THE STELLAR CONTENT AND DISTANCE OF THE GALAXY NGC 2403 IN THE M81 GROUP

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ABSTRACT

Fifty-nine variables have been found in the nearby Sc galaxy NGC 2403, which is a member of the M81 group. Of these, seventeen are Cepheids ranging in period from 87 d48 to 20 d230; eight are very bright irregular blue variables of the type previously found in M31 and M33; seventeen are bright, red irregular supergiant variables similar to those in h and χ Per; there is one eclipsing binary; and sixteen are unclassified variables of undetermined nature. NGC 2403 is the first galaxy outside the Local Group in which Cepheids have been detected.

Light-curves have been detected.

Light-curves have been determined relative to a photoelectric sequence of seventy-three stars which covers the interval from B=9.15 to B=22.70, V=8.39 to V=21.80. Three-color photoelectric observations of the sequence stars brighter than V=19.5 show that the local reddening due to the galactic system is E(B-V)=0.06 mag. The period-luminosity relations for Cepheids in B and V at maximum light provide two well-determined upper envelope fits to the standard P-L function, giving apparent distance moduli of NGC 2403 of $(m-M)_{AB}=27.80\pm0.1$ and $(m-M)_{AV}=27.75\pm0.1$. These reduce to true moduli of $(m-M)_{0,B}=27.56$, and $(m-M)_{0,V}=27.57$ from the

Cepheids alone.

Four other distance indicators give closely comparable values. (1) Star counts across the face of NGC Four other distance indicators give closely comparable values. (1) Star counts across the face of NGC 2403, corrected for foreground contamination, give B = 18.25 for the brightest resolved stars. Previous calibration of $M_B = -9.3$ in galaxies of the Local Group gives $(m - M)_{AB} = 27.55$. (2) The brightest blue irregular variable occurs at $B(\max) = 18.2$, giving $(m - M)_{AB} = 27.5 \pm 0.2$ if $M_B(\max) = -9.3$ is adopted from M31 and M33. (3) The brightest irregular red variable occurs at $V(\max) = 19.98$, $B(\max) = 22.02$. Calibration via the LMC, NGC 6822, and the SMC gives a preliminary value of $M_V(\max) = -8.00$, $M_B(\max) = -6.00$ for these stars, giving apparent moduli of $(m - M)_{AB} = 28.02$, and $(m - M)_{AV} = 27.98$. (4) The angular sizes of the largest, and mean of the first five largest H II regions, calibrated via the LMC and M33, give $(m - M)_{0,L} = 27.54 \pm 0.18$ and $(m - M)_{0,5} = 27.52 \pm 0.40$. The average of all methods is given in Table 12 as $(m - M)_0 = 27.55 \pm 0.13$ (AD). The agreement between the methods is good and provides evidence that no systematic difference exists from galaxy to galaxy among methods is good and provides evidence that no systematic difference exists from galaxy to galaxy among the various distance indicators.

One unexpected result is that the red supergiants, both constant and variable, may be a new and precise distance indicator. There appears to be an upper envelope to the absolute luminosity of these stars at about $M_V = -8.0$. Such red stars can be located with ease in all Sc and Irr galaxies with $(m - M)_{AV} < 29$ by comparing red and blue plates and, therefore, they can be important in an intermediate step for the redetermination of the Hubble constant.

The ratio of mean redshift of the M81 group—each galaxy corrected individually for solar motion—to the distance to NGC 2403 of $r=(3.25\pm0.20)\times10^6$ pc is $v/r=(65\pm15)$ km sec⁻¹ Mpc⁻¹. This is not claimed to have any relation to the Hubble constant because the sample contains only one group, but similar analysis of many additional groups may eventually lead to an adequate value of H.

I. INTRODUCTION

NGC 2403 ($\alpha_{1950} = 7^h32^m0$, $\delta = +65^\circ43'$; $l^{II} = 151^\circ$, $b^{II} = +29^\circ$) is a bright, relatively nearby galaxy beyond the Local Group which closely resembles M33 in stellar content and spiral structure. It has a small or possibly nonexistent nucleus, broad and ill-defined spiral arms, and pronounced resolution into stars beginning at $B \simeq 18.3$ mag. Both galaxies are late Sc systems in the Hubble classification, Sc⁺ in Holmberg's system (1958), Sc III by van den Bergh (1960), and aS4 according to Morgan's system (1958). The galaxy is illustrated in The Hubble Atlas of Galaxies (Sandage 1961).

The galaxy forms the western terminus of the group whose central and most prom-

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inent member is M81 (Holmberg 1950), and which includes NGC 2366, M82, NGC 3077, NGC 2976, IC 2574, NGC 4236, Ho I, Ho II, and at least six faint red dwarf elliptical galaxies of the Sculptor and Fornax type (Bowen 1954). This group, together with the M101 group (Holmberg 1950), is of major importance in the systematic redetermination of the Hubble constant, because the galaxies in both are near enough that their stellar contents are highly resolved. Bright stars, H II regions, normal novae, and several types of variable stars can be identified with certainty on plates taken with large reflectors. To determine the Hubble constant these indicators must be calibrated in the nearby groups and then must be located and measured in more distant galaxies where the cosmological redshift becomes significantly larger than the random motions. The M81 and M101 groups do, for the first time, yield to major resolution with the 200-inch reflector, a circumstance which increases substantially the number of galaxies available for the calibration study.

When the Hale telescope went into routine operation in 1949, Hubble, with the help of other members of the nebular department, began a systematic search for variable stars in NGC 2403, M81, M101, and NGC 5194. The first Cepheids outside the Local Group were found in the initial phases of the study, and by 1953 Hubble had isolated twenty-seven variables of various types in NGC 2403, of which seven were definitely Cepheids for which preliminary periods could be assigned.

The problem was continued after Hubble's death, and a report of progress on NGC 2403 and M81 was published in 1954 (Sandage 1954). More plates were obtained until the close of the observing season in 1963, and the present paper is a discussion of the material now available. This is the first of a projected series of reports on the redetermination of the Hubble constant. Future papers will deal with the variables in M81, the variables and resolved stars in M101, the calibration of the linear size of the largest H II regions in Sc and Irr galaxies, and the application of these distance indicators to galaxies out to redshifts of about 2000 km/sec where the angular size of the largest H II region region is expected to be close to 2".

II. THE PHOTOGRAPHIC MATERIAL

A total of one hundred sixty blue and twenty-two yellow plates are available, covering a time interval from 1910 to 1963. The early plates from 1910 to 1938, twenty-nine in number, were taken with the 60-inch reflector on Mount Wilson by Ritchey, Pease, Duncan, Smith, Hubble, and Baade. No 100-inch plates are available because the galaxy is too far north to be reached by this telescope, due to its particular yoke-type mounting.

The 200-inch material consists of 115 blue plates, taken with Eastman 103aO emulsion, and sixteen photovisual plates taken with Eastman 103aD emulsion. After 1951, most of the blue plates were taken behind either a Schott GG1, a Schott WG2, or a Schott GG13 filter of 2 mm thickness to eliminate the spectral region shortward of $\lambda \simeq 3800$ Å. No filter was used before that date. The photovisual plates were taken behind a Schott GG11 filter, or occasionally behind a Schott GG14, again of 2 mm thickness, a system which defines a band pass from $\lambda \simeq 5100$ Å to $\lambda \simeq 6300$ Å.

No color equation has been applied to magnitudes determined from the blue plates taken with or without filters. The effect is negligible in all cases where the colors of the sequence stars are similar to the color of the relevant variable star, and the correction for other variables is so much smaller than other errors that it has been neglected. However, the secondary sequence stars are strictly on the B, V system because all transfers from the primary photoelectric sequence were made on plates taken with the standard filters of this system.

Plate information such as name, date, exposure time, and quality is listed in the relevant tables given in the Appendix. The notation, standard at the Observatories until recently, gives the telescope designation as suffix, the running personal number of each observer, and the last name initial of the observer. The telescope designation is S for

60-inch and PH for Palomar-Hale (the 200-inch). The observer's initials are Ri(Ritchey), P(Pease), SS(Sinclair Smith), D(Duncan), H(Hubble), MH(Humason), M(Minkowski), B(Baade), Bm(Baum), A(Arp), and S(Sandage). Thus, plate S-454-H is the 454th plate taken by Hubble at the 60-inch.

III. THE MAGNITUDE SEQUENCES

a) Photoelectric Data

A primary photoelectric sequence of seventy-three stars was determined with the 60- and 200-inch telescopes during the 1958–1964 observing seasons. The photometry brighter than V=19.5 presented no particular difficulties because stars could be visually centered in the measuring diaphragm at the prime focus of the 200-inch telescope. Positions for sky readings were determined by inspection of the best plates with limiting magnitude fainter than B=23.5 mag, V=22.5 mag. The mean photometric error for stars brighter than V=19.5 is about ± 0.02 mag in all three colors.

Measurement of stars fainter than V=19.5 required blind offset procedures. Stars for the sequence were chosen from photographic plates so as to be relatively free of background. The X and Y offsets of the faint stars relative to selected bright stars were measured on the plates and were used at the telescope after adjustment insured that the orientation of the photometer base corresponded with the orientation of the plate previously measured in the laboratory.

Uncertainties of the final magnitude values for stars fainter than about V=21.5 arise because there is no assurance that the regions chosen for the sky readings are free from contaminating stars fainter than the plate limit. The influence of such stars on the photoelectric values can be considerable. For example, a star of B=21.4 mag would be measured 0.5 mag too faint if the comparison sky region is contaminated with four stars of B=24.0 mag, or 0.5 mag too bright, if the contaminating stars are in the object hole.

Errors of this size are expected in the NGC 2403 field according to the following calculation. A circular measuring aperture of 6.77 diameter was usually used for the faintest stars, and this corresponds to a column through NGC 2403 of 8.8×10^3 pc² cross-sectional area, or a volume of 2.6×10^6 pc³ for a thickness of the disk of 300 pc, assuming a true modulus of m-M=27.56 as derived later. The sequence stars are located in the outer regions of NGC 2403 where the surface brightness is comparable to that of the solar neighborhood in the galactic system. Taking McCuskey's (1966) luminosity function for the solar neighborhood at $M_B=-3.8$ (corresponding to an observed B=24.0 in NGC 2403 at its apparent blue modulus of $[m-M|_{AB}=27.8)$, gives 10^{-6} stars per pc³ within the 1-mag interval centered at $M_B=-3.8$. From this, one would expect an average of 2.6 stars of $B=24.0\pm0.5$ mag within the diaphragm. This value will vary from star to star depending on the actual background.

Because the effect is statistical and occurs with both signs, the average of many sequence stars should closely define a true Pogson scale. For this reason, we have smoothed the photoelectric sequence by eye estimates using a step-scale plate selected from a library of such plates made with the 200-inch in different seeing conditions. The smoothing was done for all photoelectric stars fainter than B=18.24 on seven blue and four yellow plates, each measured three times. The mean of the smoothed values is adopted as the primary magnitude sequence as listed in Table 1. The stars are identified in Figure 1 (Plate 2). The magnitude differences between the adopted values and the direct photoelectric values are shown in Figure 2. The agreement is excellent over the entire range.

A check on both the scale and the zero point of this primary sequence was made by measurement of four photographic transfers from SA 51 to NGC 2403 made on nights of excellent seeing. The photoelectric sequence in SA 51 (Baum, unpublished) extends to B = 22.35. Three of the four transfers gave concordant results, while the fourth

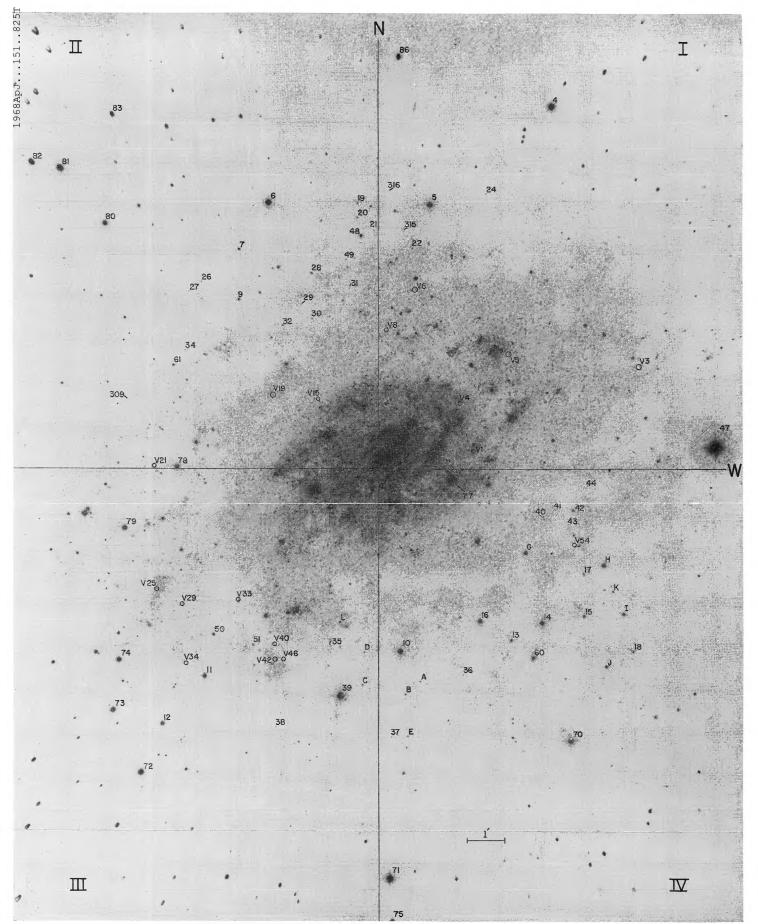


Fig. 1.—Identification chart for the photoelectric standards of Table 1, reproduced from a 200-inch plate of 30-min exposure on Eastman 103aO emulsion behind a Schott GG1 filter. The 17 Cepheids are also identified with their variable star numbers of Table 5.

 ${\tt TABLE\ 1}$ PHOTOELECTRIC STANDARDS AND THE ADOPTED SEQUENCE

				<u> </u>		Photoelectric		Ado	pted
No.	B	hotoelecti	ric U	No.	В	V	U	В	V
BD+65°394.	9 15	8 39	9 50	9 .	17 72	16 85	18 21		
47 .	10 36	9 35	11 14	28 .	18 16	17 21	18 77		
77	11 32	10 57	11 66	19	18 24	17 40	18 48	18 26±0 03	17 38±0 04
71 .	12 58	12 01	12 57	K	18 25	17 65	18 29	18 24±0 03	17 65±0 03
39 .	12 68	11 86	13 05	17	18 37	17 91	18 24	18 40±0 02	17 95±0 04
4	12 81	12 14	12 96	В.	19 12	18 82	19 24	19 04±0 04	18 67±0 07
70 .	13 26	12 91	13 34	32 .	19 25	18 36		19 23±0 01	18 47±0 02
81 .	13 30	12 57	13 60	c	19 51±0 03	18 31±0 01	20 65±0 12	19 49±0 01	18 39±0 04
6.	13 31	12 77	13 23	20 .	19 73±0 02	18 80±0 04	20 39±0 08	19 78±0 03	18 82±0 04
5 .	13 379	12 858	13 311	22 .	19.79±0 01	18 97±0 03	20 11±0 11	19 78±0 02	19 04±0 05
10 .	13 473	12 862	13 404	D	19 85±0 01	18 51±0 03	20 73±0 11	19 88±0 02	18 43±0 07
72 .	13 54	13 05	13 50	A	19 86±0 01	18 40±0 03		19 86±0 03	18 33±0 05
73 .	14 06	13 30	14 28	30 .	19 90±0 03	(19 52±0 06)	20 09±0 11	19 88±0 03	19 97±0 02
14 .	14 069	13 146	14 651	Е	20 08±0 04	18 71±0 01	21 24±0 08	20 09±0 03	18 74±0 05
75 .	14 21	13.65	14 20	43 .	20 37±0 01	20 55±0 09	20 43±0 06	20 43±0 01	20 60±0 03
74	14 29	13.37	14 95	36	20 58±0 01	19 15±0 01		20 61±0 07	19 10±0 02
78	14 34	13 52	14 71	34 .	20 65±0 02	19 65±0 03		20 68±0 01	19 59±0 03
80 .	14 43	13 47	15 14	44	20 82±0 04	19 89±0 03		20 81±0 02	19 80±0 04
79 .	14 46	13 78	14.60	38	20 84±0 02	20 86±0 06	21 10±0 10	20 85±0 05	20 95±0 04
16	14 597	14 068	14 536	24 .	20 88±0 02	19 30±0 04	••	20 82±0 04	19 18±0 07
82 .	14 62	14.07	14 63	26	21 11±0 02	21 05±0 08		20 89±0 05	21 06±0 04
н.	14 64	13 94	14 83	49 {	21 09±0 05	19 75±0 04		} 20 87±0 06	19.71±0 03
86	14 66	14 16	14 59		21 19±0 05*	19 71±0 04*		,	
12	14 82	14 21	14 80	21	21 18±0 05	19 84±0 03		21 19±0 04	19 88±0 02
G	14 91	14 33	14 91	41 .	21 22±0 07	19.59±0 04		21 33±0 10	19 67±0 03
11	14 96	14 46	14 87	37	21 27±0 04	21 29±0 11		21 20±0.07	21 17±0 08
60	15 31	14.67	15 43	ĺſ	(21 88±0 11)	(21 22±0 14)]	
83	15 430	14 825	15 49	35	(22 80±0 15)	(21 40±0 18)		21 40±0 05	20 85±0 04
I	15 83	15 18	15 91	\	(22 15±0.10)*	(21 19±0 16)*		J	
48	16 20	15 65	16 14	27 .	21 55±0 06	21 33±0 05	21 05±0 05	21 53±0 05	21 31±0 03
13 .	16 311	15 771	16 229	315	21 74±0 10	20 22±0 08	•	21 86±0 07	20 16±0 02
J	16 32	15 40	16 98	31 {	(21 59±0 04)	20 20±0 06		} 21 98±0 02	20 18±0 04
42	16 52	15 66	17 00	, ,	21 81±0 10*	(20 49±0 09)*		99 04.0 05	01 60.0 00
50	16 62	16 02	16.62	309	22 22±0 17			22 04±0.05	21.62±0.02
15 . 61	16.65 17 41	15 98 16 76	16 70 17 45	316	(21 91±0 16) 22 65±0.15*	21.60±0 19	• •••••	22 54±0 04	21.75
	17 41	16 85	17 45		22 65±0.15* 22 66±0 04	(22 52±0 15	• • • • • • •	,	
L , 7 .	17 47	16 49		29	(23 22±0 23)*	(22 32±0 15 (22 38±0 30)*	•	22 67	21 67
	l .	Į.			('	••		
18	17 55	16 50		40	22 76±0 10	21 79±0 15	•• ••	22 70	21 80
51	17 71	16 90	18 13						

^{*}Data obtained by pulse-counting techniques; all other values are from D $\,$ C $\,$ methods using a strip-chart recorder

differed in zero point from the other three by 0.25 mag and was discarded. The magnitude of sixty secondary standards, listed among others in Table 2 as discussed in § IIIb were determined in NGC 2403 by step-scale estimates of the transfer plates measured in the order SA 51-NGC 2403-SA 51, each pair of plates measured three times. Independent magnitudes of these sixty stars were also determined by internal measurements of the NGC 2403 plates themselves relative to the adopted primary sequence of Table 1. The mean difference between the primary and the secondary sequence (tied now to SA 51) is $+0.03 \pm 0.01$ mag in the range 20.0 < B < 21.0; -0.03 ± 0.01 for 21.0 < B < 22.0; and $+0.02 \pm 0.02$ for 22.0 < B < 22.5, in the sense primary minus secondary. The agreement is excellent and shows that the scale and zero point of the primary sequence have negligible error to at least B = 22.5.

