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THE BINARY NATURE OF THE SINGLE-LINE WOLF-RAYET STAR EZ CANIS MAJORIS = HD 50896^{1}

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ABSTRACT

Results of spectral and photoelectric observations of HD 50896 obtained in the period 1975 February-1978 March are presented. The variations in emission-line profiles, radial velocities, and light are found to be consistent with the 3.76 day period. It is concluded that the binary hypothesis is the most likely one to explain the periodic variations, and that the companion is probably a neutron star of mass $m_2 = 1.3 \pm 0.4 M_{\odot}$. In addition, it is found that the eccentricity differs considerably from zero. It is suggested that this eccentricity is responsible for some of the more extraordinary variations observed in HD 50896.

Subject headings: stars: binaries — stars: individual — stars: Wolf-Rayet

I. INTRODUCTION

With visual magnitude v = 6.94, HD 50896 = EZ CMa = MR 6 is the sixth brightest Wolf-Rayet star in the sky. It is classified WN5 by Smith (1968*a*) and is located toward galactic longitude l = 234°.8 and latitude b = -10°.1 at a distance d = 1.59 kpc (Smith 1968*b*).

HD 50896 lies within the boundaries of the open cluster Collinder 121, with an age of 7×10^6 years (Lundström and Stenholm 1976). This is slightly older than ages estimated for W-R stars whose cluster membership is nearly certain (Moffat and Seggewiss 1979). If associated with the cluster, the W-R star would have an absolute magnitude $M_v = -2.9$, which is much less luminous than the mean value of -4.3given for WN5 by Smith (1973). The interstellar reddening of HD 50896 is small, like that of the cluster, but the reddening of stars in general remains small out to very large distances in this part of the Galaxy. Thus, Lundström and Stenholm concluded that HD 50896 is probably not a member of Cr 121.

Spectral variations were first reported by Wilson (1948) and H. Smith (1955). Subsequently, Barbon *et al.* (1965) made a radial velocity study of this object, disclosing variations with a mean amplitude of 300 km s^{-1} but no correlation between the displacements of the different lines investigated. They concluded that, if HD 50896 is a binary, its period should be less than a day. Smith (1968c) has noted an

¹ Based partly on observations collected at the European Southern Observatory, La Silla, Chile.

occasionally asymmetric He II λ 4686 emission line profile while Irvine and Irvine (1973) also reported the occasional appearance of "a fairly narrow emission" superposed on the redward side of this He II band. This phenomenon is similar to that reported by Sahade (1958) for V444 Cygni, a well-known WN5 + O6 binary system. From the profile changes of He II λ 4686 in HD 50896, Schmidt (1974) derived a possible period of 13 days or multiple thereof.

Kuhi (1967) observed light variations of 0.3– 0.4 mag in the continuum, leading him to propose a period of 1.01 days. However, Lindgren, Lundström, and Stenholm (1975) found light variations in the emission lines compatible with a 1.03 day period, but not in the continuum. This was interpreted by them as a possible occultation phenomenon in a binary system.

Serkowski (1970) has reported strong variations in both degree and angle of polarization in HD 50896. These were verified and extended by McLean *et al.* (1979).

However, until now there has been no conclusive evidence presented in favor of a clear, unique periodicity associated with this object.

There are several characteristics of HD 50896 which should be emphasized. The strong spectral, light, and polarization variations tend to favor its binary nature, although the spectrum does not show the explicit presence of a companion. The nine galactic W-R stars that, like HD 50896 (Johnson 1971), are associated with ring nebulae (Smith 1973), are currently regarded as single stars. The duplicity of HD 50896 (if demonstrated) will open the possibility that all these objects

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TABLE 1APhotoelectric Observations 1975

JD 2,442,000+	m(5640)	m(4680) - m(5640)	m(3635) -m(5640)
447.594	0.776	-1.237	-1.300
	0.782	-1.244	-1.301
	0.783	-1.244	-1.312
	0.784	-1.259	-1.318
	0.784	-1.255	-1.301
453.542	0.782	-1.248	-1.314
454.531	0.784	-1.257	-1.313
455.531	0.772	-1.232	-1.304
456.526	0.794	-1.263	-1.321
457.521	0.776	-1.242	-1.305
458.535	0.776	-1.245	-1.306
459.523	0.777	-1.257	-1.302
460.521	0.773	-1.229	-1.307
460.529	0.776	-1.236	-1.310
461.536	0.773	-1.237	-1.303
462.532	0.778	- 1.238	-1.303
463.549	0.781	- 1.248	-1.306
463.558	0.785	- 1.248	-1.310
463.561	0.789	- 1.247	-1.315
463.567	0.784	- 1.247	-1.310
464.523	0.775	-1.237-1.233-1.233-1.226-1.236	-1.302
464.529	0.771		-1.307
464.532	0.775		-1.309
464.535	0.771		-1.300
464.674	0.774		-1.304
464.677	0.774	-1.237-1.240-1.239-1.239-1.229	-1.318
465.521	0.775		-1.315
465.528	0.776		-1.314
465.575	0.776		-1.317
465.575	0.765		-1.307
465.581	0.768	-1.233	- 1.312
465.590	0.770	-1.235	- 1.305
465.593	0.771	-1.236	- 1.305
465.597	0.771	-1.231	- 1.305
465.663	0.771	-1.236	- 1.305
465.667	0.764	-1.233	-1.302
465.675	0.772	-1.234	-1.302
465.680	0.780	-1.244	-1.309
465.686	0.779	-1.242	-1.308
465.690	0.779	-1.243	-1.317
465.697	0.784	-1.248	-1.323
465.701	0.776	-1.237	-1.305
466.522	0.774	-1.241	-1.306
466.530	0.780	-1.250	-1.315
466.534	0.776	-1.249	-1.309
467.535	0.777	- 1.247	-1.307
	0.782	- 1.248	-1.308
	0.780	- 1.241	-1.313
	0.773	- 1.240	-1.310
	0.769	- 1.243	-1.298
469.586	0.770	- 1.241	-1.308
	0.777	- 1.246	-1.310
	0.769	- 1.236	-1.304
	0.781	- 1.249	-1.310
	0.782	- 1.255	-1.317
470.674	0.781	- 1.251	-1.314
	0.780	- 1.254	-1.311
	0.777	- 1.249	-1.301
	0.773	- 1.244	-1.298
	0.775	- 1.239	-1.305
473.513	. 0.772	-1.244	-1.305
474.512	. 0.775	-1.238	-1.305
474.515	. 0.774	-1.241	-1.306

