SPECTRAL AND LUMINOSITY CLASSIFICATIONS AND MEASUREMENTS OF THE STRENGTH OF CYANOGEN ABSORPTION FOR LATE-TYPE STARS FROM OBJECTIVE-PRISM SPECTRA

KENNETH M. YOSS

Astronomy Department, Mount Holyoke College Received May 19, 1961; revised June 10, 1961

ABSTRACT

Objective-prism spectra of 684 stars of spectral type G8-K2 have been classified for luminosity and cyanogen absorption. The spectra have been obtained with the Curtis Schmidt telescope of the University of Michigan, using the combined 4° and 6° prisms. The luminosity estimate is based on the strength of the λ 4077 line of ionized strontium, while the cyanogen absorption is measured by the break in density at the cyanogen band head at λ 4216. Ten per cent of the giants are classified as "weak CN" stars Slit spectrograms have been obtained for 37 program stars (including 29 weak and slightly weak CN giants) with the 60-inch reflector of Mount Wilson Observatory. Absolute magnitudes were obtained from direct-intensity microphotometer tracings. Space velocities have been determined for over 200 stars, for which radial velocities are available. The frequency distribution of space velocities for the weak CN giants has a higher dispersion than the frequency distribution for giants with normal cyanogen absorption.

I. INTRODUCTION

Late-type stars can be classified into four spectroscopic groups, each characterized by distinct dynamical properties, as shown by the frequency distributions of their space velocities (Roman 1952). Miss Roman's samples are sufficiently large for two of the groups—the "strong-line" and the "weak-line" stars—to define well-determined frequency distributions for space velocity and to determine relative space densities. The samples for the other two groups—the "4150" and the "weak CN" stars—consist of 25 and 12 members, respectively, and therefore only approximately define the properties of these two groups. The present investigation is concerned primarily with the weak CN group, members of which can be detected spectroscopically on objective-prism plates.

A number of methods for measuring the strength of the cyanogen absorption band have been developed, notably the photographic method developed by Lindblad and others (e.g., Ramberg 1941) and more recently the photoelectric methods of Strömgren and Gyldenkerne (1955), Crawford (1960), and Griffin and Redman (1960). In none of these methods, however, is it possible to distinguish between giants with weak cyanogen absorption and normal subgiants or dwarfs.

The Curtis Schmidt telescope of the University of Michigan, with combined 4° and 6° prisms, gives a dispersion of 110 A/mm at H γ . With this dispersion it is possible to estimate luminosity classes visually from the strength of the λ 4077 line of ionized strontium relative to nearby iron lines, permitting statistical separation of giants and subgiants. Furthermore, the break at the λ 4216 band head of cyanogen is easily visible, and its strength is not greatly influenced by the blending of atomic lines, as is the case with the spectrophotometric cyanogen equivalent or the photoelectric CN measurements.

II. OBSERVATIONS

Using the combined prisms with the Curtis Schmidt, spectra have been obtained for 87 standard stars classified on the Morgan-Keenan system, from spectral type G5 through K3, and luminosity class Ib through V. The plates, IIa-O emulsion, have been developed in a fine-grain developer suggested by Morgan (1937). Three variable factors

influence classification of objective-prism spectra: seeing, which influences resolution; sky fog, which affects contrast; and image density, which also affects contrast. The standard star plates, which generally have short exposure times, are usually not heavily fogged. Appreciable systematic error in classification due to variable seeing or density is introduced only in the case of extremely poor plates. Comparison between the published spectral types and luminosity classes and those estimated from the Schmidt plates gives mean errors of one spectral subclass and one half-luminosity class, or, in terms of absolute magnitude, approximately 1 mag.

The measurement of cyanogen absorption consists of an estimate of the difference in density of the continuum on each side of the λ 4216 band head and is recorded in five steps, from 0 for equal density to 4 for the strongest differences measured. The CN estimates for the standard stars are given in Table 1. The MK classifications for the stars with asterisks are from Johnson and Morgan (1953) or Morgan and Roman (1950). The remainder are from Keenan and Keller (1953), Roman (1952, 1955), and Halliday (1955). In addition to the MK standards, 16 stars are included for which the spectral types are from Wilson's radial-velocity catalogue (1953). The CN measurements usually depend on one plate, occasionally on two or more, with two or three exposures of varying density per plate.

Seventy-four stars listed in Table 1 have been classified by Griffin and Redman (1960). A linear relationship exists between their measurements and the Schmidt values, notwithstanding the fact that different quantities are measured in the two methods. No noticeable variation with spectral types is evident. The least-squares line of regression is

CN (Schmidt) = -17.81 + 8.95 CN (Cambridge),

with a mean error in the Schmidt measurements $= \pm 0.5$ step. This value agrees with estimates of the internal mean error based on duplicate plates and reclassifications of the same plates. Thirty-seven of the program stars listed in Table 2 have also been classified by Griffin and Redman. The agreement with the regression line for the standard stars is satisfactory in most cases.

Six of the Schmidt standard stars are included in Keenan's list of CN standard stars (1958a), in which the measurement of cyanogen absorption refers to deviation from normal absorption. On the basis of the six stars in common, the Schmidt CN steps 2, 3, and 4 correspond approximately to Keenan's CN -1, 0, and +2, respectively, for luminosity class III. Thirty-one of the Schmidt standard stars are included in Miss Roman's list (1952), four falling in her weak CN group. All four of these giants show weaker than normal cyanogen absorption on the Schmidt spectra, two being classified as CN 1 and two as CN 2, while most, but not all, of the other 26 stars show normal cyanogen absorption, CN 3.

The distinction between giants with normal and weak cyanogen absorption is arbitrary, but, on the basis of the above comparisons, G8-K2 stars of luminosity class III with CN steps 0, 1, and 2 would be considered weak CN stars. An alternate method of defining "weak CN" stars is based on the frequency distribution of cyanogen absorption for a random sample of luminosity III stars. For the program stars listed in Table 2, the maximum in the frequency distribution for G8-K2 stars with luminosities II-III through III-IV varies from $2\frac{1}{2}$ at G8 to 3 at K2. The distribution is relatively symmetrical for CN 2, 3, and 4, but about 10 per cent of the stars fall into an asymmetrical wing extending to CN 0. Thus, for this spectral and luminosity range, stars with CN 0 and 1 are classified as weak CN stars. In addition, stars with CN $1\frac{1}{2}$ have been included. These are stars for which more than one classification is available and the mean equals $1\frac{1}{2}$. The frequency distribution for luminosity class IV extends from a maximum at CN 0 through CN 2 with little decrease, then drops quickly at CN 3. The majority of luminosity class V stars have been classified as CN 0.

Figure 1 shows Schmidt spectra of several standard and program stars. The standard