Most of the bright photoelectric stars of Table 1 were measured only once except for the following cases: Nos. 39(three 200-inch), 6(three 60-inch), 5[3(60), 2(200)], 10[5(60), 10(200)], 14[5(60), 7(200)], 16[3(60), 4(200)], 13[3(60), 1(200)], 15[2(60), 1(200)], and 7[2(60)]. The mean errors quoted in Table 1 for the photoelectric values

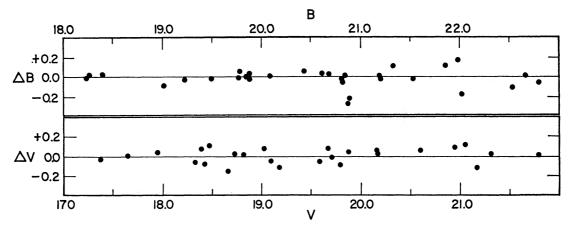


Fig. 2.—Comparison between the adopted and the photoelectric values for stars in Table 1, in the sense "adopted" minus photoelectric. The comparison in B is given at the top, and V at the bottom.

fainter than B = 19.51 were computed from the internal consistency of the many separate star *minus* sky values which make up each determination. The mean errors of the adopted values were obtained from the internal consistency of the eye estimates from the smoothing process.

Finally, Table 1 lists individual photoelectric values for five faint stars remeasured by pulse-counting techniques near the end of the calibration program where the D.C. values could not be reconciled with the smoothed adopted values. Such unreconciled values are listed in parentheses in Table 1. We believe that the large differences between the photoelectric values themselves and between the mean of these values and the adopted sequence is a result of severe background problems of the type already discussed. The adopted sequence is to be preferred.

b) Secondary Sequences

A sequence of secondary magnitude standards was determined near each variable star by step-scale estimates relative to the adopted sequence. Values for 174 stars were determined from seven blue plates and four yellow plates. Each star was estimated three times on each plate except for those stars near the center of the galaxy in heavy background, where six estimates per star on each plate were made. Table 2 lists the adopted secondary sequences near each of the seventeen Cepheids discussed in § VI. The sequence has been extrapolated from the photoelectric limit at B = 22.70 (star 40)

SECONDARY STANDARDS USED FOR CEPHEIDS AND FOR THE ECLIPSING BINARY V55 TABLE 2

r†	(21.8 20.84 (21.8	21.77 (21.8 21.62	21.7	21.62 21.77 (21.8 21.62		21.47 21.45 20.18 21.7 21.67
В	22.66 22.72 22.82	22.60 22.75 22.93	22.58 22.90 23.05	22.60 22.75 22.93	of V46) of V46) 22.74 22.87 23.1	le)? 21.78 21.93 21.98 22.35 22.45
Star*	209 <i>b</i> 209 <i>a</i> 209 <i>c</i> (<i>b</i>)	$203 \\ 202 \\ 201(c) \\ b \\ a$	$200 \ 200a \ 200b(c) \ b$	204 203 202 201(c)	b (South of Ve a (South of Ve 322a 22 322c(c) 23 b	a(variab 217 218 31 220a 220 29
Variable	V34	V40	V42	V46	V54	V55
V+	21.47 21.45 21.7 (21.7	21.34	21.7	21.8 (21.8 20.37 21.29	21.43 19.87 21.29 21.43	19.87
В	21.78 21.93 22.35 22.48		22.53		21.51 21.69 21.89 22.08 21.32 21.32	
Star*	217 218 220 219	221(c) b a 216 215	212	$213 \\ 212a(b) \\ a \\ 211 \\ 208$	209 210 210 <i>a</i> 210 <i>b</i> 208	210 210c(b) a 205 205 207 205a(b) a
Variable	V15	V19	V21	V25	V29	V33
1.4	21.7 21.8 20.86	(21.8	21.7 (21.8	21.09 21.33 21.54 21.54	21.58 21.74 (21.8 21.8	20.98 (21.8 (21.8
В	21.88 22.10 22.36	21.97 22.54 23.1	22.31 22.67	21.45 21.87 22.27 22.28 22.58	22.12 22.63 22.63 22.70 22.95	22. 02 22. 31 22. 85
Star*	277 279 278 a	318a 318b 318c(c) b a	281 280(c) b a	230 229 227 228 228(6)	224 2254 225 225 225a(c) b	a 223 223 223a(b) a
Variable	V1	V3	ν4	V5	V6	. : :

*The single-letter designations in parentheses for secondary standards are used in Table A1 for the upper end of the arbitrary Argelander scale, which is described in § VI and in the Appendix.
† The symbol "(" means "fainter than."

to $B \simeq 23.0$ by means of the step scales. The mean internal error of a tabulated magnitude is about ± 0.05 mag. The magnitudes of those stars near the center of the galaxy in heavy background are more uncertain with systematic errors perhaps as high as ± 0.2 mag.

Table 3 lists the additional sequence stars which were used in magnitude estimates for the remaining, non-Cepheid, variables discussed in later sections.

All secondary sequence stars and variables are identified on the large-scale charts of Figures 3-6 (Plates 3-6). The stars are numbered from 200 to 295 in the intermediate and inner regions of the galaxy, and from 300 to 320 in the extreme outer zone. Stars between numbers 245 and 295 lie in regions of heavy background and are undoubtedly affected by the substantial systematic errors quoted above $(\pm 0.2 \text{ mag})$.

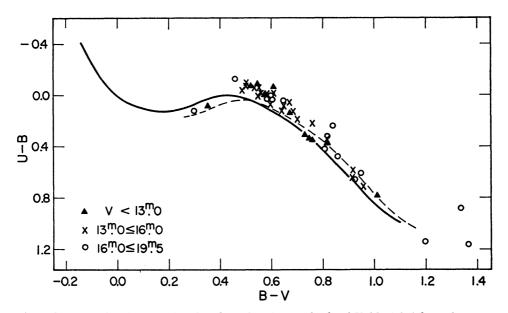


Fig. 7.—The two-color diagram for the photoelectric standards of Table 1 brighter than V = 19.5, coded according to magnitude. The solid line is the unreddened relation. The dashed line represents E(B - V) = 0.06 mag.

IV. REDDENING DUE TO ABSORPTION WITHIN THE GALACTIC SYSTEM

Figure 7 shows the two-color diagram for the photoelectric standards of Table 1 brighter than V=19.5, coded according to magnitude interval. The standard unreddened relation is drawn as a solid line. The distribution of stars above the standard line in the color interval 0.45 < B - V < 0.7 cannot be explained by reddening alone, but is undoubtedly caused by a combination of reddening and blanketing. The separation of the two effects, although possible in principle (Eggen and Sandage 1964), is difficult with any precision unless the data are of exceptional quality. Nevertheless, we have used the separation method, adopting the plausible shifts of $\Delta(B-V)=0.00$, $\Delta(U-B)=-0.10$; and $\Delta(B-V)=+0.04$, $\Delta(U-B)=0.00$ along the color axes for two separate color intervals centered at B-V=0.6 and B-V=0.8. The results, obtained by simultaneous solution of the two relevant equations, are E(B-V)=0.066 and E(B-V)=0.052, respectively.

A second estimate is obtained by considering only those stars with B - V > 0.8 where the effects of blanketing are effectively guillotined by the steepness of the blanketing vector in the two-color plane. These stars give E(B - V) = 0.06 as shown by the dashed line shifted along a reddening trajectory by this amount.

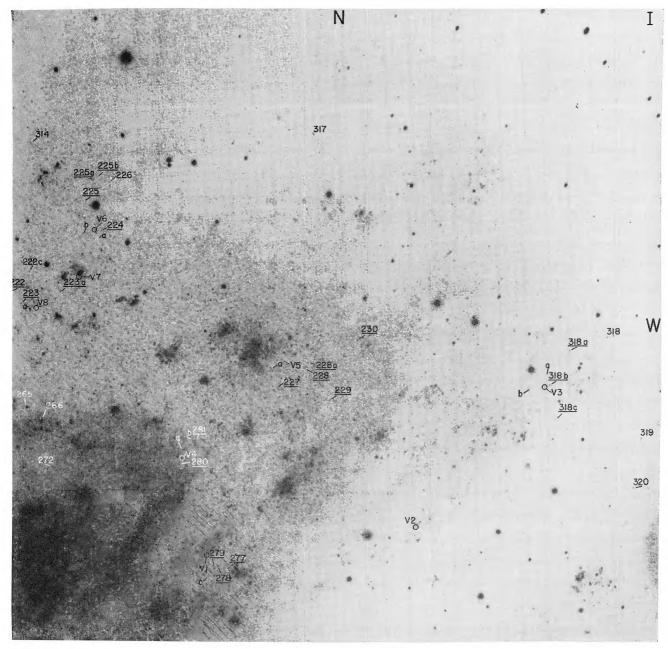


Fig. 3.—Enlargement of Fig. 1 showing Sector I in the N.W. quadrant of NGC 2403. All variable stars, together with the secondary standard stars of Tables 2 and 3, are identified.

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PLATE 4

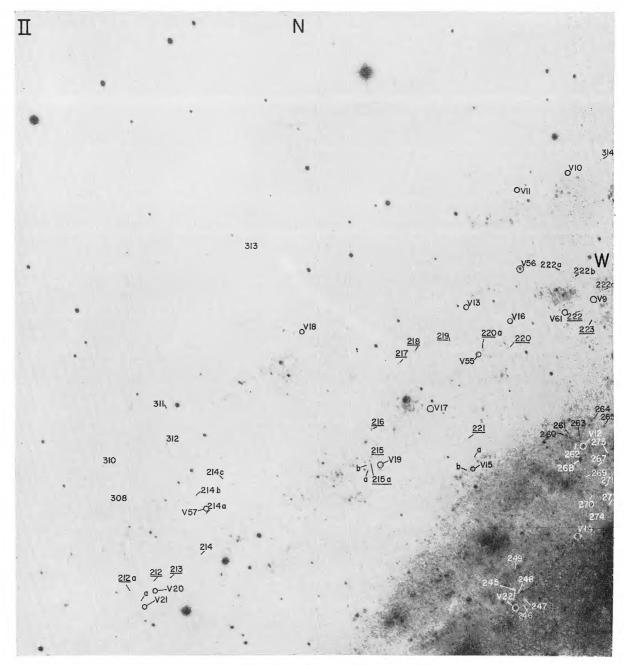


Fig. 4.—Same as Fig. 3 but for Sector II in the N.E. quadrant $\,$

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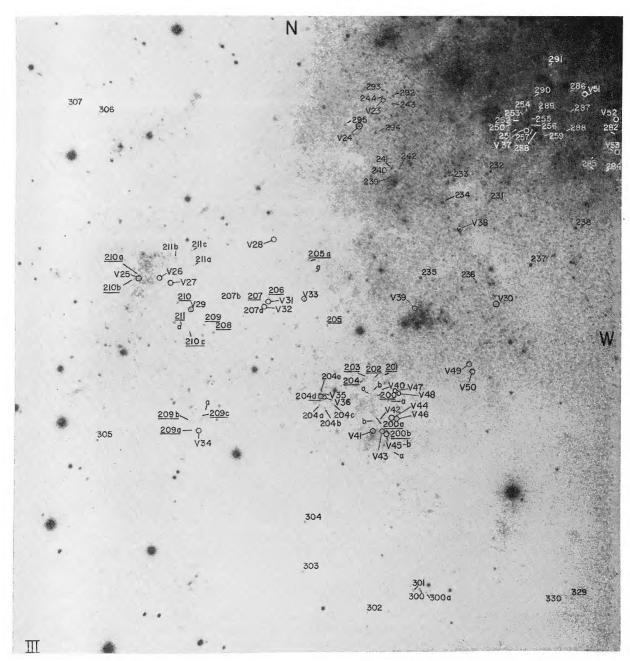


Fig. 5.—Same as Fig. 3 but for Sector III in the S.E. quadrant

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PLATE 6

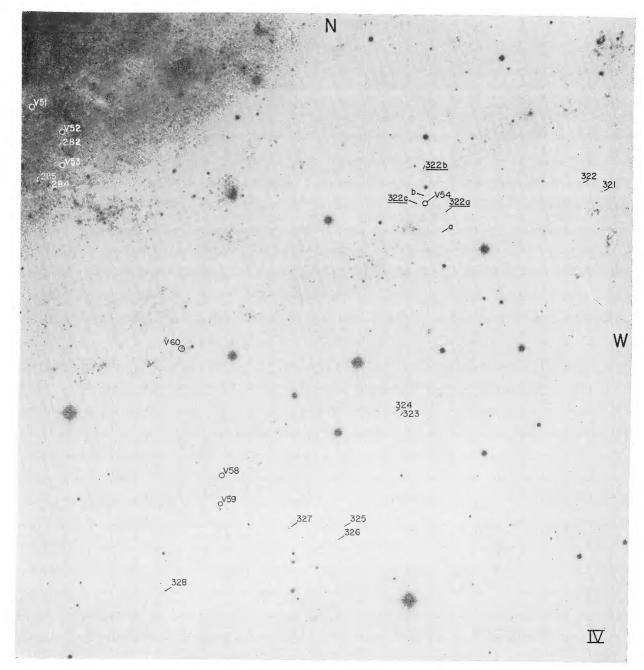


Fig. 6.—Same as Fig. 3 but for Sector IV in the S.W. quadrant

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TABLE 3

ADDITIONAL SECONDARY STANDARDS IN NGC 2403

Quadrant and Remarks*	
٨	21. 23 20. 63 20. 63 20. 87 20. 87 20. 87 20. 36 20. 36 20. 36 20. 36 21. 48 21. 48 21. 45 21. 45 21
В	20. 15 20. 26 20. 34 20. 36 20. 36 20. 36 20. 36 20. 37 20. 38 20. 38 20
No.	290. 291. 292. 293. 294. 294. 295. 300a. 30a. 3
Quadrant and Remarks*	HILLING POPULATION POP
<i>N</i>	21. 14 (21. 31 (21. 31 (21. 31 (21. 31 (21. 31 (21. 32 (21. 32 (21. 32 (21. 33 (21. 32 (21. 33 (21. 33
В	21. 94 20. 62 20. 62 21. 39 20. 62 20. 62 20. 62 20. 63 20. 63 20. 39 20. 32 20. 32 20. 32 20. 33 20. 33 20
No.	248 249 250 251 251 251 251 251 251 251 251 261 261 261 261 261 261 261 261 261 26
Quadrant and Remarks*	
7	2012 2012 2012 2012 2012 2012 2012 2012
B	22.22.22.22.22.22.23.34.34.35.35.35.35.35.35.35.35.35.35.35.35.35.
No.	2045. 2046. 2046. 2046. 2046. 2046. 2011b. 2012b. 2014. 2012b. 2014b. 20

*Diffuse images denoted by "d"; heavy background denoted by "b."

