98	1	1	2
ρ Herculis.....	52. 43	58.87	58.45	+ 0.42	3	3	6
ν Aurigæ.....	52. 44	5.90	4.79	+ 1.11	1	1	2
1 Lacertæ.....	52. 53	53.40	51.79	+ 1.61	2	2	4
π Herculis.....	53. 2	34.50	34.21	+ 0.29	1	1	2
70 Cygni.....	53. 26	50.57	49.85	+ 0.72	4	4	8
14 Canum Venaticum..	53. 30	17.62	18.00	- 0.38	1	1	2
2 Aurigæ.....	53. 31	9.11	10.36	- 1.25	1	1	2
Piazzi XVII. 3.....	53. 53	40.89	39.55	+ 1.34	2	2	4
21 Leonis Minoris.....	54. 7	22.62	21.79	+ 0.83	2	3	5
61 Ursæ Majoris.....	55. 3	51.23	50.43	+ 0.80	5	5	10
46 Leonis Minoris.....	55. 5	6.81	5.41	+ 1.40	2	2	4
δ Boötis.....	56. 11	56.10	55.07	+ 1.03	3	3	6
ρ Coronæ.....	56. 18	11.26	9.99	+ 1.27	1	2	3
56 Persei.....	56. 20	33.12	31.61	+ 1.51	2	2	4

EXCESS OF REFLEXION-RESULTS ABOVE DIRECT-RESULTS FOR OBSERVATIONS
OF ZENITH DISTANCES WITH THE TRANSIT-CIRCLE, 1870—continued.

Name of Star.	Approximate N. P. D.	Seconds of R.	Seconds of D.	R.—D.	Number of Obs.		Weight.
					R.	D.	
δ Trianguli	56. 22	18. 98	19. 72	— 0. 74	3	3	6
ϵ Cygni	56. 30	55. 16	54. 63	+ 0. 53	2	2	4
β^1 Lyræ	56. 47	13. 29	11. 91	+ 1. 38	1	8	4
ϵ Aurigæ	57. 2	32. 47	31. 91	+ 0. 56	2	4	5
20 Leonis Minoris	57. 26	16. 93	16. 64	+ 0. 29	5	7	12
γ Lyræ	57. 29	14. 82	13. 52	+ 1. 30	4	5	9
38 Pegasi	58. 5	31. 91	30. 88	+ 1. 03	2	2	4
49 Cygni	58. 9	14. 30	13. 15	+ 1. 15	1	1	2
ζ Herculis	58. 9	37. 96	35. 91	+ 2. 05	2	4	5
ϵ Herculis	58. 52	51. 42	49. 68	+ 1. 74	3	3	6
ρ Boötis	59. 3	24. 32	24. 02	+ 0. 30	3	3	6
41 Cygni	60. 3	51. 45	50. 15	+ 1. 30	1	1	2
ϕ Cygni	60. 8	42. 36	41. 94	+ 0. 42	3	6	8
12 Trianguli	60. 54	43. 67	44. 03	— 0. 36	2	2	4
28 Andromedæ	60. 57	56. 87	56. 77	+ 0. 10	1	1	2
α Herculis	61. 15	14. 66	12. 17	+ 2. 49	1	1	2
ρ^1 Cancræ	61. 15	17. 86	16. 07	+ 1. 79	1	2	3
78 Pegasi	61. 21	30. 52	29. 45	+ 1. 07	1	2	3
ϵ Andromedæ	61. 23	41. 27	38. 91	+ 2. 36	1	3	3
β Tauri	61. 30	19. 26	18. 17	+ 1. 09	2	8	6
41 Comæ	61. 40	36. 14	36. 35	— 0. 21	1	1	2
Bradley 3212	61. 41	45. 39	45. 35	+ 0. 04	1	1	2
31 Comæ	61. 45	4. 61	4. 02	+ 0. 59	4	4	8
μ Herculis	62. 12	6. 06	4. 94	+ 1. 12	2	7	6
β^1 Cygni	62. 18	42. 82	42. 30	+ 0. 52	3	3	6
χ Cancræ	62. 21	48. 65	48. 08	+ 0. 57	3	3	6
ϵ Boötis	62. 22	35. 09	34. 20	+ 0. 89	3	8	9
136 Tauri	62. 25	17. 25	15. 04	+ 2. 21	2	3	5
32 Vulpeculæ	62. 26	8. 74	6. 68	+ 2. 06	1	4	3
61 Pegasi	62. 27	37. 61	37. 49	+ 0. 12	2	2	4
ν Geminorum	62. 49	4. 87	4. 60	+ 0. 27	1	1	2
α Coronæ	62. 50	47. 49	46. 29	+ 1. 20	1	1	2
μ Leonis	63. 22	56. 21	54. 84	+ 1. 37	7	9	16
89 Herculis	63. 55	39. 05	37. 42	+ 1. 63	2	2	4
3 Vulpeculæ	63. 59	8. 36	6. 61	+ 1. 75	3	3	6
49 Arietis	64. 3	15. 31	12. 70	+ 2. 61	1	1	2
ψ^2 Cancræ	64. 6	1. 33	0. 88	+ 0. 45	2	2	4
87 Herculis	64. 19	55. 58	55. 06	+ 0. 52	1	2	3
16 Pegasi	64. 41	7. 17	6. 90	+ 0. 27	1	6	3
κ Pegasi	64. 57	5. 26	5. 38	— 0. 12	3	4	7
11 Tauri	65. 5	35. 69	34. 77	+ 0. 92	2	2	4
56 Pegasi	65. 13	59. 24	56. 82	+ 2. 42	1	1	2
7 Comæ	65. 19	54. 37	53. 48	+ 0. 89	2	3	5
ϵ Leonis	65. 37	43. 47	42. 47	+ 1. 00	2	6	6
μ Pegasi	66. 5	2. 45	2. 73	— 0. 28	2	4	5
ζ Andromedæ	66. 26	25. 76	25. 00	+ 0. 76	3	3	6
Piazzæ XVIII. 116	66. 28	42. 04	41. 95	+ 0. 09	4	6	10
34 Vulpeculæ	66. 41	25. 40	24. 46	+ 0. 94	2	2	4
1 Geminorum	66. 43	56. 24	55. 86	+ 0. 38	1	2	3
Bradley 2308	66. 46	44. 61	43. 66	+ 0. 95	1	1	2
λ Pegasi	67. 7	4. 72	4. 53	+ 0. 19	2	2	4
α Arietis	67. 9	13. 53	12. 41	+ 1. 12	2	13	7

DISCORDANCE OF DIRECT AND REFLEXION RESULTS.

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EXCESS OF REFLEXION-RESULTS ABOVE DIRECT-RESULTS, FOR OBSERVATIONS
OF ZENITH DISTANCES WITH THE TRANSIT-CIRCLE, 1870—*continued*.

Name of Star.	Approximate N. P. D.	Seconds of R.	Seconds of D.	R.—D.	Number of Obs.		Weight.
					R.	D.	
1 Comæ	67. 10	52.26	52.76	— 0.50	1	1	2
υ Pegasi	67. 18	41.77	40.45	+ 1.32	1	1	2
δ Geminorum	67. 46	51.16	49.73	+ 1.43	1	2	3
γ ₁ Pegasi	68. 13	6.67	8.90	— 2.23	2	2	4
δ Leonis	68. 45	51.73	51.21	+ 0.52	3	7	8
τ ¹ Arietis	69. 19	24.65	24.15	+ 0.50	1	1	2
1 Boötis	69. 23	9.68	8.20	+ 1.48	7	8	15
γ ¹ Leonis	69. 30	7.01	6.86	+ 0.15	3	8	9
ω ² Tauri	69. 44	37.56	36.31	+ 1.25	1	6	3
β Arietis	69. 49	47.93	42.50	+ 5.43	1	4	3
Arcturus	70. 8	23.08	22.56	+ 0.52	1	18	4
f Boötis	70. 11	13.98	13.39	+ 0.59	2	5	6
δ Arietis	70. 45	59.69	59.46	+ 0.23	1	3	3
Piazzì XIII. 228	72. 37	39.44	38.30	+ 1.14	1	2	3
η Piscium	75. 19	31.74	29.28	+ 2.46	1	6	3
γ Virginis	75. 31	32.85	32.42	+ 0.43	2	3	5
α Ophiuchi	77. 20	36.31	34.64	+ 1.67	1	15	4
Regulus	77. 23	54.89	53.88	+ 1.01	2	20	7
ξ Leonis	78. 7	33.58	33.02	+ 0.56	1	3	3

EXCESS OF REFLEXION-RESULTS ABOVE DIRECT-RESULTS FROM GROUPS OF
STARS OBSERVED WITH THE TRANSIT-CIRCLE.

Extent of Group.	Weight.	Mean N. P. D.	Mean Value of R.—D.
Groombridge 2196 to 40 Draconis....	43	9. 6	— 0.77
Bradley 24 to 50 Draconis	55	13. 5	— 0.50
β Ursæ Minoris to Groombridge 2437.	69	16. 40	+ 0.31
54 Cassiopeiæ to ω Draconis	73	20. 2	— 0.02
Bradley 2636 to 55 Draconis	51	22. 46	+ 0.06
A Ursæ Majoris to 28 Ursæ Majoris..	63	24. 50	+ 0.41
ξ ² Cephei to β Camelopardali	55	27. 57	— 0.08
τ Andromedæ to μ Andromedæ	67	51. 12	+ 0.62
Piazzì I. 170 to 46 Leonis Minoris....	51	53. 47	+ 0.70
δ Boötis to γ Lyræ	53	56. 53	+ 0.70
38 Pegasi to 31 Comæ	68	60. 16	+ 0.96
μ Herculis to 87 Herculis	78	63. 0	+ 1.15
16 Pegasi to Piazzì XVIII. 116	48	65. 42	+ 0.48
34 Vulpeculæ to δ Leonis	39	67. 33	+ 0.43
τ ¹ Arietis to Piazzì XIII. 228	48	69. 54	+ 1.13
η Piscium to ξ Leonis	22	76. 46	+ 1.13

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This table indicates with tolerable clearness the law of the values of $R - D$, the mean numbers being mostly negative for stars north of the Zenith, and always positive for stars south of the Zenith; so that a positive correction is required for Direct Observations south of the Zenith, and a negative correction to Reflexion Observations. Assuming that the correction can be represented by—

$$x + y \cos^2 Z.D. \text{ south} \times \sin Z.D. \text{ south},$$

it is found by calculation, that the following expressions, when tabulated, will give the values which best agree with the errors in the table above, namely :—

For direct observations

$$+ 0''.181 + 0''.729 \sin Z.D. \cos^2 Z.D.$$

For reflexion-observations

$$- 0''.181 - 0''.729 \sin Z.D. \cos^2 Z.D.$$

For use, these formulæ have been tabulated as follows; and the corrections have been applied to all the observations of Zenith Distance made throughout the year; that is, to the mean result for N.P.D. of each star, and to every North Polar Distance of the Sun, Moon, and Planets in the section of Planetary Results.

CORRECTION FOR DISCORDANCE OF DIRECT AND REFLEXION RESULTS, 1870.

N. P. D.	Corrections to Results of Direct- Observations.	Corrections to Results of Reflexion- Observations.
— 40°	+ 0''.15	— 0''.15
30	0''.09	0''.09
20	+ 0''.01	— 0''.01
— 10	— 0''.06	+ 0''.06
0	0''.10	0''.10
+ 10	0''.09	0''.09
20	— 0''.03	+ 0''.03
30	+ 0''.08	— 0''.08
40	0''.20	0''.20
50	0''.32	0''.32
60	0''.41	0''.41
70	0''.46	0''.46
80	0''.45	0''.45
90	0''.40	0''.40
100	0''.33	0''.33
110	0''.25	0''.25
+ 120	+ 0''.20	— 0''.20

RESULTING CORRECTION FOR R.—D; CORRECTION TO ASSUMED LATITUDE. lxxiii

The law assumed for these numbers, it will be remarked, is different from that of the years preceding 1862.

The general system of corrections for R—D which has been followed for many years has been retained in the present volume. A careful examination of the different values obtained in different years has convinced me that the quantity is real, but I am still unable to explain perfectly its origin. So long as the evidence for its existence depended on the Mural Circle only, where the flexure of the telescope could not be independently ascertained, it might be attributed to flexure: but its persistent appearance in the observations with the Transit-Circle (where there is no sensible doubt on the magnitude of flexure of the telescope, and where the corresponding correction has been applied), as well as the general consistency in the results obtained for colatitude in different years, while different values have been used for $\frac{R-D}{2}$, seems to prove that it does not depend on mechanical disturbance of the instrument. On these points I would refer the reader to the Introduction to the Seven-year Catalogue for 1860; or to a paper in volume xxxii. of the *Memoirs of the Royal Astronomical Society*, entitled, "On the Discordance between Reflexion and Direct Observations in Zenith Distance."

The observations of circumpolar stars have been reduced for the determination of latitude in the same manner as in preceding years. The computations below are directed to the determination of the quantity z which ought to be added to the colatitude assumed in the reduction of the observations, namely, $38^{\circ}.31'.21''.60$.

The weights used in the following table are determined by use of the "Probable Errors of Greenwich Observations in Zenith Distance," given by Mr. Stone in the *Monthly Notices of the Royal Astronomical Society* for 1869, June 11, page 324. Putting n for the number of observations of a star above the pole, e for the probable error of one observation; n_1 and e_1 , the similar quantities for the observations below the pole; the formula employed to determine the weight to be given to that star is

$$\frac{n n_1}{n_1 e^2 + n e_1^2}.$$

CORRECTION TO ASSUMED LATITUDE, 1870.

Star's Name, and Mode of Observation.	Number of Obs.	N. P. D. Uncorrected.	Result Corrected for Dis- cordance.	Number of Obs.	Concluded N. P. D. on assumed Latitude.	Number of Obs.	Algebraic Sum of Determina- tions.	Weight.	Product.
Polaris D.	79	1. 23. 1' 47	1' 37	79	1' 37	145	+ 0' 24	123	+ 29' 52
S.P.... D.	66	— 1. 23. 1' 23	— 1' 13	66	— 1' 13				
Cephei 51 D.	12	2. 45. 37' 51	37' 41	12	37' 41	46	— 0' 77	31	— 23' 87
S.P.... D.	34	— 2. 45. 38' 27	— 38' 18	34	— 38' 18				

GREENWICH OBSERVATIONS, 1870.