TABLE 1

STANDARD S'	TARS FOR	SCHMIDT	CLASSIF	ICATION

HD	Sp	CN	HD	Sp	CN
$\begin{array}{c} 417\\ 2589\\ 2774\\ 3712\\ 6186\\ 6582\\ 12929\\ 17506\\ 20630\\ 27022\\ 77912\\ 82885\\ 101501\\ 137759\\ 140573\\ 141714\\ 143393\\ 144287\\ 144889\\ 145148\\ 146084\\ 149161\\ 150275\\ 151937\\ 152391\\ 152879\\ 153344\\ 153472\\ 156283\\ 157617\\ 157999\\ 160315\\ 160346\\ 160781\\ 161096\\ 161198\\ 163588\\ 164922\\ 165760\\ 166229\\ 166460\\ 166229\\ 166460\\ 166620\\ 166620\\ 166620\\ 166640\\ 167042\\ 167768\\ 168322\\ 168656\\ 168723\\ 174980\\ 175305\\ 175515\\ 175515\\ 175515\\ 175515\\ 175515\\ 175541\end{array}$	KO III KO IV K2 III KO II-III KO II-III G5 VI* K2 III* K3 Ib* G5 V* G5 III G8 Ib-II G8 IV-V* G8 V* K2 III* K2 III* K2 III* K2 III G8 V K4 III K1 II-III G6 V K4 III K1 II-III G6 V K4 III K1 II-III G6 V K4 III K3 II* gG9 dK3 gG7 K2 III* K0 V K2 III K3 II gG9 dK3 gG7 K1 III K0 IV G8 III-IV K2 III K0 V K2 III K3 II gG9 dK3 gG7 K1 III K0 II-IV K2 III K0 V K2 III K0 V K3 III K3 II gG9 dK3 gG7 K1 III K0 II-IV K2 III K0 V K2 III K0 III K0 V K2 V* K2	1134203302 ⁻¹ 10341402131120203344440430203202132224130	175751 176678 180262 180809 181655 182572 182762 184406 184467 185958 188056 188326 188512 188947 190360 191026 194152 195506 196755 197989 199191 199580 199870 200577 203344 203504 203504 203846 205512 206078 206778 206778 206859 207134 209747 210745 212943 215549 218101 218792 219134 219615 219945 219945 219945 22954 22115 221148 22107 222404 223047	K2 III gK1 G5 II K0 II* G8 V G8 IV K0 III K3 III K3 III K3 III G8 IV G8 IV* K0 III G8 IV* K0 III G6 IV K0 IV gK0 K2 III G5 IV K0 III* K0 III* K0 III* K0 III K1 II G5 IV K1 III* K0 III K1 III G8 III K2 Ib* G5 Ib* K0 III K1 III-IV G8 III K1 III-IV G8 III K1 III-IV G8 III K1 III-IV G8 III K1 III G8 III K1 III K3 III	424 ³⁰ 0230 ³ 311311421211123233331444214211202223332124

 $\overset{*}{\odot}$ Johnson and Morgan (1953) or Morgan and Roman (1950). $^{\odot}$ American Astronomical Society $\overset{*}{\bullet}$ Provided by the NASA Astrophysics Data System

stars are indicated by the designation "MK" following the spectral types. The exposure times for the program stars are 30 minutes in all cases. The spectra of HD 3712 and HD 3681 have been increased to twice their original width by printing two strips side by side, in order to illustrate the spectral features more clearly. The intensity of the λ 4077 line of ionized strontium relative to the λ 4063 and λ 4071 lines of neutral iron increases from dwarf to supergiant. The break in the continuum at the cyanogen band head at λ 4216 does not increase uniformly but varies in strength within a given luminosity class. HD 209992 and HD 211153 appear to be more luminous than the standard II–III star HD 3712. The cyanogen absorption in HD 209992 appears normal, but in HD 211153 it is definitely weak. HD 205836, which is underexposed on the original plate, appears brighter than the standard III star HD 12929, yet shows weak cyanogen absorption. HD 208107 and HD 3681 appear to have normal cyanogen absorption for their luminosity, while HD 218935 has weak absorption.

Long exposures, using the combined prisms, have been obtained over a number of years with the Curtis Schmidt, primarily in four declination zones, $+23^{\circ}$, $+27^{\circ}$, $+53^{\circ}$, and $+58^{\circ}$. The plate centers are such that about 10 per cent of each 5° circular field overlaps the next field. Generally a 10-minute and a 30-minute exposure have been obtained for each center. Additional plates have been obtained for many of the centers; the result is that 42 per cent of the stars classified have been exposed on two or more plates. The quality of the spectra is relatively independent of exposure time. On nights of good seeing, the 30-minute plates have resolution essentially equal to that of the 10-minute plates, as is well illustrated in Figure 1, where the standard star exposures are very short. Comparison of the long- and short-exposure plates shows no systematic effect in classification due to exposure time or, more specifically, due to sky fog and resolution. The internal accuracy for spectral and luminosity classification is in agreement with that found for the standard stars.

Eight hundred and seventy-one stars brighter than photographic magnitude 9.5, primarily in the three declination zones, $+23^{\circ}$, $+27^{\circ}$, and $+58^{\circ}$, have been classified within the spectral range G8-K2. The results for 684 are given in Table 2. The number of plates and the average quality of the classification are given in the fourth column. Quality "a" implies plates of good definition and well-exposed images, while quality "b" implies lower definition and/or faint images. The additional 187 stars have not been included because the images, although classifiable, are underexposed. Classifications from poor-quality plates have been excluded entirely. One hundred and forty-nine of the program stars in Table 2 have been classified on the MK system elsewhere, primarily at David Dunlap Observatory (Heard 1956). These stars have asterisks following their classifications. Comparison of the Schmidt and Dunlap spectral classifications gives a mean error of ± 0.9 subclass for one Schmidt spectrum and a small systematic difference, the Schmidt spectra being one half-subclass earlier. Sixty per cent of the luminosity classifications agree, 35 per cent disagree by one half-luminosity class, and 5 per cent disagree by one or two luminosity classes. A few stars included in Table 2 have been classified outside the G8-K2 limit. In these cases, the mean of the Schmidt and the Dunlap classifications is within the limit.

Of the 684 stars included in Table 2, 31 have been classified from faint images but were included either because they have been classified as weak CN stars or because they have published radial velocities. These are designated quality "c." Of the 653 stars classified from well-exposed plates, 3 per cent are luminosity classes V and IV–V, 15 per cent are luminosity classes IV, 83 per cent are luminosity classes III–IV, III, and II–III, and 6 per cent are luminosity classes II and I. Of the stars in luminosity classes II–III through III–IV, 10 per cent are classified as heaving weak cyanogen absorption (CN 0, 1, and $1\frac{1}{2}$).

III. DISTRIBUTION PERPENDICULAR TO THE GALACTIC PLANE

If a correlation exists between cyanogen absorption and space velocity, it will be evident in the density distribution as a function of distance from the galactic plane for



FIG. 1.—Schmidt objective-prism spectra of three standard stars, designated by MK after the spectral types, and seven proam stars, showing luminosity criteria and cyanogen absorption.

