THE ASTROPHYSICAL JOURNAL, 205:688-695, 1976 May 1 © 1976. The American Astronomical Society. All rights reserved. Printed in U.S.A.

THE EXTENSION OF THE HUBBLE DIAGRAM. I. NEW REDSHIFTS AND BVR PHOTOMETRY OF REMOTE CLUSTER GALAXIES, AND AN IMPROVED RICHNESS CORRECTION

ALLAN SANDAGE, JEROME KRISTIAN, AND JAMES A. WESTPHAL Hale Observatories, Carnegie Institution of Washington and California Institute of Technology Received 1975 September 5

ABSTRACT

Absorption-line redshifts for 37 galaxies in 31 remote clusters have been measured with the new sky-subtracting prism spectrograph, using an SIT television detector with digital readout. Twenty-five galaxies in the sample have redshifts larger than z = 0.20. New photoelectric *BVR* photometry has been obtained for 16 of the clusters. Magnitudes corrected for aperture effect, *K*-dimming, galactic absorption, cluster richness, and Bautz-Morgan contrast effect are listed. The data permit an improvement in the statistics of the Hubble diagram to z = 0.28 and a new

The data permit an improvement in the statistics of the Hubble diagram to z = 0.28 and a new determination of the dependence of the absolute magnitude of the brightest cluster galaxy on cluster richness. A small correlation with richness is found whose amplitude is 0.20 ± 0.18 mag over all Abell richness classes 0-4. As in previous studies, the shallowness of the correlation requires that if M(1) is governed by a general luminosity function, $\phi(M)$, for fainter members, then the slope of $\phi(M)$ at M(1) must be very steep.

The 16 new clusters with photometry have a dispersion in M(1) of 0.26 mag. The dispersion of fully corrected magnitudes for the 65 clusters in the total sample is 0.276 mag.

The new points in the Hubble diagram give no indication that the (m, z) relation deviates from the q_0 (formal) = +1 line (i.e. with no evolutionary correction applied), nor that 3C 295 is abnormally bright. The need for more data with z > 0.3 is stressed.

Subject headings: cosmology — galaxies: clusters of — galaxies: redshifts

I. INTRODUCTION

Absorption-line redshifts of faint galaxies can now be measured routinely with the Hale 5 m reflector, using a new sky-subtraction prism spectrograph with an SIT television detector. The system and its first results were described by Westphal, Kristian, and Sandage (1975; hereafter WKS). We have started a program, using this instrument, to extend the Hubble diagram beyond the photographic cutoff at $z \approx 0.2$. The initial effort has been mainly on the bright end of this range, z = 0.2-0.3, so as to gain experience with the system and test the redshift limits of various cluster surveys.

The present paper gives the results obtained to 1975 June on clusters which are not known radio sources (§ II). Most of these are clusters at the largest distance (range 6) of the Abell (1958) catalog. Other clusters are from special fainter surveys. A modest improvement in the statistics of the Hubble diagram to z = 0.3 is achieved (§ IV) by combining the redshift data with new *BVR* broad-band photometry (§ III) for 16 of the clusters. New information on the absolute magnitude of first-ranked galaxies as a function of cluster richness has also been derived from the material (§ IV).

II. NEW REDSHIFTS

a) Sample

To improve our knowledge of the variation of absolute magnitude of first-ranked cluster galaxies with cluster richness, we plan to measure substantially all Abell clusters of richness class $R \ge 3$ (distance ranges 4, 5, and 6) as well as a number of sparser clusters in the same distance interval. Correlation of the absolute magnitude residuals with richness over a small redshift range gives the $M = f(N_c)$ relation, independent of assumptions about q_0 .

In addition to these relatively bright Abell clusters, two sources of fainter clusters are available. Beginning in 1952, a search for clusters at the limit of the red Sky Survey plates was undertaken by Humason and Sandage (1957; hereafter HS) to find clusters more distant than Hydra (0855+0321). Direct plates of the candidates were taken with the Hale reflector between 1952 and 1957 to determine if the most distant suspects were real. Many proved to be, and Humason (1957) attempted redshift measurements for a number of them, but was unsuccessful due to night-sky contamination. Later, redshifts for two of them (0024 + 1654 and 1447 + 2617) were measured by Baum (1962) from the shift of the continuum energy distribution. Baum's measurements were repeated by Oke (1971), using the multichannel scanner. Nine clusters found in this early survey are included in the present list, identified by HS in column (2) of Table 1.

More recently, we have begun a systematic survey for more distant clusters in the north and south galactic polar regions using the Palomar Schmidt, first with Eastman IIIaJ plates with a Wratten 4 filter, and now using the new fine-grain red 127-04