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CORRECTION TO ASSUMED LATITUDE, 1870—continued.

Star's Name, and Mode of Observation.	Number of Obs.	N. P. D. Uncorrected.	Result corrected for Dis- cordance.	Number of Obs.	Concluded N. P. D. on assumed Latitude.	Number of Obs.	Algebraic Sum of Determina- tions.	Weight.	Product.
δ Ursæ Minoris . . . D.	36	° ' " 3. 23. 38. 49	" 38. 39	36	" 38. 39		"		"
S.P. . . . D.	10	— 3. 23. 38. 79	— 38. 70	10	— 38. 70	46	— 0. 31	25	— 7. 75
ϵ Ursæ Minoris . . . D.	3	7. 45. 11. 39	11. 30						
R.	1	7. 45. 10. 23	10. 32	4	11. 06				
S.P. . . . D.	1	— 7. 45. 11. 46	— 11. 39	1	— 11. 39	5	— 0. 33	2	— 0. 66
ζ Ursæ Minoris . . . D.	1	11. 48. 25. 15	25. 07	1	25. 07				
S.P. . . . D.	4	— 11. 48. 25. 17	— 25. 13	4	— 25. 13	5	— 0. 06	3	— 0. 18
γ Cephei D.	1	13. 5. 35. 22	35. 15	1	35. 15				
S.P. . . . D.	2	— 13. 5. 34. 34	— 34. 31	2	— 34. 31	3	+ 0. 84	2	+ 1. 68
β Ursæ Minoris . . . D.	7	15. 18. 47. 30	47. 24						
R.	6	15. 18. 47. 16	47. 22	13	47. 23				
S.P. . . . D.	6	— 15. 18. 46. 36	— 46. 33	6	— 46. 33	19	+ 0. 90	10	+ 9. 00
κ Draconis D.	1	19. 29. 40. 99	40. 96						
R.	1	19. 29. 42. 07	42. 10	2	41. 53				
S.P. . . . D.	1	— 19. 29. 42. 09	— 42. 09	1	— 42. 09	3	— 0. 56	2	— 1. 12
β Cephei D.	7	20. 0. 34. 97	34. 94						
R.	4	20. 0. 35. 07	35. 10	11	35. 00				
S.P. . . . D.	6	— 20. 0. 34. 15	— 34. 16	6	— 34. 16	17	+ 0. 84	9	+ 7. 56
π Draconis D.	10	24. 32. 8. 20	8. 23						
R.	5	24. 32. 8. 64	8. 61	15	8. 36				
S.P. . . . D.	1	— 24. 32. 8. 02	— 8. 08	1	— 8. 08	16	+ 0. 28	2	+ 0. 56
ξ^2 Cephei D.	1	26. 0. 16. 03	16. 07						
R.	1	26. 0. 17. 04	17. 00	2	16. 54				
S.P. . . . D.	2	— 26. 0. 18. 07	— 18. 13	2	— 18. 13	4	— 1. 59	2	— 3. 18
θ Cephei D.	1	27. 26. 32. 47	32. 52						
R.	1	27. 26. 31. 65	31. 60	2	32. 06				
S.P. . . . D.	3	— 27. 26. 33. 18	— 33. 25	3	— 33. 25	5	— 1. 19	3	— 3. 57
α Ursæ Majoris . . . D.	8	27. 32. 51. 87	51. 93						
R.	5	27. 32. 51. 18	51. 12	13	51. 62				
S.P. . . . D.	3	— 27. 32. 51. 96	— 52. 04	3	— 52. 04	16	— 0. 42	4	— 1. 68

CORRECTION TO ASSUMED LATITUDE.

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CORRECTION TO ASSUMED LATITUDE, 1870—continued.

Star's Name. and Mode of Observation.	Number of Obs.	N. P. D. Uncorrected.	Result Corrected for Dis- cordance.	Number of Obs.	Concluded N. P. D. on assumed Latitude.	Number of Obs.	Algebraic Sum of Determina- tions.	Weight.	Product.
α Cephei.....D. R.	6 2	$27.57.52.70$ $27.57.52.71$	52.76 52.65	8	" 52.73	15	" — 0.22	8	" — 1.76
S.P....D.	7	—27.57.52.87	—52.95	7	— 52.95				
ν Cephei.....D. R.	5 2	$29.28.42.46$ $29.28.42.72$	42.53 42.65	7	42.56	9	+ 0.86	3	+ 2.58
S.P....D.	2	—29.28.41.62	—41.70	2	— 41.70				
α Cassiopeiæ.....D.	1	$34.10.32.98$	33.11	1	33.11	7	— 0.02	3	— 0.06
S.P....D.	6	—34.10.33.02	—33.13	6	— 33.13				
γ Ursæ Majoris...D.	2	$35.34.56.75$	56.90	2	56.90	3	+ 1.53	1	+ 1.53
S.P....D.	1	—35.34.55.24	—55.37	1	— 55.37				
κ Cygni.....D.	3	$36.52.13.52$	13.68	3	13.68	5	+ 1.55	2	+ 3.10
S.P....D.	2	—36.52.12.00	—12.13	2	— 12.13				
β Draconis.....D.	3	$37.36.4.88$	5.06	3	5.06	4	+ 1.09	1	+ 1.09
S.P....D.	1	—37.36.3.83	— 3.97	1	— 3.97				
θ Ursæ Majoris...D.	1	$37.43.54.24$	54.42	1	54.42	5	— 0.17	2	— 0.34
S.P....D.	4	—37.43.54.45	—54.59	4	— 54.59				
η Ursæ Majoris...D.	6	$40.2.13.42$	13.62	6	13.62	8	+ 1.34	1	+ 1.34
S.P....D.	2	—40.2.12.13	—12.28	2	— 12.28				
ω^1 Cygni.....D.	1	$41.2.49.27$	49.48	1	49.48	3	+ 2.74		
S.P....D.	2	—41.2.46.59	46.74	2	— 46.74				
ι Ursæ Majoris...D.	5	$41.26.59.30$	59.51	5	59.51	7	+ 0.97		
S.P....D.	2	—41.26.58.39	—58.54	2	— 58.54				
f^1 Cygni.....D.	4	$42.59.7.46$	7.70	4	7.70	9	+ 0.89		
S.P....D.	5	—42.59.6.64	— 6.81	5	6.81				
τ Herculis.....D.	3	$43.22.33.63$	33.87	3	33.87	4	+ 2.14		
S.P....D.	1	—43.22.31.56	—31.73	1	— 31.73				
Capella.....D.	6	$44.8.14.59$	14.84	6	14.84	10	+ 0.75		
S.P....D.	4	—44.8.13.91	—14.09	4	— 14.09				

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CORRECTION TO ASSUMED LATITUDE, 1869—concluded.

Star's Name, and Mode of Observation.	Number of Obs.	N. P. D. Uncorrected.	Result corrected for Dis- cordance.	Number of Obs.	Concluded N. P. D. on assumed Latitude.	Number of Obs.	Algebraic Sum of Determina- tions.	Weight.	Product.
β Aurigæ.....D.	1	45. 4. 8.10	8.36	1	8.36	5	+ 1.22		"
S.P....D.	4	-45. 4. 6.96	- 7.14	4	- 7.14				
α Cygni.....D.	5	45. 10. 58.89	59.15	5	59.15	8	+ 0.45		
S.P....D.	3	-45. 10. 58.52	-58.70	3	- 58.70				
δ Cygni.....D.	4	45. 11. 6.82	7.08	4	7.08	6	+ 0.07		
S.P....D.	2	-45. 11. 6.83	- 7.01	2	- 7.01				
ξ Cygni.....D.	3	46. 35. 22.49	22.77	3	22.77	5	+ 2.34		
S.P....D.	2	-46. 35. 20.24	20.43	2	- 20.43				

The observations of the last nine stars have not been used for the correction of the assumed colatitude.

If z be the correction to the assumed colatitude, $2z$ + the algebraical sum of determinations ought to be equal to 0. Combining the whole with the weights above attached to them, $2z + 0''.058 = 0$, or $z = - 0''.03$. From this the colatitude would be $= 38^\circ. 31'. 21''.57$.

The diminution in the colatitude below that found in former years (about $38^\circ. 31'. 21''.80$) appears to have been caused entirely by the diminution of the adopted tabular refraction.

§ 7. *Observations of Azimuth with the Altazimuth*, page [i] to [liii].

The first *eleven* columns, on the left-hand page, require little explanation, except that by "Horizontal Transit" is meant the resolved horizontal part of the inclined movement of the object in passing through the field of the telescope. In making the observation, the instrument is clamped in azimuth, and the moderately-slow-motion screw of the Vertical Circle is used to make the transit of the object take place over the middle of each vertical wire. The observations have in general been made by the chronographic method, excepting at times when the galvanic apparatus has been out of order. Such cases are always distinctly marked whenever they occur.

The *twelfth* column is occupied by the personal equation of each observer, referred to Mr. Dunkin as a standard, deduced from the observations of transits in the year 1869 (see Introduction to Greenwich Observations 1869, page li), as the observations of 1870 are not available for the daily reductions of 1870. This personal equation is applied to the mean of observed transits (without application of any correction for omitted wires, if the transit is imperfect) to form the "Concluded Clock Time" in the *thirteenth* column.

The column *following* the "Concluded Clock Time" contains the error of the clock; that is, of Hardy, the Transit-Clock, when the observations are made by galvanic contact; or of Graham 1, when they are made by eye and ear. The number of seconds by which the Transit Clock is slow is, before application, corrected by the quantity $-0^s.03$ for the difference of longitude between the position of the Transit-Circle and that of the Altazimuth. This difference of longitude has been obtained by measurement on the plan of the Observatory, of which a reduced copy is attached to the volume for 1862.

By the application of the Clock Error to the Clock Time, the Sidereal Time in the *next* column is formed.

The last *four* columns contain the readings of the micrometers of the four microscopes of the Horizontal Circle. The designations a, b, c, d , are so distributed among these microscopes that the observer, walking round the pier in the direction of the Sun's diurnal movement, passes them in the order a, b, c, d .

From the readings of the microscope-micrometers in the *last four* columns on the left-hand page, together with the pointer-reading (which is not inserted in the printed columns), the Concluded Reading of Horizontal Circle in the *first* column of the right-hand page is formed in this manner:—Suppose it is found, on examining the runs, that an arc of $5'$ requires $7^{\text{rev.}}.8 - p$ of micrometer a , $7^{\text{rev.}}.7 - q$ of micrometer b , $7^{\text{rev.}}.9 - r$ of micrometer c , and $8^{\text{rev.}}.0 - s$ of micrometer d . Then p, q, r, s , are very small quantities. Now, suppose that the micrometer-readings in any observation are w, x, y, z : these four quantities being very nearly equal. Then the Concluded Circle-Reading ought to be

$$\frac{5'}{4} \times \left\{ \frac{w}{7.8-p} + \frac{x}{7.7-q} + \frac{y}{7.9-r} + \frac{z}{8.0-s} \right\}$$

or

$$\frac{5'}{4} \times \left\{ \frac{w}{7.8} + \frac{x}{7.7} + \frac{y}{7.9} + \frac{z}{8.0} \right\} + \frac{5'}{4} \times \left\{ \frac{w}{7.8} \cdot \frac{p}{7.8} + \frac{x}{7.7} \cdot \frac{q}{7.7} + \frac{y}{7.9} \cdot \frac{r}{7.9} + \frac{z}{8.0} \cdot \frac{s}{8.0} \right\}.$$

From the near equality of $\frac{w}{7.8}, \frac{x}{7.7}, \&c.$, and the smallness of $p, q, \&c.$, the factors of p, q, r, s , may be considered equal: and the whole expression then becomes

$$w \times \frac{5'}{4 \times 7.8} + x \times \frac{5'}{4 \times 7.7} + y \times \frac{5'}{4 \times 7.9} + z \times \frac{5'}{4 \times 8.0} \\ + \frac{1}{4} \left\{ w \times \frac{5'}{4 \times 7.8} + x \times \frac{5'}{4 \times 7.7} + y \times \frac{5'}{4 \times 7.9} + z \times \frac{5'}{4 \times 8.0} \right\} \times \frac{p+q+r+s}{7.85}$$

If the quantity $\frac{1}{4} \times \frac{100''}{7.85} \times (p+q+r+s)$ be called *Correction for Runs for 100''*, then the expression is

$$w \times \frac{5'}{4 \times 7.8} + x \times \frac{5'}{4 \times 7.7} + y \times \frac{5'}{4 \times 7.9} + z \times \frac{5'}{4 \times 8.0} \\ + \frac{1}{100} \left\{ w \times \frac{5'}{4 \times 7.8} + x \times \frac{5'}{4 \times 7.7} + y \times \frac{5'}{4 \times 7.9} + z \times \frac{5'}{4 \times 8.0} \right\} \times \text{Correction for Runs for 100''}.$$

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The separate terms of the first line are taken from four separate tables, entered with the respective arguments w, x, y, z ; and, when they are added together, the value of the second line is rapidly computed by a short multiplication (usually effected with the sliding rule).

Another correction is occasionally necessary. When the transit of the object has not been observed across every one of the six vertical wires, the mean of the times actually observed is retained unaltered; but a correction is applied to the circle-reading, representing the difference between the azimuth of the mean of the wires actually observed and the azimuth of the mean of the six vertical wires. This correction is equal to the angular distance between the mean of the wires observed and the mean of the six wires, multiplied by the cosecant of zenith distance. The angular distances from the several wires to the mean, which have been used in the year 1870, are the following, the designations of wires being the same as in preceding years: and the signs given suppose the Face of the Vertical Circle to be to the Right, and are changed when the Face is Left.

For wires used in chronographic observations :—

Wire s	— 120.22
t	— 73.49
u	— 25.47
v	+ 24.57
w	+ 72.79
x	+ 121.80

For wires used in observations by eye and ear :—

Wire q	— 601.33
r	— 359.78
s	— 121.48
x	+ 120.54
y	+ 359.58
z	+ 602.45

These intervals have been used from 1864, August 7.