TABLE 1A-Continued

JD 2,442,000+	m(5640)	m(4680) -m(5640)	m(3635) — m(5640)
475.514 475.518	. 0.781 . 0.780	-1.239 - 1.240	-1.309 - 1.303
476.509	. 0.776	$-1.233 \\ -1.238 \\ -1.240 \\ -1.250 \\ -1.257$	-1.314
476.512	. 0.767		-1.305
477.538	. 0.782		-1.308
478.520	. 0.776		-1.302
478.524	. 0.782		-1.312
479.511	. 0.777	-1.249	$-1.312 \\ -1.312 \\ -1.313 \\ -1.313 \\ -1.308$
479.514	. 0.771	-1.245	
480.508	. 0.766	-1.241	
480.511	. 0.765	-1.235	
481.509	. 0.770	-1.243	
481.512	. 0.782	$-1.253 \\ -1.246 \\ -1.262 \\ -1.237 \\ -1.239$	-1.320
482.503	. 0.772		-1.306
483.653	. 0.779		-1.303
483.657	. 0.769		-1.305
484.624	. 0.775		-1.310

TABLE 1B

PHOTOELECTRIC OBSERVATIONS 1976

JD 2,442,000+	m(5640)	m(4680) - m(5640)	m(3635) -m(5640)	m(5876) -m(5640)
857.557. 857.572. 858.590. 859.558. 860.569.	0.765 0.762 0.769 0.759 0.744	-1.249 -1.250 -1.246 -1.238 -1.238	-1.302 -1.300 -1.317 -1.306 -1.303	
861.558	0.757	-1.235	-1.285	-0.280
862.570	0.740	-1.220	-1.298	-0.231
863.603	0.765	-1.243	-1.288	-0.279
864.507	0.752	-1.247	-1.306	-0.294
870.501	0.747	-1.239	-1.296	-0.300
872.512	0.757	-1.244	-1.296	-0.247
873.500	0.768	-1.256	-1.313	-0.276
874.586	0.757	-1.244	-1.311	-0.305
875.534	0.723	-1.226	-1.305	-0.269
876.534	0.751	-1.240	-1.290	-0.236
882.494	0.748	-1.227	-1.294	-0.247
883.551	0.762	-1.253	-1.307	-0.309
888.487	0.751	-1.233	-1.301	-0.280
889.513	0.768	-1.233	-1.299	-0.300
890.496	0.730	-1.221	-1.305	-0.268
891.489 892.491	0.754 0.761	- 1.241 - 1.247	$-1.287 \\ -1.307$	$-0.253 \\ -0.283$

TABLE 1C

PHOTOELECTRIC OBSERVATIONS 1977

JD 2,442,000+	m(5200)	m(4500) - m(5200)
1441.958	0.686	-0.575
1442.99	0.694	-0.570
1443.95	0.741	-0.569
1444.96	0.724	-0.577
1446.98	0.722	-0.611
1448.95	0.692	-0.562
1449.94	0.696	-0.576
1450.96	0.727	-0.567
1454.94	0.730	-0.576

are binary W-R stars with an invisible companion. Also, its distance from the galactic plane, $d \sin b = 279$ pc, is significantly larger than the average for extreme Population I objects: $\langle |z| \rangle = 60$ pc (Cruz-González *et al.* 1974).

These characteristics could be interpreted, at least in principle, in terms of van den Heuvel's (1976) evolutionary framework in the late stages of massive binary stars, in which HD 50896 would be a binary W-R star with a collapsed companion. The variability could then be largely attributed to its binary orbit. The large distance from the galactic plane could be the result of the runaway kick received from a supernova explosion (even if it is symmetric) of the primary star: because of mass transfer, the primary will explode as the less massive star; the binary system hence will not be disrupted, and it will evolve to the W-R-pluscollapsed-object phase. The ring nebula could be associated with the ejection of gas in the process of nonconservative mass transfer leading to the formation of the present W-R component. This process has been suggested by Wendker et al. (1975) as the origin of the ring nebula NGC 6888 surrounding the single-line WN6 star HD 192163.

The crucial point of this picture is the duplicity of HD 50896. The purpose of this paper is, therefore, primarily to present strong evidence in favor of the binary nature for HD 50896. A preliminary report of some of the results has already been published (Firmani *et al.* 1979).