688

TABLE 1

REDSHIFTS DETERMINED FROM OCTOBER 1974 TO JUNE 1975 USING THE DIGITAL SUBTRACTION

(1) (2) (3) (4) (5) (6) (7) (8) (9) (10) 0024 + 1654 HS 00 24 00 +16 53 24 -45° 0, 391 G (2) III WKS A 98 00 43 50, 9 +20 11 53 -42 0, 1036 E 3 II - III WKS A 222 HS 01 35 35, 0 -13 00 34 -72 0, 206 E 3 II - III WKS A 223 B HS 01 35 37, 4 -12 59 55 -72 0, 408 E Foregar A 278 01 54 22, 4 +32 00 15 -29 0, 0885 E 0 WKS A 376 01 54 22, 4 +32 00 15 -29 0, 0485 E 0 WKS A 545 04 51 27 +02 48 42 -24 0, 203 E 3 II - III WKS A 550 07 20 08, 6 +31 44	CLUSTER	SOURCE	α 1950	δ 1950	ь ^Ш	z	Quality	R	BM	NOTES
OD24 + 1654 HS OO 24 00 + 16 53 24 -45° 0.391 G (2) III WKS A 98 OU 43 50.9 + 20 11 53 -42 0.1036 E 3 II - III WKS A 222 HS OI 35 35.0 -13 00 34 -72 0.217 E 3 II - III WKS A 223 A HS OI 35 37.4 -12 595 -72 0.206 E 3 II - III WKS A 223 (FG) OI 54 22.4 +32 00 15 -29 0.0885 O $\Delta V_{x} \sim 50$ A 278 OI 54 22.4 +32 00 15 -29 0.0885 O WKS A 376 OI 24 258.6 +36 4150 -20 0.0485 E 0 WKS A 545 OF 29 08.6 +31 44 22 +22 0.172 E 3 II - III WKS A 580 OF 29 08.6 +	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
A 9800 43 \$0, 9+20 11 \$53-420, 1036E3II - IIIWKSA 222HS01 35 06, 0-13 10 34-720, 217E3II - IIIWKSA 223 AHS01 35 35, 0-13 00 34-720, 206E3II - IIIWKSA 223 BHS01 35 37, 4-12 59 55-720, 049E $AV_{x} \sim 50$ A 27801 54 22, 4+32 00 15-290, 0885E0WKSA 27802 21 31, 7-08 49 14-610, 274G1WKSA 37602 21 31, 7+02 48 42-240, 203E3IIIWKSA 52004 51 27+02 48 42-240, 203E3IIIWKSA 58607 29 08, 6+31 44 22+220, 172E3IIIIA 53307 46 01, 9+72 54 36+300, 226G3II - IIIWKSA 63908 12 04, 2+68 04 05+330, 2291P3II - IIIShould HA 65509 23 27, 0+78 30 28+340, 226P4II - IIIZ 0, 01A 77709 21 21, 3+14 23 28+400, 1361E3II - IIIWKS0939 + 0912H5(A1993)104 41 8, 2+09 19 37+560, 2075	0024 + 1654	HS	00 24 00	+16 53 24	-45 ⁰	0.391	G	(2)	ш	WKS
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	A 98	•••	00 43 50.9	+20 11 53	-42	0.1036	E	3	II - III	WKS
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	A 222	HS	01 35 06.0	-13 14 48	- 72	0.217	E	3	II - III	WKS
A 223 BHS01 35 28,4-13 04 19-720, 208E $\Delta V_r \sim 50$ A 223 (FG)01 35 37,4-12 59 55-720, 049EForegreeA 27801 54 22,4+32 00 15-290, 085E0WKS0221 - 0849HS(A348)02 21 31,7-08 49 14-610, 274G1WKSA 37602 42 58,6+36 41 50-200, 0485E0WKSA 52004 51 27+02 48 42-240, 203E3IIIWKSA 54505 30 07-11 35 02-230, 154E4IIIObscursA 58607 40 01,9+72 54 36+300, 226G3II - IIIWKSA 63908 15 04,2+68 04 05+330, 291:P3II - IIIShould 1A 65508 21 21+47 17+350, 1245E3Iconfu0851 + 65193al(C6)08 51 01,4+65 19 14+370, 228E1<-II	A 223 A	HS	01 35 35.0	-13 00 34	-72	0.206	E	3	и - ш	WKS
A 223 (FG) 01 35 37.4 -12 59 55 -72 0.049 E Foregree A 278 01 54 22.4 +32 00 15 -29 0.0885 E 0 WKS A 278 01 54 22.4 +32 00 15 -29 0.0885 E 0 WKS A 376 02 42 58.6 +36 41 50 -20 0.0485 E 0 WKS A 545 04 51 27 +02 48 42 -24 0.203 E 3 III WKS A 545 07 46 01.9 +72 54 36 +30 0.226 G 3 II - III Shold 1 A 639 08 15 04.2 +68 04 05 +33 0.2145 E 3 I confit 0851 + 6519 3aJ(C6) 08 51 01.4 +65 19 14 +37 0.283 E I - II X 0.075 E 1 II III x 50.07 0839 + 0912 H6549 93 92.9 +09 12 00 +42 0.2075 <td>A 223 B</td> <td>HS</td> <td>01 35 28.4</td> <td>-13 04 19</td> <td>-72</td> <td>0,208</td> <td>E</td> <td></td> <td>•••</td> <td>∆V_r~500 k/s</td>	A 223 B	HS	01 35 28.4	-13 04 19	-72	0,208	E		•••	∆V _r ~500 k/s
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	A 223 (FG)	•••	01 35 37.4	-12 59 55	- 72	0.049	E		10 · • • *	Foreground
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	A 278	•••	01 54 22.4	+32 00 15	- 29	0.0885	E	0	•••	WKS
A 376 02 42 58,6 + 36 41 50 - 20 0,0485 E 0 WKS A 520 04 51 27 +02 48 42 - 24 0,203 E 3 III WKS A 545 05 30 07 -11 35 02 -23 0,154 E 4 III Obscure A 586 07 29 08,6 + 31 44 22 +22 0,172 E 3 I - II A 593 07 46 01,9 +72 54 36 +33 0,226 G 3 II - III WKS A 639 08 15 04,2 +68 04 05 +33 0,226 G 3 II - III WKS A 655 08 22 12 +47 17 +35 0,1245 E 3 I confin 0851 + 6519 3a](C6) 08 51 01,4 +65 19 14 +37 0,283 E I - II A 777 09 23 27,0 +78 30 28 +34 0,226 P 4 II - III WKS A 795 09 21 21,3 +14 23 28 +40 0,1361 E 3 II - III WKS A 963 10 14 05,8 +39 17 39 +56 0,207 E 1 II - III WKS A 963 10 14 05,8 +39 17 39 +56 0,207 E 3 II WKS A 1146 12 15 24,4 +20 57 00 +80 0,200 G 3 II - III WKS A 1146 12 15 24,4 +20 57 00 +80 0,200 G 3 II - III WKS A 1758 13 30 38,7 +50 49 01 +65 0,226 E 1 II - III WKS A 1758 13 30 48,7 +50 49 01 +65 0,226 E 3 II - III WKS A 1758 13 30 48,7 +50 49 01 +65 0,226 E 1 II - III WKS A 1758 13 30 48,7 +50 49 01 +65 0,220 G 3 II - III A 1758 13 30 48,7 +50 49 01 +65 0,220 E 3 III - III A 1759 ////////////////////////////////////	0221 - 0849	HS(A348)	02 21 31.7	-08 49 14	-61	0.274	G	1	•••	WKS
A 52004 51 27+02 48 42-240.203E3IIIWKSA 54505 30 07-11 35 02-230.154E4IIIObscureA 58607 29 08, 6+31 44 22+220.172E3IIIIA 59307 46 01.9+72 54 36+300.226G3II - IIIWKSA 63908 15 04.2+68 04 05+330.291:P3II - IIISolubleA 65508 22 12+47 17+350.1245E3I-onfit0851 + 65193aJ(C6)08 51 01.4+65 19 14+370.283EI<-II	A 376	•••	02 42 58.6	+36 41 50	- 20	0.0485	Е	0	~ • • •	WKS
A 545 05 30 07 -11 35 02 -23 0, 154 E 4 III Obscure A 586 07 29 08, 6 +31 44 22 +22 0, 172 E 3 I - III WKS A 639 08 15 04, 2 +68 04 05 +33 0, 226 G 3 II - III WKS A 635 08 22 12 +47 17 +35 0, 1245 E 3 I II confin 0851 + 6519 34J(C6) 08 51 01, 4 +65 19 14 +37 0, 283 E I - III Z $\pm 0, 01$ A 777 09 21 21, 3 +14 23 28 +40 0, 1361 E 3 II - III WKS 0939 + 0912 HS(A854) 09 39 20, 9 +09 12 00 +42 0, 2075 E 1 II - III WKS 1044 + 0918 (FG) HS 10 44 18, 2 +09 19 37 +56 0, 207 E 1 II - III WKS 1044 + 0918 (FG) HS 10 44 18, 2 +09 19 37 +56 0, 200 G	A 520	•••	04 51 27	+02 48 42	-24	0,203	E	3	III	WKS
A 58607 29 08.6 $+31 44 22$ $+22$ 0.172E3I - IIA 59307 46 01.9 $+72 54 36$ $+30$ 0.226G3II - IIIWKSA 63908 15 04.2 $+68 04 05$ $+33$ 0.291:P3II - IIIShould I0851 + 65193aj(C6)08 51 01.4 $+65 19 14$ $+37$ 0.283EI - IIIIIA 77709 23 27.0 $+78 30 28$ $+34$ 0.226P4II - III $z \pm 0.00$ A 79509 21 21.3 $+14 23 28$ $+40$ 0.1361E3II - IIIWKS0939 + 0912HS(A854)09 39 20.9 $+09 12 00$ $+42$ 0.2075E1II - IIIWKS044 + 0918 (FG)HS10 44 05.8 $+39 17 39$ $+56$ 0.207E3IIWKS1044 + 0918HS(A1093)10 44 18.2 $+09 19 37$ $+56$ 0.206E1II - IIIA 1093A 114610 58 47.1 $-22 27 34$ $+34$ 0.137P4I - IIIWKSA 155012 26 44.6 $+47 58 00$ $+60$ 0.254E3IIIIIIA 155012 26 44.6 $+47 58 00$ $+60$ 0.254E3IIIIIIA 175813 30 38.7 $+50 49 01$ $+65$ 0.280E3IIIIIIA 1759/6013 31 40.3	A 545	•••	05 30 07	-11 35 02	-23	0.154	E	4	ш	Obscured?