For daily observation of the image of the collimator, it is necessary to make use of a single wire, and the wire x has generally been employed for this purpose. The angular depression of the collimator below the horizon being $12^{\circ}.18'$, the correction to be made to the Circle Reading in chronographic observations is $\pm 2'.1''.80 \times \secant 12^{\circ}.18' = \pm 2'.4''.66$; and similarly with the other systems. This value is applicable for reduction to the mean of wires s, t, u , &c.; but, when the transits are observed by eye and ear, over the wires q, r, s , &c., the correction to be made to the Circle Reading is $\pm 2'.0''.54 \times \secant 12^{\circ}.18' = \pm 2'.3''.37$.

INTERVALS OF VERTICAL WIRES OF ALTAZIMUTH;
SMALL CORRECTIONS FOR AZIMUTHS.

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By the application of this final correction, when necessary, the Concluded Reading in the *first* column on the right-hand page is formed.

The *second* column on the right-hand page contains the Approximate Apparent Zenith Distance taken from the Tabular Computations.

The *third* column contains the corrections to be applied to the Concluded Circle Reading on account of the error of collimation (the term having the same meaning as for a transit instrument) of the imaginary point in the field of view, which corresponds to the mean of the six vertical wires. The amount to be applied is, Horizontal Correction for Collimation $\times$ cosecant of Zenith Distance. The sign will change according as the Face of the Vertical Circle is Right or Left. The value of Horizontal Correction or Coefficient of Correction for Collimation, Face Right, is given at the bottom of the page; the method by which it is obtained will be explained in a subsequent section.

The next eight columns (from the *fourth* to the *eleventh*) contain the readings of the level-scales of the four levels which are parallel to the axis of the Vertical Circle, *e* and *f* being the readings of the two ends of one of the lower levels, *g* and *h* those of the other lower level, *i* and *k*, *l* and *m*, those of the two upper levels. As the reading of each level-scale proceeds in continuous order from the end next the Graduated Face of the Vertical Circle to the other end, it follows that the equivalents for the scale-values of both end-readings must be added; and that, when their mean is diminished by the reading corresponding to the horizontal position of the Horizontal Axis, the excess must be used (multiplied by the appropriate factor, viz., the cotangent of Zenith Distance) with its proper sign when the Graduated Face is Right, and with sign changed when the Graduated Face is Left.

The *twelfth* column contains the Concluded Level Indication. It is assumed that each division on the four levels represents one second of arc; and the process for forming the Concluded Level Indication has been, to add together the eight numbers from the eight preceding columns, omitting 1000 from that sum, and to divide the remainder by 8.

From this Concluded Level Indication is subtracted the Level Indication for Horizontal Position of Axis of Vertical Circle given at the foot of every page (the method of obtaining which will be explained in a subsequent section); and the remainder, which represents the angular elevation of that end of the Horizontal Axis which is farthest from the Graduated Face, is multiplied by the cotangent of Zenith Distance. When the Graduated Face is Left the sign of the product is changed. The resulting number is given in the *thirteenth* column as the Correction for Level.

The *fourteenth* column contains the Corrected Reading of Horizontal Circle, as affected by all these corrections.

The *fifteenth* column contains the Concluded Azimuth, measuring from the South towards the West, which is formed by merely subtracting, from the Corrected Reading

of Horizontal Circle, the Zero of Azimuth given at the bottom of the page. The method of determining the Zero of Azimuth will be explained in a subsequent section.

In cases wherein both limbs of the Moon have been observed, one of the limbs is usually defective through want of illumination. A correction to the Azimuth (always mentioned in the foot-notes) is applied in all such cases; this correction is computed by finding first the azimuth of a point opposite the Sun, and then multiplying the distance between the azimuth of this point and that of the Moon's limb by the sine of the Sun's zenith distance; the correction is, Versed Sine of this difference multiplied by the Moon's azimuthal semidiameter.

§ 8. *Observations of Zenith Distance with the Altazimuth*, page [lvi] to [xciii].

The *first eleven* columns require no explanation, except that by "Vertical Transit" is meant the resolved vertical part of the inclined movement of the object in passing through the field of the telescope. The Vertical Circle is clamped, and the moderately-slow-motion of the Horizontal Circle is used to make the transit of the object take place over the middle of each horizontal wire. The methods of observing and recording the times of transit are the same as for the Horizontal Transits.

The *twelfth* column contains a correction which exists theoretically in all cases, but which in the Azimuths is practically insensible, although for the Zenith Distances, more especially those which are observed near the Meridian, it sometimes becomes important. The nature of it is this: In the subsequent calculations it is tacitly assumed that at the mean of the observed times of passage across the six horizontal wires (supposed free from error of observation), the body was at the point which represents the mean of all the six wires. This, however, is true only on the supposition that the vertical movement of the body is uniform. The correction is investigated in the following manner. In the spherical triangle whose sides are a, b, c , and where C is the angle opposite to c , let a and b be respectively the colatitude of the zenith, and the north polar distance of the object; then C is the hour-angle, and c the zenith distance. Suppose these letters to correspond truly to the position of the object when it passes the geometrical mean of the six horizontal wires: then if δC be the addition (expressed in parts of the radius), or $\delta C \times 15 \sin 1''$ (δC , being expressed in seconds of time), which must be made to C in order to express the hour-angle when the object passes one wire, and if δc (expressed in parts of the radius), or $\delta c \times \sin 1''$ (δc , being expressed in seconds of arc), be the addition which must be made to c in order to give the zenith distance of the same wire, we have

$$C + \delta C \times 15 \sin 1'' = C + \frac{dC}{dC} \cdot \delta C + \frac{d^2 C}{d^2 C} \cdot \frac{(\delta C)^2}{2}.$$

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CORRECTION FOR WANT OF UNIFORMITY IN VERTICAL MOTION.**

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Now $\cos a \cdot \cos b + \sin a \cdot \sin b \cdot \cos C = \cos c$.

Therefore $\sin a \cdot \sin b \cdot \sin C \cdot \frac{dC}{dc} = \sin c$.

And $\sin a \cdot \sin b \left\{ \cos C \cdot \left(\frac{dC}{dc} \right)^2 + \sin C \cdot \frac{d^2C}{dc^2} \right\} = \cos c$.

Whence $\frac{dC}{dc} = \frac{\sin c}{\sin a \cdot \sin b \cdot \sin C}$

and $\frac{d^2C}{dc^2} = -\frac{\cos C}{\sin C} \left(\frac{\sin c}{\sin a \cdot \sin b \cdot \sin C} \right)^2 + \frac{\cos c}{\sin a \cdot \sin b \cdot \sin C}$

In the case before us C is a small quantity, but no other quantity is small. Hence the first term of $\frac{d^2C}{dc^2}$ is the principal term, and the second may be neglected in comparison with it. And thus the equation becomes,

$$C + \delta C \times 15 \sin 1'' = C + \frac{\sin c}{\sin a \cdot \sin b \cdot \sin C} \delta c - \frac{\cos C}{\sin C} \left(\frac{\sin c}{\sin a \cdot \sin b \cdot \sin C} \right)^2 \cdot \frac{(\delta c)^2}{2}.$$

An approximate solution gives $\delta C \times 15 \sin 1'' = \frac{\sin c}{\sin a \cdot \sin b \cdot \sin C} \delta c$.

Substituting this in the last term, we have

$$C + \delta C \times 15 \sin 1'' = C + \frac{\sin c}{\sin a \cdot \sin b \cdot \sin C} \delta c - \frac{\cot C}{2} \cdot (\delta C)^2 \cdot (15 \sin 1'')^2;$$

or, putting C_1 for the value of C in seconds of time,

$$C_1 + \delta C_1 = C_1 + \frac{\sin c}{\sin a \cdot \sin b \cdot \sin C_1 \cdot 15 \sin 1''} \delta c - \frac{\cot C_1}{2} \cdot (\delta C_1)^2 \cdot 15 \sin 1'';$$

and, taking the mean of both sides, attributing successively to each the value which it obtains for each of the six wires, we have,

Mean of observed hour-angles in seconds of time =

$$C_1 + \frac{\sin c}{6 \sin a \cdot \sin b \cdot \sin C_1 \cdot 15 \sin 1''} \Sigma \delta c - \frac{\cot C_1 \cdot 15 \sin 1''}{12} \cdot \Sigma (\delta C_1)^2.$$

As c refers to the point which is the mean of the six wires, $\Sigma \delta c = 0$. For the convenient expression of the last term, let I be the interval in seconds of time from the first wire to the last. Then, for the first wire, $\delta C_1 = -\frac{5}{10} I$; for the second, $\delta C_1 = -\frac{3}{10} I$; for the third, $\delta C_1 = -\frac{1}{10} I$; for the fourth, $\delta C_1 = +\frac{1}{10} I$; for the fifth it is $+\frac{3}{10} I$; for the sixth, $+\frac{5}{10} I$. Hence the equation becomes,

Mean of observed hour-angles in seconds of time =

$$\begin{aligned} & C_1 - \frac{\cot C_1 \cdot 15 \sin 1''}{12} \cdot \frac{70}{100} \times I^2, \\ & = C_1 - \frac{7}{8} \cdot \sin 1'' \times \cot C \times I^2. \end{aligned}$$

Hence the correction to be applied to the mean of the observed hour-angles, in order

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to obtain the true hour-angle corresponding to the zenith distance at the mean of the wires, is:—

$$+ \frac{7}{8} \cdot \sin 1'' \times \cot C \times I^2.$$

If the transit be imperfect, but the wires observed be consecutive, the following corrections will be applicable, being easily deduced from the preceding investigation:—

When three wires are observed, if I_3 be the interval in seconds of time from the first to the third, the correction in seconds of time will be $+ \frac{5}{4} \sin 1'' \times \cot C \times (I_3)^2$.

When four wires are observed, if I_4 be the interval from the first to the fourth, the correction will be $+ \frac{25}{24} \sin 1'' \times \cot C \times (I_4)^2$.

When five wires are observed, if I_5 be the interval from the first to the fifth, the correction will be $+ \frac{15}{16} \sin 1'' \times \cot C \times (I_5)^2$.

If the wires are not consecutive, the corresponding correction will be found, on the same principles, with little difficulty.

This correction will be subtractive from the mean of times when the hour-angle is diminishing, or before the object has passed the meridian, and additive to the mean of times when the object has passed the meridian. A small table of double entry is prepared with arguments C and I , and from this the correction is readily taken.

The *thirteenth* column is occupied by the personal equation (referred to Mr. Dunkin as standard), and this is applied to the mean of wires, corrected as above mentioned, to form the concluded Clock-time in the *fourteenth* column. The *two last* columns require no explanation beyond that in the section of Azimuths.

The *first four* columns on the right-hand side give the readings of the four microscope-micrometers, which are converted into arc by the aid of the numbers given at the bottom of the page, in the same manner as the similar numbers in the section of Azimuths.

When the observer views the graduated face of the vertical circle, the microscopes are seen in the position $\begin{smallmatrix} A & D \\ B & C \end{smallmatrix}$.

When the transits over any number of wires are omitted, the time of transit retained is the mean of the transits actually observed, corrected if necessary for personal equation; but a correction in arc is applied to the circle-reading, corresponding to the interval between the mean of the wires actually observed and the mean of the six wires. Calling the whole system of wires (including both the eye-and-ear and the galvanic wires) in the order in which a star on the West side of the meridian passes them when the Graduated Face of the Vertical Circle is Right, $Q, R, S, T, U, V, W, X, Y, Z$, then the correction to reduce each of the wires to the mean of either system of wires, is:—

INTERVALS OF HORIZONTAL WIRES OF ALTAZIMUTH;
LEVEL CORRECTIONS; BAROMETER.

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For wires used in chronographic observations :—

	"
Wire <i>S</i>	— 61.93
<i>T</i>	— 37.53
<i>U</i>	— 13.72
<i>V</i>	+ 12.92
<i>W</i>	+ 37.76
<i>X</i>	+ 62.53

For wires used in observations by eye and ear :—

	"
Wire <i>Q</i>	— 301.06
<i>R</i>	— 179.94
<i>S</i>	— 61.49
<i>X</i>	+ 62.97
<i>Y</i>	+ 178.52
<i>Z</i>	+ 300.99

These intervals have been used from 1864, August 7.

The Concluded Reading in the *fifth* column is formed; in the instances when the celestial body's transit has been observed over all the wires, by the simple mean of the equivalents for readings of microscope-micrometers (duly corrected for runs); in the instances in which the transits over a part only of the wires are obtained, by applying to the mean of equivalents the correction (stated in the foot-notes) for the difference between the mean of all the wires and the mean of the wires observed; and in observations of the collimator, by applying to the mean of equivalents the entire correction corresponding to the single wire employed.

The four columns from the *sixth* to the *ninth* give the readings of the two ends of the two levels which are parallel to the plane of the Vertical Circle, *E* and *F* being the readings of the two ends of the lower level, and *G* and *H* those of the two ends of the upper level. As, when the Graduated Face is Right, the Circle-Readings increase with the increasing Zenith Distance, and as in the same case the numeration of the levels increases from the end next the object to the end next the observer, it follows that the indication of the levels is in all cases additive to the Circle-Reading; and that the equivalents for the two ends of each level are to be combined additively. For both levels, one division of the scale is assumed to be equal to a second of arc (the zeros of *E* and *G* being 0^{div.}, and those of *F* and *H* being respectively 200^{div.} and 250^{div.}), and then the mean of the four readings is taken to form the Level-Indication in the *tenth* column.

The Barometer, whose reading is contained in the *eleventh* column, is by Simms, with adjustable bag and float: it is placed in a small recess of the dome. Comparisons with the Standard Barometer made between 1863, January 28 and 31, appeared to indicate that the readings of the Altazimuth Barometer require a correction — 0ⁱⁿ.07; this correction has been applied to the readings of the Barometer during the year.

The Thermometer, whose reading is contained in the *twelfth* column, is by Simms: it is placed on the East side of the tower carrying the dome, where its case is carried by long iron rods attached to the brickwork; it is mounted with its bulb inclosed by a double case, which is silvered by electro-plating, allowing a perfectly free passage for the air; it is read from a new window pierced in the eastern side of the Altazimuth observing room. The corrections required for its errors, ascertained by comparison with the Standard Thermometer, are as follows:—

CORRECTION TO ALTAZIMUTH (PORCELAIN) THERMOMETER.