II. OBSERVATIONAL DATA

The observations consist of the following:

a) 1975 February–March: photoelectric observations through ~100 Å wide interference filters centered at $\lambda 3635$ (near UV continuum), $\lambda 4680$ (strong emission superposed on a continuum) and $\lambda 5640$ (green continuum).

b) 1975 March–April: photoelectric scans (2 Å per channel) at $\lambda\lambda$ 4560–4760.

c) 1976 January: repeat of (a) with the addition of a filter at λ 5876 (He I emission superposed on a continuum).

d) 1977 22 February-9 March: 13 coudé spectra (12 Å mm⁻¹ from $\lambda\lambda$ 3400-5000).

e) 1977 February—April (epoch I): 14 sets of two to five SIT spectra (0.7 Å per channel, $\lambda\lambda$ 4460–4810).

f) 1977 24 October-7 November: intermediateband photoelectric observations at λ 4500 and λ 5200, width of the filters approximately 300 Å.

g) 1977 October–November (epoch II): 11 sets of two or three SIT spectra.

h) 1978 February–March (epoch III): 20 sets of one to five SIT spectra.

a) Photoelectric Observations

The 1975 photoelectric observations (a) were obtained during a continuous run of 38 nights with repeated measurements on a few nights. Two nearby, constant comparison stars, HD 50853 (A1) and HD 50711 (A2), were measured alternatingly with HD 50896. External errors are about ± 0.006 mag for each point. The 1976 photoelectric observations (c) were obtained during a run of 36 nights on the same telescope using the same comparison stars. The external errors are slightly larger (± 0.01 mag). Both sets of data, obtained with the single channel, dry-ice cooled photometer attached to the Bochum University's 61 cm telescope on La Silla, Chile, are listed in Table 1. The photoelectric scans (b) were obtained with a single channel scanner at the same telescope as described elsewhere (Moffat and Seggewiss 1977).

Further differential photometry (f) was made by E. de Lara and one of the authors (C. F.) at the 1.5 m telescope of the San Pedro Mártir Observatory during 1977 with the 45 and 52 filters of the 13 color photometric system (Johnson and Mitchell 1975). The same two comparison stars as above were used. The relative magnitudes can be found in Table 1.

b) Photographic Coudé Observations

The high dispersion spectra (d) were obtained on N₂ baked IIa-O plates during a continuous run of 16 nights at the coudé focus of the ESO 1.5 m telescope at La Silla, Chile. Photographic density scans and radial velocities were obtained using the PDS at the David Dunlap Observatory, Toronto (cf. Moffat 1978 for a description of the method). Only the positions of the central absorptions of N IV λ 4058 and He II and the violet absorption edges of He I, whose profiles tend to be irregular, were measured from tracings. A journal of observations is presented in Table 2.

c) SIT Observations

The silicon-intensifier target (SIT) observations (e, g, h) were carried out with the 1 m telescope of the National Astronomical Observatory at Tonantzintla using a Cassegrain low-dispersion spectrograph and a television multichannel analyzer. The detector consists of an SIT camera coupled to a 500 multichannel memory device, whose final digital output can be programmed to yield the sum of numerous integrations (Ruiz 1974; Solar 1977). The spectra were obtained with a diffraction grating working in the second order in the range $\lambda\lambda 4460-4810$ with a resolution of 0.7 Å per channel. Normally the exposure time was 3 minutes, during which 40 elementary integrations were carried out in order to avoid saturation of the camera tube target near the peak on the He II λ 4686 line. The average signal-to-noise ratio in the λ 4686 region was 300, and the stability in wavelength was +0.1 Å.

Wavelengths were calibrated using a standard He-Ar source. The W-R continuum, defined by windows at $\lambda\lambda 4475-4500$, 4576-4580, and 4770-4800, was normalized at all wavelengths by a second order

	НЈО СапК СапН			СапН	He II em. PICKERING					
Plate	-2,443,000	Phase ^a	(1.5.) 3933.664	(I.S.) 3968.470	3968.43	4100.04	4199.83	4338.67	4541.59	4859.32
G8153	196.557	0.209		· · · ×						
8165	198.529	0.734	+32.8	+34.4	+200	+92	+162	+167	+130	+103:
8170	199.504	0.993	33.8	34.0	232	81	169:	192	140	87:
8187	201.497	0.523	36.1	36.3	259	71	138	160	117	95:
8197	202.500	0.790	34.5	34.4	194:	62	147	187	140:	75:
8215	204.496	0.321	34.7	33.6	174:	101:	138	155	128	102
8227	205.496	0.587	33.9	34.5	220	83	160	167	120	100:
8243	206.715	0.911	32.4	34.5	204:	33:	138	155	118	90
8248	207.500	0.120	32.8	31.3	284:	65:	240	206	160:	72:
8265	208.591	0.410	35.2	35.2	219	63	117	132	135:	110
8274	209.495	0.651	32.9	32.5	167	89	143	141	132	90
8290	210.498	0.917	34.4	38.0	154:	73	125	149	80	50
8301	211.554	0.198	33.0	32.8	249	69	204	195:	171	136
Mean			33.9	34.3	213	73	157	167	131	92
σ			1.1	1.8	39	18	35	23	23	21

HELIOCENTRIC PADIAL VELOCITIES (km s⁻¹)

^a Zero phase is defined by the ephemeris from N IV 3483e; passage of W-R star through y-velocity from negative to positive.

polynomial interpolation. Since variations were not found to occur on a time scale of an hour, the final profiles generally consist of the average of two or more spectra. Columns (1) and (2) in Table 3 give the mean Julian day of observations and the number of spectra averaged, respectively.

Some of the first epoch SIT data were unknowingly obtained during the same time as the coudé observations; both are in excellent accord in the region of spectral overlap.

The SIT data were processed to obtain the follow-

ing: (1) the centers of lines, (2) the line "flux" relative to the continuum.