A 59307 46 01.9+72 54 36+300.226G3II - IIIWKSA 63908 15 04.2+68 04 05+330.291:P3II - IIIShould IA 65508 22 12+47 17+350.1245E3Iconfit0851 + 65193aj(C6)08 51 01.4+65 19 14+370.283EIIA 77709 23 27.0+78 30 28+340.226P4II - III $z \pm 0.00$ A 79509 21 21.3+14 23 28+400.1361E3II - IIIWKS0939 + 0912HS(A854)09 39 20.9+09 12 00+420.2075EIIIIWKS1044 + 0918HS(A1093)10 44 10.9+09 18 53+560.207E3IIWKS1044 + 0918HS(A1093)10 44 10.9+09 18 53+560.226E1II - IIIA 1093A 116610 58 47.1-22 27 34+340.137P4I - IIIA 1093A 155011 2 26 44.6+47 58 00+690.254E3II - IIIA 175811 3 140.3+20 30 53+780.168:P3IIINot con1411 + 2914 10 39.6+29 28 13+720.254P(I - II):Foregre1411 + 2914 10 39.6+29 28 13+720.254P	A 586	•••	07 29 08.6	+31 44 22	+22	0,172	E	3	I - II	
A 63908 15 04.2+68 04 05+330.291:P3II - IIIShould HA 65508 22 12+47 17+350.1245E3Iconfix0851 + 65193aJ(C6)08 51 01.4+65 19 14+370.283EI- IIA 77709 23 27.0+78 30 28+340.226P4II - III $z \pm 0.00$ A 79509 21 21.3+14 23 28+400.1361E3II - IIIWKS0939 + 0912HS(A854)09 39 20.9+09 12 00+420.2075E1II - IIIWKS0144 + 0918 (FG)HS10 44 18.2+09 19 37+560.207E3IIWKS1044 + 0918HS(A1093)10 44 10.9+09 18 53+560.226E1II - IIIA 1093A 114610 58 47.1-22 27 34+340.137P4I - IIIWKSA 151412 15 24.4+20 57 00+800.200G3II - IIIA 1759/6013 31 40.3+20 30 53+780.168:P3IIIMA 1759/6013 31 40.3+20 30 53+720.222G1(I - I):Foregree1411 + 2914 10 39.6+29 28 13+720.254P(I - I):14 101438 + 2850sal (C5)14 38 56.2+28 5000+660	A 593		07 46 01.9	+72 54 36	+30	0,226	G	3	II - III	WKS
A 65508 22 12 $+47$ 17 $+35$ 0.1245E3Iconfin0851 + 65193aJ(C6)08 51 01.4 $+65$ 19 14 $+37$ 0.283EI - IIIA 77709 23 27.0 $+78$ 30 28 $+34$ 0.226P4II - III $z \pm 0.01$ A 79509 21 21.3 $+14$ 23 28 $+40$ 0.1361E3II - IIIWKSA 79509 39 20.9 $+09$ 12 00 $+42$ 0.2075E1II - IIIWKSA 96310 14 05.8 $+39$ 17 39 $+56$ 0.207E3IIWKS1044 + 0918 (FG)HS10 44 18.2 $+09$ 19 37 $+56$ 0.206E1II - IIIA 10931044 + 0918HS(A1093)10 44 10.9 $+09$ 18 53 $+56$ 0.226E1II - IIIA 1093A 114610 58 47.1 -22 27 34 $+34$ 0.200G3II - IIIA 1093A 151412 5 24.4 $+20$ 57 00 $+80$ 0.200G3II - IIIA 175813 3 0.38.7 $+50$ 49 01 $+65$ 0.280E3IIIA 175813 3 14 0.3 $+20$ 20 30 53 $+72$ 0.222G1(I - II):1411 + 2914 10 39.6 $+29$ 28 13 $+72$ 0.254P(I - II):1438 + 28501411 + 2914 38 56.2 $+28$ 50 00 $+66$	A 639		08 15 04.2	+68 04 05	+33	0.291:	Р	3	п - Ш	Should be
$0851 + 6519$ $3aJ(C6)$ 085101.4 $+651914$ $+37$ 0.283 E $I - II$ $A777$ \cdots 092327.0 $+783028$ $+34$ 0.226 P 4 $II - III$ $z \pm 0.00$ $A795$ \cdots 092121.3 $+142328$ $+40$ 0.1361 E 3 $II - III$ $Z \pm 0.00$ $0939 + 0912$ HS(A854) 093920.9 $+091200$ $+42$ 0.2075 E 1 $II - III$ WKS 0936 \cdots 101405.8 $+391739$ $+56$ 0.207 E 3 II WKS $1044 + 0918$ HS(A1093) 104418.2 $+091937$ $+56$ 0.206 E 1 $II - III$ $A 1093$ $A 1146$ \cdots 105847.1 -222734 $+34$ 0.137 P 4 $I - II$ WKS $A 1146$ \cdots 105847.1 -222734 $+34$ 0.200 G $II - III$ MKS $A 1146$ \cdots 12524.4 $+205700$ $+80$ 0.200 G $II - III$ MKS $A 1550$ \cdots 122644.6 $+475800$ $+69$ 0.254 E III III $A 1759/60$ \cdots 133140.3 $+203053$ $+78$ $0.168:$ P $(I - II):$ Foregreat $1411 + 29$ $HS(A1878)$ 141039.3 $+292830$ $+72$ 0.222 G $(I - II):$ $Foregreat1438 + 2850=A1952143853.7+285000+660.2448EIIII$	A 655	•••	08 22 12	+47 17	+35	0.1245	Е	3	I	confirmed
A 77709 23 27.0+78 30 28+340.226P4II - III $z \pm 0.00$ A 79509 21 21.3+14 23 28+400.1361E3II - IIIWKS0939 + 0912HS(A854)09 39 20.9+09 12 00+420.2075E1II - IIIWKSA 96310 14 05.8+39 17 39+560.207E3IIWKS1044 + 0918 (FG)HS10 44 10.9+09 18 53+560.226E1II - IIIA 1093A 114610 58 47.1-22 27 34+340.137P4I - IIIWKSA 151412 15 24.4+20 57 00+800.200G3II - IIIA 1093A 175913 30 38.7+50 49 01+650.226E3IIINot con1411 + 29HS (A1878)14 10 39.3+29 28 30+720.222G1(I - II):Foregrad1438 + 28503aJ (C5)14 38 53.7+28 50 00+660.247EIII $\Delta V_{T} \sim 1$ 1438 50.2+28 50 12+660.241G3(I - II):1438 + 2850= A195214 38 56.2+28 50 12+660.241G3(I - II):Foregrad1438 + 2850= A195214 38 56.2+28 50 12+660.244E3II - III1438 + 2850= A195214 38 56.2+28 50 12+660.244 <t< td=""><td>0851 + 6519</td><td>3aI(C6)</td><td>08 51 01.4</td><td>+65 19 14</td><td>+37</td><td>0.283</td><td>Е</td><td></td><td>I - II</td><td></td></t<>	0851 + 6519	3aI(C6)	08 51 01.4	+65 19 14	+37	0.283	Е		I - II	
A 79509 21 21.3 $+14 23 28$ $+40$ 0.1361E3II - IIIWKS0939 + 0912HS(A854)09 39 20.9 $+09 12 00$ $+42$ 0.2075E1II - IIIWKSA 96310 14 05.8 $+39 17 39$ $+56$ 0.207E3IIWKS1044 + 0918 (FG)HS10 44 18.2 $+09 19 37$ $+56$ 0.207E3IIWKS1044 + 0918HS(A1093)10 44 10.9 $+09 18 53$ $+56$ 0.226E1II - IIIA 1093A 114610 58 47.1 $-22 27 34$ $+34$ 0.137P4I - IIWKSA 151412 15 24.4 $+20 57 00$ $+80$ 0.200G3II - IIIWKSA 175813 30 38.7 $+50 49 01$ $+65$ 0.280E3IIINot conA 1759/6013 31 40.3 $+20 28 30$ $+72$ 0.222G1(I - II):Foregrad1411 + 2914 10 39.6 $+29 28 13$ $+72$ 0.224P(I - II):Foregrad1438 + 2850= A195214 38 53.2 $+28 50 00$ $+66$ 0.248E2III1438 + 2850= A195214 38 53.7 $+28 50 00$ $+66$ 0.248E2III1438 + 2850= A195214 38 53.7 $+28 50 12$ $+66$ 0.141EForegrad1438 + 2850= A195214 38 53	A 777		09 23 27.0	+78 30 28	+34	0.226	Р	4	II - III	$z \pm 0.005$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	A 795	•••	09 21 21.3	+14 23 28	+40	0.1361	Е	3	II - III	WKS
A 963 10 14 05.8 $+39 17 39$ $+56$ 0.207 E 3 II WKS 1044 + 0918 (FG) HS 10 44 18.2 $+09 19 37$ $+56$ 0.0908 E Foregrad 1044 + 0918 HS(A1093) 10 44 10.9 $+09 18 53$ $+56$ 0.226 E 1 II - III A 1093 A 1146 10 58 47.1 $-22 27 34$ $+34$ 0.137 P 4 I - II WKS A 1514 12 15 24.4 $+20 57 00$ $+80$ 0.200 G 3 II - III MKS A 1750 12 26 44.6 $+47 58 00$ $+69$ 0.254 E 3 III M A 1758 13 31 40.3 $+20 30 53$ $+78$ 0.168: P 3 III Not con 1411 + 29 HS (A1878) 14 10 39.6 $+29 28 30$ $+72$ 0.222 G 1 (I - II): Foregrad 1438 + 2850 3aJ (C5) 14 38 53.2 $+29 28 30$ $+72$ 0.2254 P <td>0939 + 0912</td> <td>HS(A854)</td> <td>09 39 20.9</td> <td>+09 12 00</td> <td>+42</td> <td>0.2075</td> <td>Е</td> <td>1</td> <td>II - III</td> <td>WKS</td>	0939 + 0912	HS(A854)	09 39 20.9	+09 12 00	+42	0.2075	Е	1	II - III	WKS
1044 + 0918 (FG)HS10 44 18, 2+09 19 37+560.0908EForegrad1044 + 0918HS(A1093)10 44 10, 9+09 18 53+560.226E1II - IIIA 1093A 114610 58 47, 1-22 27 34+340.137P4I - IIWKSA 151412 15 24, 4+20 57 00+800.200G3II - IIIA 155012 26 44, 6+47 58 00+690.254E3IIIA 175813 30 38, 7+50 49 01+650.280E3IIIA 1759/6013 31 40, 3+20 30 53+780.168:P3IIIA 141 + 29HS (A1878)14 10 39, 3+29 28 30+720.222G1(I - II):Foregrad1411 + 2914 10 39, 6+29 28 13+720.254P(I - II):Foregrad1438 + 28503aJ (C5)14 38 53, 2+28 50 00+660.248E2III1438 + 2850= A195214 38 53, 7+28 50 00+660.247EIII $\Delta V_r \sim 1$ 1438 + 2850= A195214 38 56, 2+28 50 12+660.141EForegrad1438 + 2850 (FG)14 41 10, 9+31 23 24+650.241G3(I - II):A 195714 44 208, 4+31 28 11+650.241G3II - III	A 963		10 14 05.8	+39 17 39	+56	0.207	E	3	II	WKS