We adopt $E(B-V)=0.06\pm0.015$ in the subsequent discussion, although the value is unexpectedly low. Hubble's cosecant law, with an absorption half-thickness of $A_B=0.25$ mag predicts $A_B=0.52$ or E(B-V)=0.13 at the latitude of NGC 2403 if a normal ratio of $A_B/E(B-V)=4$ is used. The difference of this prediction from the observed value means either that the normal absorption-to-reddening ratio does not hold in regions out of the plane, as the colors of some high-latitude objects have often suggested, or that NGC 2403 is in a direction of abnormally high transparency. Until the problem of $A_B/E(B-V)$ in high latitudes is solved, we adopt this latter view and accept $A_B=0.24$ mag, $A_V=0.18$ mag for the galactic absorption between us and NGC 2403.

V. SEARCH FOR VARIABLES

By the end of 1953, Hubble had marked at least twenty possible variables in NGC 2403, seven of which were definitely Cepheids. We have confirmed all of his suspects, have added new variables from the complete plate material, and have confirmed four of Hubble's suggested periods for the Cepheids.

We wish to comment on the extreme difficulty of work on variable stars at the exceedingly faint light levels encountered here. None of the Cepheids become brighter than B=21.2 at maximum light, and most are fainter than B=22.0 at maximum. Due to the inevitable variation of plate quality caused by differences in seeing, slight inaccuracies of focus, and a small and variable astigmatism of the 200-inch mirror from 1949 to 1955 (typically 0.4 mm difference of focus in the two perpendicular astigmatic planes out of a total focal length of 18644 mm) for declinations north of $+60^{\circ}$, images near the plate limit show large variations in structure and surface brightness. Slight variations in the grain clumpiness, small changes of emulsion sensitivity, and variations of background density also contribute to the problem. It is often impossible to prove if an actual change of intensity between two plates of different quality has taken place for a given star. Often, inspection of a large fraction of the plate material is necessary before the variability of the faintest stars can be proved. Because of these factors, Hubble's early detection of Cepheids in galaxies outside the Local Group must be considered a remarkable achievement.

When the complete plate material was available, we began a new systematic search for variables over the face of the galaxy. Twenty-seven pairs of plates of comparable quality were blinked, and about eighty suspected variables were marked. All of Hubble's original suspects were rediscovered in this search.

Twenty additional faint suspects were added by successive inspections of small regions of NGC 2403 with a hand magnifier. The complete list of one hundred prospects was reduced to fifty-nine by inspection of all the available plate material. This final sample still contains several stars for which variability could not be established with complete certainty, but these stars have been retained to simplify future work. The fifty-nine variables are identified in Figures 1 and 3–6 (Plates 2 and 3–6).

The variables are separated into the following classes: (1) seventeen definite Cepheids for which light-curves and periods are derived; (2) eight very bright blue variables with irregular light-curves like those found in M31 and M33 (Hubble and Sandage 1953); (3) seventeen bright, very red variables with irregular light-curves similar to the supergiant stars in h and χ Per; (4) one eclipsing binary whose light-curve resembles β Lyrae; (5) sixteen unclassified variables among which are undoubtedly Cepheids of undetermined period. Most of the unclassified variables are fainter than B = 22.5 at maximum.

Table 4 contains a summary of the classification of the variables, together with the sector number of Figures 3-6 (Plates 3-6) within which the star is located, and remarks on previous discovery. The type symbols used in the table are: Cepheid (δ) , bright blue (BB), bright red (BR), eclipsing (E), unclassified (U), and irregular (I). Details for certain stars are given in later sections under the appropriate class designation.

We cannot accurately determine the completeness of our search. However, from the

rediscovery of all of Hubble's variables, and by a thorough search of the available good plates, we estimate that all variables have been discovered which are (1) brighter than $B \simeq 22.0$ mag; (2) have amplitudes greater than 0.5 mag; (3) lie outside the dense background of the central parts of the galaxy; and (4) are uncrowded by companions. Variables which fulfil the same local requirements of background and crowding and which are brighter than B = 22.5 at maximum should have been found if their amplitudes are greater than 1 mag. The discovery of variables fainter than this limit must be quite incomplete.

VI. THE CEPHEIDS

Figures 8 and 9 show the light-curves for the seventeen definite Cepheids, arranged in order of period. Magnitude estimates for each variable were made relative to the appropriate secondary standards of Table 2. Three independent estimates were made

TABLE 4
CLASSIFICATION AND FINDING DIRECTORY FOR THE VARIABLES IN NGC 2403

No.	Туре	Quad- rant	Re- marks*	No	Туре	Quad- rant	Re- marks*	No.	Туре	Quad- rant	Re- marks*
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15	δ BR δ δ δ BR δ BR U, δ? BR BB U, I? BB		H H H	21 22 23. 24 25. 26 27 28 29 30 31 32 33. 34	δ BB U, δ? Constant δ U, δ? BR U, I? δ BR BR BR δ δ BB		H H H H	41 42 44	BR δ BR U, δ? U, δ? δ U, δ? U, δ? U, δ? Constant BB BB δ E	III	н
16 17. 18. 19. 20	BR U, Ε? U, Ι? δ U, δ?	11 11 11 11 11	H H H H H	36 37 38. 39 40	BB BB BB BR δ		M H	56 57 58. 59 60 61.	U BR BR U, I? BR BR	II II IV IV IV II	

^{*} H and M refer to previous discoveries by Hubble and by N. U. Mayall.

on each plate for each variable in such a way that no memory of previous estimates was available. The mean error of the final magnitudes, listed in Tables A1 and A2 of the Appendix, depends on plate quality, on the regional background density, and on the apparent brightness. The mean error is not greater than ± 0.05 mag for variables brighter than B=22.8, V=21.6 on good quality plates and in regions of light background.

A horizontal line is drawn within the blue light-curve for each variable in Figures 8 and 9. Fainter than this line no numerical magnitude values are available due to differences of background, blends, and lack of suitable nearby secondary standards; rather, only estimates relative to arbitrary standards are available. The ordinate magnitude values do not, therefore, apply for any variable below the line.

Although most of the Cepheids become fainter than the sequence limit at B=23.0 during part of their cycle, intensity estimates fainter than this limit are important for period determinations. An uncalibrated Argelander method was employed, using several very faint comparison stars labeled c, b, and a near each Cepheid, as identified in Fig-

ures 3-6 (Plates 3-6). Star c is always the brightest of the sequence, and the notation is such that c2b means that the star is fainter than c, but brighter than b, and is 0.2 of the way from c to b. In cases where the variable is still fainter than the faintest comparison star, an open Argelander scale is used such that a4 means fainter than a by four arbitrary steps. The estimates are given in the tables of the Appendix.

The adopted elements of the seventeen Cepheids are given in Table 5, listed in order of period. Column (2) gives the uncertainty of the period as determined by inspection of the effect of slightly different trial periods on the conciseness of the light-curve. Column (4) is the epoch of maximum near J.D. 2435500. Columns (5) and (6) list the observed B and V magnitudes at maximum light. These values, corrected for galactic absorption, are given in columns (7) and (8). Column (9) gives B - V at maximum

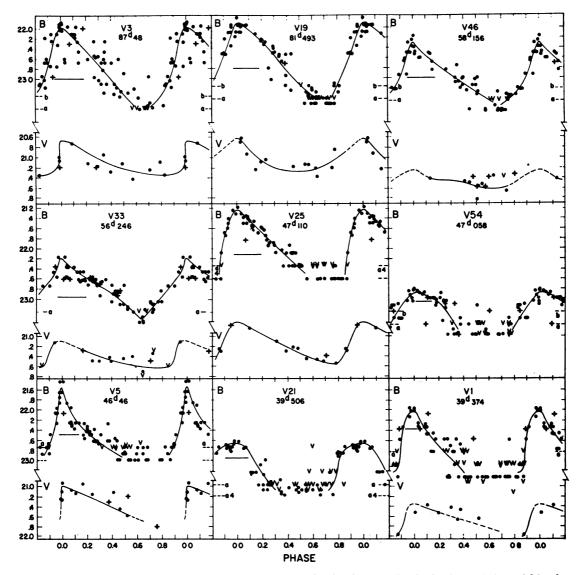


Fig. 8.—Light-curves in B and V for the first 9 Cepheids of Table 5. The horizontal line within the B light-curve of each variable shows the limit fainter than which no numerical magnitude estimates are available, and therefore, in the region where the ordinate values do not apply. The plus signs indicate uncertain values. The inverted carets indicate "fainter than." The magnitudes are from Tables A1 and A2 of the Appendix.

light as corrected only for E(B-V)=0.06 galactic reddening. No correction has been applied for internal reddening in NGC 2403, as justified in § XII. Column (10) shows the difference between column (9) and the ridge line of the period-color relation for Cepheids in galaxies of the Local Group as derived elsewhere (Sandage and Tammann 1968, Fig. 6). A positive sign indicates that the NGC 2403 variables are redder than the normal relation. Columns (11) and (12) list the magnitude residuals in B and V of each variable from the ridge-line of the adopted period-luminosity relation at maximum light

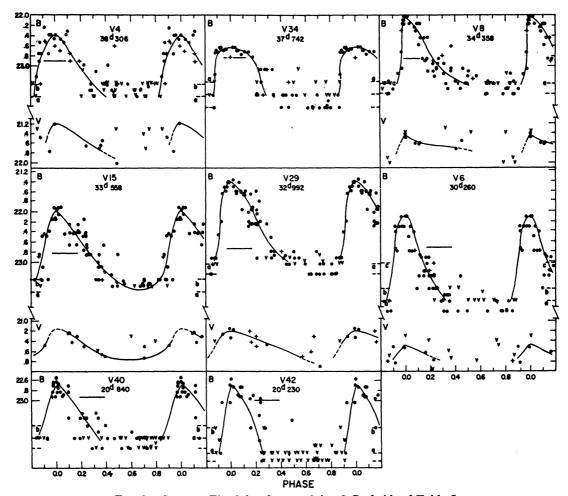


Fig. 9.—Same as Fig. 8 for the remaining 8 Cepheids of Table 5

(Sandage and Tammann 1968, Fig. 5, Table A1), using a true modulus of $(m - M)_0 = 27.56$ for NGC 2403 as derived later. Column (13) lists the background density upon which the Cepheid lies. The abbreviations are I for light, m(medium), h(heavy), vh(very heavy), and bl(blends).

Because nearly all Cepheids decline below the plate limit at minimum light, no information is available on the amplitudes of light variation. To follow the variables through the entire cycle would require plates and a magnitude sequence reaching nearly a full magnitude below what we now possess.

Comments on particular Cepheids are as follows:

V3: The abnormally large scatter of the light-curve is unexplained. It is not due to variations from cycle to cycle, because magnitude estimates within a single cycle contribute to the full scatter.

TABLE 5
PARAMETERS FOR THE 17 CEPHEIDS

Bkg (13)	ml mh vh vh vh vh ml ml mh ml mh ml
R _V (12)	+ + + + + + + + + + + + + + + + + + +
$R_B \tag{11}$	++++++++++++++++++++++++++++++++++++++
$\delta(B-V) \tag{10}$	++++++++++++++++++++++++++++++++++++++
(B-V)° max (9)	1. 23 1. 21 1. 00: 1. 02: 0. 45 1. 03: 0. 60 1. 12 1. 04: 0. 50 0. 57 0. 57 0. 57
V° max (8)	20.50 20.46 21.07: 20.93 20.82 20.82 21.4: 21.02 21.24: 21.27 21.27 21.27 21.27 21.27 21.27 21.27 21.27 21.27
B° max (7)	21.73 22.07 21.95 21.95 21.95 22.63 22.78 22.78 22.38 21.77 21.77 21.74 22.38 22.46:
V _{max} (6)	20.02 21.25 21.25 21.25 21.25 21.25 21.45 21.45 21.45 21.78
B _{max} (5)	22.197 22.197 22.197 22.197 22.197 22.197 22.107 22
Epoch J.D. 2435503+ (4)	36.9 286.9 15.9 27.7 286.9 27.7 22.2 22.2 23.3 24.3 25.3 25.3 27.3 27.3 27.3 27.3 27.3 27.3 27.3 27
log <i>P</i> (3)	1.942 1.911 1.765 1.673 1.673 1.673 1.597 1.595 1.595 1.536 1.536 1.536 1.536 1.536 1.536 1.536 1.536 1.536 1.536 1.536 1.536
ϵ (<i>P</i>)	0.42 0.66 0.3 0.03 0.05 0.05 0.05 0.05 0.05 0.05
P (days) (1)	87 48 81.493 58.156 56.246 47.110 47.058 39.506 39.374 38.374 38.374 38.374 38.376 39.506 37.30 37.42 38.306 37.42 38.306 37.4354 38.306 37.202 37.20
No.	25533. 25533. 25533. 2573. 2573. 260. 279. 279. 279. 279. 279. 279. 279. 279

V25: This brightest of all Cepheids lies at the edge of a bright patch of a spiral arm. Two neighboring stars, 3" distant, are of comparable brightness and cause difficulties in the magnitude estimates fainter than $B \simeq 22.1$. The star cannot be followed with any accuracy below B = 22.6. There is no reason, however, to expect inaccuracies in $B(\max)$ and $V(\max)$.

V54: This faintest and reddest of all variables lies in the center of the best-defined outer spiral arm. The star undoubtedly suffers from local obscuration. The tabulated

magnitudes are the mean of four estimates. The period is not beyond doubt.

V1 and V4: Discovered by Hubble, these variables are the innermost Cepheids yet known in this Galaxy. Hubble believed them to be novae from his study of the partial material available in 1952, but later rejected this possibility. The very heavy background makes the magnitude estimates extremely difficult. The period of V4 is not beyond doubt.

V34: A brighter comparison, 2'' distant, makes magnitude estimates difficult fainter than B = 22.8. However, $B(\max)$ should be accurate.

V8: Situated in a spiral arm and surrounded by faint companions. Magnitude estimates fainter than $B(\max)$ and $V(\max)$ are uncertain on plates of poor seeing.

V15: Although on rather heavy background and surrounded by faint, nearby stars, this Cepheid is one of the few for which the light-curve is determined through minimum. However, the minimum lies, as in all other cases, well beyond the photoelectric sequence.

V29: This is the bluest of the Cepheids by a very large margin. Although the abnormal color could be caused by an unseen bright blue companion, such cannot be the case here because the variable has an amplitude of at least $A_B = 1.6$ mag which is close to the maximum amplitude of $A_B \simeq 1.9$ mag at log P = 1.52 (Kraft 1961, Fig. 5) for galactic Cepheids. Although the star is among the brightest of the Cepheids in $B(\max)$, we accept the star as single and use it in the upper-envelope fit to the P-L relation in § XII.

V40: Due to its faintness, B(max) is not well determined.

V42: The period is not beyond doubt because the star is below the plate limit (invisible) on most of our available plate material.

VII. THE VERY BRIGHT BLUE VARIABLES

a) Light-Curves

Five certain (Nos. 12, 22, 35, 37, and 38) and three probable (Nos. 14, 52, and 53) bright blue irregular variables of the M31 and M33 type (Hubble and Sandage 1953) have been found in NGC 2403. Light-curves in B for the interval from 1910 to 1963 are shown in Figure 10 for seven of the stars; the eighth member is the remarkable variable V12 illustrated in Figure 11. The individual B and V magnitude values are listed in Tables A3 and A4 of the Appendix. The magnitudes before 1950 are determined from the 60-inch reflector plates, and it is interesting to note that the limiting magnitude of that telescope was about $B \simeq 21.5$ in the early days of its operation.

The light-curves of V22, V35, V37, and V38 are quite similar. They have relatively small amplitudes of about 2 mag and characteristic fluctuation times of several years. There is also clear similarity in light variations and colors between these variables and their prototypes in M31 and M33. Values of B-V, obtained from the estimated V magnitudes of Table A4 in the Appendix, combined with interpolated B magnitudes

from the light-curves, are indicated in Figures 10 and 11.

The colors and magnitudes show that the stars are F supergiants in the most extreme upper region of the H-R diagram where incipient pulsational instability, perhaps of the type discussed by Ledoux (1941) and by Schwarzschild and Härm (1959), is present. The stars are presumably very massive and may be just below the mass limit of disruptive instability ($M \simeq 60~M_{\odot}$). There are no stable stars, either in this galaxy or in M33 and M31, brighter than the brightest of these variables.

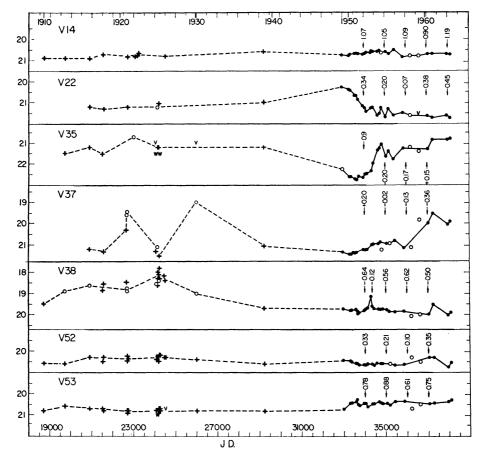


Fig. 10.—Light-curves in B for 7 of the 8 bright blue irregular variables listed in Table 6 from 1910 to 1963. The magnitudes are from Table A3 of the Appendix.