Temperature.	Correction.	Temperature.	Correction.
°	°	°	°
28	+ 0.1	66	+ 0.1
30	0.0	68	+ 0.2
32	0.0	70	+ 0.2
34	0.0	72	+ 0.2
36	— 0.1	74	+ 0.3
38	— 0.1	76	+ 0.2
40	— 0.1	78	+ 0.2
42	— 0.2	80	+ 0.1
44	— 0.2	82	0.0
46	— 0.2	84	0.0
48	— 0.2	86	0.0
50	— 0.1	88	0.0
52	— 0.1	90	+ 0.1
54	— 0.1	92	+ 0.1
56	0.0	94	+ 0.1
58	0.0	96	+ 0.2
60	0.0	98	+ 0.2
62	+ 0.1	100	+ 0.2
64	+ 0.1	102	+ 0.2

An approximate Zenith Distance being obtained by the use of an approximate zenith-point, the refraction in the *thirteenth* column is computed by the use of the tables printed in the Appendix to the Greenwich Observations, 1836, and reprinted (with an addition, including Bessel's supplementary table for Zenith-Distances exceeding 85°) as an Appendix to the Volume for 1853, giving the same results as the tables in the *Tabulæ Regiomontanæ*; with alterations in the mean refractions equivalent to a reduction of the mean refractions of Bessel's Fundamenta, in the proportion of 1: 0.99797. This refraction is always additive to the observed Zenith Distance, and therefore it is added to the Reading of the Vertical Circle when the Graduated Face is Right, and subtracted when it is Left.

By the combination of these various quantities, the Corrected Reading in the *four-*

THERMOMETER, REFRACTION, AND SMALL CORRECTIONS FOR ALTAZIMUTH Z. D.; lxxxv
COMPARISON OF TABULAR AND OBSERVED AZIMUTHS AND ZENITH DISTANCES.

teenth column is formed. It is to be remarked that this Corrected Reading contains implicitly a constant depending on the assumed zeros of the Level-Scales, and equal to the Level-Indication when the axis of azimuthal rotation is vertical. In this respect it differs from the Corrected Reading of the Horizontal Circle, which contains no such constant.

The Zenith-Point, whose value is given at the foot of each page, is obtained by a process which will be explained hereafter: it is sufficient here to state that it also contains implicitly the same constant depending on the assumed zeros of the Level-Scales. The concluded Zenith-Distance therefore in the *fifteenth* column, which is formed by subtracting the Zenith-Point from the Corrected Reading when the Graduated Face is Right, and by subtracting the Corrected Reading from the Zenith-Point when the Graduated Face is Left, is freed from this constant.

In cases wherein both the upper and the lower limb of the Moon have been observed, one limb is usually defective through want of illumination. A correction for this defect is applied, computed by a method analogous to that used for correcting the Zenith Distance of the defective limb of the Moon when observed on the meridian (see page lxi). The corrections for defect of illumination are always mentioned in the notes.

§ 9. *Comparison of Tabular Azimuths and Zenith Distances with Azimuths and Zenith Distances observed*, page [xcvi] to [cxli].

The *three first* columns need no explanation.

The Mean Solar Time in the *fourth* column is formed from the Sidereal Time in the two preceding sections, by the same process as in the formation of Mean Time for the observations of Planets (which will be described hereafter).

The Tabular R.A. of Center in the *fifth* column is thus formed. For stars in the list of the Nautical Almanac, there are applied, to the places given in the Nautical Almanac, corrections fundamentally deduced from the Right Ascensions given in the Greenwich New Seven-year Catalogue of 2760 Stars for the epoch 1864 (see page xxxvii). For the Moon, the Tabular R.A. of Center is formed by interpolating with second differences between the hourly places of the Moon given in the Nautical Almanac, using as argument the Mean Solar Time of the *fourth* column.

The Hour Angle in the *sixth* column is the difference (without respect of sign, but taken less than 180°) between the Tabular R. A. and the Sidereal Time in the two preceding sections. The East or West side of the Meridian is indicated by the letter E or W in the *seventh* column.

The *eighth* column contains the Tabular Geocentric N.P.D. of Center. It is thus formed. For stars, the places in N.P.D. are derived from the same sources as those

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in R.A. For the Moon, the N.P.D. is formed by interpolating with second differences between the hourly places of the Nautical Almanac.

It may be proper here to describe the method which has been adopted since the beginning of 1862 for the computation of Interpolations with second differences, with the view of avoiding all changes of sign. Up to that time the practice had been as follows. If we took from the Ephemeris the values x_1, x_2, x_3 , corresponding to the equidistant times T_1, T_2, T_3 , and if we wished to compute the value of x for the time $T_2 + \tau$ (where τ is expressed by a number whose unit is $T_2 - T_1$ or $T_3 - T_2$, and is always less than ± 1 , and practically always less than $\pm \frac{1}{2}$), we begin by taking the differences, thus :—

		First difference.	Second difference.
T_1	x_1		
		$\Delta' (1)$	
T_2	x_2		$\Delta (2)$
		$\Delta'' (1)$	
T_3	x_3		

Then, forming the coefficients $\frac{1}{2} \{ \Delta' (1) + \Delta'' (1) \}$ and $\frac{1}{2} \Delta (2)$ numerically, the required quantity x is :—

$$x_2 + \frac{1}{2} \{ \Delta' (1) + \Delta'' (1) \} \times \tau + \frac{1}{2} \Delta (2) \times \tau^2.$$

This formula is very conveniently adapted to logarithmic computation, but it is subject to the very serious inconvenience of numerous changes of sign. For all elements, τ and $\Delta (2)$ may be + or — ; for all elements except the Moon's R. A., $\Delta' (1)$ and $\Delta'' (1)$ may be + or —, and may even have different signs.

The formula of interpolation may be varied ; but in every form, without a radical change in the character of the numbers between which the interpolation is to be effected, there will be a great number of changes of sign.

In order to escape these difficulties, the following process has been devised :—

First: although it is usual still to select, for the middle tabular time T_2 , that tabular time which is nearest to the time for which interpolation is required, whether before it or after it, yet, in the formula of interpolation, the adopted tabular number (to which the results of the interpolation-formula are added) is the first of the three, or x_1 . Call the time for which the interpolation is made, $T_1 + t$. It will be easily seen that the formula for x now is,

$$x_1 + \left\{ \Delta' (1) - \frac{1}{2} \Delta (2) \right\} \times t + \frac{1}{2} \Delta (2) \times t^2.$$

As t is the measure of the interval by which the time for interpolation follows T_1 , t is always positive, and therefore in this formula the coefficients depending on the time are always positive.

Secondly ; the tabular quantities x_2, x_3 , before further use is made of them, are

increased by constants which will in all cases make the first difference and the second difference positive. Thus the numbers whose differences we actually take are:—

For Moon's R. A.	For Moon's N. P. D.
x_1	x_1
$x_2 + 40^s$	$x_2 + 20'$
$x_3 + 90^s$	$x_3 + 41'$

For Moon's Parallax and Semidiameter.
x_1
$x_2 + 40''$
$x_3 + 90''$

Then every operation of forming differences is a numerical subtraction of an upper number from a lower, every number so formed is positive, every number to be substituted in the last formula of interpolation is positive, and every operation of connexion of results is a numerical addition.

But, in this process, we have introduced into our final sum a quantity which depends upon our additive numbers (40 and 90, or 20 and 41), which quantity must now be subtracted. Taking the differences of these,

0				0		
	40				20	
40		10	or	20		1
	50				21	
90				41		

it will be seen that we have introduced the quantity,

$$0 + 35 \times t + 5 \times t^2 \quad \text{or} \quad 0 + \frac{39}{2} \times t + \frac{1}{2} \times t^2.$$

Tables of these quantities (called Table T^* and Table T^{**}) are computed with the argument t ; and from these tables T^* or T^{**} is taken (according to the series of additive constants which has been used), and is applied, in all cases subtractively, to the number produced by the interpolation-formula.

Great numbers of errors produced by changes of sign are avoided by this method of interpolation.

It will be remarked that, for computing the Moon's R.A., in which $\Delta' (1)$ and $\Delta'' (1)$ are always positive, there is no theoretical necessity for making any addition to x_2 . The same additions, however, are made for the Moon's R.A. as for other elements, because the trouble of doing so is inconsiderable, and it dispenses with the necessity of a special table for the Moon's R.A.

The *ninth* column contains the correction to the Moon's N.P.D., necessary for referring her place to the point of the Earth's axis at which the normal drawn from Greenwich meets the axis. It is thus investigated: Let a and b be the semi-major and semi-minor

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axes of the terrestrial ellipse, in the proportion of 300 to 299; x and y the co-ordinates parallel to them, their equation being $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$; then the subnormal upon the minor axis $= -x \frac{dx}{dy} = \frac{a^2}{b^2} y$, and the part of this included between the origin of co-ordinates and the foot of the normal, is $\frac{a^2 - b^2}{b^2} y$. To find y , we remark that the tangent of the astronomical latitude of Greenwich, or $\tan l = -\frac{dx}{dy} = \frac{a^2}{b^2} \cdot \frac{y}{x} = \frac{a}{b} \cdot \frac{y}{\sqrt{(b^2 - y^2)}}$; whence $y = \frac{b^2}{\sqrt{b^2 + a^2 \cotan^2 l}}$; and the distance from the center of the spheroid to the foot of the normal, measured along the Earth's axis, is $\frac{a^2 - b^2}{\sqrt{b^2 + a^2 \cotan^2 l}}$; or, in parts of the semi-major axis, it is $\frac{a^2 - b^2}{a \sqrt{b^2 + a^2 \cotan^2 l}}$. The logarithm of this quantity is 7.7174788.

Now if, from the Earth's center, we draw a perpendicular to the Moon's radius vector reaching the line drawn from the Moon to the foot of the normal, the length of that perpendicular will sensibly be, $a \times [7.7174788] \times \sin \text{Moon's N.P.D.}$; the angle which it subtends as seen from the Moon will be $\frac{a}{\text{Moon's distance}} \times [7.7174788] \times \sin \text{Moon's N.P.D.} = [7.7174788] \times \sin \text{Moon's hor. equat. parallax} \times \sin \text{Moon's N.P.D.}$; and the value of this in seconds of arc will be $[3.0319039] \times \sin \text{Moon's hor. eq. par.} \times \sin \text{Moon's N.P.D.}$; or $[7.7174788] \times \text{seconds of Moon's hor. eq. par.} \times \sin \text{Moon's N.P.D.}$. In this manner the number in the ninth column has been computed. It is always subtractive.

The assumed colatitude $38^\circ.31'.21''.89$ is deduced from observations with the Transit-Circle, corrected by the quantity $+0''.29$ for the difference of latitude of the positions of the two instruments as found by measurement on the plan of the Observatory before mentioned.

With the Hour Angle unaltered, and the N.P.D. altered (for the Moon) by the correction just described, and with the colatitude $38^\circ.31'.21''.89$; the Tabular Azimuth in the *tenth* column of the left-hand page, and the Tabular Normal-centric Zenith Distance in the *fifth* column of the right-hand page, are computed by the following formulæ:—

$$\text{Log tan } \alpha = \text{log cos hour-angle} + \text{log tan Normal-centric N.P.D.}$$

$$\beta = \alpha - \text{colatitude.}$$

$$\text{Log tan zenithal angle} = \text{log sin } \alpha + \text{log tan hour-angle} - \text{log sin } \beta.$$

$$\text{Log cotan zen. dist.} = \text{log cotan } \beta + \text{log cos zenithal angle.}$$

SMALL CORRECTIONS TO TABULAR PLACES FOR ALTAZIMUTH OBSERVATIONS. lxxxix

As a check upon the accuracy of a large part of this computation, the terms of the following equation are computed numerically:—

$\log \sin \text{zenithal angle} + \log \sin \text{zen. dist.} = \log \sin \text{hour-angle} + \log \sin \text{N.P.D.}$; and, if the numbers are not strictly equal, the computation is again examined.

The correction to Azimuth for Moon's Semidiameter, in the *first* column of the right-hand page, is thus computed. The semidiameter is interpolated with second differences from the Nautical Almanac, and then increased by $0''.49$. (See Introduction to Greenwich Observations, 1863, pages lxxxvii and lxxxviii.) There is then applied the correction required for the difference between the distance of the Moon from the foot of the normal and her distance from the Earth's center. The former distance is greater than the latter by $a \times [7.71748] \times \cos \text{Moon's N.P.D.}$, and therefore her angular semidiameter is diminished in the proportion of Moon's distance to Moon's distance $- a \times [7.71748] \times \cos \text{Moon's N.P.D.}$, or $1 : 1 - \sin \text{hor. eq. par.} \times [7.71748] \times \cos \text{Moon's N.P.D.}$: or, using the mean parallax $57'$, the proportion is $1 : 1 - [5.93708] \times \cos \text{Moon's N.P.D.}$. The correction required is taken out from a small table. The Correction to Azimuth is computed by the formula

$\frac{\text{Corrected semidiameter}}{\text{Sine Normal-centric Zenith Distance}}$; the term depending on the difference between the sine of semidiameter and the arc being insensible.

By application of this correction to the Tabular Azimuth in the last column of the left-hand page, the Tabular Azimuth of Limb in the *second* column of the right-hand page is formed. This Azimuth is necessarily the same at the place of observation as at the foot of the normal, for which the computation has been made.

The seconds of Observed Azimuth in the *third* column are transcribed from the section of Azimuths: and the apparent error of Tabular Azimuth in the *fourth* column is formed by subtracting the Observed Azimuth from the Tabular Azimuth in the last column of the left-hand page (for a star), or from that in the second column of the right-hand page (for the Moon).

The computation of the *fifth* column has already been mentioned.

The Normal-centric Semidiameter for the Zenith Distances in the *sixth* column is interpolated from the Nautical Almanac, increased by $1''.01$ (see Introduction, 1863, as above), and corrected for reduction to the foot of the Normal. The last correction is $-930'' \times [5.93708] \times \cos \text{Moon's N.P.D.}$, and is readily tabulated.