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1044 + 0918 (FG)	HS	10 44 18.2	+09 19 37	+56	0.0908	Е		• • •	Foreground
A 1146 10 58 47.1 $-22 27 34$ $+34$ 0.137 P 4 I - II WKS A 1514 12 15 24.4 $+20 57 00$ $+80$ 0.200 G 3 II - III WKS A 1550 12 26 44.6 $+47 58 00$ $+69$ 0.254 E 3 II - III A 1758 13 30 38.7 $+50 49 01$ $+65$ 0.280 E 3 III A 1759/60 13 31 40.3 $+20 30 53$ $+78$ 0.168: P 3 III Not con 1411 + 29 14 10 39.6 $+29 28 30$ $+72$ 0.222 G 1 (I - II): 1438 + 2850 3aJ (C5) 14 38 53.2 $+28 28 13$ $+72$ 0.2254 P (I - II): 1438 + 2850 3aJ (C5) 14 38 53.2 $+28 28 13$ $+72$ 0.2254 P (I - II): 1438 + 2850 aJ (C5) 14 38 53.2 $+28 50 00$ $+66$ 0.247 E III $\Delta V_r \sim 1$ 1438 + 2850 (FG)	1044 + 0918	HS(A1093)	10 44 10.9	+09 18 53	+56	0,226	E	1	Ц – Ш	A 1093
A 1514 12 15 24.4 +20 57 00 +80 0.200 G 3 II - III A 1550 12 26 44.6 +47 58 00 +69 0.254 E 3 II - III A 1758 13 30 38.7 +50 49 01 +65 0.280 E 3 III A 1759/60 13 31 40.3 +20 30 53 +78 0.168: P 3 III Not con 1411 + 29 HS (A1878) 14 10 39.6 +29 28 30 +72 0.222 G 1 (I - II): Foregrad 1438 + 2850 3aJ (C5) 14 38 53.2 +28 50 00 +66 0.248 E 2 III 1438 + 2850 = A1952 14 38 53.7 +28 50 00 +66 0.247 E III $\Delta V_r \sim 1$ 1438 + 2850 = A1952 14 38 56.2 +28 50 12 +66 0.141 E Foregrad 1438 + 2850 (FG) 14 41 10.9 +31 23 24 +65 0.241 G 3 (I - II): A 1961 <	A 1146		10 58 47.1	-22 27 34	+34	0.137	Р	4	I - II	WKS
A 1550 12 26 44.6 +47 58 00 +69 0.254 E 3 II - III A 1758 13 30 38.7 +50 49 01 +65 0.280 E 3 III A 1759/60 13 31 40.3 +20 30 53 +78 0.168: P 3 III Not con 1411 + 29 HS (A1878) 14 10 39.3 +29 28 30 +72 0.222 G 1 (I - II): Foregrad 1431 + 29 14 10 39.6 +29 28 13 +72 0.224 P (I - II): Foregrad 1438 + 2850 3aJ (C5) 14 38 53.2 +28 50 00 +66 0.248 E 2 III 1438 + 2850 = A1952 14 38 53.7 +28 50 00 +66 0.247 E III $\Delta V_r \sim 1$ 1438 + 2850 = A1952 14 38 56.2 +28 50 12 +66 0.141 E Foregrad A 1957 14 41 10.9 +31 23 24 +65 0.241 G 3 (I - II): A 1961 <t< td=""><td>A 1514</td><td></td><td>12 15 24.4</td><td>+20 57 00</td><td>+ 80</td><td>0,200</td><td>G</td><td>3</td><td>II - III</td><td></td></t<>	A 1514		12 15 24.4	+20 57 00	+ 80	0,200	G	3	II - III	
A 1758 13 30 38.7 $+50 49 01$ $+65$ 0.280 E 3 III A 1759/60 13 31 40.3 $+20 30 53$ $+78$ 0.168: P 3 III Not con 1411 + 29 HS (A1878) 14 10 39.3 $+29 28 30$ $+72$ 0.222 G 1 (I - II): Foregrad 1411 + 29 14 10 39.6 $+29 28 13$ $+72$ 0.222 G 1 (I - II): Foregrad 1438 + 2850 3aJ (C5) 14 38 53.2 $+28 50 00$ $+66$ 0.248 E 2 III 1438 + 2850 = A1952 14 38 56.2 $+28 50 12$ $+66$ 0.414 E Foregrad 1438 + 2850 (FG) 14 41 10.9 $+31 23 24$ $+65$ 0.241 G 3 (I - II): 1438 + 2850 (FG) 14 41 10.9 $+31 23 24$ $+65$ 0.241 G 3 (I - II): A 1957 14 42 08.4 $+31 28 11$ $+65$ 0.234 E 3 III	A 1550	•••	12 26 44.6	+47 58 00	+69	0.254	Е	3	п - Ш	
A 1759/60 13 31 40.3 +20 30 53 +78 0.168: P 3 III Not con 1411 + 29 HS (A1878) 14 10 39.3 +29 28 30 +72 0.222 G 1 (I - II): Foregrad 1411 + 29 14 10 39.6 +29 28 13 +72 0.222 G 1 (I - II): Foregrad 1438 + 2850 3aJ (C5) 14 38 53.2 +28 50 00 +66 0.248 E 2 III 1438 + 2850 = A1952 14 38 53.7 +28 50 00 +66 0.247 E III $\Delta V_r \sim 1$ 1438 + 2850 = A1952 14 38 56.2 +28 50 12 +66 0.141 E Foregrad 1438 + 2850 (FG) 14 41 10.9 +31 23 24 +65 0.241 G 3 (I - II): A 1957 14 41 10.9 +31 23 12 +65 0.241 G 3 II - III A 1961 14 42 08.4 +31 28 11 +65 0.241 G II - III A 2111	A 1758		13 30 38.7	+50 49 01	+65	0.280	E	3	ш	
1411 + 29 HS (A1878) 14 10 39.3 +29 28 30 +72 0.222 G 1 (I - II): Foregrad 1411 + 29 14 10 39.6 +29 28 13 +72 0.224 P (I - II): Foregrad 1438 + 2850 3aJ (C5) 14 38 53.2 +28 50 00 +66 0.248 E 2 III 1438 + 2850 = A1952 14 38 53.7 +28 50 00 +66 0.248 E 2 III 1438 + 2850 = A1952 14 38 56.2 +28 50 12 +66 0.141 E Foregrad 1438 + 2850 (FG) 14 41 10.9 +31 23 24 +65 0.241 G 3 (I - II): A 1957 14 42 08.4 +31 28 11 +65 0.234 E 3 II - III A 1961 14 42 08.4 +31 28 11 +65 0.228 E 3 III A 2111 15 37 43.5 +34 35 12 +53 0.228 E 3 III	A 1759/60		13 31 40.3	+20 30 53	+78	0.168:	Р	3	ш	Not confirmed
$1411 + 29$ $14\ 10\ 39.6$ $+29\ 28\ 13$ $+72$ 0.254 P $(I - II):$ $1438 + 2850$ $3aJ(C5)$ $14\ 38\ 53.2$ $+28\ 50\ 00$ $+66$ 0.248 E 2 III $1438 + 2850$ $= A1952$ $14\ 38\ 53.7$ $+28\ 50\ 00$ $+66$ 0.248 E 2 III $1438 + 2850$ $= A1952$ $14\ 38\ 56.2$ $+28\ 50\ 02$ $+66$ 0.247 E III $\Delta V_r \sim 1$ $1438 + 2850$ (FG) $14\ 41\ 10.9$ $+31\ 23\ 24$ $+66$ 0.141 E Foregrad $A\ 1957$ $14\ 41\ 10.9$ $+31\ 23\ 24$ $+65$ 0.241 G 3 $(I - II):$ $A\ 1957$ $14\ 42\ 08.4$ $+31\ 28\ 11$ $+65$ 0.241 G 3 II - III $A\ 2111$ $15\ 37\ 43.5$ $+34\ 35\ 12$ $+53$ 0.228 E 3 III $A\ 2125$ $15\ 40\ 47.9$ $+66\ 25\ 41$ $+43$ 0.2465 4 II<-IIII	1411 + 29	HS (A1878)	14 10 39.3	+29 28 30	+72	0.222	G	1	(І – Ц):	Foreground?
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1411 +29	•••	14 10 39.6	+29 28 13	+72	0.254	Р		(І-Ц):	
$1438 + 2850$ = A1952 $14\ 38\ 53.7$ $+28\ 50\ 00$ $+66$ 0.247 E III $\Delta V_r \sim 1$ $1438 + 2850$ (FG) 14 38 56.2 $+28\ 50\ 12$ $+66$ 0.141 E Foregrowth A 1957 14 41 10.9 $+31\ 23\ 24$ $+65$ 0.241 G 3 (I - II): A 1961 14 42 08.4 $+31\ 28\ 11$ $+65$ 0.234 E 3 II - III A 2111 15 37\ 43.5 $+34\ 51\ 2$ $+53$ 0.228 E 3 III A 2125 15\ 40\ 47.9 $+66\ 25\ 41$ $+43$ 0.2465 E 4 II - III	1438 + 2850	3aI (C5)	14 38 53.2	+28 50 00	+66	0.248	E	2	ш	
1438 + 2850 (FG) 14 38 56.2 + 28 50 12 + 66 0.141 E Foregray A 1957 14 41 10.9 + 31 23 24 + 65 0.241 G 3 (I - II): A 1961 14 42 08.4 + 31 28 11 + 65 0.234 E 3 II - III A 2111 15 37 43.5 + 34 35 12 + 53 0.228 E 3 III A 2125 15 40 47.9 + 66 25 41 + 43 0.2465 E 4 II - III	1438 + 2850	= A1952	14 38 53.7	+28 50 00	+66	0,247	E		ш	$\Delta V_{\rm m} \sim 100 \ \rm k/s$
A 1957 14 41 10.9 +31 23 24 +65 0.241 G 3 (I - II): A 1961 14 42 08.4 +31 28 11 +65 0.234 E 3 II - III A 2111 15 37 43.5 +34 35 12 +53 0.228 E 3 III A 2125 15 40 47.9 +66 25 41 +43 0.2465 E 4 II - III	1438 + 2850 (FG)		14 38 56.2	+28 50 12	+66	0.141	Е			Foreground
A 1961 14 42 08.4 +31 28 11 +65 0.234 E 3 II - III A 2111 15 37 43.5 +34 35 12 +53 0.228 E 3 III A 2125 15 40 47.9 +66 25 41 +43 0.2465 E 4 II - III	A 1957		14 41 10.9	+31 23 24	+65	0.241	G	3	(I - II):	
A 2111 15 37 43.5 +34 35 12 +53 0.228 E 3 III A 2125 15 40 47.9 +66 25 41 +43 0.2465 E 4 II - III	A 1961		14 42 08.4	+31 28 11	+65	0.234	Е	3	ш - ш	
A 2125 15 40 47.9 +66 25 41 +43 0.2465 E 4 II - III	A 2111		15 37 43.5	+34 35 12	+53	0.228	Е	3	III	
	A 2125		15 40 47.9	$+66\ 25\ 41$	+43	0.2465	Е	4	II - III	
1613 + 3104 $3a_1$ (C7) 16 13 49.6 + 31 04 57 + 46 0.415 E	1613 + 3104	3aJ (C7)	16 13 49.6	+31 04 57	+46	0.415	E			