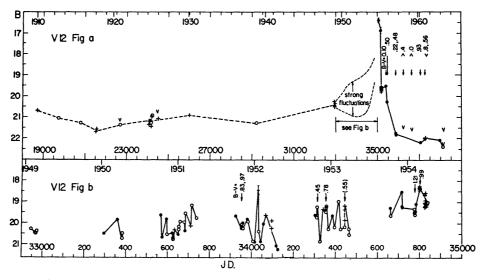


Fig. 11.—Light-curve in B for the bright blue irregular variable V12. The upper panel illustrates the variation from 1910 to 1963. The lower panel shows the variations from 1949 to 1954 on an expanded time scale.

The variations of V14, V52, and V53 are not as pronounced as for the variables just discussed. The fluctuations are small, with a total amplitude of only 0.5 mag. Each plate was estimated five times, and although we are rather convinced that the light variations are real, the case is not proved conclusively.

The most remarkable of the variables is V12 shown in Figure 11a and b. The star behaved in a normal manner, fluctuating irregularly around $B \simeq 21$ with a total range of about 1 mag until 1950, at which time large, short-period variations began which lasted until the beginning of 1955. During the 4-year interval beginning in 1950, the star would often vary by 1 mag between observing periods of 10 days. The variations were so unusual in 1951, 1952, and 1953 that we believed at first that the star might be a field RR Lyrae variable superposed upon the field. In 1954, a special series of plates was obtained in a 4-night interval with the 60-inch (Plates S-247-S to S-266-S in March, 1954; see Table A3) to check for night-to-night variations. Although the seeing was exceedingly poor, the star was visible on all plates and seems to vary by about 0.5 mag from night to night, although this result is not beyond doubt.

During the 7-month interval between the last plate in April, 1954, and the first plate of the 1954/1955 season, taken on November 2/3, 1954, V12 underwent a major outburst, reaching B=16.46. The absolute magnitude of V12 was $M_B=-11.3$ on this date, adopting an apparent blue modulus of $(m-M)_{AB}=27.80$ as derived later, but in view of the subsequent rapid decline, the star may have been even brighter before this time. During the outburst, V12 was by far the brightest object in NGC 2403.

The variable declined rather smoothly at a rate of about 0.20 mag/month during the first 825 days after the observed maximum, until it reached B = 21.8 in February, 1957. The star then dropped below B = 22 and has remained fainter than this level on all subsequent plates.

V12 is similar in some respects to the remarkable galactic star η Carinae. The history of this star has been reviewed by Gratton (1963), where references to the extensive earlier literature can be found. The star η Car reached apparent visual magnitude of -1 in 1843, remained near V=0 until 1855, after which it declined over a period of 15 years to $V \simeq 8$. After 1941 it began a steady increase from $B \simeq 8.5$ in 1940 to $B \simeq 7.1$ in 1952 (de Vaucouleurs 1952; de Vaucouleurs and Eggen 1952; O'Connell 1956; Gratton 1963). Adopting Gratton's apparent visual modulus of $(m-M)_{AV}=11.6$ gives $M_V(\max)=-12.6$ for η Car, which is of the same order as V12 in NGC 2403.

The general spectral characteristics of η Car are also similar to the bright blue variables in galaxies. Bok (1930) concluded from his study of objective-prism plates taken at Arequipa between 1889 and 1893 that the spectral type of η Car was cF5. A subsequent analysis by Whitney (1952) supports this conclusion. The spectral type assigned by Hubble and Sandage (1953) to the variables in M31 and M33 was supergiant F, with P Cyg absorption characteristics for M33 Var B, as are also present in η Car (Gratton 1963).

Finally, the color of η Car was $C_P = +0.42$ in 1952 (de Vaucouleurs and Eggen 1952), which is consistent with the colors of the bright blue variables in NGC 2403, M31, and M33.

b) Absolute Magnitudes

Table 6 lists some of the photometric properties of these variables, calculated with an apparent blue modulus of $(m-M)_{AB}=27.80$ for NGC 2403. The mean blue absolute luminosity at maximum, excluding V12, is $\langle M_B(\max)\rangle = -8.0 \pm 0.8$ (AD), which is considerably fainter and has a larger dispersion than the variables in M31 and M33 for which the following new calibration is available. Direct photoelectric calibration (Sandage, unpublished) of the sequence stars used by Hubble and Sandage in M33 shows that $B-m_{pg}(HS)=+0.1$ near $m_{pg}=15.5$, which is the relevant range. This correction, together with the apparent blue modulus of $(m-M)_{AB}=24.84$ for M31,

based on the definitive work of Baade and Swope (1963), together with $(m - M)_{AB} = 24.74$ for M33 gives $M_B(\text{max}) = -9.1$ for M31, V19; -9.2 (M33,V2); -8.9 (M33,A); -9.5 (M33,B); and -9.3 (M33,C) for a mean of $\langle M_B(\text{max}) \rangle = -9.2 \pm 0.16$ (AD).

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Unpublished data also now exist for seven members of the class in M81. If $(m-M)_{AB}=27.8$ applies, then the individual $M_B(\max)$ values for these new variables are -7.3, -9.1, -9.4, -8.4, -7.4, -8.3, and -8.3 giving $\langle M_B(\max) \rangle_{M81} = -8.3 \pm 0.6$ (AD), which again is considerably fainter than for M31 and M33. It is, however, interesting to note that the *brightest* variable in each galaxy defines a more comparable sample. The values for the four galaxies in question are $M_B(\max) = -9.5$ for M33, $B_{ij}=0.6$ (NGC 2403,V38); -9.1 (M31,V19); and -9.4 (M81).

We can summarize the results as follows. The twenty members of the class now known (one in M31, four in M33, eight in NGC 2403, and seven in M81) suggest that (1) the range of $M_B(\max)$ is about 3 mag, and (2) $M_B(\max)$ for the first-ranked variable appears to be a good statistic with $\langle M_B(\max) \rangle_{1st} = -9.4 \pm 0.2$ (AD), if the occasional

TABLE 6

Data for the Bright Blue Irregular Variables

V	B (D	P (:)	DATE AT MIN	Asm	В-	-V*	M_B
VARIABLE	B (max)	DATE AT MAX.	B (min)	DATE AT MIN	AMPL	Bluest	Reddest	(max)†
V12 V22 V35 V37 V38 V14 V52 V53	16 46 20 18 20 7 19 0 18 2‡ 20 49 20 27 20 26	Nov. 3, 1954 Feb. 26, 1949 Jan. 5, 1921 Jan 22, 1930 Mar. 1, 1925 Dec. 15, 1955 Dec. 23, 1960 Dec. 12, 1950	(22 40) 21 76 22 90 21 48 20 08 20 90 20 73 20 8	Mar 19, 1963 Mar. 21, 1963 Feb. 3, 1951 Apr. 13, 1950 Jan 16, 1958 Feb. 1, 1957 Nov. 5, 1962 Long	5 94 1 6 2 2 2 5 1 9 0 5 0 5 0 5	+0 04 + 01 26 42 - 70 + 84 + 04 +0 55	+1 15 +0 39 +0 8 +0 14 -0.24 +1 03 +0 29 +0 82	-11 3 - 7 6 - 7 1 - 8 8 - 9 6 - 7 3 - 7 5 - 7 .5

^{*} Corrected for galactic reddening of 0 06 mag.

spectacular bursts of individual stars (NGC 2403,V12; η Car) are ignored. If conclusion (2) is valid, these stars can serve as rough distance indicators for galaxies out to moduli of $(m - M)_{AB} \simeq 30.5$.

VIII. RED SUPERGIANT IRREGULAR VARIABLES

Seventeen variables were found which fulfil the conditions: $V(\max) < 21.05$, B - V > 1.5. The stars are exceedingly red and are very bright intrinsically with $M_V(\max)$ brighter than -6.5, adopting an apparent visual modulus of $(m - M)_{AV} = 27.74$ as later derived. The variables form part of a larger population of non-variable red supergiants whose progenitors are the brightest main-sequence O and B stars. Such stars, whose somewhat fainter analogues in the galactic system are the supergiants of h and χ Persei, have been found in all galaxies of the Local Group so far studied (Humason and Sandage 1957 in M33; Walker 1964, 1967 in M33; Hodge 1961, 1965 in LMC; Arp 1961 in SMC; and Kayser 1967 in NGC 6822).

Table 7 summarizes the photometric data for the red variables in NGC 2403. The individual magnitude estimates are given in Table A4 of the Appendix. The stars are of Population I as shown by their concentration near the spiral arms.

Similar variables are known in the LMC, SMC, NGC 6822, and M33. Only small-sample fields have been searched in LMC (Shapley and Nail 1948, 1955), SMC (Shapley

[†] Based on the observed $B(\max)$ and an apparent blue modulus of $(m-M)_{AB}=27~80$

[‡] This value is the mean of the plotted values near March 1, 1925, shown in Figure 10

and Nail 1951), and M33 (Humason and Sandage 1957), but the entire field of NGC 6822 has been searched by Kayser (1967). To the extent that the partial search across the LMC and SMC is representative, mean absolute luminosities of the brightest red supergiant variables can be obtained and tested as a distance criterion.

The agreement in $M_V(\max)$ and $M_B(\max)$ for the first-ranked red variable in LMC, SMC, and NGC 6822 is quite good. The brightest red irregular in SMC is HV 11423 at $B(\max) = 12.9$, $V(\max) \simeq 10.9$ (assumed), which, with apparent distance moduli of $(m-M)_{AB} = 19.05$, $(m-M)_{AV} = 19.00$ (Sandage and Tammann 1968), give $M_V(\max) = -8.10$, $M_B(\max) = -6.15$. The brightest red variable listed in the LMC is HV 5582 (Shapley and Nail 1948, 1955) with $B(\max) = 12.5$, $V(\max) \simeq 10.5$ (assumed), giving

TABLE 7

ELEMENTS OF SEVENTEEN VERY RED, SUPERGIANT IRREGULAR VARIABLES

No.	B (max)	V (max)	ΔV	$B_m - V_m$	Quad- rant	Location	<i>M</i> _V (max)*	M_B (max)†
V2. V7. V7. V9. V11. V16 V27 V30 V31. V32 V36. V39 V41 V43 V57 V58 V60	(23 (23 22 02 22 80 22 62 (23 22 9 22 9 22 8 (22 85 (22 6 22 40 22 50 22 70 21 7:	20 94 20 30 20 27 20 88 20 17 21 05 20 41 20 95 21 04 20 74 20 78 19 98 20 45 20 05 21 05 20 20	0 54 1.17 0 7 0 53 1 26 0 35 0 6 0 5 1 05 >0 6 0 43 0 85 1 14 0 5 1 05	>2 0 >2.7 1 75 1 92 2 45 >1 8 2 5 1.9 1 8 >2 1 >1 8 2 42 2 16 2 45 1 65 1 5:	I I II III III III III III III IV IV	In spiral arm Close to H II In spiral arm In spiral arm Isolated Near arm In spiral arm In spiral arm 13" from V31 In arm Near H II region Near H II region 18" from V41 Isolated In outer arm In spiral arm, within faint nebulosity, nearby blue companions Inner edge of spiral	-6 80 -7 44 -7 47 -6 86 -7 57 -6 69 -7 .33 -6 79 -6 .70 -7 00 -6 96 -7 .76 -7 29 -7 69 -7 54	-5 78 -5 00 -5 18 -4 9 -4 90 -5 00 -5 30 -5 30 -5 10 -6 1:

^{*} M_V based on an apparent visual modulus of $(m-M)_{AV} = 27.74$.

 $M_V(\text{max}) = -8.10$, $M_B(\text{max}) = -6.15$. Kayser's work (1967) in NGC 6822 gives V18 as the brightest variable with V(max) = 16.76, B(max) = 19.17, $(m - M)_{AV} = 24.56$, $(m - M)_{AB} = 24.83$ giving $M_V(\text{max}) = -7.80$, $M_B(\text{max}) = -5.66$. These calibrations, especially in the LMC and SMC, can be improved by a complete search over the face of the clouds and by photoelectric measurement, but for the moment we can adopt $\langle M_V(\text{max}) \rangle_{1st} = -8.00 \pm 0.1$, $\langle M_B(\text{max}) \rangle_{1st} = -6.00 \pm 0.2$ as working values for the brightest red irregular variable, and check for consistency in other galaxies.

The brightest variable of this type in V wavelengths in NGC 2403 is V41 at $V(\max) = 19.98$, giving $(m - M)_{AV} = 27.98 \pm 0.1$ if we adopt $M_V(\max) = -8.00$. The brightest reliable variable in B wavelengths is V9 at $B(\max) = 22.02$ giving $(m - M)_{AB} = 28.02 \pm 0.2$. These apparent moduli are remarkably close to $(m - M)_{AV} = 27.74$, $(m - M)_{AB} = 27.80$ which are later derived from the Cepheids in NGC 2403, and this agreement shows that the supergiant red irregulars have promise as good distance indicators. All effort will be made to improve the calibration in the coming year by more detailed work in the LMC and SMC.

[†] M_B based on an apparent blue modulus of $(m-M)_{AB}=27.80$

The number of observations required to determine $V(\max)$ and $B(\max)$ for the red irregular variables is prohibitive in most galaxies, and a simpler criterion using non-variable red stars is desired. The discovery of the reddest and brightest supergiants in any resolved galaxy is moderately easy by blinking red and blue plates. If the upper luminosity of these stars is well defined, as is suggested by the foregoing results on the variables, and assuming that the variables and non-variables attain nearly the same luminosity as indicated by Kayser's complete work (1967, Fig. 2) on the C-M diagram of NGC 6822, then the red supergiants with B - V > 1.5 themselves can be used as distance indicators, whether they are variables or not. Kayser's diagram shows that an upper envelope of the distribution of such red stars in NGC 6822 exists at about V = 16.6 or $M_V^{\circ} = -8.0 \pm 0.3$.

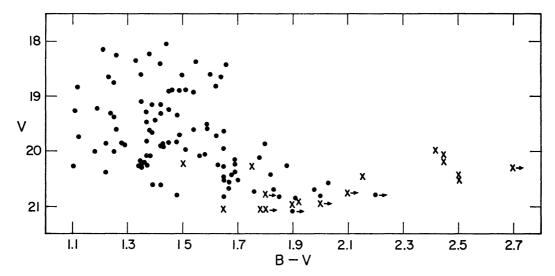


Fig. 12.—The color-magnitude diagram for the reddest stars in the neighborhood of NGC 2403, listed in Table 8. The red irregular variables listed in Table 7 are shown as crosses. Those variables which are invisible at maximum on blue plates are marked with arrows, indicating that the B-V values are redder than the plotted value. We assume that stars bluer than B-V=1.9 are foreground stars from our Galaxy.

We have made a blink survey for the reddest stars in NGC 2403 and have determined colors and magnitudes of 114 such stars by step-scale estimates on four yellow plates and three blue plates. The results are shown in Figure 12 and Table 8. The stars are identified in Figure 13 (Plate 7) which is from a limiting yellow exposure with the 200-inch. The brightest of the red supergiant stars appear at V = 19.85, which gives $(m - M)_{AV} = 27.85$, using $M_V = -8.00$ for the upper limit. This modulus is in excellent agreement with $(m - M)_{AV} = 27.74$ derived from the Cepheids.

We believe this method of distance determination has great power for other resolved Sc and Irr galaxies because the red supergiants are easy to locate and to measure. If future work continues to show that the upper limit is near $M_V = -8.0$ and is stable, then distance moduli as great as $(m - M)_{AV} = 29.0$ can be reached, and the method will have important use in the redetermination of the Hubble constant.

IX. THE ECLIPSING BINARY

One eclipsing binary, V55, has been found with a period of 6 4 06702. The light-curve is shown in Figure 14 and is of the β Lyrae type. The magnitude estimates are given in Table A3 of the Appendix. The maximum brightness of B = 21.77 mag indicates, for equal components, that each star has an absolute magnitude of $M_B = -5.3$, adopting

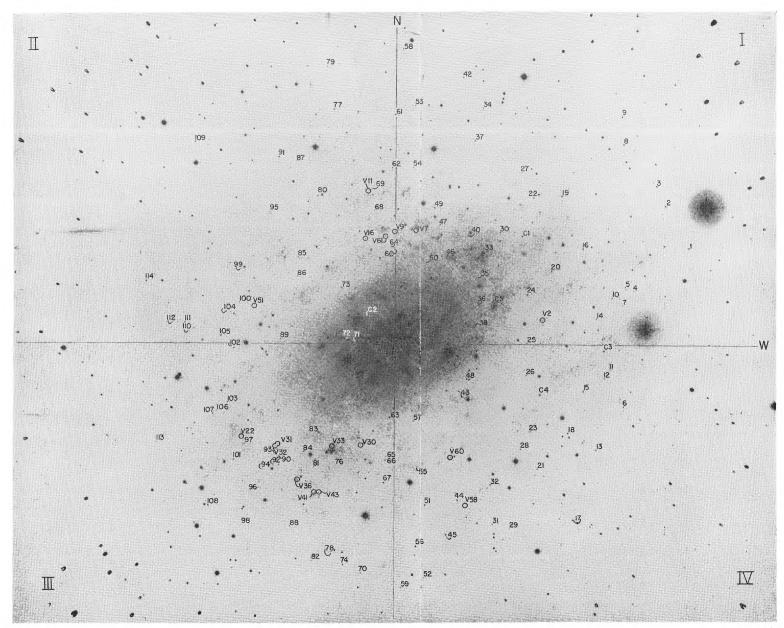


Fig. 13.—Identification chart for the red stars of Table 8, together with the red irregular variables of Table 7, and the five clusters listed in Table 11. The reproduction is from a 40-min exposure on Eastman 103aD + G11 emulsion with the 200-inch.