The centers of the N va features were estimated visually from the computer television display of the reduced spectra. The centers of the He II λ 4686 line were calculated at different levels above the continuum. The results for the velocity variations of the N va features and He II λ 4686 at an intensity level of 7 above the continuum, where the line is steepest and least perturbed, can be found in Table 3 in columns (4)-(6).

The flux is the area between the emission feature and

Plate	Phase ^a	He 11e 4685.682	<he iia=""> 5 Lines</he>	Absorption Dip	N va 4621.	N ive 3483.	N iva 4057.759	He 1a 3888.646	He 1a 4471.507
G8153	0.209		9	strong!			-460. +90	- 1410	- 1475
8165	0.734	+150.:	+149:	very weak	-977:	+28	(-350), +110	-1455, -1170	-1270
8170	0.993	106	-186	strong	-1025	57	-65	-1495, -1205	-1560
8187	0.523	144	-251	weak	-842	36	-200, +215	-1495, (-1390)	-1445
8197	0.790	139	-121		-951	17	-45	-1530	-1315
8215	0.321	197	+37		-821	57	[-140e], +25	-1520	-1600
8227	0.587	149	+232	weak	- 789	29	-140	-1465, -1160	-1155
8243	0.911	140:	-93	4686 double	- 1049 :	27	-85	(-1625), -1180	-1305
8248	0.120	160:	- 84	{4686 double; {strong	-971:	80	+175	-1400 (broad)	-1525
8265	0.410	170	[-214e]	emis, tip	-817	44	[-85]	-1270	-1250
8274	0.651	156	- 195:	very weak	- 894	22	(-110)	(broad, asym.) - 1260	- 1290
8290	0.917	134	-177	{4686 double;	-1074	28	- 150	-1335	- 1360
8301	0.198	108	-37	strong!	-878	98	+110	-1290?	-1360
$Mean \dots \dots \dots \dots \dots \dots \sigma \dots $. 146 . 25							

TABLE 2B

^a Zero phase is defined by the ephemeris from N IV 3483e; passage of WR star through γ-velocity from negative to positive. HJD 2,443,199.53 $\pm 0.18 + (3.763 \pm 0.002) \cdot E.$

Note.— \langle He IIa \rangle is defined by the absorption dip relative to the profile bisection at a width of 22.5 Å; mean of lines λ 4200, 4339, 4542, 4859, and 4686. Internal standard error of the mean is 18 km s⁻¹. N Iva λ 4058: italicized \rightarrow strong feature; bracket \rightarrow weak (also He Ia λ 4472). All emission (absorption) lines were measured for top (bottom) ~ half of line (PDS parabolic fit to profile in photographic density) except He IIa, N IVa λ 4058, He Ia λ 3889, and 4472 which were measured by hand from tracings.

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TABLE 3

SIT OBSERVATIONS

		V_{FLOCITY} $(lm e^{-1})$		-1)	FLUX (Å) ^a	(Å) ^a	
	No. OF SCANS					Ν ν λλ4604–21	Не п λ4686
JD – 2,443,000	AVERAGED	PHASE	N va λ4604	N va λ4621	Не п λ4686	(4590–4630)	(4650–4725)
Epoch I:							
195.67	3	0.977	-977	-974	+172	+30.2	+282.2
197.65	3	0.500	782	779	198	31.2	280.0
197.79	1	0.538	782	714	185	31.9	281.9
198.59	4	0.750	1043	974	192	30.7	284.8
199 60	2	0.019	977	941	189	30.8	201.0
199 79	2	0.069	912	974	243	29.5	270.1
200.60	4	0.007	717	714	245	20.0	279.1
200.00	5	0.204	651	714 944	230	30.9	200.4
220.08	2	0.018	1042	044	192	30.9	207.4
221.05	3	0.870	1043	9/4	217	28.5	273.9
222.59	- 3	0.128	912	941	230	28.1	275.1
223.58	3	0.391	<u></u>		236	29.4	274.1
224.69	2	0.636	782	844	185	29.8	287.8
225.64	3	0.936	1043	974	198	29.7	279.1
251.66	4	0.840	1043	974	230	28.6	292.3
Epoch II:							
431.94	3	0.762	977	974	198	30.1	313.2
437.90	3	0.364			185	30.5	278.4
438.89	3	0.609	651	714	144	31.7	293.7
439.89	1	0.875	1043	844	230	29.6	289.1
446.92	3	0.743	977	844	172	30.0	295.4
447.85	2	0.990	977	974	204	29.5	294.6
448 78	3	0 237	782	779	217	30.9	305.3
452.94	2	0.237	586	714	108	20.2	281.0
453.91	3	0.545	521	640	124	20.5	201.9
453.51	2	0.000	1042	049	109	32.7	292.3
455.93	3	0.874	847	974 844	198 249	30.1	297.2
Enoch III:	5	0.157	047	044	24)	20.0	275.0
555.62	1	0.632	506	714	102	21.2	200 5
555 40	1	0.032	560	714	192	31.3	288.5
555 74	1	0.048	631	/14	192	31.5	289.2
555.92	1	0.001	521	649	1/9	31.6	289.0
555.82	2	0.682	/1/	/14	185	32.6	300.3
556.57	1	0.882	(977)	(1039)	236	28.1	325.0
558.74	3	0.458	(391)	(454)	153	29.8	313.7
559.66	2	0.706	586	779	211	31.2	297.8
559.79	1	0.737	717	779	230	30.5	298.4
564.60	3	0.013	912	844	224	28.8	308.2
564.76	5	0.058	912	844	262	29.2	319.3
565.62	3	0.287	586	714	275	33.4	305.8
566.77	2	0.592	586		236	33.3	327.0
567.56	2	0.802	912	779	230	29.6	285.0
567.77	$\overline{2}$	0.858	912	909	256	29.7	328.5
568.58	$\overline{2}$	0.073	782	909	268	28.8	314.8
568 75	2	0 1 1 9	782	000	256	20.0	310 7
568.80	$\frac{2}{2}$	0.132	012	909	250	27.2	210.0
560.50	2	0.132	912	044	202	20.0	212.0
540 74	2	0.339	201		230	34.4	312.8
570.60	2	0.38/	391	584	1/2	30.9	309.5
5/0.00	2	0.610	280	(519)	224	31.0	299.7