experimental emulsion. Many remote clusters have been found, and three of the brighter ones from the IIIaJ survey are included in the redshifts reported here.

b) Data

The redshifts were determined with the spectrograph in the two-prism mode, which gives a spectral resolution (including detector) of 7 Å at a dispersion of 125 Å mm⁻¹ at H γ . The measurements were made by cross-correlating the sky-subtracted spectrum of the unknown galaxy with a standard spectrum of the center of M31, shifted and degraded in resolution to match the cluster in question, as described by WKS (1975).

The results for 37 galaxies in or near 31 clusters are listed in Table 1. The cluster name (column [1]) is

either the Abell number, designated as A, or an HS 1952 survey cluster designated in standard notation by the 1950 right ascension and declination, or a IIIaJ survey cluster, named the same way. Column (2) is the survey source, if it is not an Abell cluster. Columns (3) and (4) are the coordinates of the observed galaxy as estimated from transparent overlays placed over photographs. The accuracy of the coordinates is generally better than 15 seconds of arc. Column (5) gives the galactic latitude. The measured redshift and its quality (excellent, good, fair, poor) are listed in columns (6) and (7). The richness class for the Abell clusters are given in column (8), and the Bautz-Morgan cluster type in column (9). These types were either taken from Sandage and Hardy (1973, Table 1) or were estimated by us from prints. Some of the redshifts have been previously published in WKS, as 690

noted in column (10), and are included here for convenience.

The accuracy of the tabulated redshifts is estimated to be about $\Delta z = \pm 0.001$. Several redshifts which were measured more than once reproduce to this accuracy. The listed redshifts have not been corrected for galactic rotation, since the correction is at most of the order of our accuracy, and in any case is negligible in the present context. The three foreground galaxies (A223, 1044+0918, 1438+2850) were expected to be foreground objects from their appearance on direct photographs.

The redshifts listed for the two galaxies in the cluster 1411+29 (A1878) differ by almost 10,000 km s⁻¹. Although neither spectrum is of the best quality and one is rather poor, there is clearly a large velocity