For computation of the Parallax; in the first place, the horizontal equatoreal parallax is interpolated from the Nautical Almanac without alteration. It is then necessary to deduce from this the parallax referred to the foot of the Normal (the Moon's center having been referred to that point): and for this purpose, first, the Equatoreal Horizontal Parallax must be corrected so as to make the Horizontal Parallax depend on the Normal-centric radius, and must therefore be multiplied by $\frac{\text{Normal-centric Radius of Greenwich}}{\text{Earth's semi-major axis}}$. Using the

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same notation as before, the factor is found to be $= \frac{1}{a \sin l} \cdot \frac{a^2}{b^2} y = \frac{a}{\sqrt{b^2 \sin^2 l + a^2 \cos^2 l}}$; the logarithm of which is 0.0008851. Secondly, it must be made to depend on the Moon's distance from the foot of the normal, and for this must therefore be multiplied by $1 - [5.93708] \times \cos \text{Moon's N. P. D.}$. These two corrections are embodied in one logarithmic table with argument N. P. D., the number for 60° being 0.0008664, that for 90° being 0.0008851, and that for 120° being 0.0009037. By the addition of this logarithm to the logarithm of the seconds of parallax (corrected as above) which is interpolated from the Nautical Almanac with second differences, the logarithm in the *seventh* column is formed.

The parallax in the *eighth* column is computed by the formula, Normal-centric horizontal parallax $\times$ sine of observed zenith distance of limb + small correction. The observed zenith distance of limb is taken from the section of Zenith Distances. The small correction is the sum of two terms, namely, $-\frac{P^2}{6} \sin^2 1'' \cdot \sin(\text{zen. dist.}) \cos^2(\text{zen. dist.})$ (which gives the correction for the error produced by using the parallax instead of its sine, P being $= 3420'' =$ number of seconds in Moon's mean parallax), and $\sin \text{zen. dist.} \times \text{Airy's correction}$ as given in the section of Occultations. The table of corrections used is given in page lxiv.

By application of this parallax, the Tabular Apparent Zenith Distance of Limb in the *ninth* column is formed; the numbers in the *tenth* column are transcribed from the section of Zenith Distance; and the numbers in the *eleventh* are formed by subtracting those in the tenth from those in the ninth column.

§ 10. *Computation of Clock Errors and Instrumental Errors for the Observations with the Altazimuth; and of Errors of the Moon's Tabular R. A. and N. P. D., page [cxliii] to [clxvi].*

In general, the times of the transits taken with the Altazimuth by means of the method of galvanic contact are those of the Transit-Clock (Hardy), and no comparisons of clocks are necessary. The errors of the Transit-Clock are obtained for the time of each observation, and, after correction by $-0^s.03$ for difference of longitude, and for personal equation, are applied to the registered times of transit, to form the sidereal time. When, however, through failure of the galvanic apparatus, it is necessary to observe by eye and ear, the comparisons of the Transit-Clock and the Clock (Graham 1) of the South Dome, used with the Altazimuth, are usually made by means of a solar chronometer, whose name is mentioned. The chronometer is brought close to each of the clocks, and the time of accurate coincidence of beats is noted; the chronometer-interval between the comparisons, which is expressed as an interval of Solar Time, is converted into an interval of Sidereal Time; and the sidereal time at the

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comparison with the transit-clock, being found by correcting the transit-clock-time for error and rate of the transit-clock, for personal equation, and also for difference of longitude, the sidereal time at the comparison with the South Dome Clock is found, and thus the Error of that Clock is ascertained. From the successive Errors, rates of the Clock are deduced; and the Errors applicable to the observations, and which are given in the sections of Azimuth and Zenith Distance, are computed.

The instrumental constants of correction in Azimuth are thus investigated:—Let w be the correction to the computed tabular azimuth of a high star, depending upon the error in the star's assumed place: w will be an exceedingly small quantity, and will not sensibly vary between the observations made in reversed positions of the instrument. Let x be the constant of correction for error of collimation, taken with that sign which corresponds to the position of the instrument with Graduated Face Right; y the level-indication corresponding to horizontal position of the Horizontal Axis; and z the Zero of Azimuth. Also, let O_r and O_l be the Concluded Readings of Horizontal Circle from observations of a high star, with Face Right and Face Left; C_r and C_l the corresponding computed azimuths; L_r and L_l the level indications; D_r and D_l the zenith distances; and let $o_r, o_l, c_r, c_l, l_r, l_l, d_r, d_l$ be the similar quantities for a low star. Then the true azimuth of the high star deduced from observation, Face Right, is

$$O_r + x \cdot \text{cosecant } D_r + (L_r - y) \cdot \text{cotangent } D_r - z;$$

the computed azimuth corrected is

$$C_r + w;$$

hence this observation gives the equation

$$O_r + L_r \cdot \cotan D_r - C_r = -x \cdot \text{cosec } D_r + y \cdot \cotan D_r + z + w.$$

The true azimuth determined from observation, Face Left, is

$$O_l - x \cdot \text{cosecant } D_l - (L_l - y) \cdot \text{cotangent } D_l - z;$$

and this observation therefore gives the equation,

$$O_l - L_l \cdot \cotan D_l - C_l = +x \cdot \text{cosec } D_l - y \cdot \cotan D_l + z + w.$$

Subtracting the first equation from the second,

$$(O_l - L_l \cdot \cotan D_l - C_l) - (O_r + L_r \cdot \cotan D_r - C_r) = x \cdot (\text{cosec } D_l + \text{cosec } D_r) - y \cdot (\cotan D_l + \cotan D_r).$$

$$\text{Or } \frac{(O_l - L_l \cdot \cotan D_l - C_l) - (O_r + L_r \cdot \cotan D_r - C_r)}{\cotan D_l + \cotan D_r} = x \times \frac{\text{cosec } D_l + \text{cosec } D_r}{\cotan D_l + \cotan D_r} - y.$$

A similar treatment of the observations of the low star gives

$$\frac{(o_l - l_l \cdot \cotan d_l - c_l) - (o_r + l_r \cdot \cotan d_r - c_r)}{\cotan d_l + \cotan d_r} = x \times \frac{\text{cosec } d_l + \text{cosec } d_r}{\cotan d_l + \cotan d_r} - y.$$

Subtracting the former from the latter, x is given by a simple equation.

It has been already stated that, in 1850, a Collimator or Reversed Telescope was mounted, admitting of accurate observation with the telescope of the Altazimuth, and requiring for its observation that the telescope be directed at an angle of $12^\circ.18'$ below

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the horizon. It is evident that, for the instrumental adjustments, the Collimator may be used as an immovable star, and that, considered as the low star in the preceding investigation, its position is exceedingly favourable. The preceding formulæ apply with no other changes than the following: for d_r and d_l put $102^\circ.18'$, and for c_r and c_l put the same symbol c . It is by this use of the Collimator in combination with a high star that the error of collimation has been found throughout the year 1870.

The construction of the instrument gives us reason to believe that the error of collimation is probably less variable than any other instrumental constant; it is usual, however, to make a new determination of the value of this element at the end of every lunation, founded on the observations of that lunation.

Every set of four azimuths like those above will give a value of y ; implying that, for that determination, the varying or slightly erroneous value of x , deduced from that individual combination, has been employed in the preliminary correction for collimation. But as, on account of the steadiness of collimation, it appears better to use a mean value of x throughout, a fresh investigation of y is afterwards made from every pair of observations. Thus, let O'_r , O'_l , be the concluded readings of horizontal circle corrected for the adopted error of collimation. Then the first equations are,

$$O'_r + L_r \cdot \cotan D_r - C_r = +y \cdot \cotan D_r + z + w,$$

$$O'_l - L_l \cdot \cotan D_l - C_l = -y \cdot \cotan D_l + z + w.$$

$$\text{Whence } \frac{(O'_r + L_r \cdot \cotan D_r - C_r) - (O'_l - L_l \cdot \cotan D_l - C_l)}{\cotan D_r + \cotan D_l} = y.$$

Any one star, or the collimator, suffices for this determination; a high star, however, is best; and high stars have been exclusively used throughout the year.

The number y , it is to be observed, corresponds strictly with the horizontal position of the Horizontal Axis of the Vertical Circle, and has no relation whatever to the Level-Zero corresponding to a vertical position of the Vertical Axis of Azimuthal Rotation: except that, supposing the workmanship of the vertical pivots to be perfectly good, and the position of the horizontal axis in its Y's to be invariable, there ought to be a constant difference between them. The latter Level-Zero would be the mean of the level-indications in opposite positions of the instrument: and it would be found with sufficient accuracy for this purpose by taking the mean of the level-indications for positions used in successive observations of the same object (though the instrument was not exactly reversed). The following are the results of comparisons of these Level-Zeros since the erection of the Altazimuth. By inspection of these results, it will be seen that the relative difference between the two zeros had been steadily increasing, the pivot on the same side as the Graduated Face of the Vertical-Circle being too high. This difference may have arisen from a wear of one of the horizontal pivots, or in the bearing of a horizontal pivot, or in one of the vertical pivots. The inconvenience produced by large numerical corrections on account of this discordance became at length so great that an instrumental correction of the error was attempted in 1859, March, by filing away the surfaces of the Y of the pivot on the same side as the Graduated Face.

LEVEL ZEROS AND ZEROS OF AZIMUTH FOR ALTAZIMUTH OBSERVATIONS.

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EXCESS OF THE LEVEL INDICATION FOR HORIZONTAL POSITION OF THE AXIS OF THE VERTICAL CIRCLE ABOVE THE LEVEL INDICATION FOR VERTICAL POSITION OF THE AXIS OF REVOLUTION, SINCE THE ERECTION OF THE ALTAZIMUTH.

Year.	Mean Excess.	Year.	Mean Excess.
1848	+ 1'13	1860	— 4'91
1849	+ 2'33	1861	— 5'48
1850	+ 6'67	1862	— 6'24
1851	+ 8'75	1863	— 5'39
1852	+ 10'50	1864	— 5'01
1853	+ 11'36	1865	— 4'56
1854	+ 11'71	1866	— 5'07
1855	+ 12'51	1867	— 4'30
1856	+ 13'23	1868	— 5'94
1857	+ 13'59	1869	— 5'06
1858	+ 13'70	1870	— 3'28
1859 { Jan. & Feb.	+ 13'75		
Mar. to Dec.	— 4'23		

The comparison of the Observed Circle-Reading for a star, corrected for Collimation and Level, with the computed Azimuth for the same star, gives the Zero of Azimuth. Since the time of the establishment of the instrument, this Zero has been subject to greater and more sudden variations than any other element of reduction; and great pains have been taken to discover the source of the instability. In the Introduction to the volume for 1850 will be found an investigation, based on the Theory of Probabilities, for determining the relative stability of the Azimuthal Circle and of the Collimator, and the Error due to the transmission of time from the Transit-Instrument, on the assumption that there is no movement of the ground which carries both the Circle and the Collimator. From this investigation it seemed to be established that the Azimuthal Circle was the most stable part of the instrument, that the fluctuations of the position of the Collimators were somewhat greater, but that the principal source of errors was in the comparison of the circle-reading with the azimuth computed from the time-observation; and, in consequence, it became the practice to rely solely on the stability of the Azimuthal Circle, and, for a limited period, to use the same Zero of Azimuth, determined from the mean of all the separate determinations from star-observations on every day during that period, without special reference to the star-observations of the day of observation. In later years, however, the propriety of this proceeding has become questionable from two considerations; the first of which is that, since the introduction of the galvanic registration of transits, in which one source of error arising from the comparison of clocks is completely removed, the stability of the Zero of Azimuth does not seem at all to have improved; and the second, that there is now great reason to doubt the immobility of the ground carrying the Collimator and the Circle. From an investigation of the changes of azimuth of the Transit-Circle, it seems certain that the ground carrying that instrument is subject to frequent and sudden shifts, and a somewhat similar investigation made for the Altazimuth seems to prove instability of the ground on which it stands. In both instances, the changes appear to be connected with sudden changes of atmospheric temperature. Under these

circumstances it has been thought best during the year 1870 to use, for each day's observations, the Zero of Azimuth determined by the star-observations of that day, whenever the changes appear greater than would warrant the combination with other days.

In the Zenith Distances, the only instrumental constant deduced from observation is the Zenith Point (including so much of the level-indication as corresponds to a vertical position of the axis of azimuthal rotation). In two successive observations of the same star, Face Right and Face Left, let O_r and O_l be the observed circle-readings of the vertical circle corrected for level; C_r and C_l the computed Zenith Distances; e the possible error, which will be sensibly the same for both; Z the Zenith Point. Then we have

$$\begin{aligned} O_r - Z &= \text{true Zenith Distance with Face Right} = C_r + e \\ Z - O_l &= \text{true Zenith Distance with Face Left} = C_l + e \end{aligned}$$

Subtracting the first from the second,

$$\begin{aligned} 2Z - (O_r + O_l) &= C_l - C_r, \\ Z &= \frac{(O_r + O_l) - (C_r - C_l)}{2} \end{aligned}$$

When, instead of a star, the Collimator is used, C_r and C_l are necessarily equal, and the formula is simply,

$$Z = \frac{O_r + O_l}{2}.$$

The only point which it is now necessary to explain is the method of investigating the Errors of the Moon's Tabular Place in Right Ascension and North Polar Distance. The following method is based upon the assumption that, although the Moon's positions in respect of the meridian and horizon of Greenwich are very different at the different observations made in the same evening, and although the Errors of Tabular Azimuth and the Errors of Tabular Zenith Distance will vary much in the course of an evening, yet the Moon's North Polar Distance will not vary much, and the Errors of Tabular Right Ascension and Tabular North Polar Distance may be assumed to be invariable. It is also necessary to take into account, in arranging the form of calculation, that the Error of Tabular Azimuth and the Error of Tabular Zenith Distance are never observed at the same time.