^a Flux computed after the continuum normalization (see text).

the normalized continuum within a certain wavelength interval. Columns (7) and (8) of Table 3 give the calculated fluxes for N v $\lambda\lambda$ 4604–4621 in the interval $\lambda\lambda$ 4590–4630 and He II λ 4686 in the interval $\lambda\lambda$ 4650–4725.

III. PROFILE VARIATIONS

The emission bands in the $\lambda\lambda4470-4800$ wavelength range suffer strong profile variations from one spectrum to another. The periodicity of these variations appeared for the first time as a result of a morphological classification of the profiles of the emission bands N v $\lambda\lambda$ 4604–4621 and He II λ 4686 in the SIT spectra. The most obvious of these variations appear on the uppermost part of He II λ 4686: they may best be described in terms of a relatively narrow feature superposed on the broad band below it. From a purely morphological standpoint we can classify the appearance of this He II emission in three general groups:

Group A. A sharply peaked, almost triangular profile with extended wings.

Group B. A profile with less extended wings and

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having, at least during the first two epochs, an absorption-like feature centered on $\lambda 4686$. Because the emission is shifted by about 2 Å to the red, this absorption gives the impression of cutting into the blue side of the emission below it.

Group C. Profiles which can be classified as transitions between Groups A and B.

Accompanying these variations are changes in the configurations of N v $\lambda\lambda4604-4621$:

i) When the He II λ 4686 line falls in Group A, the two N ve lines λ 4604 and λ 4621 have approximately equal intensity and their violet absorption edges are either absent or very weak.

ii) When the He II emission line falls in Group B, N ve $\lambda 4604$ is weaker than N ve $\lambda 4621$.

Both absorption components are very intense and blueshifted by 15–16 Å.

The transitions from one configuration to another are smooth, and each configuration is repeated with a period of 3.763 days. This period has been checked by applying a search method similar to that of Lafler and Kinman (1965) to the N va 4621 SIT velocities, normalized to constant velocity amplitude from one epoch to another; the result was $P = 3.763 \pm 0.002$ days. An alias period of about 1.36 days also shows up in the data, but the resulting phase diagrams are



FIG. 1.—(a) SIT intensity scans of the peak region of He II λ 4686 ordered in phase; the three epochs of observations are presented separately. The dotted profile is the superposed scan at phase 0.7 of epoch I; the phase can be read off from the peak of each reference profile. The position of λ 4685.7 is marked at bottom. (b) Smoothed coudé photographic density tracings of five He II emission lines. The phase can be read off from the peak of each profile. The tracing at phase 0.917 (like that at phase 0.911) has been emitted due to crowding.

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noisier. We adopt a period of 3.763 days. With this period and setting zero phase at HJD 2,443,199.53 (cf. § IV), we find that the spectra in Group A have phases $\sim 0.4-0.6$ while those in Group B have phases $\sim 0.9-$



FIG. 2.—SIT intensity scans of the N v $\lambda\lambda$ 4604–4621 features as in Fig. 1*a*. The position of λ 4610.0 is marked at bottom.

1.15. Figure 1*a* shows the peak region of the SIT He II λ 4686 profiles folded in phase and separated into three columns, corresponding to the three epochs of observation. The phase increases downward and can be found by drawing a horizontal line from the top of the dotted reference spectrum to the vertical scale. The rest wavelength, λ 4685.7, is marked by vertical lines. Figure 1*b* shows the complete set of He II coudé profiles; although He II λ 4686 is overwhelmingly the strongest line, all observed He II lines behave similarly. The corresponding N v profiles (SIT) are presented in Figure 2 where the position of λ 4610.0 is marked. The phase is indicated by the top of the N ve λ 4621 reference spectrum, in the same way as in Figure 1*a*.

The two N IV features at λ 3483 and λ 4058 behave very differently from the N v lines and from each other (as has also been noted for V444 Cyg by Münch 1950). N IV λ 4058 is similar to He II λ 4686 in that it has a superposed central absorption whose position (cf. § IV), width, and intensity vary with phase:

i) The absorption is strongest at phases $\sim 0.9-1.2$. ii) A sharp emission feature appears to replace the absorption around phase 0.4 ± 0.05 .



FIG. 3.—Smoothed coudé photographic density tracings of (a) the N IV λ 3483 blend and (b) N IV λ 4058, as in Fig. 1b.



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FIG. 4.—Fluxes (Å) ordered in phase from the SIT data: (a) He II λ 4686 and (b) N v $\lambda\lambda$ 4604–4621. Flux is defined as the area between the emission feature and the normalized continuum in the wavelength intervals $\lambda\lambda$ 4650–4725 and $\lambda\lambda$ 4590–4630, respectively.

iii) The absorption is very weak at the remaining phases, in particular 0.5–0.8.

The mild profile variations in the N IV λ 3483 line seem to affect only its uppermost part and are only vaguely reminiscent of the variations of He II λ 4686. This may be due to the smearing effect of the superposition of three lines at $\lambda\lambda$ 3478, 3480, and 3483. Figure 3 shows the tracings of the coudé spectra for the two N IV lines ordered in phase.