	TABLE 2	
PHOTOMETRY OF	16 CLUSTERS THAT HAVE NEW REDSHIFTS	

CLUSTER	OBJECT	z	ып	ap	V mag	B mag	R mag	B - V mag	V - R mag	V _{SM} mag	V _{SM} -A _v -K _v mag	log cz
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)
A 586	G1	0.172	+ 22 ⁰	12″2 18. 8	17.26 ± .022 16.74 ± .020	18.67 ± .035	16. 19 [±] . 027 15. 69 [±] . 021	1.41 ±.041	1.07 ±.035 1.05 ±.028	16.85	16.38	4.713
A 593	G1	0.226	+ 30	7.6 12.2 18.8	18.20 ± .023 18.06 ± .037	19.97 ± .061	17.51 ± .028 17.10 ± .017 16.99 ± .017	1.77 ±.065	1.10 ±.029 1.07 ±.041			
										18.04	17.46	4.831
A 639	G1	0.291:	+ 33	12,2	18.40 ± .037	••••	••••	••••	••••	18,30	17.48	4.941
A 777 $\Delta V (1-B) = 0.2 mag.$	G1 + A	0.226	+ 34	18.8	17.49 ±.022	19.27 ±.048	16.50 ± .022	1.78 ±.053	0.99 ±.031	17.49	17.49(G1)	4.831
4 (1 <i>b</i>) - 0.2 mag.	В	0.226	+ 34	12.2	18.84 ±.032	••••	17.72 ±.030		1.12 ±.044	18.68	18. 12(B)	
A 795	G1	0.1361	+ 40	12.2	16.89 ±.013	18.20 ±.019	15.90 ± .019	1.31 ±.023	0.99 ±.023	16.57	16.29	4.610
A 963 Double ∆m = 1.25	G1 + G2	0.207	+ 56	12. 2 18. 8	17.24 ± .016 17.07 ± .008	18.92 ± .019 18.79 ± .026	$16.14 \pm .008$ $16.01 \pm .036$	1.68 ±.025 1.72 ±.027	1.10 ±.018 1.06 ±.037	17.36	16.97	4.791
A 1146	G1	0.137	+ 34	12.2 18.8	16.59 ± .015 16.18 ± .009	18.22 ± .026 17.63 .023	15.61 ±.015 15.23 ±.028	1.63 ±.030 1.45 ±.025	0.98 ±.021 0.95 ±.029	16.20	15, 98	4.614
A 1514	G1	0.200	+ 80	12.2 18.8	17.71 [±] .010 17.39 [±] .012	19.34 ± .034 19.04 ± .026	16.67 ±.009 16.36 ±.018	1.63 ±.035 1.65 ±.029	1.04 ±.013 1.03 ±.022	17.44	17.05	4.778
A 1550 A triple. One dominant and two	GI	0.254	+ 69	12.2 18.8	18.09 ± .028 17.86 ± .025	19.79 ±.046	17.02 ±.024 16.79 ±.028	1.70 ±.054	1.07±.037 1.07±.037	17.93	17.34	4.883
A 1758	GI	0.280	+ 65	12.2	18 37 ± 028	20 12 ± 047	17 31 ± 038	1 75 ± 055	1.06 ± 047			
х. х.	01	0.200	1 00	18.8	$18.12 \pm .020$		16,95 ±.020		1. 17 ±.028	18.21	17.51	4.926
A 1759	G1	0.168:	+ 78	12.2 18.8	17.58 ±.017 17.43 ±.021	19.19 ±.018 19.01 ±.043	$16.57 \pm .013$ $16.44 \pm .011$	1.61 ±.024 1.58 ±.048	1.01 ±.021 0.99 ±.024	17.36	17.07	4.702
A 1957	A	0.241	+ 65	12.2	18.30 ±.040	19.97 ±.037	17.16 ± .030	1.67 ±.054	1.14 ±.050	18, 16	17.63	4.859
A 1961	G1	0.234	+ 64	12.2	17.57 ±.020	19.26 ± .034	16.50 ±.017	1.69 ±.039	1.07 ±.026	17.43	16.91	
	G2	* <u>#</u>	" - X -	12.2 18.8	17.72 ± .022 17.73 ± .053	19.46 ± .037	$16.65 \pm .014$ $16.55 \pm .033$	1.74 ±.043	1.07 ±.026 1.18 ±.062	17.66	17.14	4.850
A 2111	G1	0.228	+ 53	12.2 18.8	17.96 ± .012 17.68 ± .020	$19.70 \pm .031$ $19.37 \pm .032$	$16.91 \pm .013$ $16.60 \pm .024$	1.74 ±.033 1.69 ±.038	1.05 ±.018 1.08 ±.031	17.76	17.27	4, 835
A 2125 A is 3 galaxies	A	0.2465	+ 43	18, 8 30, 6	16.84 ±.016 16.62 ±.012	18.51 ± .038	15.71 ± .009 15.61 ± .022	1.67 ±.041	1.13 ±.018 1.01 ±.025 Single Bgts	17.67	17.07	1.00
	G3				17.93 ± .026	19.78 ± .054	16.90 ± .012 16.50 ± .025	1.85 ±.060	1.03 ±.029	17 66	17.06	4.869
0939 + 0912	K	0.2075	+ 42	12.2 18.8	17.82 ±.016 17.52:±.082	19.35 ±.031	$16.75 \pm .013$ $16.47 \pm .022$	1.53 ±.035	1.07 ±.021 1.05 ±.085	17.00	17.00	

© American Astronomical Society • Provided by the NASA Astrophysics Data System

1976ApJ...205..688S

difference. The smaller redshift galaxy is centrally located in the cluster, and is its brightest member, but it is photometrically peculiar, and may be a foreground object. This cluster will be discussed further in a later paper of this series.

The geometry of A222–223 is interesting. There are three separate condensations of galaxies lying nearly on a straight line 15'8 long. The entire configuration was listed by HS as a single field. The southwest condensation (z = 0.217) is listed by Abell as A222, while the northeast pair (separation 4'2) is apparently listed by Abell as a single cluster, A223. The galaxies listed as A223A and A223B in Table 1 are the brightest members of the northeast pair of condensations, and the similarity of their redshifts suggests that they are in fact at the same distance.

Abell (1958) gives positions for A1759 and A1760 which are only 2'.4 apart. Both are listed as richness 3, with appreciably different magnitudes (17.6 and 17.2). We do not find a similar configuration at the listed position, but rather a very extended grouping ($\sim 10'$ in diameter) with no striking subcondensations.

Table 1 suggests that the redshift limit of the Abell catalog is just less than z = 0.3. The HS survey clusters overlap the faint end of the Abell catalog and extend to larger redshifts (z = 0.39 for 0024+1654). We do not yet know the limits of the IIIaJ and 127-04 surveys. The brightest of the clusters from these special surveys were selected to overlap the faint end of the Abell survey, and the redshifts of the three clusters listed (z = 0.252, 0.283, and 0.415) indicate that this expectation is met. These clusters are well above the faint survey limit, and no serious attempt was made during these initial measurements to push to the faint-ness limits of the spectrograph.

III. MAGNITUDES AND COLORS

a) Measurements

Broad-band BVR photometry for 16 of the 31 clusters of Table 1 was done using the same procedures, techniques, filters, photocell (S20, FW130), and corrections previously used for a sample of nearer clusters (Sandage 1972b, Paper II).

Most of the galaxies were measured with two apertures to provide an internal check on the aperture correction to a standard metric diameter. The diameters used, in arcsec, are listed in column (5) of Table 2. Columns (6)–(8) give the magnitudes through the corresponding apertures. The tabulated magnitude errors are rms values, calculated from variations of the net counts over many individual 10 s integrations.¹

b) Corrections for Aperture Effect, K-Dimming, and Galactic Absorption

We have used the same aperture correction as for the nearer clusters (Sandage 1972*a*, Table 3). The aperture growth curve was adopted here as if $q_0 = +1$, which requires the argument of the curve to be log $[\theta z/(1 + z)^2]$. The results, however, are not very sensitive to this assumption, since the standard diameter is very large (86 kpc if $H_0 = 50$). At this diameter, the gradient of the growth curve is small, which ensures that the correction itself is nearly independent of q_0 because we are already close to an "asymptotic" magnitude. Stated differently, it does not much matter where we read the abscissa of the $\Delta m = f(\theta, z)$ function as long as θ is large enough so that the function is nearly flat. The difference in the aperture corrections between the $q_0 = +1$ case used here and the $q_0 = 0$ case (abscissa of the growth curve = log $[\theta z(1 + z/2)/(1 + z)^2]$) is only 0.03 mag at z = 0.28. Since

$$m = 5 \log cz + 1.086(1 - q_0)z + O(z^2) + C$$

(Robertson 1955), it follows than an error of 0.03 mag at z = 0.28 corresponds to an error $\delta q = \delta m/1.09z \approx$ 0.10, which is only 10 percent of the difference in the assumed values of q_0 between the two models.

assumed values of q_0 between the two models. The V magnitudes, reduced to the standard metric size by the adopted precepts, and denoted as $V_{\rm SM}$, are listed in column (11) of Table 2. Corrections for galactic absorption (Sandage 1973, Paper V) and for Kdimming (Whitford 1971) have been applied in column (12).

c) Extension of the Color-Redshift Relation

The observed colors from columns (9) and (10) of Table 2 are plotted as open circles versus redshift in Figure 1. The error bars are the listed rms values. The data for nearer clusters are shown as closed circles, and are taken from previous measurements [Paper II, Table 1; Paper V, Table 6]. The solid lines are the expected $K_B - K_V$ reddening trajectories from the measurements of Whitford (1971), calculated by him from his absolute energy distributions. The curve for V - R is taken from Table 5 of Paper V.

While the agreement between the observations and the predicted V - R values is satisfactory to within systematic differences of $\sim \pm 0.03$ in the range 0 < z < 0.5, it is not good in B - V. A systematic difference of ~0.06 mag exists for z > 0.2; the observed values are redder than the prediction. At present, we feel that the effect may not be real, but that it may be due to a combination of the technical problem mentioned above (footnote 1, § IIIa) and a possible breakdown of the defining equation (A7) of Matthews and Sandage (1963) that relates the natural b - v system to standard B - V colors. No calculations were made in that reference for such red stars, and special spectrum-scanner observations are required to rederive the necessary transformation equation for B - V > 1.6.