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 $\label{eq:table 8}$ Red Stars in NGC 2403 with $B-V \! \geq \! 1 \; 10$

			1		· · · · · · · · · · · · · · · · · · ·			<u> </u>
No.	V	B-V	No	v	B-V	No	V	B-V
1	19 14:	1 77:	39 .	20 80	1 48	77.	19 27	1 11
	19 38	1 46:	40	19 70	1 49	78†	20 38	1 22
3	19 08	1 62:	41 .	18 90	1 49	79 '	20 05:	1 65:
4	20 51	1 65	42	19 76:	1 45:	80	18 88	1 46
2 3 4 5†	20 06	1 58	43.	20 25	1 37	81.	19 85	1 80
6	19 86	1 43	44*	19 16	1.42	82†	20 42	1 82
7† 8 9	20 39	1 69	45	20 27	1 10	83	20 74	1.76
8	18 88:	1.57:	46	19 72:	1 27:	84	19 48	1 37
9	19.10:	1.70:	47	20 23	1 35	85	20.26	1 88
10	19 44	1 40	48	19 97:	1 38	86	20.25	1 63
11	20 60	1 39	49	18 65	1 64	87.	20.57	2 03
12.	20 01	1 18	50	20 09	1 56	88†.	19.85	1 22
13	19 66	1 39	51	18 35	1 33	89	19 60	1 26
14.	20 24	1 69	52	20 20	1 36	90	19 85	1 28
15.	18 88	1 51	53.	20 47	1 65	91	18 15	1 21
16.	18 60	1 60	54†	20 16	1 69	92	19 63	1.38
17.	19 10	1 35	55.	20 27	1 65	93.	20 08	1 38
18	19 15	1 39	56*	18 75	1 25	94†	20 85	1 91
19 .	18 54	1.26	57	20 24	1 34	95†	20 61	1 42
20	19 61	1.54	58	19 80:	1 72:	96†	20 82	1 85
21	20 39	1 43	59	19 96:	1 21:	97†	19 95	1 65
22	19 50	1 59	60	19 32	1 42	98.	20 66	1 67
23	19 98	1 51	61.	18 42	1 66	99†	20 82	1 65
24	18 22	1 38	62*	19 83	1 37	100	19 87	1 29
25.	20 02	1 25	63	18 05	1 44	101	19 39	1 25
26* .	19 71	1 62	64	21 09	>1 9	102	19 21	1 19
27	20 69	1 98	65	20 07	1 37	103	19 82 18 82	1 48
28.	19 59	1 59	66.	19 91	1 42	104		1 62
29†	20 52	1 70	67*	18 37	1 55	105	18 83	1 12 1 68
30.	18 65 19 84	1 23 1 45	68* 69*	20 12 19 74	1 78 1 12	106 107	20 42 18 60	1 35
31† 32	18 94	1 45 1 54	69** 70	20 25	1 35	107	18 61	1 50
33	18 94	1 65	70 71	20 25 20 07:	1 33:	108	19 94:	1 36:
34	20 04	1 85:	71 72	19 90:	1 43:	1109	20 79	> 2 2
35 .	20 04 20 54	1 67	73	18.90	1 45:	1111	19 31	1 24
36 .	20 50	1.31:	74	19 29	1 37	1112	20 80	2 0
37	19 35	1.31:	75.	20 29:	1 76:	1113	20 27	1 35
38	18 40	1.48	75. 76‡	20.70	1.83	113	19 25	1 45
JU	10.40	1.44	10‡	20.70	1.00	11.4	17 40	1 17

^{*} p.e. standard; independent estimates

[‡] Possibly variable.

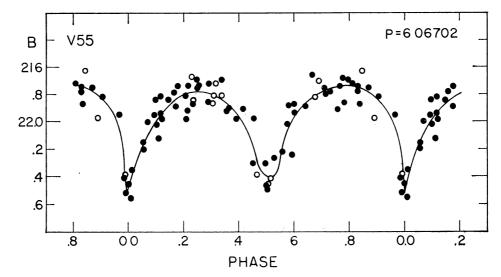


Fig. 14.—Light-curve in B for the eclipsing binary V55

[†] Secondary standard; independent estimates.

 $(m-M)_{AB} = 27.80$. Similar eclipsing binaries are known in M31 (Gaposchkin 1962a, b; Baade and Swope 1963, 1965) and in the Magellanic Clouds (Shapley and Nail 1953; Russell 1956).

X. UNCLASSIFIED VARIABLES

Table 9 summarizes the available information on sixteen variables whose type could not be determined. These stars are generally so faint that no individual magnitude values are listed in the tables of the Appendix because, on most plates, the variables are invisible. Only three of the stars, V28, V59, and V56, are seen on the yellow plates, indicating that most of the variables are not particularly red. Extensive attempts to find periods proved to be unsuccessful, but the presence of several maxima, as listed in Table 9, suggests that some of the variables are Cepheids.

TABLE 9
SIXTEEN UNCLASSIFIED VARIABLES

Variable	B (max)	Type	J D of Maximum (2400000+)	Remarks
V10	22 80	Cepheid?	33980 9, 34778 7, 38109 7	Small amplitude
V13	22 8	Irr?	34058 7, 35456 9, 35874 8, 38107 7	Small amplitude, changes within 3 days
V17	22 50	Eclipsing?	Min.: 33361 8, 33569 0, 33598 0, 33650 8	Near nebulosity
V18	22.85	Irr?	34125 7, 34454 7	
V20	22 9	Cepheid?	33660.8, 33681 8, 34356 9, 34454 6, 34719 9	
V23	22 8	Cepheid?	33956 9, 34327 9, 35049 9, 38109.7	Heavy background
V26	22 75	Cepheid?	33624.9, 33681.8, 33960.0, 33980 9, 34719 9, 38107.7	
V28	21 90	Irr?	32969 7/73 7, 34118 7, 34778 7/ 802 6	V(max) = 21.73 on J.D. 2434 779 7
V44	22 9	Cepheid?	33650.8, 34015.9, 34661 0, 34718 8, 34780 7, 35874 8	
V45 .	23 0	Cepheid?	33685.8, 33983.9, 34125.7, 34717.8/ 19.8, 34779.7, 35049.9, 37974 0	
V47	23 0	Cepheid?	33383.8, 33593.0, 33951.0, 33959 0, 33980 9, 34035 8, 34312 0 34661 0, 34802 6, 35049 9	
V48	23 0	Cepheid?	33685 8, 34442 6, 35191 7, 35870 8	Small amplitude
V49	22 9	Cepheid?	33623 0, 33650 8, 33925 0, 34779 7	Small amplitude
V50 .	22 9	Cepheid?	33681 8, 34664 0, 34719 9, 34802 6	Small amplitude
V56	19 65:	Diffuse ob- ject		See text, $V(max) = 1976$ to 2058
V59	22.5	Irr?		V(max) = 21.7

The most interesting variable of the group is V56. This object appears very diffuse on blue plates, but completely star-like on yellow plates. The estimated B magnitudes show considerable scatter, most, or all, of which can be explained as a photographic effect due to the image quality. However, we are convinced that the variation in V is real and is not caused by a spurious effect of diffuseness. The object is extremely bright, reaching $B \simeq 19.7$, $V \simeq 19.8$ at maximum: values which correspond with $M_B(\max) = -8.1$ and $M_V(\max) = -7.9$. V56 is also very blue. The enigma is that, to appear diffuse, the true image size must be at least 0.5" in diameter which, at a true distance of $r = 3.3 \times 10^6$ pc, requires a linear diameter of 8 pc. Evidently the object cannot be an ordinary planetary nebula with a variable central star because the size is much too large (O'Dell 1962), even though the absolute luminosity is approached by at least a few central stars of such nebulae (O'Dell 1963), and central stars of planetary nebulae are known to vary (Kohoutek 1966). We do not know if the nebulosity is bright in $H\alpha$. The nature of the object remains a mystery.

XI. OTHER COMPONENTS OF THE STELLAR CONTENT

a) Brightest Stars

In late Sc and Irr galaxies of absolute integrated magnitude brighter than $M_B = -18$, the brightest resolved stars occur at about $M_B = -9.3 \pm 0.2$ (m.e.) (Sandage 1962). The calibration can eventually be improved by more precise photometry in galaxies of the Local Group and in other nearby systems. As a first step in this recalibration, we have counted stars over the face of NGC 2403, together with a nearby comparison field so as to determine the B magnitude at which appreciable numbers of stars belonging to NGC 2403 first appear.

A circular area of radius 9'.53, centered on NGC 2403, was chosen for the count of galaxy stars. The region has an area of 0.080 sq. degree and encompasses the entire visible region of the galaxy. Counts were made on two good 200-inch plates by constructing a photometric catalogue of all stars in the interval $16.50 \le B < 19.95$. Magnitudes of 315 objects, most of which are not clusters or emission patches as judged by the crispness of the images, were estimated relative to the adopted magnitude sequence by use of a step-scale plate. A third 200-inch photograph was used to strengthen the estimated magnitudes for objects with $17.50 \le B < 19.25$. The mean error of the adopted magnitudes is less than 0.1 mag except for stars on heavy background where the error is considerably greater. The magnitude distribution of the stars in the field of NGC 2403 is given in the first column of Table 10.

A comparison field was chosen in an annular ring centered on the galaxy whose inner radius (11.5) was large enough to be completely removed from NGC 2403. The outer radius of the annulus was 22.3, giving an area for the comparison field of 0.32 sq. degree. Magnitudes of all stars in this field, within the interval 16.60 < B < 19.50, 413 in number, were estimated on a short-exposure 48-inch Schmidt plate using a step scale. The average error of an estimated magnitude is 0.1 mag.

Column (2) of Table 10 lists the comparison field star counts reduced by a factor of 4 to normalize to the same area as the galaxy field.

The difference between columns (1) and (2) is listed in column (3) and represents the excess of stars in the NGC 2403 field. Histograms of columns (1) and (3) are shown in Figures 15a and 15b. The statistical significance of the excess values of column (3) can be tested by noting that the variance in the foreground count of column (2) is the square root of the number listed therein. Inspection of Figures 15a and 15b shows that stars first appear in NGC 2403 in numbers in excess of 2.5 \sqrt{n} of the foreground count in the interval 18.15 < B < 18.35, thereafter dropping in the next two intervals of 0.2 mag, and rapidly rising again for B > 18.8. These data suggest that $B = 18.25 \pm 0.1$ is the magnitude of first occurrence of stars in NGC 2403, although from this material alone, it could be as faint as 18.8 due to our poor statistics.

However, there is strong additional support that B=18.25 is correct. The six counted stars within the galaxy field in the interval 18.20 < B < 18.33 all have quite distinctive positions relative to the galaxy, a fact which strongly suggests that they are members. The stars are close to heavy concentrations of fainter stars in the spiral arms, or to H II regions. Furthermore, two of the six have negative $(B-V)_0$ values, as determined from the blue plates and from two excellent V plates. Although none of the bright blue variables of § VII are among the six stars because they are faint on the plates which were counted, these variables do reach comparable magnitudes of $B \simeq 18.2$, and there is no question of their membership in NGC 2403. We, therefore, conclude that the brightest stars in NGC 2403 appear at B=18.25+0.1 mag which gives M_B (brightest stars) = -9.55 mag if we adopt an apparent blue modulus of $(m-M)_{AB}=27.80$ as derived in the next section.

b) Clusters

During the inspection of each image in the preceding count program we noticed four diffuse objects which have all the characteristics of clusters similar to those found by

Hubble (1932) in M31. Table 11 gives the estimated B and V magnitudes together with a description of the image appearance. A fifth very bright object at the center of a large, circular H II region was found at $V \simeq 17.0$ which is so much brighter than the brightest resolved stars that we consider it to be a group of several OB stars, such as the cluster at the center of NGC 604, the brightest H II region of M33. We originally suspected this object to be variable with $\Delta B \simeq 1$ mag, but it was later found that the estimated brightness is a clear function of the plate quality. The object seems bright on plates with lightly exposed background and faint on heavily exposed plates. This fact indicated that estimated magnitudes of objects superposed on very heavy background can be subject to large, spurious photographic effects which can only be evaluated by using comparison stars on similar background densities.

Four of the five clusters have negative color indices. They, therefore, cannot be globular clusters, but rather resemble very young galactic clusters such as NGC 457, NGC 663, and h and χ Persei, which have quite blue total colors, and integrated magnitudes between $M_B = -9$ to $M_B = -10$ (Buscombe 1963; Sandage 1963, Table 3).

TABLE 10
STAR COUNTS IN THE FIELD OF NGC 2403 AND IN A
NEARBY COMPARISON AREA

В	Counts in NGC 2403 Field (1)	Normalized Comparison Field (2)	Excess
16 45-16 55 16 55-16 65 16 65-16 75 16 65-16 95 16 95-17 05 17 05-17 15 17 05-17 15 17 15-17 25 17 25-17 35 17 35-17.45 17.45-17 55 17.55-17 65 17 65-17.75 17 65-17.75 17 95-18 05 18 05-18 15 18 15-18.25 18 25-18 35 18 35-18 45. 18 45-18 55 18 55-18 65 18 65-18 75 18 75-18 85 18 85-18 95 18 95-19 05 19 05-19.15 19 .15-19 25 19 .35-19 45 19 .45-19 55 19 55-19 65 19 .55-19 65 19 .75-19 85 19 .75-19 85 19 .75-19 85 19 .75-19 85 19 .75-19 85	3 2 2 4 3 3 3 5 1 3 4 4 1 3 1 3 7 8 4 7 4 4 7 14 11 12 13 12 13 12 13 13 13 13 13 14 11 12 13 14 14 15 16 16 17 18 18 18 18 19 19 19 19 19 19 19 19 19 19 19 19 19	(1 5) 3 8 4.0 3.2 3.5 2 0 3 8 5 1.5 2 10 2 2 0 3 8 5 1.5 2 2 0 3 8 5 1.5 2 2 0 3 8 5 1.5 2 2 0 3 8 5 4 2 0 2 8 0 5 2 2 0 4 5 2 0 4 5 2 0 4 5 2 0 4 5 5 2 8 8 8 8 8 7 (4 8) 	+(1 5) - 1.8 - 2 0 + 0 2 + 1 5 + 3 0 - 0 8 - 0 5 + 1 5 - 2 0 + 1.5 - 2 0 + 1.5 - 2 0 + 1.5 - 2 0 + 1.5 - 4 2 8 + 1.5 - 4 3 0 - 1.5 - 2 0 + 1.5 - 2 0 - 1.8 - 1.5 - 2 0 - 1.8 - 1.5 - 2 0 - 1.5 - 1.

On the other hand, cluster C4 with $(B-V)_0=+0.85$ and $M_B=-9.6$ could well be a globular cluster such as ω Cen or 47 Tuc which have $M_B\simeq -10.3$, $(B-V)\simeq +0.8$, and $M_B\simeq -9.9$, $(B-V)\simeq +0.9$, respectively (Gascoigne and Burr 1956; van den Bergh 1967).

c) H II Regions

There are at least one hundred H II regions over the face of NGC 2403 as found by Véron and Sauvayre (1965) and in an unpublished study with the 200-inch telescope

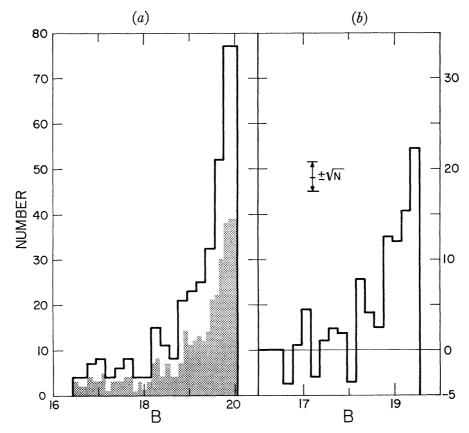


Fig. 15a.—Histogram of the number of stars in a circular area of 0 08 sq. degree centered on NGC 2403. The stippled region represents the counts per 0.1 mag interval. The solid outline represents counts per 0.2 mag interval.

Fig. 15b.—The excess of the number of stars in the field of the galaxy over that in the comparison field, plotted from the data of Table 10. The bar indicates the mean value of \sqrt{N} of the number of stars in the comparison area, normalized to 0.08 sq. degree.