We can make the following general remarks regarding the phase-dependent profile variations: (1) At phases 0.8-1.2 both violet and central absorptions are most intense. (2) At phases 0.3-0.8 both violet and central absorptions are very weak, disappear completely, or are replaced by relatively sharp emission. The N v absorptions are completely absent for phases 0.60-0.65.

Comparing the profiles at different epochs, we note the following:

1. The central "absorption" feature on He II λ 4686, particularly at phases ~0.9–1.2 (Group B), has diminished in intensity from epoch I to epoch III (as can be seen in Figure 1*a*). This is also reflected in a plot of flux for this line versus phase in Figure 4*a* which shows an increase in flux in epoch III during phases 0.9–1.6. The He II λ 4686 emission profile at phases 0.6–0.65 has remained nearly identical in shape and level throughout the three epochs. According to Figure 4*a*, the flux remained virtually constant for the three epochs over the phases 0.6–0.8.

2. The N v $\lambda\lambda$ 4604–4620 profiles, on the other hand, have not changed appreciably over the three epochs. Again, this is reflected in the variation of flux with phase for this feature in Figure 4b. This figure also illustrates the prominent dip in intensity at phases 0.0 \pm 0.2, presumably due to increased N v absorption and the possible presence of a secondary dip at phases \sim 0.4–0.5.

In Figure 5 we present the skewness $\beta_1^{1/2}$ of the He II λ 4686 line as a function of phase for the photoelectric scanner data, which are of too low resolution to be studied in more detail. These show that, at phase zero, the line asymmetry is skewed most toward the blue. This parameter was calculated in exactly the same way as by Schmidt (1974), who obtained scans of the same line but at lower resolution (7.5 Å per channel). Assuming $\beta_1^{1/2}$ to be constant yields a mean value, $\langle \beta_1^{1/2} \rangle$, for the present data of 0.059 ± 0.019 s.d. Allowing for a phase-dependent variation as indicated in Figure 5 reduces the rms deviation significantly to ± 0.013 , which is very close to that expected (± 0.012) from a comparison of simultaneous forward and reverse scans. Thus, the systematic phase variation



FIG. 5.—Skewness versus phase, using the ephemeris in the text, for the photoelectric scan data (1975) of He II λ 4686.



FIG. 6.—Heliocentric radial velocity versus phase, using the ephemeris in the text, of the *emission lines*: (a) the blend N IV λ 3483 (coudé), showing the velocity curve calculated from Table 4, (b) mean of He II λ 4200 and 4339 (coudé), (c) He II λ 4686 (coudé), (d) interstellar Ca II, mean of H and K (coudé), for comparison, and (e) He II λ 4686 (SIT, three epochs).

appears to be real. The data of Schmidt (1974) yield $\langle \beta_1^{1/2} \rangle = 0.054 \pm 0.131$ and show no pattern with 3.76 day phases. This is very likely due to the noise introduced by the low resolution; his claimed 13 day (or multiple thereof) period is probably spurious, not being found in any other data.

IV. RADIAL VELOCITY VARIATIONS

Radial velocity variations have been detected for almost all the features measured; the majority are periodic. However, the amplitude of the variations differs from feature to feature, as well as the phases of radial velocity minima and maxima and the noise level.

a) The Emission Lines

Figure 6 shows radial velocity-phase curves from the coudé data for (a) N IVE λ 3483, (b) He IIE λ 4200– 4339, which are the least blended Pickering lines, and (c) He II λ 4686. The Ca II interstellar lines (d) give an idea of the high quality of the direct coudé plates. All emission lines yield essentially the same radial velocity curve, with a semiamplitude of approximately 40 km s⁻¹. As expected from the smoothness and constancy of its line profile, N IV λ 3483 gives the cleanest velocity variation with phase. The apparently high noise level of the three epochs of SIT data, shown in Figure 6e, allows little to be said about this strong, variable line except that the amplitude of the variations may have increased from epoch I to epoch III (K_1 = 30, K_{II} = 45, K_{III} = 55 km s⁻¹).

b) The Central Absorption Lines

Figure 7 indicates radial velocity-phase curves for (a) the mean of five He IIa lines, and (b) N IVa λ 4058. These vary around zero velocity with the following traits: during phases of strong absorption, the velocity increases from ~ -30 or ~ -80 km s⁻¹ to $\sim +100$ km s⁻¹, while during the short interval of sharp emission, velocities are ~ -90 km s⁻¹.

c) The Violet Absorption Edges

Figure 8 shows the radial velocity-phase plots of the violet absorption edges in order of increasing separation from the central W-R core for (a) N va λ 4621 (N va λ 4604 shows the same trend), (b) He Ia λ 4471, generally very weak, and (c) He Ia λ 3888.

The latter is very noisy and shows no apparent systematic variation with phase except a tendency for doubling at phases $\sim 0.6-1.0$. From the curves we can say the following:

1. The violet absorption radial velocity-phase curves lag in phase with respect to the N IVe λ 3483 (and less clearly, He IIe λ 4200–4339 and 4686) radial velocity curves by about 0.2–0.3.

2. The semiamplitudes of the absorption curves are much greater ($\sim 100 \text{ km s}^{-1}$) than those of the abovementioned emission lines.



FIG. 7.—Heliocentric radial velocity versus phase, using the ephemeris in the text, of the *central absorption lines*: (a) mean of five He II lines from Fig. 1b (coudé), (b) H IV λ 4058 from Fig. 3b (coudé). Near phase 0.4 (companion in front) the absorption changes into relatively sharp emission, indicated by a cross.