¹ A technical problem exists concerning the present photometry. Some of the galaxies are redder in B - V than the standard stars observed on the nights in question, and an extrapolation of about 0.3 mag was required in the transformations that relate $(b - v)_{natural}$ to B - V. The problem does not exist in V - R. The listed rms errors are from the photon statistics alone.

692

1976ApJ...205..688S



FIG. 1.—Observed colors of the brightest several E and S0 galaxies in clusters as a function of redshift. Open circles are the 16 new clusters with redshifts and photometry from Tables 1 and 2. Closed circles are for clusters with previous data (Sandage 1972b, Table 1; Sandage 1973, Table 6). Solid lines are from Whitford's (1971) calculated K-corrections for a standard elliptical galaxy.



FIG. 2.—The Hubble diagram for first-ranked members of 50 previously measured clusters (*open circles*), and for the 16 new clusters with photometry (*closed circles*). The magnitudes have been corrected for aperture effect, K-dimming, and galactic absorption. The line has the equation $V_c = 5 \log cz - 6.803$. The mean dispersion of the absolute magnitude of the first-ranked galaxy is 0.305 mag.

IV. RICHNESS CORRECTION

The data for the 16 new clusters are plotted as closed circles in Figure 2, together with 50 clusters (*open circles*) from previous work. The corrections to the magnitudes are for aperture effect, K-dimming, and galactic absorption only. The line has a slope of 5 as required by a linear velocity-distance relation in empty Euclidean space, or by a Friedmann model with $q_0 = +1$. (We do not mean to suggest that either of these models is true: the line is drawn only for convenience.) Its equation is $V_C \equiv V_{\rm SM} - K_V - A_V = 5 \log cz - 6.803$, where the constant has been adjusted for a zero mean residual for the open circles.

Two noteworthy features of Figure 2 are (1) the small dispersion in M_v^c of the 16 new points alone ($\sigma = 0.26$ mag), showing again the remarkably well defined mean absolute magnitude of the first-ranked cluster galaxy, and (2) the slight offset toward brighter magnitudes of the new data compared with the old. The difference amounts to $M_v^c(1) = 0.139 \pm 0.081$ mag which, although small, seems real. We believe that this difference is due to a weak correlation between M (brightest) and cluster richness, since there is a strong correlation between richness and redshift in our data. In the redshift range 0 < z < 0.12, the mean richness class is $\langle R \rangle = 0.6$, with all clusters in the range $0 \leq R \leq 2$. For redshifts 0.12 < z < 0.22 the mean richness is $\langle R \rangle = 3.3$.

Ideally, to sort out the richness correction from possible time-dependent effects such as deceleration and evolution one should examine the correction at each redshift from coeval data. To do this would No. 3, 1976

1976ApJ...205..688S

require extensive material, uniformly distributed in richness, over each small redshift interval. Such data do not now exist, and we have adopted a crude first approximation which seems to be all that can be supported by the data in hand. The principal change from earlier work is a substantial increase in the number of clusters with R = 3 and 4.

The data were split into the two redshift intervals 0 < z < 0.10 and 0.13 < z < 0.26, and within each interval a mean value of the quantity $5 \log cz - V_c$ was computed separately for the clusters in each richness class. The assumptions underlying this procedure are that M(1) for each richness class has a well-defined mean magnitude over a given redshift range, and that the function $M(\log cz)$ is adequately represented over the redshift range by a straight line of slope 5. Since the correction is so small (see below), these assumptions appear to be justified *a posteriori* for the present data.

The results are given in Table 3. Within each redshift range, there appears to be a small but systematic correlation between R and $\langle 5 \log cz - V_c \rangle$. Although the distribution of richness in the two redshift intervals is quite different, there is an overlap in richness classes 1 and 2. The values of $\langle 5 \log cz - V_c \rangle$ are not well determined, but they agree within the errors between the two redshift ranges, and we have adopted the simplifying assumption that there is a single correction over the entire redshift range considered. The values are given in the last part of Table 3.

The values of $\langle 5 \log cz - V_c \rangle$ with their rms errors are plotted in Figure 3, together with the older determinations (*open squares*) from Sandage and Hardy (1973, Table 4). Shown along the right-hand ordinate, and listed in the penultimate column of Table 3

TABLE 3

DEVIATIONS FROM THE MEAN HUBBLE LINE AS A FUNCTION OF RICHNESS IN TWO REDSHIFT RANGES

R	$\langle 5 \log cz - V_c \rangle$	п	$\sigma(M_v^c)$ (mag)
	0 < z <	0.10	
0 1 2	$\begin{array}{c} 6.746 \pm 0.074 \\ 6.793 \pm 0.058 \\ 6.837 \pm 0.148 \end{array}$	18 8 6	0.303 0.154 0.332
	0.13 < z	< 0.26	
1 2 3 4	$\begin{array}{c} 6.693 \pm 0.186 \\ 6.834 \pm 0.128 \\ 6.903 \pm 0.084 \\ 6.923 \pm 0.178 \end{array}$	5 5 15 4	0.373 0.257 0.315 0.308
R	$\begin{array}{c} \text{Mean} \\ \langle 5 \log cz - V_c \rangle \end{array}$	$\begin{array}{c} {\rm Adopt} \\ {\left< \Delta M_v \right>} \end{array}$	n
0 1 2 3 4	$\begin{array}{c} 6.746 \pm 0.074 \\ 6.755 \pm 0.072 \\ 6.835 \pm 0.090 \\ 6.903 \pm 0.084 \\ 6.923 \pm 0.178 \end{array}$	-0.07 -0.02 +0.02 +0.07 +0.12	18 13 11 15 4



FIG. 3.—Derived dependence of M(1) on cluster richness in two redshift ranges. The dependence derived earlier (Sandage and Hardy 1973, Table 4) is shown by open squares.

(bottom), are the values of the correction, $\langle M_v \rangle$, normalized to zero between richness class 1 and 2.

The most striking feature of the richness correction is that it is so small. This near independence of the brightness of the brightest member on the total membership of the cluster is also known to extend to groups with less than 10 members (Sandage 1975, Paper VIII), and this requires that the integrated luminosity function $\phi(M)$ for cluster galaxies be nearly vertical at the bright end, *if* the absolute magnitude of the first-ranked member is governed by the luminosity distribution of the fainter members. It can be shown that the slope of $\phi(M)$ at M(1) must be $d \log \phi(M)/dM \ge 5$ to explain the data of Figure 3 in this way.

V. CORRECTED HUBBLE DIAGRAM

a) Data

From the discussion in § IV, it is clear that the richness correction derived there will largely remove the "excess" brightness of the 16 new clusters. But the argument still seems somewhat tautological, and it will be desirable to reexamine the question with more extensive material in the future. Since there are very few nearby rich clusters ($R \ge 3$), the new data will have to be for distant sparse clusters.

In addition to the corrections discussed in § III and § IV, a further correction for Bautz-Morgan (BM) cluster type has been applied 2 to obtain the data in Table 4.

The columns of Table 4 are mostly self-explanatory. The richness class in column (4) is from the Abell catalog except for 0024 + 1654, which was estimated by us. As before, V_c magnitudes in column (6) are corrected only for aperture effect, K-dimming, and galactic absorption; the $V_c^{R,BM}$ values in column (7) are additionally corrected for richness and Bautz-Morgan effects.

The data in Table 4 are plotted in Figure 4. The equation of the line is

$$V_c^{R, BM} = 5 \log cz - 6.865$$
.

² Note the typographical error in $\Delta M_{\nu}^{c}(1)$ for BM type II–III in Table 3 of Sandage and Hardy (1973). The entry should read +0.05. All calculations here and in that paper were, however, made with the correct value: the error is in the table only.