TABLE 11
PROPERTIES OF FIVE POSSIBLE CLUSTERS

Name	В	V	$(B-V)_0$	M_B	M_V	Remarks
C1 C2 C3 C4 C5 .	18 50 18 59 18 25 18 22 17 0:	18 54 18 49 18 41 17 31 17 25:	$ \begin{array}{rrrr} -0 & 10 \\ + & 04 \\ - & 22 \\ + & 85 \\ -0 & 25 \end{array} $	- 9 3 - 9 2 - 9 5 - 9 6 -10 8:	$ \begin{array}{rrr} - 9 & 2 \\ - 9 & 3 \\ -10 & 4 \end{array} $	Clearly diffuse: stellar core Clearly diffuse: stellar core Clearly diffuse: stellar core Very dense; image diffuse Stellar image; in center of H II

using an 80 Å half-width Ha interference filter (Sandage 1962). The angular sizes and distribution across the galaxy will be discussed elsewhere, and we only note here that the angular diameters of the largest and the mean of the first five largest regions are 15".6 and 11".5, respectively (Sandage 1962), values which we have rechecked in the present investigation. These disagree with values given by Véron and Suavayre, but it should be pointed out that the scale of the plates used by these authors is exceedingly small, and that the data from the 200-inch plates are to be preferred.

d) Novae

No novae have been found in NGC 2403. After very detailed re-examination of the discovery plate, the nova reported by Ritchey (1917) proved to be a dust grain. By use of typical parameters of the light-curves for novae, and making allowance for time coverage of our plates and their different quality, we estimate the upper limit for novae in NGC 2403 to be <1 nova/year as compared to 26 novae/year in M31 (Arp 1956). This is in agreement with Hubble's result (Bowen 1954) that the occurrence of novae seems to be very unlikely in Sc galaxies (M33, NGC 2403) as compared with Sb galaxies (M31, M81).

XII. DISTANCE TO NGC 2403

The following distance indicators have been used: (1) the Cepheid variables in B and V light; (2) the brightest of the blue irregular variables; (3) the brightest resolved stars, presumed to be A and F supergiants; (4) the brightest red irregular variables; and (5) the angular sizes of the first ranked, and the mean of the first five largest of H II regions. The calibration of some of these indicators via galaxies in the Local Group has been partially discussed in the previous sections.

a) Cepheids

The period-luminosity relation defined by the seventeen stars of Table 5 shows considerable scatter in $B(\max)$, but surprisingly is much more concise in $V(\max)$, even though the light-curves in V wavelengths are more sparsely defined. The first thought that much of the scatter is caused by variable internal absorption is not correct if the normal ratio of absorption to reddening applies. This follows because the correlation between the magnitude residuals R_B and R_V and the color residuals $\delta(B-V)$ listed in Table 5 have very much smaller slopes than 4 and 3, respectively. These correlations, which the reader can plot from Table 5, are remarkably good considering the great difficulty of the color determination. The slopes of the relations are $\Delta R_B/\Delta \delta(B-V)=$ 1.60 and $\Delta R_V/\Delta \delta(B-V)=0.73$, which differ significantly from the reddening values. However, they also differ somewhat from similar relations derived for galaxies in the Local Group (Sandage and Tammann 1968, Fig. 7), correlations which have slope coefficients of 2.6 and 1.7, respectively. Although we have no explanation for this difference, we are convinced that the scatter in the B(max)-P relation is not primarily caused by local obscuration, because if this were so, the spread in $\delta(B-V)$, ranging from -0.2 to +0.7, should cause an observed spread of 3.6 mag in $B(\max)$, whereas the observed scatter is only $\Delta B(\text{max}) = 1.6 \text{ mag}$. We therefore conclude that much of the scatter is intrinsic and due to the causes discussed elsewhere (Sandage and Tammann 1968). These causes also explain why the scatter in the $V(\max)-P$ relation is smaller than that in the $B(\max)-P$ function.

The one remaining problem in the present data concerns the observed colors of about half the Cepheids at maximum light. These colors, assumed now to be nearly intrinsic values because of our assumption of nearly negligible internal absorption, average about 0.4 mag redder than the normal colors of galactic Cepheids (Sandage and Tammann 1968, Fig. 7), and this is part of the same problem for which we have no explanation.

The distance to NGC 2403 can now be determined from the Cepheids by comparing our observed P-L relation with that previously derived at maximum light from Cepheids in the Local Group, calibrated with the nine Cepheids in galactic Cepheids and associations (Sandage and Tammann 1968; Fig. 5; Table A1). Because the sample of Cepheids at a given period must be incomplete in NGC 2403 due to our working so close to the plate limit, we assume that the brightest observed Cepheids fall on the upper envelope of the standard relation. This assumption has the added advantage that if there is local absorption for some of the Cepheids, as must be the case for at least V54, the upper envelope line, defined by the brightest and bluest of the stars, is unaffected. Justification for this view is available from the fact that the six brightest Cepheids with log $P \ge 1.481$ have observed colors which lie within the intrinsic scatter of the calibrated period-color relation given elsewhere (Sandage and Tammann 1968, Fig. 6).

The upper envelope of the plotted data from Table 5, compared with the upper envelope of the standard P-L relation at maximum light gives apparent blue and visual distance moduli of $(m-M)_{AB}=27.80\pm0.1$ and $(m-M)_{AV}=27.75\pm0.1$. Assuming absorptions due to the galactic system of $A_B=0.24$ and $A_V=0.18$ gives true moduli of $(m-M)_{0,B}=27.56$ and $(m-M)_{0,V}=27.57$ for NGC 2403 from the Cepheids alone. The agreement between the blue and visual data are, of course, better than the errors involved and should be considered fortuitous. A realistic estimate of the error is perhaps ±0.2 mag in each color.

b) Brightest Blue Irregular Variable

V38 reaches $B(\max) = 18.2$. If we use as calibration only the brightest variable in M33 (star B) at $M_B(\max) = -9.5$ and the brightest in M31 (V19) at $M_B = -9.1$ for a mean of -9.3 + 0.2, then $(m - M)_{AB} = 27.5 \pm 0.2$ or $(m - M)_{0,B} = 27.3 \pm 0.2$ for NGC 2403. The determination obviously has small weight due to the size of the sample. Agreement with the Cepheid modulus can be obtained if we adopt $M_B(\max) = -9.60$ for the brightest blue variable.

c) Brightest Resolved Stars

The star counts discussed in § XI show that the blue stars begin to appear in NGC 2403 at $B=18.25\pm0.1$ mag. The calibration suggested previously (Sandage 1962) gave M_B (brightest star) = -9.3 ± 0.2 , but among these stars are the bright blue variables in M31 and M33. Therefore, this method is only partially independent of method b. Adopting M_B (brightest star) = -9.3 gives $(m-M)_{AB}=27.55\pm0.3$ or $(m-M)_{0,B}=27.3\pm0.3$ for NGC 2403.

d) Brightest Red Irregular Variables

As shown in § VIII, the brightest red variable in V and B gives distance moduli for NGC 2403 of $(m-M)_{A,V}=27.98\pm0.1$, $(m-M)_{0,V}=27.80\pm0.1$ and $(m-M)_{A,B}=28.02\pm0.2$, $(m-M)_{0,B}=27.78\pm0.2$, when the calibration of absolute magnitudes of corresponding variables in the LMC, SMC, and NGC 6822 are used. As mentioned previously, the calibration can be improved by a more complete sampling of the Magellanic Clouds and by a study of the red variables in M33. Furthermore, the upper envelope of the red supergiant population can eventually be used rather than the bright red variables.

e) Sizes of H II Regions

Preliminary calibration (Sandage 1962) suggests that the largest, and the mean of the first five largest H II regions in late Sc and Irr galaxies have linear diameters of 245 \pm 20pc and 178 \pm 33 pc, respectively, based only on M33 and the LMC. The calibration

can soon be greatly improved with NGC 6822, IC 1613, and all members of the M81 group using the results of this paper. Adopting these calibrations for the moment, and using angular diameters in NGC 2403 of 15".6 and 11".5 for the largest and the first five largest give $(m-M)_{0,L}=27.54\pm0.18$, and $(m-M)_{0,5}=27.52\pm0.40$ which are almost identical to the Cepheid values.

f) Summary

The individual results of all the methods are summarized in Table 12. The agreement of the methods is excellent, which shows that there is strong evidence that the distance indicators calibrated within the Local Group, relative to the Cepheids in each galaxy, show no systematic deviation greater than about ± 0.2 mag (which is the accuracy of each method) among themselves when taken in this single step to NGC 2403 beyond the Local Group.

Although the final mean modulus of $(m-M)_0 = 27.55 \pm 0.13$ (A.D.) is almost identical to the Cepheid value alone, a realistic estimate of the errors again shows this to be fortuitous. Adopting the Cepheid modulus of $(m-M)_{0,V} = 27.56$, we can now

TABLE 12

SUMMARY OF INDIVIDUAL MODULI FOR NGC 2403

Method	$(m-M)_0$
Cepheids (B)	27.56 ± 0.1
Cepheids (V) .	$27\ 57\pm\ .1$
Brightest blue variable.	$27.3 \pm .2$
	$27.3 \pm .3$
	$27.78 \pm .2$
	$27.80 \pm .2$
	$27\ 54\pm\ .18$
H II region (5)	$27.52 \pm .40$
Mean	$27.55 \pm 0 \ 13 \ (A.D.)$

turn the problem around and can calibrate the individual indicators in NGC 2403, and indeed, all members of the M81 group to obtain better statistics. Such a discussion will be given in future papers, when photometry of NGC 2366, M81, IC 2574, Ho II, and NGC 4236, is complete.

Besides the distance modulus, we believe the most interesting result to come from this study is the possibility that red supergiants are good distance indicators. Not only are these easy to discover, but they are unique and occur singly, rather than in clusters or in multiple aggregates as for the O, B, and A supergiants. Furthermore, they are so red that confusion with nearby galactic foreground stars is largely avoided, which is not the case for stars bluer than B - V = 1.9, as seen from Becker's (1967) results in SA 51 at $b^{\text{II}} = +21^{\circ}$ where large numbers of stars bluer than B - V = +1.9 were found to $V \simeq 21.2$ mag, but no redder objects were present. The result is also consistent with the Greenwich proper-motion study in the field of the LMC (Woolley 1963), which shows that confusion between local and extragalactic stars dominates the statistics in the range 0.5 < B - V < 1.5.

Figure 12 suggests that an upper envelope exists for the reddest stars in NGC 2403 at about V = 20.0, which, with $(m - M)_{AV} = 27.74$, gives $M_V = -7.7$ as determined from this galaxy alone. Use of this indicator in M101 will be discussed in a future paper.

As a final remark, we found it amusing to apply the distance of $(3.25 \pm 0.20) \times 10^6$ pc for NGC 2403 to the remainder of the M81 group, and to combine this value with the mean redshift of the group determined from nine of its members. Individual redshifts are known for M81, M82, NGC 2403, IC 2574, Ho II, NGC 2366, NGC 2976, NGC 3077,

and NGC 4236 (Humason, Mayall, and Sandage 1956; Epstein 1964, neglecting his value of M82), each corrected for a solar motion of 300 sin $l^{\rm II}$ cos $b^{\rm II}$. These data are used to obtain the ratio of redshift to distance. The mean corrected redshift for the group is 210 ± 33 km/sec, giving

$$\frac{v}{r} = 65^{+15}_{-14} \text{ km/sec Mpc}.$$

Although we do not claim that this value bears any relation to the Hubble constant because: (1) the result is so sensitive to the correction for solar motion; (2) no cognizance is taken of possible non-isotropic effects in the velocity field (de Vaucouleurs 1958, 1966); and (3) the back-to-front ratio of dr/r = 0.24 for the M81 group of radius 14° (Holmberg 1950) is neglected, it is interesting that the value is close to the range in which the Hubble constant is believed to lie. The current plan for the redetermination of H is to apply some of the calibrators discussed in this paper to many galaxies in the nearby field so as eventually to determine the regression of v on r, using an adequate statistical sample.

One of us (G. A. T.) wants to express his deep gratitude to Drs. I. S. Bowen and H. W. Babcock, and to the staff members of the Mount Wilson and Palomar Observatories for their hospitality and their continuous encouragement. He is also indebted to the Swiss Holderbank Foundation for a travel grant.

We both are grateful to many members of the nebular department, especially Dr. M. L. Humason, who obtained a number of plates at the beginning of the program.

APPENDIX

Table A1 lists individual B magnitudes and phases for the seventeen Cepheids in Table 5 of the text. Estimates on an uncalibrated Argelander scale, relative to faint sequence stars a, b, and c, are given when the star is fainter than the calibrated stars of Table 2. It is always the case that when three arbitrary stars are used, c is the same as the faintest calibrated star of the sequence. When only two fainter stars are used, b is identical with the faintest calibrated star of Table 2. The symbol "(" means "fainter than." The symbols b and b mean "faint" and "bright" and are used only on poor-quality plates where magnitude values are uncertain, but where estimates are important for the period determination.

Table A2 lists similar data for V magnitudes of the Cepheids.

Table A3 lists B magnitudes for the eight blue irregular variables of Table 6, and for the eclipsing binary V55 with phases computed with a period of $6^{4}06702$.

Table A4 gives V magnitudes for the blue irregular variables, together with magnitudes for all of the red supergiant irregulars of Table 7, except for V58, which is so faint as to be invisible on most plates. No B magnitudes are tabulated for the red stars, although the data for $B(\max)$ are listed in Table 7 of the text.