TABLE 2	
---------	--

PROGRAM STARS

HD or BD	Sp	CN	Number; Quality	S (km/sec)	HD or BD	Sp	CN	Number; Quality	S (km./sec)
71 112	KO III KI III-IV	43	1-a 2-a	19	6634 6833	KO III-IV KO III*	1031	1-a 1-b	249
417 554 638	G8 III K2 III	4 4 2 7	1-0 1-c 1-a	50	7087 +56°221	KÕ Ib* Kl II-III	223 8	1-5 1-5 1-a	12
697 756	G8 III K0 III	3 21	1-a 1-b 3-b		+56°232 +56°234	K2 II-III K2 III K2 III	3 31	1-a 2-a	12
1254 1449 1535	G9 III G9 III G9 III	2 1 2	2-b 1-b	51	+22°205 +56°242	KI III-IV KI III KI III-IV	31 2	1-a 1-b 1-b	
1583 2234 2372	K1 III G9 III-IV KO III	$\begin{array}{c} 4\\ 2\frac{1}{2}\\ 3\end{array}$	2-b 2-b 1-b		+55°300 8200 +57°277	KI 11-111 G8 III-IV KO IV-V	2 <u>1</u> 2 <u>1</u> 0	2-b 1-b 2-b	
2469 2824 2925	G8 III-IV K2 III G8 III*	2 3 1	2-a 1-a 3-b	30 155	+57°280 +56°279 8997	G8 III-IV K1 Ib K2 V	4 2 0	1-a 1-a 2-b	
3250 3253 3293	KO II-III K2 III K2 III	$\frac{\overline{3}}{2}$	1-a 1-b 2-b		9033 9109 9277	K2 III KO III KO III-IV	3 0 1	2-b 1-c 1-b	
3323 3409	KI III KI III	$\tilde{3}^2$	1-b 1-a		9493 9900	G8 II-III Kl Ia	$\frac{1}{2}$	3-b 2-a	118
3411 3468 3651	K2 III K1 III K2 V X		3-b 1-b	42	9939 10309 10437	KO IV G8 III-IV	1 2 2⊥	1-b 2-b 2-a	100
3681 3690	KO III-IV KO III-IV		2-a 1-b	19 21	+57°375 +55°402	G8 IV KO III-IV	$\tilde{1}^2$	1-c 2-a	
3757 3767 3828	KO III-IV KI III	22	2-b 3-b 1-b		+58°295 +58°296	G9 III-IV KO IV	2 2 0	2-a 1-a 1-a	
3943 4029 4105	G9 III G8 III-IV K0 III	$\begin{vmatrix} 1 \\ 2 \\ 3 \end{vmatrix}$	2-b 1-b 2-b	52	10806 11043 11103	G9 Ib G8 III K2 II	3 2 34	4-b 2-b 2-b	
4407 4688	KO III KO III	3	1-b 1-b		11363 11383	KO III G9 III-IV	$1\frac{1}{2}$ 4	2-b 2-b	34 14
4719 +55°175 4831	KO III KI III KO III*		2-b 1-a 2-b	51	12139 12202	KO III-IV G8 III-IV	21 21 3	2-a 1-a	44
4832 4833 4934	K2 III G8 III K0 III	322	3-b 2-b 3-b		12306 12494 12772	G8 111 G8 IV K0 111	2 1 2	2-a 1-b 2-a	
5197 5234	KO III K2 III*	232	1-b 1-b	34	13056 13149 13437	K1 IV K2 III G9 II	0 4 31	1-a 2-b 2-b	44
5286 5361	K1 IV G9 III-IV	$\begin{bmatrix} 2\\2\\1 \end{bmatrix}$	2-b 1-b	7	13482 13982	K1 III-IV K2 III	$\begin{vmatrix} 0^2 \\ 3 \end{vmatrix}$	2-a 4-b	22
5395 5396 5430	G8 III-IV* K2 III G8 IV	3 4 21	1-b 1-a	57	13994 14039 14346	G8 11-111 K1 V K0 11	323	4-b 1-b 4-b	31
5516 5556	G8 III* K2 III	2 24	1-b 1-b	32	14571 14914 15440	K1 III K0 III-IV	322	2-b 2-b 2-b	48
+08°146 5747 5981	KO III K1 III	3 3	2-a 2-a	19	15499 15498 15619	KÎ III G9 III	3 21	2-b 2-b	11
6009 6098 6238	G9 III-IV K0 III-IV G8 II-III	$\begin{vmatrix} 0^{-} \\ 3^{+} \\ 3^{-} \end{vmatrix}$	2-b 1-a 2-a	74 39	15665 15673 15734	G8 Ib K2 III K0 III		1-b 1-b 1-b	
+56°195 6555	G8 III K0 III-IV	322	1-a 1-b		15953 16039	KO III KI III	$\begin{vmatrix} \tilde{1}^2 \\ 4 \\ 2 \end{vmatrix}$	1-b 2-b 2-b	

S Number: S Number: HD or BD Sp CN HD or BD Sp CN Quality (km/sec) Quality (km/sec) 3<u>1</u> 0 16448 K2 III 2-b 56 46316 K2 III 222211233231433123 2**-a** 16644 16843 G8 III-IV G8 III-IV 46607 G8 III 1-c 2**-a** G8 III-IV G9 III-IV G8 III-IV 2 1 0 1-b 46702 1-a 17046 17190 G8 K2 III-IV 2-b 47254 2-a IV* 2-b 126 47586 1-c KÕ G9 III II K2 K0 K1 K0 III III 17309 2312222322 3-b 47587 1-c 17346 4-a 47726 2-a III III-IV 17675 G9 III 2-Ъ 58 48091 2-a 18560 Kl III 1-a 48432 2-a 18 KO KO KO K2 18749 II l-a 49116 III 1-a 18991 ĪV 2-a 15 49237 ĪĪĪ 1-a 19077 Kl 49399 III l-a Kl I٧ 1-a 1-b 19089 KŌ ĪĪ 58680 G8 ĪİI 1-a +58°569 K2 III 58944 G8 III-IV 1-b l-a 20524 ĸĩ III-IV 59506 ĸō ĪĪĪ 2-b 13220313333332222222333 1-a KI III-IV KI III-IV 20762 KŌ 1-a 59621 II-III 2-b III III-IV III-IV 20930 KÌ 1-a 61 59642 2-b K1 K0 K2 K0 22400 60252 KO ĪĪĪ 1-a 2-b 22844 1-b 60272 G9 V 0333233333203310 2-b 22886 ĨĨĨ 1-b 60294 K2 III 2-b 12 24154 II-III 1-b K2 III 2-b 61 60982 25877 G8 Ib-II* K2 III 1-b 1-b 62564 KO 1-a III ĪĪ-III 26755 1-a G8 42 +57º1104 KO III-IV K1 III 27029 2-b 2-b 3-b K1 III 62808 27224 KŌ III 1-a 63628 III* III-IV III 27371 KO 2-b 2-b 6-a 33 33 66660 K1 K1 27697 ĸŏ 67368 68077 3-а G8 II G9 II-III* 2-b 1-b 28085 1-b G9 III 13 5-a 23 35 68193 K2 II-III 28100 6**-a** 1-b 2-b 1-b 28307 G9 III* 68638 G8 V 68683 +55°1275 G8 III-IV KO III 29117 2-b 2-b 30166 KO III G8 III-IV 1-b 70918 31324 Kl III 46 KO III 2-Ъ 31646 31757 32547 G9 III-IV +57°1141 1-b 2-b KO V 70985 G9 III 2-Ъ G8 III 3233311 2333223 2-b G8 III K2 III K1 III K0 II-G8 II-2-b 71111 KO III 1-b 12 21 33618 3333232323443335<mark>1</mark> 23344333232333 2-b 71224 K1 G9 K1 K0 G8 III-IV 2-b 34786 1-b +56°1305 III 1-b II-III II-III III-IV III-IV 2-b 2-b 34853 1-b 71905 72003 36770 1-b K1 G9 ÎÎI III III II 36850 1-b 72604 3-a 1-b 37007 ī-b 72742 4333303222322323332343 37601 KO K2 K2 K2 K0 K0 K0 K0 III 1-b 49 73469 III-IV 2-ъ 73553 ĪĪĪ 39628 I٧ 1-b G8 1-b G8 G9 40141 III 1-b 73598 III-IV **4-**b 28 4082 III 1-b 73665 III 4-b 40872 II-III 1-b 74150 KO III-IV 1-c KO K1 KO 41589 ĪĪĪ 1-b 74379 III 1-b 41597 III* 1-b 37 74442 III-IV* 3-a 43 41783 III 1-b 74908 III 1-b 42721 G8 II-III 75697 KO III-IV 1-b 1-b KI III KI III KI III 43352 2-a 76428 G8 III-IV 2-a KI III-IV KI III 78249 86 44061 3-a 2-a 44123 3**-a** 78865 2-a III III-IV III-IV III 44647 G9 2-b 78937 2-а Kl III III 44648 Ğ8 79675 KI 2**-a** 4-a $1\frac{1}{2}$ 4 $2\frac{1}{2}$ 4344649 45388 G8 K2 79702 80792 Kl IV III-IV 1-b 1-a 2-b KO 1-a III-IV III 45410 III III ĩ-b 2-b 123 81338 K2 KO 2-a 83285 1-a KO 45636 K2 KI III-IV G8 III G8 III K2 III-IV 83491 83564 45742 2**-a** $\frac{1}{3}^{\frac{1}{2}}$ 2-b 45878 1 1-c 2-a