SUMMARY OF PARAMETERS	FOR 66 CLUSTERS	WHICH HAVE FIRST	CLASS DATA

			P			- 12 DM	
CLUSTER (1)	ABELL (2)	z (3)	к (4)	ВМ (5)	V <u>C</u> (6)	^V C ^{K, DIVI} (7)	log cz (8)
	(27	EROM TAL					
VIRGO	••••	0,00379	(1)	ш	8.45	8.21	3.056
FORNAX		0.00509	(1)	п - ш	8.90	8.83	3.184
PEG I	•••	0,0128	(0)	ш	11.20	11.15	3.584
0122 + 3305	···	0.0170	(1)	ш п_ш	11.70	11.70	3.710
COMA	A 1656	0.0222	2	п-ш	(11.51)	11.55	3, 824
HERCULES	A 2151	0.0341	2	ũ	13.12	12,92	4.017
2308 + 0720	•••	0.0428	(0)	ш - ш	13.57	13.45	4.109
2322 + 1425	A 2589	0.0440	0	I	14.08	14.37	4.120
1145 + 5559	A 1377	0,0516	1	п - ш	14.39	14.32	4.191
0106 - 1536	A 151	0.0526	1	ш	14.03	14.03	4.198
1024 + 1039	A 1020	0.0649	1		14.81	14.57	4.290
1239 ± 1852 1520 ± 2754	A 1589	0.0718	0	ш-ш	14.52	14.40	4.333
1520 + 2754 0705 + 3506	A 568	0.0779	0	п - Ш	15.15	15.03	4.369
1513 ± 0433	A 2048	0.0944	1	ш	15, 50	15.26	4,452
1431 + 3146	A 1930	0.1312	ĩ	ш	16.06	15,82	4.595
1055 + 5702	A 1132	0.1345	1	п - ш	15.93	15,86	4.606
1153 + 2341	A 1413	0.1426	3	I	15.46	15.89	4.631
1641 + 1327	A 2224	0.1499	3	ш	16.61	16.46	4.652
1534 + 3749	A 2100	0.1532	3	ш	16.55	16.40	4.662
0025 + 2223	A 31	0.1594	2	. Ш.	16.58	16.38	4.680
1228 + 1050	A 1553	0.1651	2	п-ш	16.90	16.87	4.695
0138 ± 1832 1200 0105	A 234	0.1745	1	ш.	1/.1/	17.19	4.714
1309 = 0105	A 1677	0.1/45	4	п – п	16,95	16 70	4.719
1304 + 3110 0925 + 2044	A 801	0.1917	2	и. П. П	16.54	16, 69	4,760
1253 + 4422	A 1643	0. 1979	1	III	17.66	17.42	4.774
0855 + 0321	A 732	0.2018	1	ц-ш	17.07	17.00	4.782
1447 + 2617	•••	0.36	(2)	н - ш	18.77	18,74	5.033
0024 + 1654	•••	0.392	(2)	ш	18.34	18.14	5.0 <u>57</u>
		3C RAI	DIO CLUSTER	S			
3C 31		0.0169	(0)	TT	11.90	11.61	3, 706
3C 40	A 194	0.0180	0	Π	12.24	12, 19	3,732
3C 66	A 347	0.0215	0	п - ш	12.69	12.57	3.810
3C 465	A 2634	0.0301	1	I - II	13.06	13.17	3.956
3C 338	A 2199	0.0303	2	I	12.53	12.91	3,958
3C 317	A 2052	0.0351	0	п	13.38	13.33	4.022
M23-112	(A 2638)	0.0825	2	ш	15.33	15,13	4.394
3C 219	••• A 115	0, 1745	(2)	ш	10.88	16,92	4,719
3C 295	A 115	0.461	<u>(1)</u>	I	18.63	18.97	5,141
	WEST	ERLUND AND WA	LL (SOME A	RE HMS GROUP	S)		
·····			* .				
0036 + 03	•••	0.0145	0	ш	12.11	11.82	3.697
0152 - 30	•••	0.0298	0	111	13.19	12.90	3.951
0133 + 03	•••	0.0100	0	ц т	13 50 13 50	13 27	J 104
1245 - 41	•••	0.0113	2	'n	10-90	10.94	3,498
1332 - 33		0.0114	õ	Ĩ	10.87	11.16	3,535
1400 - 33		0.0138	Ő	Ī	11.01	11,30	3,617
2152 - 69	•••	0.0266	0		13,19	•••	3,902
2247 + 11	•••	0,0268	00	ш	12,40	12.11	3.906
		THE 16 N	EW CLUSTER	RS HERE			
0729 + 3144	A 586	0.172	3	I II	16 38	16 58	4, 713
0746 + 7254	A 593	0.226	3	II - III	17.46	17.49	4, 831
0815 + 6804	A 639	0.291?	3	ш - ш	17.48	17.50	4.941
0923 + 7830	A 777	0,226?	4	11 - 111	17.49	17.56	4.831
0921 + 1423	A 795	0.1357	3	и - ш	16.29	16.31	4.610
1014 + 3917	A 963	0,206	3	ш	16 . 97	17.06	4.791
1058 - 2227	A 1146	0.137	4	I - II	15.98	16.23	4.614
1215 + 2057	A 1514	0.200	3	ш - ш	17.05	17.07	4.778
1226 + 4758	A 1550	0.2545	3	ш - ш	17.34	17.36	4.883
1330 + 5049	A 1758	0.281	3	ш	17.51	17.36	4.926
1001 + 2000	A 1057	0 241	3	(I = II)•	17 62	10,92	4.702
1442 + 3128	A 1061	0.236	3	ц-ш): ц-ш	17.03	17.60	4, 850
1537 + 3435	A 2111	0.228	3	JII - III	17.27	17.12	4, 835
1540 + 6625	A 2125	0.2465	4	ш - Ш	17.07	17.14	4.869
0939 + 0912	•••	0.206	(3)	и - ш	17,15	17.17	4.791
			-				

(HŠ).



FIG. 4.—The Hubble diagram using fully corrected magnitudes (aperture effect, K-effect, absorption, Bautz-Morgan type, and richness) with the same coding as in Fig. 2. The line has the equation $V_c^{R,BM} = 5 \log cz - 6.865$.

The mean magnitude difference $M_v^{R, BM}$ between the open and closed circles is now reduced to 0.034 \pm 0.076 mag, which is negligible. The dispersion in $M_c^{R,BM}$ for the total sample is 0.276 mag (n = 65).

b) General Comments

The new material is too limited to justify a new discussion of the formal value of q_0 . However, from previous solutions, it is clear that q_0 (formal) = $+1 \pm \sim 0.3$ (with no evolutionary correction applied) will fit the new data well. In particular, there is no indication from the closed circles in Figure 4 that the points are curving from the $q_0(\text{formal}) = +1$ line toward fainter magnitudes, nor that 3C 295 is abnormally bright. We do not confirm the conclusions of Gunn and Oke (1975) in these two matters for reasons which are not understood at the moment. Much more data are needed at considerably larger redshifts to make progress in these problems, at which time a detailed comparison of the two independent sets of data should be profitable.

The expectations are good that such data will soon be available. The markings in Figure 4 show the progressive extension of the diagram from Slipher's last observations in 1922, through Humason's redshift of NGC 7619 in 1929, to his very large advances in 1931, 1936, and 1956, and finally to Minkowski's (1960) last point at 3C 295. The Humason 1956 limit, which is the cutoff for photographic absorption line spectra, has been the effective limit until very recent years. The three points beyond $\log cz = 5$ are all special cases: 3C 295 was measured by Minkowski on the basis of a single very strong $\lambda 3727$ emission line, and the redshifts for 0024 + 1654 and 1447 + 2617were obtained photometrically by Baum (1962) and later by Oke (1971). But the limit has now been transcended by new instruments, including, among others, Oke's multichannel scanner, Wampler and Robinson's image-dissector scanner (IDS), and our SIT-prism spectrograph. Recent absorption-line measurements of z = 0.64 for 3C 123 by Spinrad (1975), using the IDS, and z = 0.53 for 3C 330 by us show what can routinely be expected in the next few years, and offer considerable new hope for the resolution of the problem of q_0 via the Hubble diagram, plus necessary evolutionary corrections.

This work was supported in part by the National Science Foundation under grant GP-36450 X to the Carnegie Institution of Washington.

REFERENCES

. 1957, in *Carnegie Yrb.*, Vol. **56** (Washington: Carnegie Institution of Washington), p. 62. Humason, M. L., and Sandage, A. 1957, in *Carnegie Yrb.*, Vol. **56** (Washington: Carnegie Institution of Washington), p. 62 Whitford, A. E. 1971, Ap. J., 169, 215.

ALLAN SANDAGE and JEROME KRISTIAN: Hale Observatories, 813 Santa Barbara Street, Pasadena, CA 91101 JAMES A. WESTPHAL: California Institute of Technology, Geological and Planetary Sciences (170-25), Pasadena, CA 91125