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3. The semiamplitudes of the N va curves increased between the first and third epochs of observations (K_I = 130, K_{II} = 155, K_{III} = 220 km s⁻¹), in contrast to the emission line velocities of He II λ 4686 which, although noisy, appear to have increased only slightly from one epoch to another.

It is interesting to note here that both of the N v emission lines λ 4604 and 4621 have radial velocity variations identical to those of their respective violet absorptions. These variations are not true wavelength displacements of the emission components, but are the results of the displacements and variations of intensity in their respective violet absorptions. This is verified by the fact that the redward emission line flank, which is unaffected by violet absorption edges, remains viremission lines.

V. LIGHT VARIATIONS

Figure 9a shows the 1975 narrow-band photoelectric photometry (a) plotted in a phase diagram. The



FIG. 8.—Heliocentric radial velocity versus phase, using the ephemeris in the text, of the *violet displaced absorption edges*: (a) N v λ 4621 (coudé and SIT, three epochs). The radial velocity curve is shown for the coudé data. (b) He I λ 4471 (coudé). Large points refer to better determinations (c) He I λ 3888 (coudé). Points joined by a vertical line show doubling of this line. Note the lack of phase-dependent velocity.

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full amplitude is 0.008 mag in the continuum and, in antiphase, 0.004 mag in the emission line, after subtracting off the continuum variation. The latter is comparable to the behavior of the flux of N v $\lambda\lambda$ 4604–4621. While there is only one single maximum and minimum per phase interval, unlike the case of elliptical variables, there is no variation of the continuum color with phase.

The 1976 photometry (c) seen in Figure 9b is similar to that in 1975 except for a small brightening by 0.02 mag.

However, the 1977 medium band photometry (f) in Figure 9c shows a different behavior. The full amplitude is 0.04 mag in both filters, an increase over the 1975/1976 light curve amplitude by a factor 5.

Along with the previously discussed spectral variations, this may be a result of a change in activity of the star during the latter part of 1977 compared to the $2\frac{1}{2}$ preceding years, or may reflect changes in strength or position of emission lines contained in the 45 and 52 filters.

VI. INTERPRETATION

Periodic variations can conceivably be produced by several mechanisms.

Little can be said about nonradial pulsations. Radial pulsations for massive He stars occur on a much shorter time scale than 3.76 days (Stothers and Simon 1970). The recurrence of similar profile configurations for over 1 year makes the spot-rotation mechanism less feasible. The presence of an unseen companion appears to be the most likely mechanism responsible for the principal periodic spectral variations in HD 50896.

As has already been pointed out by Koenigsberger (1978) and Koenigsberger, Firmani, and Bisiacchi (1979), the spectral variations in HD 50896 are very similar to those which occur in some of the known W-R+OB binary systems where there is a strong dependence on the orbital phase. For example, Bappu and Sinvhal (1955) reported a He II λ 4686 emission profile in CQ Cep (WN7+O7) which appears to have a sharper peak and more extended wings when the W-R

component is eclipsed. This is analogous to what we observed in HD 50896 during phases ~0.4–0.6. In V444 Cyg (WN5+O6) the N v λ 4604 and 4621 absorption lines are most intense when the W-R star eclipses the O star and practically disappear when the W-R star is behind (Münch 1950) which is exactly what we observe at phase 0.0 ± 0.2 and 0.3–0.8, respectively, in HD 50896. This is evidence in favor of a binary nature for HD 50896, with the W-R component in front near phase zero and behind near phase 0.5.

Table 4 shows the results of fitting a velocity orbit to the best lines. The N IVe λ 3483 feature is by far the best line in the sense that its profile changes little with phase and it is not accompanied by a variable violet absorption edge. If phase zero is defined by the passage of the W-R star through the velocity axis from negative to positive, the ephemeris from N IVe λ 3483 indicates that phase zero in HD 50896 corresponds to the W-R star in front of the companion, as could be expected from the profile variations. If we are correct in adopting an orbit from this line, the W-R star also passes behind at phase 0.39, while the periastron and apastron passages will occur at phases ~0.15 and 0.65, respectively.

Now, with $P = 3.763 \pm 0.002$ days, $e = 0.34 \pm 0.08$, and $K_{WR} = 36.1 \pm 3.4$ km s⁻¹, we get a mass function

$$(m_2 \sin i)^3 / (m_{\rm WR} + m_2)^2 = 0.015 \pm 0.005 M_{\odot}$$
,

in which m_2 refers to the mass of the unseen star. The orbital inclination can be obtained from the binary model to explain the phase modulated linear polarization (McClean 1980): $i = 71^{\circ} \pm 3^{\circ}$. The mass of the W-R component can be assumed, by analogy with the WN5 component of the well-determined orbit of V444 Cygni, to be $m_{\rm WR} = 10 M_{\odot}$. This leads to an estimate of $m_2 = 1.32 \pm 0.15 M_{\odot}$, which is strikingly similar to the masses found for the neutron stars in X-ray binaries for which mass estimates are available (cf. Crampton, Hutchings, and Cowley 1978). Letting the W-R star's mass vary over the range acceptable from the observations of several W-R binaries (Kuhi 1973), i.e., 5–15 M_{\odot} , leads to $m_2 = 1.3 \pm 0.4 M_{\odot}$.