TABLE 2 - continued

Number: S Number: S CN CN HD or BD HD or BD Sp Sp Quality Quality (km/sec) (km/sec) 83588 3 31 2 2-b 2-b 2-b 47 K2 V 0 1-b 2-b 2-b 109654 KO III KÕ III G9 III-IV 84779 85459 109702 ĪĪĪ K2 4212230 109894 G9 III 85459 85472 85945 86217 86335 v õ 2-b 110463 K2 G8 IV 3-a 110762 III 4 4 1 3 78 K2 2-b G8 III 1-b 1-b 111093 III-IV K2 III KJ 1-b ÎV III-IV III-IV 111094 2-b 21 KO 1-c 2-b K1 198 111850 86661 2**-**b KO G8 IV ĩ-b 2-b III III-IV 2-b 2-b 112395 G9 87045 Kl III 87421 +59°1290 113253 G9 K1 III G8 III-IV 13 114107 1-b KO III-IV l-c 88800 KO III-IV 1-b 114535 K1 II-III 2-b 88999 K2 \mathbf{III} 3022224333223 2-b 114633 G9 III 2-b 89523 G8 IV 1-c 115019 K2 II 1-b 89862 KŌ III-IV 2-b 115442 KO III-IV 2-ъ 90222 G8 III 1-b 115720 G9 IV 2-b 10 90715 G8 III-IV 1-b 115749 G8 III l-c 2-b 2-b III-IV III 90859 KO 1-b 116956 G9 IV-V 21 0 91810 K2 1-b 117417 KO III KO KO K1 91971 G9 III Ī-b 119332 IV-V 2-b 93859 K2 III 2-b 119347 IV 0 3 3 2 2 2 1-b 33 26 119549 III 2-b 2-b 94631 KO III-IV 2-b 2-a 94862 ĪĪĪ 123338 KÖ III-IV G8 KO III G9 III III-IV II-III 95001 G9 2-a 123977 III-IV* 2-ъ 94 95098 K2 124319 2-b 2-a K2 G9 0 1 3 2 2 3 2 3 2 2 2 3 2 2 2 125260 95690 K2 V l-a III 2-b 96688 KÕ İII 2-b 125918 ĪĪ ĩ-b G8 IV K1 III 96708 G8 III 2-b 126186 1-b K1 K2 96717 KO ĪV +57°1509 1-b l-a 97934 127760 III 1-b KO IV l-a 98214 ĪİI +55°1691 KÕ ĪV 1-c KÓ 3-a 23 98316 128386 G9 III 1-b G8 III 1-a 99283 KO III 41 128781 K1 III 1-b l-a 129267 KO III-IV ĩ 99489 KO III 2-b 1-b Ĩ-Ď 99807 III-IV 129580 G8 IV 0 1-b 69 KO $\frac{\tilde{3}_{1}}{3}$ 21 3 129937 K2 1-b 100403 KO III 2-b III 100615 KO III 1-a 1-b 2-b 130499 K2 III 1-b 38 KO III K2 II-III K2 III K0 III K1 III 31 2 3 1 2-b 1-b 101090 4 2 3 131219 KO III G8 III 102194 148228 27 102251 9 152153 KO IV 1-b 1-b 102569 102956 +26.2979 G8 III-IV 10 $2\frac{1}{2}$ 3 $3\frac{1}{2}$ 2-b 1-c KO III KI III KI IV KO IV K2 III* K1 III-IV K0 III-IV 4 3 156774 3-b 1-a 51 103605 104239 41 1-b 29 156775 l-a 156841 4 1 2 1-b l-a 2-b 2-b III 21 0 19 105440 156874 KO 1-b +28°2720 105719 KO IV 132241222333302 G8 II-III 1-c 157150 106102 K2 2-b 1 III-IV G8 III 1-c $\frac{\overline{2}}{3}$ KO III-IV 106711 1-b 157294 G9 III* 1-a 110 107325 K2 III-IV 4-b 41 158038 Kl IV* l-a 47 88 73 G8 IV-V 107468 KO III* 2-b 158331 0 1-a 107469 KO IV 3-b 158332 K1 IV* 02023330 1-a 142 59 107854 K1 II-III 3-b 158416 K2 III l-a 107949 108123 K2 III 1-b +26°3026 G8 IV 1-c 26 KÎ III K2 III* 158507 1-a 4-b 50 G8 II-III III III* 108381 5-b 22 159027 K2 1-a 44 57 159479 162113 108466 Kl III* 3-b K2 l-a 19 G8 G9 108805 III* 3-b KO III 1-b 69 162135 108861 III 1-b 41 G9 III 1-ċ 109011 Κl V 2-b 166070 K1 III* 1-c 37 4 3 4 58 47 109012 K2 III* 3-b 77 166730 G8 III* 1-c ĩ 109508 G8 IV 166842 KO III-IV 1-a 1-c 109627 KO III-IV* 3-b 61 167132 G8 IV* 2 1-c 44

TABLE 2 - continued

TABLE 2 - continued

HD or BD	Sp	CN	Number; Quality	S (km/sec)	HD or BD	Sp	CN	Number; Quality	S (kom/sec)
167275	KO II*	4	1-a	93 45	186223	K2 III* G8 III*	3 2⊥	2-b 1-b	47 65
167472	KI III*	4	1-a	58	186378	K2 11-111	$\tilde{4}^2$	1-b	68
168293	G8 III	1	1-c	70	186486	KO II*	21	1-b	071
169573	KO III*	3	1-c	70	+27.3492	G8 III	ĩ	1-0 1-c	1
169797	G8 III-IV*	Ĭ	1-a	25	186815	K2 III	4	2-b	21
170289	KI II	1	1-c	105	+25•3944	KO II-III	1	1-c	
170737	G8 111-1V*	3	1-0 2-b	192	186930	G8 TI-TTI*	1	1-b	64
171164	KI III*	2	Ĩ-Ď	63	187193	KO II-III	$\overline{2}_{\frac{1}{2}}$	1-b	72
171830	G7 III*	3	2-b	61	187280	K1 III*	2	1-c	72
172132		缩	1-D 1-D	38	+26°3688	K2 II-III	4	1-0 1-b	≥113
173367	KO II-111*	$\tilde{2}^2$	l-b	129	188258	KĨ III-IV*	3	1-b	29
173435	G9 III*	21	2-b	26	188259	KO III-IV*	3	1-b	36
173702	K2 TTT*	$\frac{2}{3}$	2-D 1-h	9	188000	KO II-III*	22	1 1-0 1-h	52
+26°3350	KŽ III	3	2-b		189127	G9 III	ĩ	3-a	58
+27°3110	KO III-IV	2	1-b	75	189251	G8 II	3	1-b	1
+27•3112	K2 III	2	1-0 2-h	75	189533	G9 III	4	2-b	20
174180	Kĩ II-III	$\tilde{4}$	Ĩ-Ď		189843	G8 III-IV	4	Ĩ-b	
174414	K2 III*	3	1-b	36	190913	KO III	3	1-b	
174095	G9 111-IV	4^{32}	1-b 1-b	30	191009	KO III-IV	ŝ	1-b	
174881	K1 II-III	3	Ī-Đ	30	192806	K2 111*	21	1-b	26
175204	G8 III-IV*	1	1-b	42	192892	G9 II-III*	2	1-b	33
$+20^{-}3394$ 175940	K2 III*	3	1-0 1-b	40 59	+28°3682	G8 IV	0	1-0 1-c	
176230	KÕ III*	4	Ī-b	54	193094	KI III	3	1-b	19
176527	K2 III*	21	1-b	27	193221	K2 III*	4	1-b	24
+28°3155		$ \frac{4}{4} $	1-b 1-b	65	193342	KI III	2	1-b	
+27°3217	KO III-IV	ō	1-c		194033	K2 II-III	3	1-b	11
178276	K2 III-IV	$\frac{31}{4}$	l-a	16	194071	G8 II-III*	2	1-b	30
+28°3210		$\frac{4}{2}$	1-a 1-a	10	+28°3729	KO III*	3	1-b	89
+26°3472	KO II*	2	1-a	50	194260	G8 III-IV	3	5-a	
+26°3485	KO Ib	2	1-a 1 b	70	194403	K2 III*	3	1-b	26
180161	G8 V	0	1-b	52	194450	K2 II-III	3	1-b	0.5
+28°3245	KO III-IV	31	l-a		195100	G8 III*	2	4-a	
+28°3250	G8 111 K2 111	23	1-a. 1-9		+28•3761	G8 III G8 III	3	4-a 1-c	
180656	KĨ II	3 <u>1</u>	1-a 1-b		195273	KO II-III*	3	1-c	52
+28°3262	G8 II-III	31	l-a		+41 •3775	KO II	2	2-c	70
181069	KI III KO Ib-II*	$\frac{4}{3}$	1-a 2-a		+27*3773	G9 TTT*	涩	1-0 1-b	40
182617	KI III*	3	ĩ-b	28	195647	KÔ III	$\tilde{3}^2$	5-a	
183399	Kl III*	3	1-b	26	195712	G8 II*	2	1-b	51
+28°3339		4	1-C 1-h	15	195835	KO TT	4	1-b	24
183753	KŽ II-III*	ī	Î-Ď	141	195987	KO IV*	ō	5-a	70
183754	K2 II	2	1-b	5	196134	KO III-IV	놖	5-a	46
184010	KO III-IV	$\frac{1}{2}$	1-C 1-D	16	190300	K2 III	2	0-а 4-а	63
+27°3426	G8 III	ĩ	1-c		198821	K1 III*	3	1-b	13
184538	K2 III*	3	1-b	13	+25°4418	G8 IV KI III-IV ×	0 %	1-b 2-b	10
185289	G7 III*	2	1-0 1-b	12	199375	G8 III*	24	1-b	44
185982	G8 III*	2 <u>1</u>	2-b	55	199512	KI IV	2	1-b	