Let $\delta. R. A.$, $\delta. N. P. D.$, $\delta. A.$, $\delta. Z$, be the Errors of Tabular Right Ascension (expressed in arc), North Polar Distance, Azimuth, and Zenith Distance, in any observation: and (supposing the Moon to be west of the meridian) let S be the angle at the Moon made by the great circles drawn to the Pole and to the Zenith. Then we have,

$$\begin{aligned} \delta. Z &= -\sin S \cdot \sin N. P. D. \times \delta. R. A. + \cos S \times \delta. N. P. D., \\ \delta. A &= -\frac{\cos S}{\sin Z} \cdot \sin N. P. D. \times \delta. R. A. - \frac{\sin S}{\sin Z} \times \delta. N. P. D. \end{aligned}$$

Let $\sin S = p$, $\cos S = q$, $\frac{\cos S}{\sin Z} = r$, $\frac{\sin S}{\sin Z} = s$; then

$$\begin{aligned} \delta. Z &= -p \cdot \sin N. P. D. \times \delta. R. A. + q \times \delta. N. P. D., \\ \delta. A &= -r \cdot \sin N. P. D. \times \delta. R. A. - s \times \delta. N. P. D. \end{aligned}$$

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and, taking the sum of a series of equations in each element, and observing that p, q, r, s , will vary considerably during the observations,

$$\Sigma (\delta. Z) = -\delta. R.A. \times \sin N.P.D. \times \Sigma (p) + \delta. N.P.D. \times \Sigma (q),$$

$$\Sigma (\delta. A) = -\delta. R.A. \times \sin N.P.D. \times \Sigma (r) - \delta. N.P.D. \times \Sigma (s).$$

By solution of these equations,

$$\delta. R.A. = \frac{\Sigma (s) \cdot \Sigma (\delta. Z) + \Sigma (q) \cdot \Sigma (\delta. A)}{-\sin N.P.D. \cdot \{\Sigma (p) \cdot \Sigma (s) + \Sigma (q) \cdot \Sigma (r)\}},$$

$$\delta. N.P.D. = \frac{\Sigma (r) \cdot \Sigma (\delta. Z) - \Sigma (p) \cdot \Sigma (\delta. A)}{\Sigma (p) \cdot \Sigma (s) + \Sigma (q) \cdot \Sigma (r)}.$$

The expression for $\delta. R.A.$ must be divided by 15 to give the error of Tabular Right Ascension in seconds of time.

A table of double entry, appended to the Introduction to the *Greenwich Observations* of 1854, is prepared, from which the values of p, q, r, s , are taken out at sight, with arguments Hour Angle and North Polar Distance of the Moon; and then the calculation is made by means of these formulæ.

§ 11. *Catalogue of the Mean Places of Stars observed in the Year 1870; and New Constants for Stars in the Catalogue, not observed in preceding Years;*
 page 1 to 17.

The right ascensions in the catalogue are the means of all the separate determinations of the mean right ascension of each star, excluding only those which are contained in brackets. For the Nautical Almanac Stars, the annual variations in right ascension are taken from the Nautical Almanac. For all other stars, the geometrical precessions are computed independently, with the elements given by Professor C. A. F. Peters in the *Numerus Constans Nutationis*: the annual variations in right ascension set down are the precessions thus computed, affected with proper motions derived in the order of preference from Mr. Main's or Mr. Stone's papers in the *Mem. R. Ast. Soc.*, or from the *British Association Catalogue*.

The North Polar Distances in the catalogue are the means of the daily results, affected with the corrections for flexure and errors of division of the Transit-Circle, and for discordance of direct and reflexion results, as has been previously explained. The adopted seconds of N.P.D. are found by taking the means of the groups of direct and reflexion observations, giving to each a weight proportional to its number of observations. With regard to circumpolar stars, these rules have been followed:— For stars whose N.P.D. does not exceed 15° , the observations above and below the pole are considered equally good; from N.P.D. 15° to N.P.D. 36° , those below have the weight $\frac{2}{3}$ for each observation; from N.P.D. 36° to N.P.D. 41° , those below have the weight $\frac{1}{3}$; beyond 41° N.P.D., the observations are not combined. The annual variations in North Polar Distance are formed in the same manner as the annual variations in right ascension, above.

The nomenclature of the stars is identical with that described at page xxvii.

The new star-constants require no further explanation than what is given at pages xlix and lxxv. They are printed for the sake of enabling any person, using the

Greenwich Observations, to employ the same method of reduction for all the stars found in those volumes.

§ 12. *Horizontal and Vertical Diameters, Right Ascensions, and North Polar Distances, of the Sun, Moon, and Planets ; deduced from the Observations, and compared with the Nautical Almanac and other Ephemerides : with the inferred position of the Ecliptic, the Geocentric Errors of the Sun, Moon, and Planets, in Longitude and Ecliptic Polar Distance, and the Equations between the Geocentric Errors of the Planets and the Heliocentric Errors of the Earth and Planets,* page 20 to 51.

The duration of the passage of the Sun's diameter is found by subtracting the clock-time of transit of the first limb from that of the second limb in the *Transits observed*, &c., without any further correction. The tabular duration is found by doubling the time of the passage of the semidiameter given in the Nautical Almanac. The excess of the latter above the former is set down as the apparent error of the Nautical Almanac. The mean of 106 measures of the value of this error is $+0^{\circ}.12$, agreeing nearly with the results of the thirteen preceding years.

The Sun's vertical diameter is found by subtracting the zenith distance of the north limb, corrected for refraction and parallax, from that of the south limb similarly corrected. The tabular diameter is found by doubling the semidiameter of the Nautical Almanac. The excess of the latter above the former is set down as the error of the Nautical Almanac, and the mean of 119 measures of the value of this error is $+1''.29$.

For the duration of the passage of the Moon's diameter, a correction is necessary (negative to the time of passage of the first limb, or positive to that of the second limb, accordingly as the Moon had passed or had not passed the opposition in right ascension), thus investigated:—The excess or defect of the difference of R.A. of the Sun and Moon from 12^h , at the time of the Moon's transit, being found, and expressed in arc, this quantity is multiplied by the cosine of the Sun's declination, and thus an arc θ is obtained which represents the angle, upon the Moon's surface, of the unenlightened part of the disk (with respect to right ascension); the correction required is, duration of passage of semidiameter $\times$ versed sine θ . No observations, however, have been made of the duration of passage of Moon's diameter in 1870.

The Moon's vertical diameter is found in the same manner as that of the Sun (the correction for defective illumination having been already applied, see page lxi). The mean of five determinations made in 1870 is $-0''.36$.

From a comparison of the observed vertical diameters with the tabular diameters of the Moon, made from the erection of the Transit-Circle, to the end of 1863 (see 1863, Introduction, page lxxxvii) it appears that Hansen's semidiameter requires to be increased by $+0''.18$, in order to represent the observations of diameter made with the Transit-Circle.

From a similar comparison of the observations made with the Altazimuth, from

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1848 to 1863, (Introduction, 1863, pages lxxxvii and lxxxviii), it appears that the required corrections to the Nautical Almanac semidiameters (Hansen's) are,—

+ 0".49 for azimuthal observations.

+ 1".01 for zenithal observations.

For the planets, the duration of passage of diameter is found by subtracting the clock-time of transit of the first limb from that of the second limb in the *Transits observed*: no correction for defect of illumination having been necessary, except for Mars, for which the amount of correction is stated in the notes.

The vertical diameters of Mercury, Venus and Mars are found by subtracting the N.P.D. of the north limb from that of the south limb, after the correction for defective illumination has been applied, as explained at page lxii. The vertical diameters of the other planets are obtained in a similar way, excepting that there is no correction for defective illumination.

The Mean Solar Time is found, in all cases, from the Right Ascension or Sidereal Time, by adding together the Mean Solar Time at the transit of the first point of Aries next preceding, and the equivalents in Mean Solar Time for the hours, minutes, and seconds of Sidereal Time: the whole of these numbers being taken from the Nautical Almanac. In practice, this operation is made a little easier by putting the addition in the following form:—

1. Sidereal Time.
2. Mean Solar Time of preceding Transit of first point of Aries diminished by 4^m.
3. 3^m. 47'.00 — hours of Sid. Time + solar equiv. for hours.
4. 10'.00 — minutes of Sid. Time + solar equiv. for minutes.
5. 3".00 — seconds of Sid. Time + solar equiv. for seconds.

Small tables of the 3rd, 4th, and 5th quantities are prepared (see Appendix to Observations, 1837, Table No. IV.), and the operation is then very simple, consisting entirely of addition, with few figures, and no interpolation.

In the year 1870 there are very few instances in which only one element of the Sun or a planet has been observed. In any case where the North Polar Distance has been observed without the corresponding Right Ascension, the Right Ascension at Transit (for the calculation of the Mean Solar Time) is taken from the Nautical Almanac for the Sun and for Planets included in that work; and from other Ephemerides, for Planets not included in the Nautical Almanac; but in all cases as near an approximation as possible is made to the correct Right Ascension, by the application of corrections derived from neighbouring observations.

The Right Ascensions of the Sun's center are generally the means of those deduced from the observations of the two limbs; but, when one limb only has been observed, the R. A. of the center is deduced from that of the limb, by application of the duration of transit of semidiameter given in the Nautical Almanac, corrected by —0".04. The Right Ascensions are transcribed from those in the *Transits observed* without alteration, except that, when necessary, the personal equation is applied, as mentioned in a former part of this Introduction (page xlviii).

The North Polar Distances of the Sun are taken from the Section of *North Polar*
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Distances, &c., the correction for discordance of direct and reflexion results being applied. The Tabular Right Ascensions and North Polar Distances are taken without correction from the Nautical Almanac.

The observed Right Ascensions of the Moon's Center are taken from the *Transits observed*, corrected, when necessary, for personal equation, and also for the Moon's motion in R.A. during the passage from the mean of wires to the true meridian. When both limbs of the Moon are observed, the correction for defective illumination (page xcvi) is first applied to the proper limb, and the mean of the two is then taken without any farther alteration.

The Tabular Right Ascension of the Center of the Moon is found by applying to the Right Ascension of the limb (given in the section *Moon-culminating Stars* of the Nautical Almanac) the sidereal duration of passage of semidiameter, which is given in the same section of the Nautical Almanac.

The observed North Polar Distances of the Moon's Center are taken from the section of *Zenith Distances observed, &c.*, corrected solely for the values of $\frac{1}{2}(R-D)$. The motion in N.P.D. during the passage from the mean of wires to the true meridian has been applied when it amounted to $0''\cdot05$.

The Tabular North Polar Distances of the Moon's Center are taken from the section *Moon-culminating Stars* of the Nautical Almanac.

For all the planets, the Right Ascensions are extracted from the twentieth column of *Transits observed, &c.*, with no alteration, except for personal equation when necessary: the North Polar Distances are taken from the last column in the upper part of the page of the *Zenith Distances observed, &c.*, corrected for the values of $\frac{1}{2}(R-D)$, as has been previously explained. The tabular places are taken from the Nautical Almanac, for such planets as are given in that work and its appendixes. For Clotho the tabular places are taken from the *Astronomische Nachrichten*, No. 1803. For all others the tabular places are taken from the *Berliner Jahrbuch*, 1872.

In this section will be found Observations of the Asteroids made at the Imperial Observatory, Paris. The results are distinguished by the letter P.

The investigation of the position of the Ecliptic is conducted in the same manner as in preceding Volumes from the year 1836. The mean of all the errors in each month, for R.A. and for N.P.D., is supposed to be the error for the day which is nearest to the mean of all the days of observation. When the same day is not found for R.A. and for N.P.D., an alteration of a unit or more has sometimes been made. From these, the error in the Ecliptic Polar Distance is obtained by means of the factors R and S in the tables forming the second part of the Appendix to the *Greenwich Observations*, 1836. Supposing these errors to arise from an erroneous position of the ecliptic assumed in the Nautical Almanac, they may be expressed by the formula $x \times \cos \odot \text{ longitude} + y \times \sin \odot \text{ longitude} + z$. For convenience, the weight attributed to each monthly equation is so altered that the sums of those in opposite quarters of the year are equal. The rest of the process needs no explanation.

OBSERVED R.A. AND N.P.D. OF SUN, MOON, AND PLANETS; ECLIPTIC INVESTIGATION; xcix
GEOCENTRIC AND HELIOCENTRIC ERRORS OF THE PLANETS.

For the *Mean Errors of the Tabular Geocentric Places of the Sun and Planets*, the observations have been collected into groups rarely exceeding a month in duration, and the mean of all the errors in each group, for R.A. and for N.P.D., is supposed to be the error for the day which is nearest to the mean of all the days of observation in the group, an alteration of a unit or more being sometimes made, in order to refer R.A. and N.P.D. to the same day. The Errors in longitude and E.P.D. are formed by the use of the numbers P, Q, R, S, in the Appendix to the *Greenwich Observations*, 1836. For any of the older small planets, whose latitude exceeds the limits of the Tables, the longitude and E.P.D. are computed, 1st, from the R.A. and N.P.D. of the Nautical Almanac; 2nd, from these quantities affected with the Errors in R.A. and N.P.D.; and the difference between these results gives the Errors in Longitude and E.P.D.

For the *Errors in the Tabular Heliocentric Places of the Planets*, the following formulæ are used.

For the small planets, Ceres, Pallas, Juno, Vesta, and Astræa,

Let R = radius vector of planet, L = planet's heliocentric longitude,
 Δ = planet's distance from Earth, λ = planet's geocentric longitude,
 r = Earth's radius vector, l = Earth's heliocentric longitude.

Then,

$$\begin{aligned} \text{Error of geoc. long.} &= \frac{R \times \cos \text{hel. lat.} \times \cos (\lambda - L)}{\Delta \times \cos \text{geoc. lat.}} \times \text{error of hel. long.} \\ &\quad - \frac{\sin (\lambda - L)}{\Delta \times \cos \text{geoc. lat.} \times \sin 1''} \times \text{error of projection of planet's radius vector.} \\ \text{Error of Hel. E.P.D.} &= \frac{\Delta \times \cos \text{hel. lat.}}{R \times \cos \text{geoc. lat.}} \times \text{error of geocent. E.P.D.} \\ &\quad - \sin \text{hel. lat.} \times \cos \text{hel. lat.} \times \tan (\lambda - L) \times \text{error of geocent. long.} \\ &\quad - \frac{r \times \tan \text{geoc. lat.} \times \cos (L - l)}{R^2 \cos (\lambda - L) \times \sin 1''} \times \text{error of projection of planet's radius vector.} \end{aligned}$$

For the other planets, the following are used:—

$$\begin{aligned} \text{Error of geocent. long.} &= \frac{R \times \cos (\lambda - L)}{\Delta} \times \text{error of planet's heliocentric longitude} \\ &\quad - \frac{\sin (\lambda - L)}{\Delta \times \sin 1''} \times \text{error of projection of planet's radius vector} \\ &\quad - \frac{r \times \cos (\lambda - l)}{\Delta} \times \text{error of Earth's heliocentric longitude} \\ &\quad + \frac{\sin (\lambda - l)}{\Delta \times \sin 1''} \times \text{error of Earth's radius vector.} \\ \text{Error of Hel. E.P.D.} &= \frac{\Delta}{R} \times \text{error of geocen. E.P.D.} \end{aligned}$$

In the expressions above, different quantities are neglected for the small planets and for the other planets. For the small planets, the latitude cannot be neglected in any part of the expressions; while, at the same time, their errors in general are so large that, in comparison with them, the Earth may be supposed to move exactly in the orbit assigned by the tables. For the other planets, the latitude may be neglected in the formula; but it appears proper to retain the errors of the Earth's place, as probably comparable in magnitude to those of the planets.