TABLE A1

B MAGNITUDES AND PHASES FOR 17 CEPHEIDS

~	T	J D o	Exp.	Ť	V	1	v :	3	v ·	4	v	5	V 6		V 8	
Plate	Date	2430000+	Time (min)	Qual.	В	Phase	В	Phase	В	Phase	В	Phase	В	Phase	В	Phas
РН- 5-Н	1949 Jan 27/28	2944 8	30	VP	(a4	0 690 247	F	0 848 099	22 46 F	0 996 566	22 07:	0 0 16 488	F b:	0 524 248	(a F	0 70
19-H 30-H	Feb 18/19 Feb 21/22	2966 732 2969 710	45 45	P P P	a a4	323	В	133	F	644	a4	552	(b F	347	(a	43
39-H	Feb 25/26 1950 Jan 15/16	2973 664	45	P	(a	423	22 0 :	178	(b	747	(b7a a4	637	F c5b	477 189	b8a: b4a	54 98
36-MH 120-MH	1950 Jan 15/16 Mar 20/21	3297 8 3361 8	35 30	FG	a8 a8	656 281	22.61 bla	884 615	(a 22.53	880	21 76	991	a4	304	(a	84
139-MH	Apr 11/12	3383 8	30	G FG	a4	840	23.03	867	b5a	454	a4	465	22 80	031	a	48 51
148-MH	Apr 12/13	3384 8	30 26	F FG	a4 a8	865 544	c5b	878 984	22 6 :	480 310	(a a4	486 451	22. 41 c3b	064 152	b5a a4	87
71-H 318-B	Oct 13/14 Oct 17/18	3569 024 3573 027	29	G	a8	646	21 92 22 04	030	(b5a	394	24	537	la.	284	22.09	99
344-B	Nov 6/7 Nov 11/12	3592 989	30) VG	b2 5a	153	22 26	258	22 24	915	22 07	967 074	22.32	944 108	b7a a	57 71
85-H 98-H.	Nov 11/12 Dec 6/7	3597 964 3622 977	30 30	FP F	(a 22 36	279 914	23 10 (a	315 601	22 46 (b	045 698	22 27 a	613	22 80	935	a2	44
96-п. 114-М.	Dec 8/9	3624 944	30	F	21 99	964	a 22 96	624	l (b	749	la.	655	22 12	000	a	5
250-MH	Dec 15/16	3631 8 3650 8	25 30	P FG	B a8	138 631	22 96	702 919	22.53: c5b	928 424	F 22. 39	803 211	F 24	227 855	F b4a	7 2
254-MH 256-MH	1951 Jan 3/4 Jan 7/8	3654 8	30	FG	(a4	723	22 12 22 12	965	(b	529	b7a	298	22 32	987	b5a	1 3
124-M .	Jan 13/14	3660 8	30	F	(a4	875 383	22 68 22 96 22 54	033	F	685 207	(a F	427 857	b F	185 846	F B	5
263-MH 268-MH	Feb 2/3 Feb 3/4	3680 8 3681 8	30 30	P FG	(a a8	408	22 90	273	c5b	234	a	879	(a	879	22 44	1
274-MH	Feb 7/8 Mar 3/4	3685 8	30	l F	a4	510	22 56	319	F	234 338	22 27	.965	(a 22 12 F	011	22 85 22 3 :	2
289-MH	Mar 3/4	3709 8	30 30	P	b3a b5a	119 241	F	594 648	22 38	965 089	F a4	481 584	F 22 12	804 962	22. 16	1
358-B 291-MH	Mar 8/9 Apr 1/2	3714 675 3738 8	30	FG P G	(a4	856	1 22 26	925	(a	721	22 39	106	F	763	(b5a	8
546-B	Oct 4/5	3925 010	30	G	a8	585	21 97	054	b	583	22 27	114	22. 32	916 807	b5a 22 02	2
554-B	Oct 31/Nov 1	3951 951 3956 937	30	G	a8 (a	269 396	23 10 b	362 419	b (b	286 416	a4 a4	693 801	24 72 32	971	22.9:	1 1
23-S 35-S	Nov 5/6 Nov 7/8	3958 968	25 25 30	P G F	a8	448	c4b	442	(b7a	469	a2	844	22 32 22 32	039	b2a	1 :
44-S	Nov 8/9	3959 969	30	F	b5a:	473	22.61	453	(b. 7.	495 041	22.50	866 316	22 80: a4	072 762	b4a a4	
47-S 62-S	Nov 29/30 Dec 2/3	3980 859 3983 893	30 30	G FG	21 99 22 36	004 081	b7a b9a	692 727	22 7 : 22 75:	120	b5a	381	(a	862	b6a	
78-S	Dec 26/27	4007 901	30	FG	(a4	690	21 91	001	l b	747	b7a	898	a4	656	a4	
92-S	1952 Jan 3/4 Jan 23/24	4015 891	30 30	FG FG	b5a	893 399	22 12 22 68	093 320	22 38 (a	955 475	22 27 a2	070 498	22 41 (a	920 578	(a b4a	
100-S 3-Bm	I Jan 30/31	4035 813 4042 820	30	l G	(a a8	577	22.68	400	a	658 073	a2	649	`a4	810	b9a	ſ
391-MH	Feb 15/16 Feb 24/25	4058 695	30	G	22 04	980	c4b	582	1 22 53	073	21 87	991	a4 F	334	22 44	
401-MH	Feb 24/25	4067 679 4096 671	30 30	P VP	F	209 945	(a	685 016	F	307 064	22 28	184 808	F	631 589	l	1
408-MH 412-MH	Mar 24/25 Mar 25/26	4097 659	30	FG	22 16	970	22 61	027	22, 38	090	à	830	(a	622	b2a	l
420-MH	Apr 15/16	4118 672	30	FG	a8	504	22 54	268	(b5a	638	b7a	282 433	b5a	316 548	b9a 22, 23	
434-MH 158-H	Apr 22/23 Oct 14/15	4125 684 4300 985	30 30	FG VG	a8 a	682 134	22 68 22. 26	348 352	(b b	821 398	(a 22.33	206	(a b5a	341	b5a	1
180-S	Oct 25/26 Oct 26/27	4311 989	30	l G	a8	414	c6b	477	(b5a	685	b5a	443	(a	705	b7a	
193-S 209-S	Oct 26/27 Nov 10/11	4312 963 4327 934	30 30	P FG	a8	438 819	6	489 660	22 31	710 101	a4	464 786	c5b	737 232	22 72	}
209-S 231-S	Nov 24/25	4341 883	30	P	B	173	(a F	819	F	463	22 33	086	F	693	22 6	:
255-S	Dec 9/10	4356 923	25	l F	F	555	22 04	991	c8b:	858) (a.	410	c3b:	190	a2	1
264-S 290-S	Dec 10/11 Dec 22/23	4357 910 4369 851	30 30	F	F 22 4:	580	21 90 22 68	139	b: 22.9:	884 195	b3a a	431 688	c: (b3a	222 616	(a 22 44	1
309-S	1953 Jan 8/9	4386 764	30	FG	a	313	22 82	332	(b5a	637	21 87	052	i c	176	(a	1
331-S 359-S	Jan 16/17 Feb 6/7	4394 714 4415 718	30 30	FG P	(a4 22.4:	515 048	23 10 (a	423 663	(a b:	845 393	22 50 a4	223 675	c5b F	439 133	a2 F	1
375-S	Feb 17/18	4426 761	30	FG	b5a	328	र्भ ।	789	b5a	681	22.50	913	(a 22 51	498	b6a	l
393-S	Mar 5/6	4442 649	30	F	(a4	732	22 75 21 97	971	1	096	b5a	255	22 51	023	22 8	
409-S 467-S	Mar 6/7 Mar 17/18	4443 661 4454, 646	30 30	G FG	b5a 22 29	758 037	21 97	983	22 9 : b:	122 409	b5a a2	277 513	22 80 a4	056 419	a (a	ļ
468-S	/ Mar 17/18	445 4 676	10	F	22 36	037	22 12	109	b	410	1 ~ 0	514	(b	420	a4	1
598-S	Oct 9/10 Oct 12/13	4660 979	44	G	a8	277 354	b 00	467 501	b: 22, 90	796 874	22 07	954 019	b b5a	238 337	(a (a	
629-S 891-B	Dec 5/6	4663 990 4717 836	25 30	G	a8 a8	721	22 89 21 97	117	(b5a	280	22 50	178	d3c	117	b6a	
901-B	Dec 6/7	4718 848	30	G	a8	747	22 26	128	l (a.	306	22 07 21 45 22 50 22 44 22 44	200	c3b	150	a2	1
641-S 649-S	Dec 7/8 1954 Feb 4/5	4719 902 4778 681	30 30	G FG	(a4 b5a	774 266	22.47 b7a	141 812	c7b	334 868	22 44 a2	223 488	d5c d5c	185 127	b4a 22 31	l
661-S	Feb 5/6	4779 688	30	FG	b2 5a	292	clb	824	22 75 22 75	895	(a	509 531	d5c	161	22 58	l
671-S	Feb 6/7	4780 680	30	F	ll a	317	23 10	835	22 5 :	920	(a.	531	c5b	194 230	22 85	1
672-S 678-S	Feb 7/8 Feb 8/9	4781 779 4782 843	30 30	F VP	(a4	345 372	22 96 F	848 860	22 75	949 977	(a	554 577	c5b	280	22 85	1
683-S		4783 876	30	F	(a4	398	22 68	872	22 38	004	a2	600	(a F	299	b7a	
693-S	Feb 9/10 Feb 27/28	4801 774	30	VP	ll	853	22 3 :	076	1	471 494	21 66 21 66	985 004	F 22 75	891 919	a4	
700-S 851-S	Feb 28/Mar 1 Nov 2/3	4802 644 5049 946	30 20	VG FG	a8 a	875 156	22 12 22 75	913	b	950	(a 100	326	b 10	092	22 16	
893-S	Nov 2/3 1955 Jan 23/24	5131 726	21	P	ll	233	1	848		085	(a 22. 27:	087	1	795	22. 16	1
900-S 1122-S	Mar 24/25 Oct 20/21	5191 691 5401 963	30 30	VG FP	a8 22, 30	756 096	c9b	534 938	(a	650 139	b5a	377 903	a4 (a	776 725	22. 16 bla:	
1143-S	Oct 23/24	5404 976	25	FG	b5a	173	22 96: 22 33	972	(c7b	218	(a 21 97 22 28	968	a	825	b2a:	
1167-S	Dec 14/15	5456 905	30	VG	a4	492	i(a	566	(a	574	22 28	086	a4	494	(a2	1
1338-S 1355-S	1957 Jan 31/Feb 1 Feb 4/5	5870 836 5874 757	25 25	F VG	22.04 b3a	005 104	23 03 22 61	297 342	(b a	380 482	21 45 22 27	9 9 5 0 8 0	b b5a	220 349	F 22 09	1
1358-S	Feb 4/5	5874 828	25 25 30	VG	22 36	106	22 47	343	(b5a	484	21 97	081	a	352	22 02	1
32-A	1958 Jan 15/16	6219 780	30) P	F	867	1	286	1	489	F	506]	751	1 22 0 :	1
3216-A 3584-S	1959 Mar 3/4 1960 Apr 18/19	6631 766 7043 707	25 25	VP FG	(a4	331 793	B b5a	996 705	22 60:	998	22 28 22 50	373 240	l	366 980	B 22. 16	
3721-S	Nov 23/24 Dec 22/23	7263 013	25	l G	b7a	363	22 61	212	(a	723 500	22 07	960	(a	227	b9a	1
3735-A	Dec 22/23	7292 780	165	P	22 1 :	119		552	b:	500 285	22 39	601 264		211	22 16	1
4054-S 4196-S	1962 Nov 4/5 1963 Mar 18/19	7974 028 8107 723	35 35	G F	a8 a8	431 816	22 19	340 868	b5a (b	775	22 39	142	c5b	724 142	22 16	
4199-S	Mar 19/20	8108 648	35	P	11 .	840	l B	879	1	749	B	162	1	173	10	1
4213-S	Mar 20/21	8109 651	35	FP	(a	0 865	22 68	0 890	F	0 825	b3a	0 183	c5b	0 206	1	10

TABLE A1 -continued

V 29			V 25	1	V 2	9	ne l		Exp.	JD _o				
Phase	В	Phase	В	Phase	В	Phase	В	Phase	В	Qual.	(min)	2430000+	Date	Plate
0 407 072 162 282 046 713 327 448 902 902 902 902 902 902 903 904 904 904 904 904 904 904 904	22 82 1 42 21 65 21 65 62 12 65 62 22 25 25 24 62 22 25 52 62 65 62 62 22 25 52 62 62 62 62 62 62 62 62 62 62 62 62 62	Phase 0 4395 908 908 908 908 908 908 908 908 908 908	B 1 42:1 51 12	Phase 0 0460 8070 8080 9811 9811 8081 8081 8081 8081 808	B. 22.75	Phase 0 241 5 540 5 541 5 545	B (b b5a c 22 50 66 b5a c 22 52 50 6 a 44 b c 68 b 52 0 9 21 95 2 22 55 0 24 5 22 5 50 22 5 50 22 5 50 22 5 50 22 5 50 22 5 50 2 5 5 5 5	Phase 0 030 6844 7820 5949 9949 1422 6911 1424 6311 142	B	9mm		2430000- 2948 8732 2868 732 2868 732 2868 732 2868 730 2873 664 32973 664 32973 664 32973 664 32973 664 32973 664 32973 664 32973 664 32973 664 3381 8 33818 8 33818 8 33818 8 33818 8 3569 986 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 36818 8 3709 8 3885 8 3680 8 3681 8 3709 8 3885 8 3680 8 3714 675 3738 8 3885 8 3680 8 3759 8 3885 8 3680 8 3759 8 3885 8 3680 8 3759 8 3885 8 3769 8 3788 8 3885 8 3789 8 3893 8 3997 8 3988 8	Date 1949 Jan 27/28 Feb 18/12 Feb 18/12 Feb 21/28 Feb 21/28 1950 Jan 20/21 Apr 11/12 Apr 11/12 Oct 13/14 Nov 6/7 Nov 11/12 Dec 6/7 Dec 18/16 1951 Jan 3/4 Jan 18/16 Feb 1/8 Feb 1/8 Feb 1/8 Feb 1/8 Feb 1/8 Jan 18/16 Feb 1/8 Jan 18/16 Jan 18/17 Jan 18/17 Jan 18/18 Jan 18/17 Jan 18/18 Jan 18/17 Jan 18/17 Jan 18/18 Jan 24/25 Oct 23/24 Jan 24/25 Jan	Plate H- 19-H 19-H 19-H 19-H 19-H 19-H 19-H 19

TABLE A1 -continued

		JD _®	Exp.		V 3	4	V 4	0	V 4	2	V 46		V 5	4
Plate	Date	2430000+	Time (min)	Qual.	В	Phase	В	Phase	В	Phase	В	Phase	В	Phase
H- 5-H 30-H 30-H 39-H 139-H 139-H 139-MH 139-MH 148-MH 171-H 318-B 344-B 85-H 98-H 114-M 1	1949 Jan 27/28 Feb 18/19 Feb 21/22 Feb 25/26 1950 Jan 15/16 Mar 20/21 Apr 11/12 Apr 12/13 Oct 13/14 Oct 13/14 Oct 17/18 Nov 6/7 Nov 11/12 Dec 8/9 Dec 15/16 1951 Jan 3/4 Jan 13/14 Feb 2/3 Feb 3/8 Feb 3/8 Feb 3/8 Feb 3/8 Mar 3/4 Jan 13/14 Feb 2/3 Feb 3/8 Mar 3/9 Apr 1/2 Oct 31/Nov 1 Nov 5/6 Nov 7/8 Nov 8/9 Nov 29/30 Dec 26/27 1952 Jan 3/4 Jan 30/31 Feb 15/16 Feb 17/8 Mar 24/25 Mar 25/26 Mar 24/25 Mar 25/26 Mar 25/26 Apr 15/16 Apr 22/23 Oct 14/15 Oct 25/26 Oct 26/27 Nov 10/11 1953 Jan 8/9 Jan 16/17 Feb 17/18 Mar 17/18 Oct 26/23 1953 Peb 3/4 In 19/18 Oct 12/13 Dec 6/7 Feb 17/18 Mar 17/18 Oct 12/13 Dec 6/7 Feb 17/18 Feb 4/5 Feb 8/9 Feb 9/10 Feb 27/28 Feb 8/9 F	2944 8 2966 732 2969 732 2978 3604 3297 8 3361 8 3361 8 3361 8 3361 8 3361 8 3569 024 3592 989 3592 989 3597 964 3633 977 3624 944 3633 977 3624 94 3631 8 3650 8 3704 675 3738 8 3704 675 3738 8 3704 675 3738 8 3704 675 3738 8 3704 675 3738 8 3704 675 3758 968 3704 675 3758 968 3980 859 3980 859 3980 859 3980 859 3980 859 3981 969 3981 969 3982 859 3983 859 3984 859 3985 868 3987 878 4044 883 4042 824 4057 667 4097 659 4118 672 4125 684 4312 963 4312 963 4312 963 4312 963 4312 963 4312 963 4317 968 4314 646 4354 676 4436 676 4436 676 4436 676 4436 676 4437 778 681 4779 688 4719 908 4717 836 4718 848 4780 680 4717 868 4719 908 4717 868 4719 908 4717 868 4719 908 4717 868 4719 908 4717 868 4719 908 4717 868 4719 908 4717 868 4719 908 4717 868 4719 908 4717 876 5456 905 5874 877 688 4719 908 4717 868 4719 908 4717 868 4719 908 4718 843 4780 680 4781 878 681 774 4802 644 4801 977 4663 979 478 681	30 45 45 35 30 30 30 30 30 30 30 30 30 30 30 30 30	PPPPEGEE GOVEREPEER GOOGEGEGEGEGEGGGOOFFEER OOFFEER OOFFEER OOFFEER FOOOGGGEEFE VEVVEPVEEVEVVOOFFEER P	FF . (a b5a: (a4 72 a6 62 22 a4 42 73 a8 a8 22. 72 a6 32 26 69 22 71 a4 8 a8 22. 72 a6 32 26 66 a8 44 a4 a6 42 a: 22 66 a8 (a4 4 a6	0 249 830 9014 602 8880 9014 602 8890 9884 8907 7506 1220 9451 9552 1286 1292 9666 1206 1207 7696 1207 7697 7797 76	.F.:Ba444a 3 843: 67 67 68 44 93 843: 67 68 68 68 68 68 68 68 68 68 68 68 68 68	0 643 695 838 582 653 708 718 719 653 719 653 7112 653 653 743 653 743 751 751 751 751 751 751 751 751 751 751	.22 74	0 621 7053 048 0704 3211 3211 4775 6617 9677 144 241 2580 9717 012 149 4571 8584 9717 1550 881 1715 550 881 1715 550 881 1715 550 881 1715 550 881 1715 561 881 1717 1818 181	FF 22.84 c7b b5a 62 22 62 23 30 00 22 55	0 189 617 6256 6185 7386 7387 7385 7385 7385 7385 7385 7385 7385	BF F 22 98: 22 82 24 c7b: c5b (a b5a a4 a 23 04 a: a44 (a 22.98 (a	342 575 576 960 962 189 461 482 527 547 571 .952 970 225 970 225 870 7753 870 7754 085 886 3633 204