TABLE 2 - continued

		_							
HD or BD	Sp	CN	Number; Quality	S (km/sec)	HD or BD	Sp	CN	Number; Quality	S (km/sec)
199693 199717 200206 200491	K2 III G8 III-IV* K1 III G8 III*	$\frac{1}{2}$ $\frac{3}{2^{\frac{1}{2}}}$	1-c 1-b 1-b 1-b	59 56 23 27	208563 208667 208700 208799	K2 II-III K1 III-IV K1 III* K1 IV	23432	1-a 3-a 2-b 1-a	53
200578 200679 200831 200844	KO II-III* KO Ib* K2 III KO U	3 31 4 2	2-0 1-b 1-a	28 20	208839 209180 209181 209543	KI III-IV KO III-IV G9 III-IV*		1-b 3-a 3-b	48 58
201051 +28°3995	KO II-III KO III-IV	2 1 1	3-b 1-c	29	209694 209761	K1 IV K2 III	3	1-b 3-b	29
201626 +27°3988	G9 p* G8 II-III	02	2-b 1-b	≥140	209992 209994	KO Ib G6 III*	3	1-a 2-b	90
201669 201890 202089	68 111* K1 III K2 III	2 2 3 1	1-b 1-a	75	210026 210144 210211	KO IV KO IV G8 III-IV	0 0	1-a 3-a	253
202365 +27°4021 202521	G9 II-III* G8 IV K2 III* C9 II III	3041	1-0 1-0 1-c 1-b	110 71	210373 +20°5090 210608 210685	KI IV KO III-IV KO III*		3-a 1-a 2-c 2-b	28 37
202696			1-b 2-8	59	210003	K1 III-IV*	$1\frac{1}{2}$	3-b 3-a	70
203030 203344	G8 IV* K1 III*	0 ² 3	1-b 1-a	32 126	210925 211006	K1 III* K2 III	1 <u>1</u> 3 <u>1</u>	2-b 2-b	131 30
203886 204079 204415	KO III-IV* KI IV* KO III	2 1 0 2	1-a 1-b 1-a	16 139 28	211153 +28°4330 +22°4593	G8 16-11 G8 III K0 III	1 0 3	2-a 1-c 1-b	
+26°4170 204539	K1 III-IV K2 III*	4	1-b 2-b	48	+25°4696 211407 211432	K2 III G8 III-IV*	333	2-b 2-b 2-b	78
204540 204642 204711	K1 III-IV*	33	2-b 2-b 1-b	97 103	211452 211460 211555	G7 II-III* K1 III*	11	2-b 2-b 2-b	194 44
204721 204878	KO III KO II	2	1-b 1-b		+23°4513 211984	G8 III G8 II-III	12	1-b 1-a	87
204892 204923 204934	KO III-IV KI III*	24	1-b 1-b	161	212005 212136 +21 •4738	G8 III-IV	3	2-b	
205011 +26°4191	G8 Ib G8 II-III	$\begin{vmatrix} \tilde{3}_{\frac{1}{2}}^2 \\ 1 \end{vmatrix}$	1-a 1-c	116	212416 212596	K2 III-IV K2 III	3 <u>1</u> 3	2-a 1-b	
205316 205540	KO II* KO III	12	1-b 1-b	106	212750 212833	KO III* K2 III-IV	3	1-a 2-a	65
205553 205602 205760	KO III	3	1-a 2-a 1-b	12	213015 213025 +20°5162	G8 III-IV*		1-0 1-a	20 49
+29•4458 205836	G8 IV K0 II-III	1	1-b 1-b	26 187	213178 213179	KO III* K2 II	3 4	1-a 1-a	19
206027 206169	G9 III K0 III	33	2-b 1-b	29	+24 • 4603 213787	KO III G9 IV	3	1-a 3-b	76
206536 206646 206842		2 3	2-0 1-a 2-b	20 25	213803 213930 213994	G8 III-IV G8 III-IV G9 III-IV	3 ²	2-b 1-a	24 24
206889 206990	KI III* G9 III-IV	4 31	1-b 2-b	93	214099 214265	KO III-IV KO II-III*	$\begin{vmatrix} \bar{4} \\ \bar{3} \end{vmatrix}$	1-a 1-a	73
207086 207089 207134	G9 III G8 II-III*	$\begin{vmatrix} 2\frac{1}{2} \\ 4 \\ 2^{1} \end{vmatrix}$	2-b 1-a	114	214434 214543 214757	KO III-IV*	$\frac{3}{1}$	1-a 1-c 2-0	28
207134 207244 207470	KO III-IV G7 II-III*	12	1-c 1-c	44	215041 215183	K2 III-IV G9 III	24 14	2-a 2-a	65
207719 207740	KO III G8 IV*	3	1-a 1-b	32	215361 215445	K1 III-IV G9 III-IV		2-а 2-а	12
208107 208201 208330	KI III-IV G8 II-III KO III	3 11 1 1	1-a 2-b 1-c		215522 215567 215771	KO III-IV KI III KO III-IV	0 3 2 1	1-c 1-b 1-a	

œ
•
•
4
\sim
L
•
•
•
ь
Q
4
-
9
0
-

76 O

Number; Number; S S HD or BD CN HD or BD CN Sp Sp (km/sec) (km/sec) Quality Quality +25°4819 G9 III KO IIp K2 II-III G9 II 221293 3 20 0 1-b 1-a K1 V* 216046 216218 221354 221364 2-a 1-b 3 0 l-a G8 IV* 15 3 2-a 1 +28°4474 216502 221395 221639 G8 III-IV 1 1-b K2 III 3 2-b 50 24 $\frac{\hat{3}_2}{4}$ K1 III-IV* KO III-IV 2-а 1-b 35 216586 K1 III-IV* G8 III-IV G7 II-III* 1-b 60 221670 G9 \mathbf{III} 2**-a** 216712 216723 2-b 1-b 3 2 221786 K1 III-IV l-a G9 III-IV 1-b 40 222067 216730 2 2-b 222078 G8 III KO III-IV 1-b +58°2522 217673 44 G8 IV 1 l-a 222218 KO III 2**-a** 312 2 2 2 0 õ KO II-III* 3-a 222366 KO IV 2-b 217711 Kl III 2-b 12 222390 KO II-III* 4 1-b 49 III V G8 III G9 III 217797 KO l-a 222618 ž 2**-a** 16 +57°2673 217850 K2 $1\frac{1}{2}$ 2 3 0 3 3 3 3 l-a 222797 3-b 16 G8 V 0 l-a 222842 KO II-III* 1-b 26 217944 22 26 G8 IV 1 222886 G9 III-IV l-a 4-a 31 3 3 3 3 3 3 3 3-а 3-b 218187 G8 III 223019 G8 III-IV* 1-c 78 34 42 K2 III K2 II-III* Kl Ib-II* 223094 218356 1-c 14 33 218468 KO III 2-b 223165 1-b 39 218660 K1 III* 1-b 223211 K2 III-IV* 3-b 218803 G8 III-IV 21 1 1 2 4 4-a +58°2659 K1 III 1-a +59°2660 2-b 223792 212 3 2 2-b 37 KO G9 III KO III G8 III-IV 119 54 218935 ĩ-Đ 223847 KÖ ĪĪĪ 1-a 62 219110 219310 K2 III K0 III-IV 3-а 1-b G8 III K2 III 224116 Ī-b 58 2-a 332223 +56°3112 G9 III G8 III-IV* K1 III K0 III 224355 2-b 2-b G8 Ib G9 III-IV 219446 1 2 2 2 2 2 2 1 1 2 1-а 3-а 219800 220265 62 224784 65 K2 III-IV G9 III 2-b 2-b 224907 2-а 3-а 224940 +59°2815 220539 220583 G9 II-III K2 II 1-b G8 III 1-a 14203 220952 221039 221113 224981 225170 ĸ2 Kl IV 2-b 49 l-a G8 IV G9 V KO III-IV KI III-IV 2-b l-a 225261 21 2 2 2-b 58 2**-a** 221204 225274 G9 III KO III-IV 2**-**b l-a