It is to be remarked that, in the column of *Extent of Group*, the day is given which answers to that under which the observations may be found in the sections of *Transits*

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observed, and *Observations of Zenith Distance*: but in the column of *Mean Day*, the day is given whose noon is nearest to the time of observation, or to the mean of times of observation.

The errors of Tabular Longitude and Ecliptic Polar Distance of the Moon are deduced from the Errors of Tabular Right Ascension and North Polar Distance by the use of the numbers, P, Q, R, S, for all the meridian observations as well as for the observations made with the Altazimuth. For the Altazimuth, the Errors of Tabular R.A. and N.P.D. are extracted from the last section of computations of the observations made with that instrument.

§ 13. *Observations of γ Draconis, with the Reflex Zenith-Tube*; page 54 to 57.

The details of the general construction of this instrument are given in Appendix I. to the *Greenwich Observations* for 1854, and the means taken to prevent the communication of tremor to the mercury are described at page xxii of the present Introduction. For the understanding of the tabular arrangement containing the successive steps of the reduction of the observations, the following explanation will suffice.

The micrometer was originally furnished with thirty wires, and, by bringing each of these successively on the acute wire-cross of an adjustment-eyepiece which was rendered capable of being brought opposite to different wires in succession, the values of the intervals of the wires were very accurately determined, in terms of revolutions both of micrometer A and micrometer B. These intervals were afterwards measured by observing the time of transit of γ Draconis over each of the wires; and eight series of observations, nearly complete, were obtained between 1851, July 18 and August 15. By comparing then the number of revolutions of each micrometer corresponding to the interval between each pair of consecutive wires, with the time occupied by γ Draconis in passing from one wire to the other, the value of one revolution of each is obtained in terms of time; and this is readily reduced to arc by multiplying by $15 \times$ the sine of star's N. P. D. To ensure, however, the utmost accuracy, the hour-angle of each of the extreme observed wires on the two sides of wire "15" was found by successive addition of observed intervals (in time) of all the intermediate wires, assuming wire "15" to represent the meridian with sufficient accuracy; and the angular distance of wire "15" from each of the extreme wires was computed from these hour-angles. The intervals, in terms of the micrometer, of all the intermediate wires, were also added together, so as to exhibit the micrometrical distance of wire "15" from each extreme wire. By this means it was found that, on one side of the wire, 156.017 revolutions of Micrometer B corresponded to an arc of $43'.38''.48$; and on the other side, 181.936 revolutions corresponded to an arc of $50'.51''.71$.

Hence, in the first case, the value of a revolution was

$$\frac{\sin 43'.38''.48}{156.017 \times \sin 1''} = 16''.784$$

and in the other case the value was

$$\frac{\sin 50'.51''.71}{181.936 \times \sin 1''} = 16''.775.$$

The mean of these, or $16''.78$, has been used.

By obtaining the values of the intervals of several of the wires in terms of revolutions of micrometer A in a manner analogous to that explained above, and comparing them with the intervals obtained in terms of revolutions of micrometer B, it was found that 142.957 revolutions of B were equal to 142.986 revolutions of A. Hence the screws of A and B are assumed to have equal values, and one revolution of each is equal to $16''.78$, as stated in the foot-notes to the Observations.

The wires used for the bisection of the Star are usually those numbered "15" and "16," and the interval in arc between these wires, as determined in 1861, is $3'.38''.00$. This value has been used without alteration throughout the year 1870. For a few observations made on other wires, the intervals are given in the notes.

The correction due to the readings of the level-scale is determined from the following considerations:—When micrometer A is to the left—that is, south of the zenith—the micrometer readings increase as the wire moves to the left—that is, as the north zenith distance of the star increases; and, in this position, the readings of the level-scale increase from left to right, and therefore the level-indications will increase when the right or northern edge of the object-glass is raised.

Supposing this northern edge to be raised, the central ray of light for a zenithal star, descending through the focal center and reflected up through the focal center, meets the wire-frame (which is above the focal center) not at its zenithal point, but at a point which is north or to the right of the zenithal point.

Therefore the wire, when in that position it is laid upon the star, is more to the north or right than it ought to be; and therefore its micrometer-reading is smaller than it ought to be, and a positive correction is required: that is, for increasing readings of the level-scale the correction is positive.

The linear amount of the correction (omitting a constant depending on the zero of the level-scale) is {dist. from focal center to wire-frame} $\times$ $\{\frac{1}{2}$ sum of readings of level-scale} $\times$ {value of one division of level-scale}.

The angular amount of the correction is this quantity divided by the focal length of the object-glass.

From statements made by Mr. Simms, it is assumed that the focal center coincides sensibly with the upper surface of the object-glass, and therefore that the distance of plane of wires from focal center = $0^{\text{in}}.25$; and that the value of one division of the level-scale is $6''$ nearly. Also, the focal length of the object-glass, which is that of Troughton's transit instrument dismounted in the year 1851, is 116 inches.

With these data, the correction to zenith distance due to the readings of the level-scale is found to be $0''.00646 \times$ sum of readings of the level-scale.

From these numbers, the numerical value of the sums of equivalents for micrometer-readings and for level-readings is computed by the formula given in the foot-notes to the Observations; and thus is obtained the zenithal distance of the star, as measured towards micrometer B, increased by an instrumental constant, which it is necessary to determine from the observations. This constant is usually determined by forming for each day the half-sum of the two sums of equivalents in the two reversed posi-

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tions of the instrument, and by taking the arithmetical mean of those half-sums determined on different days. By subtracting this constant from the sum of equivalents when B is north, or by subtracting the sum of equivalents from this constant when B is south, the star's apparent north zenith distance is obtained; and by applying to this with reversed sign the correction for the reduction of apparent N.P.D. to mean N.P.D., the mean zenith distances north given in the last column but one of the tabular arrangement are found.

When the observation (as is usually the case) is made in both positions of the instrument, the mean of the results is given in the last column.

§ 14. *Observations of the Solar Eclipse of 1870, December 21-22, with the Equations deduced from the Differences of Right Ascension and from the Differences of North Polar Distance of the Limbs and Cusps, page 60 to 71.*

The observation of the end of the Eclipse require no special mention.

The measures of differences of R.A. and N.P.D. were made with the South-east Equatoreal.

The several classes of observations were arranged with the view of so combining in different ways the effects of the four different quantities which might require correction (namely, difference of R.A. of centers of Sun and Moon, difference of N.P.D. of centers of Sun and Moon, Sun's semidiameter, and Moon's semidiameter) that advantageous equations might be formed for determination of the numerical values of those four quantities.

It was intended to have commenced the observations with a series of differences of N.P.D. of Upper and Lower Cusps, but, owing to cloud, only an observation of one cusp was secured.

For the observations in Series 2 to 8 and 66 to 71, Difference of R.A. of Limbs of Sun and Moon, the clock movement was not used. The hour-circle was clamped firmly to the pier by the fixed clamp, and the polar axis was clamped to the hour-circle in each series by its independent clamp (unfurnished with slow motion). The transits of the limbs were observed by Mr. Christie, and recorded by galvanic contact on the chronograph-barrel.

For the observations in Series 9 to 19 and 34 to 65, Difference of N.P.D. of Sun's N.L. and Moon's N.L., the clock movement was used. Mr. Christie at the eye-end of the telescope directed the instrument approximately to the limb and clamped it; Mr. Criswick read the two declination-microscope-micrometers, and gave the readings to an assistant, who entered them on a prepared sheet of paper. Mr. Christie listened to the beats of the small chronometer on the telescope (sympathetic with the transit-clock), and at the same time turned the micrometer-screw, and when a satisfactory contact was made gave the chronometer-time to the writer, and then read the micrometer and gave its reading to the writer. The sidereal times were inferred from the chronometer-time or transit-clock-time by the application

of the error of the transit-clock. The hour-angle was found by comparing the sidereal time with the right ascension of the limb.

For the observations in Series 20 to 33, Differences of N.P.D. of Right and Left Cusp, and in Series 72 to 95, Differences of N.P.D. of Upper and Lower Cusp, the same process was used.

The adopted value of a revolution of the telescope-micrometer was obtained from observations of α Coronæ on 1860, December 1.

The refractions in N.P.D. are computed by the formula, Refraction = Number $[\log. = 1.7590] \times \tan (N.P.D. - P Q)$; where $P Q$ is an angle depending on hour-angle only, and determined by the formula, $\tan P Q = \tan \text{colat.} \times \cos \text{hour-angle.}$

The refractions in R.A. are computed by the formula, Refraction =

$$\frac{\text{Number } [\log. = 0.5829] \times \tan Z Q}{\sin N.P.D. \times \cos (N.P.D. - P Q)},$$

where $Z Q$ is determined by the formula, $\sin Z Q = \sin \text{colat.} \times \sin \text{hour-angle.}$

This completes the description of the mode of making and reducing the observations. The following applies to the mode of comparing them with the theoretical elements:—

The geocentric places were first interpolated, from the places in the Nautical Almanac, by second differences, at convenient intervals, as exhibited in the tables of the section.

The Sun's Parallax in R.A. was computed by the formula, Parallax in R.A. = $\frac{\text{Hor. Eq. Parallax} \times r \sin Z' Q'}{15 \sin N.P.D.}$, where r is the geocentric radius for Greenwich in terms of the equatoreal radius, and $Z' Q'$ is determined by the formula, $\sin Z' Q' = \sin \text{Geocentric colat.} \times \sin \text{hour-angle.}$

The Sun's Parallax in N.P.D. was computed by the formula, Parallax in N.P.D. = $\text{Hor. Eq. Parallax} \times r \cos Z' Q' \times \sin (N.P.D. - P Q)$, where $P Q$ is determined by the formula, $\tan P Q = \tan \text{Geocentric colat.} \times \cos \text{hour-angle.}$

For computing the Moon's apparent place, the Moon's normal-centric N.P.D. and normal-centric horizontal parallax were formed as in the section of observations with the altazimuth.

With the R.A. and Normal-centric N.P.D., the Azimuth and Normal-centric Z.D. were computed; with a very approximate Apparent Z.D. (found by trial) the parallax at observation was computed, and thus the Apparent Z.D. was formed; from this and the azimuth the Apparent R.A. and Apparent N.P.D. of center were computed.

The augmentation of Moon's semidiameter was taken from Loomis' Tables.

These various apparent quantities having been independently computed for every 15^m , interpolation with second differences was made for every 5^m for the Sun's place and for every 1^m for the Moon's; and interpolation with first differences only for further calculation of places.

Then the Tabular N.P.D. and R.A. of cusps were found by the following tentative process:—If Δ and δ are the N.P.D. of the centers of the Sun and Moon, x the N.P.D. of a cusp; S and s the two semidiameters; a the excess of R.A. of Moon's center above that of Sun's center; Z , z the excesses of R.A. of cusp above those of the two centers; then without sensible error,—

$$Z^2 = \frac{S^2 - (\Delta - x)^2}{\sin \Delta \sin x},$$

$$z^2 = \frac{s^2 - (\delta - x)^2}{\sin \delta \sin x},$$

$$Z + z = a.$$

Different values were tried for x , and Z and z were computed by the first and second equation respectively; and the process of trial and computation was repeated till the values found for Z and z satisfied the third equation.

If we differentiate these expressions, neglecting the variations of the quantities which will be multiplied by the small terms S^2 , s^2 , $(\Delta - x)^2$, and $(\delta - x)^2$, and if we put,—

$$Q = \frac{\Delta - x}{Z \sin \Delta \sin x},$$

$$q = \frac{\delta - x}{z \sin \delta \sin x};$$

then $(Q + q) dx = da - \frac{S}{Z \sin \Delta \sin x} dS - \frac{s}{z \sin \delta \sin x} ds + Q d\Delta + q d\delta$;
and if y be the R.A. of the cusp, A and α the R.A. of centers of Sun and Moon,

$$(Q + q) dy = q dA + Q d\alpha + \frac{q S}{Z \sin \Delta \sin x} dS - \frac{Q s}{z \sin \delta \sin x} ds + Q q (d\delta - d\Delta)$$

These give the numerical or symbolical changes in the N.P.D. and R.A. of the cusp produced by assigned numerical or symbolical changes in the tabular elements.

The change of N.P.D. of a north or south limb is simply the combination (by subtraction or addition) of the changes of N.P.D. of center and the change of semidiameter, whether for the Sun or for the Moon.

The change of R.A. of a 1 L. or 2 L. is the combination (by subtraction or addition) of the change of R.A. of center and of the change of semidiameter in R.A. The latter quantity is given by the formula for the Sun,

$$\frac{1}{\sin \Delta} dS - \frac{S \cos \Delta}{\sin^2 \Delta} d\Delta;$$

and a similar formula for the Moon.

By substitution of the proper numerical values in these formulæ, and by equating the measured quantities to the corresponding tabular quantities increased by the terms representing (by means of these formulæ) the changes in these quantities due to symbolical errors of the different elements, the equations in the section were formed. Their further treatment is sufficiently explained in the section.

OBSERVATIONS OF THE SOLAR ECLIPSE OF 1870, DECEMBER 21-22;
PHENOMENA OF JUPITER'S SATELLITES, AND OCCULTATIONS OF STARS BY THE MOON. CV
CALCULATION OF OCCULTATIONS OF STARS.

§ 15. *Eclipses, Occultations, and Transits of Jupiter's Satellites, compared with the Nautical Almanac; Occultations of Stars and of the Planet Saturn by the Moon, with the Equations deduced from the Occultations; and Eclipse of the Moon, 1870, July 12, page 74 to 82.*

The clocks used in these observations are in general compared with the Transit-Clock near the time of the observation, and the mean solar time is computed in the usual way. H signifies the Transit-Clock "Hardy;" A¹ "Arnold 1;" G¹ "Graham 1;" and E "Earnshaw."