TABLE A2

WAGNITUDES AND PHASES FOR 17 CEPHEIDS

	8	Phase	0.080 109 109 109 118 1118 1118 1449 1459 1859 1859 1859 1859 1859 1859 1859 18	33	Phase	0.567 584 735 735 735 735 7384 857 857 177 177 177 177 177 177 177 177 177			100
	Λ	۸	21. 61: (21. 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	V 3	Δ	21. 22. 22. 22. 22. 22. 22. 22. 22. 22.			
	9	Phase	0.872 .905 .905 .136 .136 .023 .573 .573 .347 .367 .979	29	Phase	0.993 0.023 0.023 0.023 0.023 0.023 0.024 0.094 0.004 0.	54	Phase	0.934 .9554 .9554 .320 .320 .992 .992 .992 .984 .984 .984 .993
	Λ	V	(21.7 (21.4 (21.4 (21.4 (21.6) (21.8) (21.6) (21.6) (21.7 (21.3) (21.3)	Λ	7	21. 15 (2: 1. 15 21. 13 22. 13 22. 14: 18 22. 18: 18: 18: 18: 18: 18: 18: 18: 18: 18:	Λ	Λ	1 1 1 1 1 1 1 1 1 1 1 1 2 2 2 3 4 5 6 6 7 8 9 9 1 1 1 2 2 3 4 5 6 6 6 7 6 7 8 9 9 9 1 1 1 2 2 2 3 4 5 6 6 6 7 8 8 9 9 1 1 1 2 2 2 3 4 4 <t< td=""></t<>
	5	Phase	0.736 .757 .757 .463 .410 .256 .510 .004 .991 .078 .974 .374 .240 .240 .260 .260 .276 .276 .276 .276 .276 .276 .276 .276	25	Phase	0.860 881 481 415 481 234 389 876 684 684 684 784 957 703 957 103	46	Phase	0.541 .558 .714 .471 .945 .136 .510 .502 .569 .569 .569 .567 .670
	Λ	Λ	21. 8; 21. 45; 21. 15; 20. 95 21. 12 21. 14 21. 14 21. 13 21. 13 21. 13 21. 13 21. 13 21. 13 21. 13	Λ	Λ	21. 26 21. 27 21. 27 21. 31 21. 27 21. 27 27 27 27 27 27 27 27 27 27 27 27 27 2	Λ	Α	12. 12. 12. 12. 12. 13. 14. 15. 15. 15. 15. 15. 15. 15. 15. 15. 15
8	4	Phase	0.357 .7363 .710 .859 .859 .895 .245 .379 .379 .480 .488 .245 .245 .245	21	Phase	0.588 614 616 760 760 960 9492 073 110 110 1208 942 1372 798 798 798	42	Phase	0.502
CEPHELLO	Λ	4	(21. 7 (21. 4 (21. 4) (21. 3) (21. 3) (21. 3) (21. 3) (21. 3) (21. 3) (21. 3)	Λ	Λ	(21. 4 (21. 4 (21. 4 (21. 4 (21. 5 (21. 8 (21. 8 (21. 5 (21. 5 (21. 5 (21. 5 (21. 5 (21. 5	Α 4	Λ	(2) (2) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4
FOR I	3	Phase	0.384 .396 .488 .991 .971 .824 .087 .577 .297 .341 .341 .36 .705 .705	19	Phase	0.624 636 .029 .029 .569 .621 .757 .079 .079 .193 427 484 .538 .538	0	Phase	0.065 1113 1293 1293 1444 1744 1746 1790 1790 1790 1790 1790 1790 1790 1790
PHASES FOR	Λ.	A	21. 34. 22. 34. 22. 34. 22. 34. 22. 35	Λ	A	21. 23 22. 40 22. 11 22. 12 23. 12 24. 27. 10 27. 10 28. 27. 10 28. 27. 10 28. 28. 28. 28. 28. 28. 28. 28. 28. 28.	V 40	٨	(21.7 (21.14) (21.8) (21.8) (21.8) (21.8) (21.6) (2
DES AND	.1	Phase	0.319 .345 .345 .558 .558 .733 .293 .876 .199 .104 .104 .104 .105 .104 .105 .105 .106 .107 .107 .107 .107 .107 .107 .107 .107	15	Phase	0.101 .130 .130 .130 .130 .393 .372 .322 .338 .338 .389 .173 .009	34	Phase	0.986 . 0136 . 6655 . 9366 . 866 . 441 . 877 . 776 . 978 . 939 . 683
V MAGNITUDES AND	>	Λ	21. 65: (21. 3 (21. 3 (21. 3 21. 43: 21. 64 21. 53: 21. 53: 21. 53: (21. 3 (21. 5): (21. 5):	Λ	Λ	21. 24 (21. 4 21. 22 21. 22 21. 73 21. 73 21. 66 21. 66 21. 56 (21. 6 (21. 6 (2	Λ	Λ	21.56 22.22.22.4 22.22.22.4 22.22.22.6 22.22.6 23.22.6 23.23.6
V N		Qual.	G VVP VVP VVD C C C C C C C C C C C C C C C C C C		Qual.	G V V V V C C C C C C C C C C C C C C C		Qual.	0 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
	Exp.	Time (min)	0558830 0588830 058888 0588 0588 05888 05888 05888 05888 05888 05888 05888 05888 05888 05888 058	Exp.	Time (mm)	058881489444964458 818884444964458	Exp.	(min)	8588548844488
	1.0	2430000+	3953.918 4954.914 4914.916 356.948 356.948 366.948 442.669 779.681 540.806 874.685 621.762 631.792 7043.682 263.041	J.D.	2430000+	3953.918 954.914 4312.938 442.669 779.720 870.681 870.806 874.685 6219.748 6311.743 631.743.682 226.005	J.D.	2430000+	3953.918 954.914 4312.938 356.948 356.948 442.669 779.720 802.631 870.806 874.685 6219.748 6219.748 7043.682 226.005
		Date	1951 Nov 3/4 1952 Oct 26/27 1952 Oct 26/27 1953 Mar 5/6 1954 Feb 5/6 1955 Oct 24/25 1955 Oct 24/25 Dec 15/16 1957 Jan 31/Feb 1 1957 Jan 31/Feb 1 1958 Jan 15/16 1958 Jan 15/16 1958 Jan 18/16 Nov 23/24		Date	1951 Nov 3/4 Nov 4/5 1952 Oct 26/27 Dec 9/10 1953 Mar 5/6 1954 Feb 5/6 1955 Feb 28/Mar 1 1955 Oct 24/25 Dec 15/16 1957 Jan 31/Feb 1 Feb 4/5 1958 Jan 15/16 Mar 3/4 1960 Mar 3/4 1960 Mar 3/4 Nov 23/24		Date	1951 Nov 3/4 Nov 4/5 1952 Oct 26/27 1953 Mar 5/6 1953 Mar 5/6 1954 Feb 5/6 1956 Oct 24/25 Dec 15/16 1957 Jan 31/Feb 1 1958 Jan 15/16 Mar 3/4 1960 Apr 18/19 Oct 17/18 Nov 23/24
		Plate	PH-569-B 1974-B 1974-B 274-B 286-S 385-S 662-S 1175-S 1175-S 1137-S 1337-S 1337-S 1337-S 1338-S 327-A 328-S 377-A 372-S		Plate	PH-569-B 574-B 192-S 266-S 396-S 396-S 101-S 115-S 1157-S 1337-S 1337-S 1337-S 1337-S 377-A 3770-S 3710-S 3710-S		Plate	PH-569-B. 574-B. 574-B. 280-S. 280-S. 280-S. 380-S. 1177-S. 1177-S. 1133-S. 3217-A. 3583-S. 3710-S. 3722-S.

 ${\tt TABLE~A3}$ ${\tt B}$ Magnitudes for 8 very bright blue variables and for the eclipsing binary

TABLE A3 -continued

		J D ₀	Exp. Time										v	55
Plate	Date	2400000+	(min)	Qual.	V 12	V 14	V 22	V 35	V 37	V 38	V 52	V 53	В	Phase
PH-598-S PH-629-S PH-821-B PH-901-B PH-901-B PH-641-S PH-661-S PH-671-S PH-672-S PH-678-S PH-683-S PH-692-S PH-693-S	1953 Oct 9/10 Oct 12/13 Dec 5/6 Dec 6/7 Dec 7/8 1954 Feb 4/5 Feb 8/9 Feb 8/9 Feb 8/9 Feb 9/10 Feb 27/28 Feb 27/28 Feb 27/28 Feb 27/28	34660 979 34663 990 34717 836 34718 848 34719 902 34778 681 34779 688 34780 680 34781 779 34782 843 34783 876 34801 676 34801 760 34801 776	44 25 30 30 30 30 30 30 30 30 30 30 30 30 30	GGGGFGFFVPFVPVPVP	19. 29 19 66 18 52 19 24 19 23 19 51 19 61 19 62 19 11 18 25 18 30 18 46 18 39 18 39	20 59 20 64 20 47 20 55 20 56 20 65 20 50 20 61 20 56 20 53 20 6 :	21 59 21 63 21 44 21 60 21 36 21 57 21 59 21 44 21 50 	21 44 21 31 21 20 21 31 21 16 21 20 21 12 21 38 21 47 21 31	21 03 20 89 21 05 20 87 20 88 20 86 20 98 20 88 20 74 	19 77 19 76 19 73 19 74 19. 74 19. 80 19 77 19 80 19 79 19 82 19. 77 19 76 19 80 19 77	20 60 20 55 20 62 20 62 20 66 20 55 20 61 20 56 20 61 	20 38 20 39 20 40 20 40 20 41 20 45 20 42 20 49 20 45 20 47	22 02 21 87 22 40 21 88 21 72 22 49 21 66 21 74 22 56 21 92	0 101 597 472 638 812 500 667 830 011 357
PH-695-S PH-696-S PH-700-S S-247-S S-250-S S-251-S S-254-S S-255-S S-256-S S-257-S S-257-S S-257-S S-257-S	reb 24 Mar 1 Mar 25/26 Mar 26/27 Mar 26/27 Mar 26/27 Mar 26/27 Mar 27/28 Mar 27/28	34801 824 34801 876 34802 644 34827 741 34828 651 34828 709 34828 709 34828 832 34828 853 34829 651 34829 714	10 10 30 20 30 25 25 25 25 25 25 25 25 25 25 25 25 25	P VP VG FG FG FG FG FG	18 39 18 67: 19 20: 19 23: 19 01: 19 68: 18 58: 18 59: 19 10:	20 7 :	21 24	21 08	21 22 21 3 :	19 81 19 76 19 8: 19 65: 19 65: 19 55: 19 45: 19 75: 19 70: 19 75:	20 58 20 6 : 20 5 : 20 5 : 20 6 : 20 6 : 20 6 : 20 6 :	20 56	22 45	450
3-262-S 3-264-S 3-266-S. PH-725-S PH-851-S PH-893-S PH-910-S PH-917-S PH-918-S PH-919-S PH-921-S PH-921-S	Mar 27/28 Mar 28/29 Mar 28/29 Apr 7/8 1955 Jan 23/24 Mar 24/25 Mar 28/29 Mar 28/29 Mar 28/29 Mar 28/29 Mar 28/29 Mar 28/29 Mar 28/29	34829 845 34830 649 34830 702 34840 667 35049 946 35131 726 35191 691 35195 645 35195 673 35195 673 35195 701 35195 701	30 21 30 8 8 8 8	FG FG FG P VG VP VP VP	19 10: 19 10: 19 2: 19 04 16 46 16 90 19 82 19 62 19 59 19 57 19 66 19 61	20 7 : 20 60 20 70 20 6 : 20 6 : 20 8 :	21 2 : 21 69 21 30	21 08 21 63 21 40	21 2 : 20 94 20 9 21 27	19 65: 19 9: 19 8: 19 74 19 79 19 86 19 78 19 85: 19 9: 19 9: 19 9: 19 85:	20 6 : 20 6 : 20 56 20 65 20 61	20 59 20 47 20 45: 20 51	21 98 21 7: 22 05	21 69 57
PH-922-S PH-923-S PH-924-S PH-925-S PH-926-S PH-927-S PH-933-S PH-935-S PH-936-S PH-938-S. PH-1122-S PH-1143-S PH-1167-S PH-1135-S	Mar 28/29 Mar 28/29 Mar 28/29 Mar 28/29 Mar 28/29 Mar 29/30 Mar 29/30 Mar 29/30 Oct 20/21 Oct 20/21 1957 Jan 31/Feb 1 Feb 4/5 Feb 4/5	35195 728 35195 728 35195 756 35195 770 35195 784 35195 788 35196 655 35196 672 35196 703 35196 703 35196 768 35401 963 35404 976 35405 976 35407 836	88888885555550505555 3250255	P P P P VP VP FG FG FG VG	19 56 19 57 19 61 19 57 19 62 19 68 19 59 19 62 19 52 19 51 20 29 21 75 21 85 21 80	20 7 : 20 7 : 20 7 : 20 7 : 20 7 : 20 6 : 20 6 : 20 7 : 20 52 20 55 20 49 20 90 20 77	21 69 21 65 21 44 21 44 21 44	21 78 21 78 21 75 21 80 21 31 21 16	21 0 : 20 9 : 20 8 : 20 8 : 20 8 : 20 81 20 74 20 88 21 19 21 12	19 85: 19 85: 8 : 19 85: 19 85: 19 85: 19 9 : 19 9 : 19 90: 19 92 19 78 19 89 19 89	6 : 20 6 : 20 62 : 20 63 : 20 70 : 20 57 : 20 67 : 20 62	20 5 20 6 20 38 20 32 20 40 20 35 20 31 20 42	21 94: 21 78 21 85 22 41: 21 78 21 89	233 730 288 518 166 173
PH-1358-S PH-32-A. PH-3216-A PH-3584-S PH-3721-S PH-3735-A PH-4054-S PH-4196-S PH-4199-S PH-4213-S	Feb 4/5 1958 Jan 15/16 1959 Mar 3/4 1960 Apr 18/19 Nov 23/24 Dec 22/23 1962 Nov 4/5 1963 Mar 18/19 Mar 19/20 Mar 20/21	35874 828 36219 780 36631 766 37043 707 37263 013 37292 780 37974 028 38107 723 38108 648 38109 651	25 25 25 30 25 25 25 25 35 35 35 35	VG PP FG PG FP FP	21 80 (21 5 (21 6 22 20 22 05 22 0 : 22 10 (21 6 (22 3	20 87 20 80 20 80 20 71 20 70 20 71 20 71 20 70 	21 59 21 60 (21 6 21 62 21 62 21 80 21 61 21 74 21 76	21 27 21 2 : 21 4 : 21 29 20 86 85 20 75 20 82	20 88 21 19 21 12 21 12 21 12 19 82 19 99 19 52 19 54 20 03 19 87	19 87 20 08 20 00 19 75 19 75 19 81 19 83 19 85: 19 85	20 62 20 3 20 5 20 30 20 34 20 27 20. 73 20 52	20 42 20 7: 20 5: 20 47 20 46 20 40: 20 37 20 25 20 33	21 89 21 87 22 52 21 74 21 97 22 26	83 98 17 21 0 52

TABLE A4

V MAGNITUDES FOR NON-CEPHEID VARIABLE STARS

V 35	(21.7 (21.4 21.3 21.44 21.57 21.63 21.66: 21.29 21.29 21.18		
V 32	21.16 21.15 21.15 21.15 21.35 21.36 21.45: 21.45: 21.5 21.2 21.15	V 61	20.70 20.70 21.12 21.12 20.33 20.76 20.76 21.08 21.14 21.1 21.1 21.1 21.1 21.1 20.70
V 31	21. 19 20.95 20.95 21. 21. 41 21. 22. 31 21. 50 21. 33 21. 33 21. 33	V 60	21. 25 20. 65 20. 55 20. 55 20. 58 20. 58 20. 65 20. 65 20. 28 20. 28 20. 65 20. 65 20
V 30	20. 94 20. 98 20. 93 20. 93 20. 65 20. 65 20. 61 20. 65 20. 61 20. 65 20. 65 20. 65 20. 65 20. 65 20. 65 20. 65 20. 65 20. 65 20. 65	V57	21. 88 20. 94 20. 40 20. 40 21. 19 21. 19 20. 73 20. 88 20. 88 20. 73 20. 45 20. 45 20. 45 20. 55 20. 25
V 27	21. 14 21. 45 21. 45 21. 05 21. 38 21. 38 21. 25 21. 27 21. 3 21. 3 21. 3 21. 3 21. 3	V56	20. 40 19. 94 19. 94 20. 58 20. 13 20. 33 20. 03 20. 03 20. 01 20. 15 20. 11 20. 11 20
V 22	20, 71 20, 75 20, 76 21, 20 21, 11 21, 14 21, 35 21, 36 21, 30 21, 30 21, 30 21, 30 21, 30 21, 30	V53	19.62 19.53 19.53 19.53 19.55 19.77 19.77 19.9 19.9 19.9
V 16	20, 23 20, 25 20, 25 21, 00 21, 23 21, 23 20, 17 20, 21 21, 3 21, 3 20, 79 20, 44	V52	20.33 20.24 20.34 21.00 20.32 20.32 20.54 20.66 20.6 20.6 19.85 19.85
V 14	19. 71 19. 62 19. 65 19. 45 19. 45 19. 79 19. 84 19. 84 19. 8 19. 8 19. 8 19. 8	V 43	20, 49 20, 138 20, 70 21, 139 21, 20 20, 80 20, 8 20, 9 20, 9
V 12	19. 29 19. 20 18. 20 18. 28 19. 45: 19. 41 19. 73 21. 53 21. 3 (21. 6 (21. 6 21. 3	V 41	20. 25 20. 26 20. 40 20. 20. 20 20. 20. 20 20. 31 20. 31 31 31 31 31 31 31 31 31 31 31 31 31 3
V 11	21. 18: 20. 88 21. 25 21. 25 21. 25 21. 32 21. 37 21. 2 21. 2 21. 2 21. 2 21. 2 21. 2 20. 98	V 39	(21.4 (21.4 21.15 20.37 20.78 21.14 21.15 21.15 21.15 21.15 21.15 21.16 21.46 21.46
6 A	20, 52 20, 52 20, 59 21, 0 20, 78 20, 64 20, 64 20, 64 20, 1 20, 32 20, 32 20, 32 20, 32	V 38	20, 59 19, 68 20, 59 20, 17 20, 30 20, 30 20, 59 20, 50 20, 50 20
1.Δ	20.87 20.75 21.14: 21.47 21.47 21.40 20.60 20.72 21.0 21.23 20.98: 21.43	V 37	21, 10 21, 02 21, 03 21, 03 20, 93 21, 28 21, 28 21, 28 21, 28 21, 33 20, 1 20, 47 19, 67
ν2	20.92 21.2 21.2 21.3 21.47 21.38 21.38 21.18 21.18 21.2 21.2 21.2 21.2	V 36	21. 03 21. 4: 21. 10: 21. 64 21. 86: 20: 74 20: 73 20: 73 21: 44 21: 64: 21: 44
J.D. 2400000+	33953, 916 954, 912 34312, 937 356, 944 442, 667 779, 717 802, 679 35406, 017 450, 802 874, 681 36219, 744 631, 790 37043, 683 226, 004 263, 038	J. D.	33953.916 954.912 34312.937 356.944 442.667 779.717 802.679 35406.017 457.883 870.802 870.802 871.883 36219.744 631.790 37043.683 226.004
Plate	PH-569-B. PH-574-B. PH-1974-B. PH-1974-B. PH-395-S. PH-662-S. PH-662-S. PH-1155-S. PH-137-S. PH-137-S. PH-337-S. PH-311-A. PH-3217-A. PH-383-S. PH-383-S. PH-3710-S.	Plate	PH-569-B. PH-192-S. PH-192-S. PH-266-S. PH-365-S. PH-662-S. PH-1155-S. PH-1177-S. PH-1177-S. PH-1377-S. PH-1353-S. PH-3583-S. PH-3583-S. PH-3583-S. PH-3710-S.

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