TABLE 2 - continued

* Also classified elsewhere on MK system.

the weak CN stars relative to normal CN stars. The "z" components of distance have been computed for the program stars listed in Table 2 with luminosities II–III through III–IV. The luminosity classes have been converted to visual absolute magnitudes with Roman's calibration (1952). Whenever MK classifications from elsewhere are available, as indicated by asterisks in Table 2, the absolute magnitude depends on the mean of the two luminosity classifications. The *Henry Draper* visual magnitudes have been used when available, with no correction for interstellar extinction. For the BD stars, the magnitudes listed in the proper-motion catalogues have been used. The largest source of error in the resulting "z" distances is the absolute magnitude. Virtually all the program stars are within 300 pc of the galactic plane. For 65 per cent of the stars, the galactic latitude is less than 30°. Thus the error in "z" is less than 50 pc in most cases.

The sampling is not uniformly distributed in galactic latitude, and the depth of the survey is relatively small. Nevertheless, the frequency distributions in "z" for the stars with both normal and weak cyanogen absorption can be approximated by normal distribution curves. The dispersions of the normal curves are 121 and 162 pc for 462 normal CN stars and 84 weak CN stars, respectively. The stars with normal cyanogen absorption actually deviate significantly from their normal distribution curve, but in that an excess of stars are concentrated within 20 pc of the galactic plane. The comparison clearly shows a lower concentration toward the galactic plane for the stars with weak cyanogen absorption.

IV. SPACE VELOCITIES

Space velocities have been computed for 256 stars with luminosity classes II–III through IV for which radial velocities are available. One hundred and twenty radial velocities are from David Dunlap Observatory (Heard 1956), 113 are from Wilson's catalogue (1953), and an additional 25 are from spectrograms obtained by the author, using the Mount Wilson 60-inch reflector and x-spectrograph. Proper motions for 239 of the stars have been take from the Yale proper-motion catalogues (Barney 1953; Barney, Hoffleit, and Jones 1959), while the remainder are from the *General Catalogue* (Boss 1937). The proper motions from the *General Catalogue* and from the $+57^{\circ}$ Yale zone have been converted to the FK3 system, using Kopff's corrections (1939). The proper motions for the remaining Yale zones are already on the FK3 system. The resulting space velocities, which have been corrected for solar motion of 15.5 km/sec toward R.A. = 265°, Dec. = $+21^{\circ}$ (Vyssotsky and Janssen 1951), are listed in the last column of Table 2.

In Table 2, the velocity of HD 201626 is based on its radial velocity alone. This is a CH star (Keenan 1958b), with no available absolute magnitude. The velocity of $+26^{\circ}3688$ is based on proper motion alone and is included in Table 2 only because it is also listed in Table 4.

The frequency distributions for the space velocities are shown in Figure 2. The stars of luminosity class II-III through III-IV have been divided into three groups, normal and strong CN, slightly weak CN, and weak CN, and are shown in Figure 2, a, b, and c, respectively. Figure 2, d, shows the distribution for stars of luminosity class IV with weak cyanogen absorption. Seven stars of luminosity class IV with stronger cyanogen absorption are included in Figure 2, a and b, shown as crosshatched areas. Figure 2, e, will be discussed in Section VI.

The accuracy of individual space velocities is limited by the largest source of accidental error—the absolute magnitude, which is accurate to about 1 mag. and which gives for typical giants an uncertainty of about 20 km/sec, as compared with about 5 km/sec for the uncertainty caused by the error in proper motion. The random errors increase the dispersions of the frequency distributions. Nevertheless, it is evident, even with the low precision of the individual velocities, that the dispersions of the frequency distributions increase with decreasing cyanogen strength.

The frequency distribution for the stars of normal cyanogen strength (Fig. 2, a) is

KENNETH M. YOSS

similar to the frequency distribution for Miss Roman's strong-line and weak-line stars combined (1952). On the other hand, the space velocities of the subgiants (Fig. 2, d) generally are less than those of the subgiants compiled by Eggen (1960).

V. 60-INCH ABSOLUTE MAGNITUDES

The precision in absolute magnitude has been increased for 37 program stars by means of slit spectrograms obtained with the Mount Wilson 60-inch reflector and x-spectrograph, using both the 4" and 8" cameras, with dispersions of approximately 80 and 40 A/mm. This group consists of 29 weak and slightly weak CN giants and subgiants, 6 normal CN giants and subgiants, and 2 weak CN supergiants (one of which is spectral type K3 and thus not listed in Table 2).

In order to establish a calibration-curve for absolute magnitude, spectra were also obtained for 42 standard stars from spectral type G0-K4. All the plates are baked IIa-O emulsion, standardized with the wedge spectrograph located in the 60-inch dome. The exposure times of the calibration plates are generally about one-third as long as the



FIG. 2.—Frequency distributions for space velocities of G8-K2: *a*, strong and normal CN giants (CN3, 4); *b*, slightly weak CN giants (CN 2, $2\frac{1}{2}$); *c*, weak CN giants (CN 0, $1, 1\frac{1}{2}$); *d*, subgiants with weak CN (CN 0, 1); and *e*, weak CN giants, based on improved absolute magnitudes. The crosshatched areas in sections *a* and *b* show stars of luminosity class IV; the crosshatched areas in section *e* show stars from Griffin and Redman's list (1960).

exposure times of the stellar plates, to compensate partially for the intermittency effect due to the multiple trailing of the stellar images along the spectrograph slit. Several calibration plates of varying exposure times were exposed at regular intervals throughout each night. Development times of both calibration plates and stellar spectrograms were $5\frac{1}{2}$ minutes at 66° F in D-19.

The 60-inch standard stars are from the lists of Wilson and Bappu (1957), Oke (1957), and Keenan and Keller (1953). A number of these stars have high space velocities and/or weak cyanogen absorption. The method of Wilson and Bappu is apparently relatively insensitive to abundance differences and has a high internal accuracy. Oke's method depends on line ratios and thus also is relatively insensitive to abundance differences, while Keenan and Keller were concerned specifically with luminosity criteria suitable for high-velocity stars. Other spectroscopic parallaxes are available but generally depend on visual estimates of line strengths or line ratios or are expressed in terms of MK luminosity classes instead of absolute magnitudes. Reliable trigonometric parallaxes are available for the majority of the stars used for calibration, except for the supergiants (Jenkins 1952). For absolute magnitudes fainter than -1, each value used for the calibration-curve is the mean of the absolute magnitudes available from the above four sources. For stars brighter than -1, the values of Wilson and Bappu are used. The internal accuracy of the absolute magnitudes of both Wilson and Bappu and Oke is ± 0.3 mag (m.e.). The resulting mean absolute magnitudes for the standard stars generally are accurate to ± 0.3 mag. also. The G5-K3 stars are listed in Table 3. The sources for the spectral and luminosity classifications are the same as for the standard stars in Table 1, and the asterisks in Table 3 have the same meaning as in Table 1. For stars in common with Table 1, the Schmidt CN strengths have been repeated in column 3 of Table 3. For an additional seven stars in Table 3, "cyanogen equivalents" have previously been measured (unpublished). The results have been discussed elsewhere (Yoss 1958). These cyanogen equivalents have been included in column 3 of Table 3 and are shown in parentheses. They have been converted to the CN step scale of the present investigation. The seventh and eighth columns of Table 3 give the mean absolute magnitude and the sources of the absolute magnitudes making up the mean.