RADIAL VELOCITI ORBIT, COODE OBSERVATIONS ONLY, $T = 3.703$ DATS							
Line	N Ive λ3483	He 11 λ 4686	He IIe λλ4200–4340	N va λ4621			
γ (km s ⁻¹)	46.9 ± 2.1	147 ± 6	163 ± 6	-915 ± 10			
K_{WR} (km s ⁻¹)	36.1 ± 3.4 0.34 ± 0.08	25 ± 9 0.34 (forced)	33 ± 9 0.34 (forced)	125 ± 13 0.12 ± 0.10			
Ω	$348^{\circ} \pm 14^{\circ}$	$307^{\circ} \pm 75^{\circ}$	$22^{\circ} \pm 46^{\circ}$	(compatible with $e = 0$) $180^{\circ} \pm 59^{\circ}$			
T_0	211.41 ± 0.14 199.53 ± 0.18	204.4 ± 0.7 200.4 ± 0.9	207.7 ± 0.4 199.14 + 0.54	206.8 ± 0.6 200.15 ± 0.06			
		20011 - 015		$(0.165 \pm 0.050$ later in phase than N ive 3483)			
$\sigma (\mathrm{km}\mathrm{s}^{-1})$	5.7	(21 with $e = 0$)	(23 with $e = 0$)	$\begin{array}{c} 26 \\ (34 \text{ with } e = 0.34, 29 \text{ with } e = 0) \end{array}$			

 TABLE 4

 RADIAL VELOCITY OPDIT COULD OBSERVATIONS ONLY: P = 3.763 Days

^a JD - 2,443,000; reference epoch for phase zero, i.e., time of passage from negative to positive through the γ -velocity.





FIG. 9.—Photometric data: (a) 1975, (b) 1976, (c) 1977. Note that the star brightened by 0.02 mag from 1975 to 1976.

Since the progenitor of the W-R star must have been at least 15 M_{\odot} , it is difficult to understand how a normal, main-sequence star of original mass ≤ 1.3 $\pm 0.4 M_{\odot}$ could have formed in this binary system of HD 50896 in view of the observed frequency of mass ratios for massive binaries (Garmany 1979). Such lowmass companions can, however, be well understood in the framework of advanced evolution in massive close binaries (van den Heuvel 1976). Additional support for this hypothesis for HD 50896 comes from the fact that it has a high z, its orbit is noncircular (although we may be seeing only a pseudo-eccentricity in an actually circular orbit: cf. Wilson and Sofia 1976), and a nebular expanding H II gas ring is present. These make a strong case for HD 50896 being a binary W-R star containing a collapsed companion, probably a neutron star. The only possible hitch is the lack of evidence that HD 50896 is an X-ray source, although in principle this can be easily explained by efficient photoelectric absorption in the dense W-R envelope as calculated for another suspected W-R + compact runaway system, HD 197406 (Moffat and Seggewiss 1979). With the assumption that we are dealing with a W-R + compact system, we postulate the following qualitative model to explain most of the observed phenomena.

Due to the high density of the W-R wind one would expect accretion onto the neutron star to exceed the Eddington limit so that any X-radiation produced would be completely degraded to lower frequencies before it escaped. This may occur in such a way that the compact star (plus its possible accretion disk) appears as a low-mass, hot stellar-like object producing continuous optical radiation surrounded by a wind that produces relatively narrow emission lines (e.g., He II λ 4686 and N IV λ 4058) much like an Of star, while heating the hemisphere of the W-R star which it is facing. Narrow emissions are indeed seen at phases when the compact star is in front. In addition, the possible secondary minimum in the N v flux at phases ~0.4 (Fig. 4b) may indicate the presence of a highly localized and ionized region between the W-R star and the collapsar, and very near the latter.

On the other hand, when the W-R star is in front (ϕ \sim 0), the collapsar is near the periastron passage and therefore in the proximity of higher excitation and lower velocity regions in the W-R envelope. The added emission produced as a result of degraded X-radiation would then be seen redshifted at these phases due to the outward motion (away from us) of the envelope (see Fig. 10). This effect, together with the absorption by the W-R envelope of the central wavelengths of the emission lines produced in the area of the collapsar, could explain the N IV λ 4058 (Fig. 3) and He II emission profiles observed during epochs I and II (Figs. 1a and 1b). The change in the He II λ 4686 profiles which occurred in epoch III could be the result of a general increase in the dimensions of the He II emitting region of the W-R star itself, in which case the importance of the perturbation produced by the collapsar at $\phi \sim 0$ would be greatly minimized. This picture would also be consistent with the widening of the He II λ 4686 feature since an increase in the emitting region implies a wider range of velocities in the accelerated W-R envelope. It is also very significant that the He II profiles that have virtually remained unchanged in epoch III are those at phases $\phi \sim 0.6$, which is the phase corresponding to the apastron passage.

The violet displaced absorptions N v and He I arise

a) CROSS - SECTION OF ORBITAL PLANE



FIG. 10.—Model with relative orbit based on the ephemeris in the text. The stratification of the W-R envelope is schematic.

in a localized region of the W-R envelope with high projected wind velocity against the W-R core and are subject to perturbations especially at phases $\sim 0.4-0.6$ when the collapsar is in front. At phase zero this source of perturbation is essentially occulted and we are seeing the true expansion velocity of expanding matter producing these violet displaced absorption lines along the line of sight, independent of the epoch. Changes in velocity of N va, for example, have occurred only at phases when the compact star is in front.

It can only be speculated that the velocity-amplitude and phase of the N IV λ 3483 emission line remains constant with time and truly reflects the orbital motion. Obviously more data are needed to check this rather crucial line.

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Note added in manuscript.—After completion of the paper, we became aware of a preprint by D. Ebbets: "The Variable Emission Line Spectrum of HD 50896: WN5" (1979, Pub. A.S.P., 91, 804). This work is based on Digicon spectral data ($\lambda\lambda$ 3900–5100, resolution

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