For the computation of the Occultations, the star's place is taken from the "Elements for facilitating the Computation of Occultations" in the Nautical Almanac. The Moon's geocentric place, semidiameter, and horizontal equatoreal parallax, are interpolated with second differences from the Nautical Almanac, and are used without alteration. The correction to be applied to the parallax of the Moon's center in order to obtain that for the point of the limb at which the occultation takes place, is derived from the following Table, for the principles of the formation of which I refer to preceding volumes, from 1843 to 1849:—

Correction to the Moon's Horizontal Parallax, to be used when the Parallax is applied to the Limb.

Angle from the Vertical as seen in an inverting Telescope.	ZENITH DISTANCE.									
	0°	10°	20°	30°	40°	50°	60°	70°	80°	90°
0 360	+0'04	+0'06	+0'08	+0'10	+0'12	+0'13	+0'15	+0'16	+0'16	+0'16
10 350	+0'04	+0'06	+0'08	+0'10	+0'12	+0'13	+0'15	+0'15	+0'16	+0'16
20 340	+0'04	+0'06	+0'08	+0'10	+0'11	+0'13	+0'14	+0'15	+0'15	+0'16
30 330	+0'04	+0'05	+0'07	+0'09	+0'11	+0'12	+0'13	+0'14	+0'15	+0'15
40 320	+0'04	+0'05	+0'07	+0'08	+0'10	+0'11	+0'12	+0'13	+0'13	+0'13
50 310	+0'04	+0'05	+0'06	+0'08	+0'09	+0'10	+0'11	+0'11	+0'12	+0'12
60 300	+0'04	+0'05	+0'06	+0'07	+0'08	+0'08	+0'09	+0'10	+0'10	+0'10
70 290	+0'04	+0'04	+0'05	+0'06	+0'06	+0'07	+0'07	+0'08	+0'08	+0'08
80 280	+0'04	+0'04	+0'04	+0'05	+0'05	+0'05	+0'05	+0'06	+0'06	+0'06
90 270	+0'04	+0'04	+0'04	+0'04	+0'04	+0'04	+0'04	+0'04	+0'04	+0'04
100 260	+0'04	+0'03	+0'03	+0'02	+0'02	+0'02	+0'02	+0'01	+0'01	+0'01
110 250	+0'04	+0'03	+0'02	+0'01	+0'01	0'00	0'00	-0'01	-0'01	-0'01
120 240	+0'04	+0'02	+0'01	0'00	-0'01	-0'01	-0'02	-0'03	-0'03	-0'03
130 230	+0'04	+0'02	+0'01	-0'01	-0'02	-0'03	-0'04	-0'04	-0'05	-0'05
140 220	+0'04	+0'02	0'00	-0'01	-0'03	-0'04	-0'05	-0'06	-0'06	-0'06
150 210	+0'04	+0'02	0'00	-0'02	-0'04	-0'05	-0'06	-0'07	-0'08	-0'08
160 200	+0'04	+0'01	-0'01	-0'03	-0'04	-0'06	-0'07	-0'08	-0'08	-0'09
170 190	+0'04	+0'01	-0'01	-0'03	-0'05	-0'06	-0'08	-0'08	-0'09	-0'09
180 180	+0'04	+0'01	-0'01	-0'03	-0'05	-0'06	-0'08	-0'09	-0'09	-0'09

Let now δ and θ be the N. P. D. and hour-angle of the star, which are the same as the apparent N. P. D. and hour-angle of the point of the Moon's limb; δ' and θ'

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those of the corresponding point of the limb as seen from the Earth's center ; l the geocentric latitude of the place ; and P' the corrected horizontal parallax ; then, by an investigation similar to that given in the Introductions to preceding volumes, from 1843 to 1849, it may be shown that

$$\sin (\theta - \theta') = \frac{\text{Radius of parallel for Greenwich}}{\text{Moon's distance from the Earth's axis}} \times \sin \theta.$$

$$\sin (\delta - \delta') = \frac{\sin l . \sin \delta . \sin \theta . \sin P'}{\sin \frac{1}{2} (\theta + \theta') . \cos \frac{1}{2} (\theta - \theta')} - \cot \frac{1}{2} (\theta + \theta') . \tan \frac{1}{2} (\theta - \theta') . \sin (\delta + \delta').$$

For the first step of the computation the following quantities are formed :—

$F = \log. \sin \text{star's hour-angle} + \log. \text{seconds of corrected eq. hor. parallax} + 9.4942224.$

$G = \log. \sin \text{star's N. P. D.} + \log. \sin \text{star's hour-angle} + \log. \text{seconds of corrected eq. hor. parallax} + 9.8913935.$

(The former numerical constant is the logarithm of half the distance of Greenwich from the Earth's axis, and the latter is the logarithm of the distance of Greenwich from the plane of the equator ; supposing the Earth's ellipticity = $\frac{1}{300}$).

The preceding formulæ are then adapted to logarithmic computation, and the equations are solved by successive trials, assuming a value for δ' , in the following manner :—

$$\begin{aligned} \log. \frac{1}{2} (\theta - \theta') \text{ in seconds} &= F - \log. \sin \delta' + \log. \frac{\text{sine}}{\text{arc}} \text{ for hor. parallax} \\ &+ \log. \frac{\text{arc}}{\text{sine}} \text{ for } (\theta - \theta'). \end{aligned}$$

$$\begin{aligned} \log. 1^{\text{st}} \text{ number} &= G + \log. \secant \frac{1}{2} (\theta - \theta') + \log. \frac{\text{sine}}{\text{arc}} \text{ for hor. parallax} \\ &+ \log. \frac{\text{arc}}{\text{sine}} \text{ for } (\delta - \delta') - \log. \text{sine } \frac{1}{2} (\theta + \theta'). \end{aligned}$$

$$\begin{aligned} \log. 2^{\text{nd}} \text{ number} &= \log. \frac{1}{2} (\theta - \theta') \text{ in seconds} + \log. \frac{\tan}{\text{arc}} \text{ for } \frac{1}{2} (\theta - \theta') \\ &+ \log. \sin (\delta + \delta' - 180^\circ) + \log. \cot \frac{1}{2} (\theta + \theta') + \log. \frac{\text{arc}}{\text{sine}} \text{ for } (\delta - \delta'). \\ \delta - \delta' &= 1^{\text{st}} \text{ number} + 2^{\text{nd}} \text{ number.} \end{aligned}$$

In the first trials, the $\log. \frac{\text{arc}}{\text{sine}}$, &c., are omitted. The convergence of these approximations is extremely rapid.

When δ' and θ' are found accurately, the distance of the corresponding point from the Moon's center is thus found, by means of a subsidiary angle ψ :—

If $\log. \tan \psi = \log. \text{diff. R. A. of Moon's center and corresponding point} + \frac{1}{2} \log. \sin \text{N. P. D. of Moon's center} + \frac{1}{2} \log. \sin \delta' - \log. \text{diff. N. P. D. of Moon's center and corresponding point} ;$

Then $\log. \text{dist.} = \log. \text{diff. N. P. D.} - \log. \cos \psi,$
 or $= \log. \text{diff. R. A.} + \frac{1}{2} \log. \sin \text{N. P. D. of center} + \frac{1}{2} \log. \sin \delta' - \log. \sin \psi.$

The coefficients of small variations of the North Polar Distance and of the Difference of Right Ascension (in the expression for distance), are computed by the formulæ:—

log. 1st number = 2 log. diff. R. A. + log. sine (sum of N. P. D.) — log. dist. + 4.0835.

log. 2nd number = log. diff. N. P. D. — log. distance.

Coefficient of variation of greater N. P. D. = 1st number + 2nd number.

Coefficient of variation of smaller N. P. D. = 1st number — 2nd number.

Log. coefficient of variation of diff. R. A. =

log. diff. R. A. + log. sin δ + log. sin Moon's N. P. D. — log. distance.

The variation of the R. A. of the corresponding point contains the following terms:—

1st. The alteration of the R. A. of the star by the quantity e'' will alter the R. A. of the corresponding point by very nearly the same quantity e'' .

2nd. The alteration of the horizontal equatoreal parallax in the proportion of 1 : $1 + \frac{m}{1000}$ will alter all the deduced parallaxes (in R. A. and in N. P. D.) in nearly the same proportion: and therefore the R. A. of the corresponding point will be altered by $\frac{m}{1000} \times$ correction for parallax in R. A.

3rd. The alteration in the position of the Moon with regard to the meridian, depending on the alteration of time t , will introduce an alteration in the correction for parallax. It is computed by the following formula:—

Alteration in correction of R. A. of corresponding point for parallax, depending on the alteration of time =

$$15'' \times t \times \left\{ \begin{array}{l} \sin P \cdot \cos l \cdot \operatorname{cosec} \text{N.P.D.} \cdot \cos \text{hour-angle} \\ + \sin^2 P \cdot \cos^2 l \cdot \operatorname{cosec}^2 \text{N.P.D.} \cdot \cos 2 \text{hour-angle.} \end{array} \right\}$$

The variation of the R. A. of the Moon's center is $x'' + t \times$ change of R. A. in 1^s.

The variation of the N. P. D. of the corresponding point contains three terms analogous to those for R. A.: namely—

1st. The alteration of the star's N. P. D. by the quantity f'' will alter the N. P. D. of the corresponding point by f'' nearly.

2nd. The correction for parallax in N. P. D. will be altered by $\frac{m}{1000} \times$ correction for parallax in N. P. D.

3rd. The increase of hour-angle (considered positive when the Moon is west of the meridian), depending on the alteration of time t , will alter the correction for parallax in N. P. D. by the following quantity:—

$$15'' \times t \times \left\{ \begin{array}{l} (-\sin P \cdot \cos l \cdot \cos \text{N.P.D.} - \sin^2 P \cdot \sin l \cdot \cos l \cdot \cos 2 \text{N.P.D.}) \times \sin \\ \text{hour-angle.} \\ (-\frac{3}{2} \sin^2 P \cdot \cos^2 l \cdot \cot \text{N.P.D.} + \sin^2 P \cdot \cos^2 l \cdot \cot \text{N.P.D.} \cdot \cos^2 \text{N.P.D.}) \times \\ \sin 2 \text{hour-angle.} \end{array} \right.$$

The variation of the N. P. D. of the Moon's center is $y'' + t \times$ change of N.P.D. in 1^s.

The computed distance, with addition of the sum of the products of the preceding variations by their proper coefficients, is made equal to the semidiameter increased by the term, semidiameter $\times \frac{n}{1000}$; and thus the final equation is formed.

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The following table contains the values of $\log. \left(\frac{\text{arc}}{\sin} \right)$, $\log. \left(\frac{\sin}{\text{arc}} \right)$, and $\log. \left(\frac{\tan}{\text{arc}} \right)$ to the extent to which they are needed for these computations.

	$\log. \left(\frac{\text{Arc.}}{\sin.} \right)$	$\log. \left(\frac{\sin.}{\text{Arc.}} \right)$		$\log. \left(\frac{\text{Arc.}}{\sin.} \right)$	$\log. \left(\frac{\sin.}{\text{Arc.}} \right)$
1	0.0000000	0.0000000	31	0.0000058	9.9999942
2	0.0000000	0.0000000	32	0.0000062	9.9999938
3	0.0000000	0.0000000	33	0.0000066	9.9999934
4	0.0000000	9.9999999	34	0.0000070	9.9999930
5	0.0000001	9.9999999	35	0.0000074	9.9999926
6	0.0000002	9.9999998	36	0.0000078	9.9999922
7	0.0000003	9.9999997	37	0.0000083	9.9999917
8	0.0000004	9.9999996	38	0.0000088	9.9999912
9	0.0000005	9.9999995	39	0.0000093	9.9999907
10	0.0000006	9.9999994	40	0.0000098	9.9999902
11	0.0000007	9.9999993	41	0.0000103	9.9999897
12	0.0000008	9.9999992	42	0.0000108	9.9999892
13	0.0000010	9.9999990	43	0.0000113	9.9999887
14	0.0000012	9.9999988	44	0.0000118	9.9999882
15	0.0000014	9.9999986	45	0.0000124	9.9999876
16	0.0000016	9.9999984	46	0.0000129	9.9999871
17	0.0000018	9.9999982	47	0.0000135	9.9999865
18	0.0000020	9.9999980	48	0.0000141	9.9999859
19	0.0000022	9.9999978	49	0.0000147	9.9999853
20	0.0000024	9.9999976	50	0.0000153	9.9999847
21	0.0000026	9.9999974	51	0.0000159	9.9999841
22	0.0000029	9.9999971	52	0.0000165	9.9999835
23	0.0000032	9.9999968	53	0.0000171	9.9999829
24	0.0000035	9.9999965	54	0.0000178	9.9999822
25	0.0000038	9.9999962	55	0.0000185	9.9999815
26	0.0000041	9.9999959	56	0.0000192	9.9999808
27	0.0000044	9.9999956	57	0.0000199	9.9999801
28	0.0000047	9.9999953	58	0.0000206	9.9999794
29	0.0000051	9.9999949	59	0.0000213	9.9999787
30	0.0000055	9.9999945	60	0.0000221	9.9999779

	$\log. \left(\frac{\tan.}{\text{Arc.}} \right)$		$\log. \left(\frac{\tan.}{\text{Arc.}} \right)$
2	0.0000000	14	0.0000024
3	0.0000001	15	0.0000027
4	0.0000002	16	0.0000031
5	0.0000003	17	0.0000035
6	0.0000004	18	0.0000039
7	0.0000006	19	0.0000044
8	0.0000008	20	0.0000049
9	0.0000010	21	0.0000054
10	0.0000012	22	0.0000059
11	0.0000015	23	0.0000065
12	0.0000018	24	0.0000071
13	0.0000021	25	0.0000077

As a general remark, applying to every class of observation above mentioned, it is proper to state that the original entries of observations are in all cases preserved. The greater part of the regular observations with the Transit-Circle are entered in small memorandum books, in which the entries are made with a metallic pencil whose marks are not easily effaced; those with the Altazimuth are entered in printed skeleton forms arranged for the purpose: and some observations are written down at once with ink in the skeleton forms in which the calculations are to be made, or in the copy which is sent to the press. All, however, are preserved. The sheets punctured by the prickers of the galvanic magnets in registration of transits by the Chronographic method are also preserved. The proof sheets are read with the first skeleton forms in which the observations are entered; and in which, in fact, the examination for accidental errors, &c., is made.

G. B. AIRY.

*Royal Observatory, Greenwich,
1871, November.*