Microphotometer tracings on a scale of direct intensity were made of all 60-inch spectrograms at the California Institute of Technology. In most cases only one plate per star is available. Therefore, the analyzing slit was set relatively wide -20 and 30μ for the 4" and 8" plates, respectively-reducing plate grain effect but, at the same time, reducing resolution. Line-intensity ratios involving lines which are luminosity-sensitive have been measured relative to a fiducial continuum. The ratios are relatively insensitive to the exact location of the continuum or zero intensity and also to the calibration-curve used to produce the direct-intensity tracing. Ratios used by Keenan and Keller (1953) and Oke (1957) were measured on the 60-inch tracings. Of these, several have steep calibration-curves, others have relatively large scatter, and two ratios in particular are strongly correlated with cyanogen absorption and therefore cannot be used. These last two ratios, $\lambda 4161/\lambda 4149$ and $\lambda 4196/\lambda 4198$, both fall within the cyanogen absorption band. The line ratios found to produce good calibration-curves for the 8" plates are $\lambda 4077/\lambda 4063$, $\lambda 4077/\lambda 4071$, $\lambda 4129/\lambda 4127$, $\lambda 4152/\lambda 4154$, and $\lambda 4215/\lambda 4250$. The line ratios producing useful calibration-curves for the 4" plates are $\lambda 4077/\lambda 4063$, $\lambda 4077/\lambda 4071$, and $\overline{\lambda} 4215/\lambda 4250$. These individual ratios have been combined to form mean line ratios for each dispersion. The mean line ratios for the 4'' dispersion are systematically less than those for the 8'' dispersion by 0.07. After this correction has been applied to the 4" ratios, they have been combined with the 8" line ratios to form a single calibration-curve relating line ratio and absolute magnitude. The mean line ratios are shown in the sixth column of Table 3, where, in the case of the 4'' plates, the ratios have been corrected to the 8" system; the number of plates is given in parentheses. The calibration-curve for the G5-K3 stars is shown in Figure 3. The slope changes slightly over

TABLE 3

60-INCH STANDARD STARS FOR SPECTRAL TYPES G5 THROUGH K3

HD	Sp	Schmidt CN	60-in. CN	60-in. △ CN	Mean Line Ratio	M.	Ref **
3546 3627 3651 4128 6582 9270 27371 124897 135204 144579 148897 150275 153210 161797 163770 163770 167042 168723 180809 182572 184406 185351 188512 197989 198149 206778 206859 212943 216228 219134 219615 222107 222404	G8 III K3 III K0 V* K0 III G5 Vp* G8 III* K0 III* K0 III* K2 IIIp* G8 V G8 V G8 II K1 III K1 III K1 III K0 III-IV* K0 III-IV K2 Ib* G5 Ib* K0 III-IV* K1 III K3 V* G8 III-IV* K1 IV*	(1) (1) (1) (3) (3) (2) (2) (1) (4) 12 3^{1} 3^{2} 3 12 14 42 02 12 12	+0.08 .21 .08 .18 .03 .22 .21 .18 .06 .03 .09 .09 .09 .09 .21 .07 .25 .11 .13 .25 .08 .23 .13 .20 .07 .15 .12 .15 .22 .11 .19 .07 .07 .40 .17	$\begin{array}{c} -0.09 \\ +0.01 \\ +0.02 \\ -0.01 \\ -0.02 \\ +0.01 \\ +0.02 \\ -0.02 \\ 0.00 \\ +0.01 \\ -0.02 \\ -0.04 \\ +0.01 \\ -0.03 \\ +0.01 \\ -0.03 \\ +0.03 \\ +0.03 \\ -0.03 \\ +0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.03 \\ -0.04 \\ +0.01 \\ -0.04 \\ +0.01 \\ -0.04 \\ +0.01 \\ -0.04 \\ +0.01 \\ -0.04 \\ +0.01 \\ -0.04 \\ +0.01 \\ -0.04 \\ +0.01 \\ -0.09 \\ +0.02 \\ -0.09 \\ +0.02 \\ -0.09 \\ +0.02 \\ -0.09 \\ +0.02 \\ -0.09 \\ +0.02 \\ -0.09 \\ +0.02 \\ -0.09 \\ +0.02 \\ -0.09 \\ +0.02 \\ -0.09 \\ +0.02 \\ -0.09 \\ +0.01 \\ -0.00 \\ -0.02 \\ -0.00 \\ $	$\begin{array}{c} 1.08 & (1) \\ 1.07 & (1) \\ 0.73 & (1) \\ 1.10 & (1) \\ 0.54 & (1) \\ 1.23 & (1) \\ 1.23 & (1) \\ 1.13 & (2) \\ 1.09 & (2) \\ 0.69 & (1) \\ 0.56 & (3) \\ 1.12 & (2) \\ 0.69 & (1) \\ 0.56 & (3) \\ 1.12 & (2) \\ 0.68 & (2) \\ 1.06 & (1) \\ 0.96 & (2) \\ 1.06 & (1) \\ 0.96 & (2) \\ 1.16 & (2) \\ 0.91 & (1) \\ 0.96 & (2) \\ 1.16 & (2) \\ 0.91 & (1) \\ 0.95 & (2) \\ 1.01 & (1) \\ 0.88 & (2) \\ 1.01 & (1) \\ 0.95 & (2) \\ 1.12 & (1) \\ 0.95 & (2) \\ 0.94 & (2) \\ 0.94 & (2) \\ 0.94 & (2) \\ 0.94 & (2) \\ 0.95 & (2) \\ 0.94 & (2) \\ 0.95 & (2) \\ 0.94 & (2) \\ \end{array}$	$\begin{array}{c} +1.7\\ +0.52\\ +50.662\\ +50.652\\ +0.52\\$	a,d c,d b,d,d b,c,d a,b,d c,d c,d c,d c,d c,d c,d c,d c,d c,d c

×

Johnson and Morgan (1953) or Morgan and Roman (1950). a) Keenan and Keller (1953), b) Oke (1957), c) Wilson and Bappu (1957), d) Jenkins (1952). **

 $\ensuremath{\textcircled{}^\circ}$ American Astronomical Society • Provided by the NASA Astrophysics Data System

the spectral range, but the change is less than the scatter of the points and therefore cannot be clearly defined. The weak CN stars are shown as open circles. No systematic dependence of the line ratios on cyanogen absorption is apparent on the basis of these relatively few data. If only trigonometric absolute magnitudes are used, individual points change, but the mean curve changes insignificantly. The solid line represents a weighted mean least-squares solution for the stars between absolute magnitudes -1and +5.5. The mean error of a single determination of absolute magnitude from one plate has been determined by intercomparison of pairs of plates, as well as by the leastsquares solution, assuming the mean error of the absolute magnitudes to be ± 0.3 mag. Both approaches give consistent results, the mean error being about ± 0.5 mag. for one 60-inch plate. For stars brighter than -1, the scatter is large and the slope steep, and thus the calibration-curve cannot be used. The line ratio used by Oke (1957) for the



FIG 3 —Calibration-curve, relating mean absolute magnitude and mean line ratio for the 60-inch standard stars The open circles represent stars with weak cyanogen absorption. The crosses represent Oke line ratios (1960), converted to the 60-inch system

bright giants and supergiants, $\lambda 4233/\lambda 4236$, produces a well-defined calibration-curve for the stars brighter than -1.

For fifteen standard stars which have also been measured by Oke (1957), the 60-inch and Oke line ratios show a linear relationship. The Oke line ratios of stars not included in the present investigation have been transformed to the 60-inch system and are shown as crosses in Figure 3. These points have not been used in the least-squares solution but do show good agreement with the curve.

The "CN discontinuity" has been formed by measuring the ratio of the continuum difference on each side of the λ 4216 band head of cyanogen divided by the strength of the continuum on the red side of the band head. The CN discontinuity is given in column 4 of Table 3. The least-squares solution for the linear relationship between the Schmidt CN measurements and the CN discontinuity of the 60-inch plates is

CN (Schmidt) = -0.1 + 15.1 CN (60-inch),

with a scatter consistent with the accuracy of the Schmidt data.

A calibration-curve relating CN discontinuity and absolute magnitude has been formed for the 60-inch standard stars with normal cyanogen absorption. Following the procedure of Keenan (1958b) and Griffin and Redman (1960), the "CN discrepancy," Δ CN, is defined as the difference between the measured CN discontinuity and the value obtained from the calibration-curve for a given absolute magnitude. The resulting CN discrepancies are given in column 5 of Table 3.

On the Schmidt scale, the weak CN stars are defined as those stars with cyanogen absorption weaker than normal by one or more steps. On the 60-inch scale, the weak CN stars thus are defined as those stars with CN discrepancies equal to, or greater negatively, than -0.07. The weak CN stars shown in Figure 3 have been defined in this manner.

A calibration-curve relating spectral type and line ratios has been formed with the mean of the following line ratios: $\lambda 4227/\lambda 4102$, $\lambda 4254/\lambda 4260$, and $\lambda 4325/\lambda 4340$. For the dwarfs and giants, the internal mean error for a single plate is one subclass. The supergiants define a calibration-curve that deviates two subclasses toward later spectral types from that of the dwarfs and giants.

Five of the standard stars also are radial-velocity standards (*Trans. I.A.U.* 1955). Seven spectrograms were obtained of all five standards with the 8" camera, while four spectrograms were obtained for three of the standards with the 4" camera. Using the effective wave lengths of Wright (1952), a number of suitable absorption lines were found that give consistent measurements of radial velocity relative to the published values for the standards. The mean errors for a single plate are ± 5 and ± 10 km/sec for the 8" and 4" cameras, respectively. The 8" radial velocities also require a systematic correction of -7 km/sec. The mean error for the 4" plates is consistent with that found by Woolley (1959), while the 8" mean and systematic errors are consistent with those found by Abt (1960).

Spectral types, CN discontinuities, CN discrepancies, radial velocities, and absolute magnitudes have been measured for the 37 60-inch program stars. The results are given in Table 4, where the spectral and luminosity types and CN strengths from Table 2 are also repeated. The radial velocities, reduced to the sun, are given except in the cases when they have been published previously or when the plate is not suitable for measurement. The number of 60-inch plates is indicated in parentheses after the visual absolute magnitude.

The calibration-curve for the absolute magnitudes depends on line ratios measured on tracings of relatively short exposures of bright standard stars. The fact that exposure times are considerably longer for the program stars may possibly introduce a systematic error when the calibration-curve is used for determining absolute magnitudes for the fainter program stars. The measurement most subject to systematic error in the photometry is the CN discontinuity, where any error in slope of the assumed characteristic curve directly affects the measurement. For the standard stars, the relationship between the CN strengths of the Schmidt and 60-inch plates, shown in columns 3 and 4 of Table 3, is approximately linear, with the expected scatter corresponding to the accidental mean errors of the measurements. The scatter is much larger for the program stars, given in columns 3 and 5 of Table 4, and the mean relationship has shifted an amount corresponding to one CN step on the Schmidt scale; the 60-inch measurements are stronger relative to the standard star relationship. The systematic difference is not correlated with luminosity class. No systematic difference is evident between the CN strengths of the Schmidt spectra on the 10- and 30-minute plates or between the stars which have been classified on both program plates and standard star plates of short exposure. Most of the systematic difference therefore probably is in the 60-inch photometry. Line ratios, on the other hand, are relatively insensitive to variations in the slope of the assumed characteristic curve, and when various curves are used to convert the microphotometer signal to direct intensity, the measured line ratios for a given plate show no significant

TABLE 4

60-INCH PROGRAM STARS

* M_v is based on the 4233/4236 line ratio. ** The 4233/4236 line ratio gives M_v = +3.5.

KENNETH M. YOSS

variation over the range in slope between the calibration-curves of long and short exposures. The mean difference between the 60-inch and Schmidt spectral types for the program stars is 0.8 subclass. If a corresponding error were present in the line ratios for absolute magnitude, the maximum error would be 0.3 mag.

VI. 60-INCH SPACE VELOCITIES

Space velocities for the weak CN stars listed in Table 4 have been recomputed, using the absolute magnitudes derived from the 60-inch spectrograms, and are shown in the last column of Table 4. The resulting frequency distribution is shown in Figure 2, e. Six stars from Griffin and Redman's list with CN anomalies greater negatively than -0.10are also included in Figure 2, e. The absolute magnitudes of five of these stars are accurate to within 0.5 mag. The stars and their space velocities in km/sec are HD 3546, 102; HD 37160, 101; HD 81192, 130; HD 188119, 14; and HD 215549, 90. Although the absolute magnitude of the sixth star, HD 199191, is not accurately known, the star has been included on the basis of its high radial velocity, 185 km/sec. These six stars are shown as crosshatched areas in Figure 2, e.

Figure 2, e, does not include all known weak CN stars with available space velocities, but the stars in the diagram have been selected from random samples on the basis of their cyanogen strengths alone. The frequency distribution for these 27 weak CN stars includes a large percentage of high-velocity stars; 32 per cent have space velocities greater than 80 km/sec, as compared with 4 per cent for the stars of normal cyanogen absorption.

This investigation has been supported by the Council on Research of the Louisiana State University and by the National Science Foundation. I would like to thank Dr. Leo Goldberg and Dr. Freeman Miller, of the University of Michigan, for making available observing time with the Schmidt and for permitting me access to the plate collection; Dr. I. S. Bowen and his colleagues for permitting me use of the 60-inch reflector; Dr. Jesse Greenstein and Dr. J. B. Oke for use of the microphotometer of the California Institute of Technology; Dr. J. F. Heard, of David Dunlap Observatory, for kindly reclassifying several of the Dunlap stars; and Miss Katherine Bracher for measuring most of the radial velocities from the 60-inch plates.

REFERENCES

- Abt, H. A 1960, private communication.

- Barney, I 1953, *Yale Astr Obs Trans*, Vol 24 Barney, I, Hoffleit, D., and Jones, R. B. 1959, *Yale Astr Obs Trans*, Vol 27. Boss, B 1937, *General Catalogue* (Washington, D.C.: Carnegie Institution of Washington). Crawford, D. L. 1960, A J., 65, 343.
- Eggen, O. J. 1960, M.N., 120, 430.

- Griffin, R. F, and Redman, R. O. 1960, *M.N*, **120**, 287. Halliday, I. 1955, *Ap. J.*, **122**, 222. Heard, J. F. 1956, *Pub David Dunlap Obs.*, Vol. 2, No. 4.
- Jenkins, L. F. 1952, General Catalogue of Trigonometric Stellar Parallaxes (New Haven: Yale University Observatory). Observatory). Johnson, H. L, and Morgan, W. W. 1953, Ap. J., 117, 313. Keenan, P. C 1958a, Trans. I A.U, 10, 447. ———. 1958b, Hdb d Phys., ed. S. Flügge (Berlin: Springer-Verlag), 50, 93 Keenan, P. C, and Keller, G 1953, Ap. J., 117, 241. Kopff, A 1939, A.N., 269, 160. Morgan, W. W. 1937, Ap. J., 85, 380. Morgan, W. W, and Roman, N. G 1950, Ap J., 112, 362 Oke, J. B. 1957, Ap. J., 126, 509. Ramberg, J M 1941, Stockholm Obs. Ann., Vol. 13, No. 9.