# AXIAL ROTATION AND LINE BROADENING IN STARS OF SPECTRAL TYPES F0-K5* 

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#### Abstract

The widths of weak lines in 656 stars of spectral types F0-K5 on the revised Yerkes Atlas system of Morgan and Keenan have been obtained from plates having a dispersion of $11 \mathrm{~A} / \mathrm{mm}$. These line widths have been expressed in terms of $v \sin i$, the projected equatorial velocity required of a rotating, spherical, limb-darkened star in order to reproduce the observed broadening. It seems reasonable that axial rotation is the principal macroscopic broadening agent in those stars less luminous than supergiants, but this is not necessarily the case for the high-luminosity stars. The main conclusions of the paper are as follows: (1) The mean rotational velocity diminishes through class F , but $v \sin i$ values of $20 \mathrm{~km} / \mathrm{sec}$ or greater can be found in types as late as F8 (in luminosity classes II, IV-V, and V) or G0 (in classes III and IV). With the exception of two binaries, no stars of type later than G5 have been found with rotationally broadened lines, and the widening in a few single stars of types G2-G5 is marginal. (2) For a given spectral type between F0 and G0, the stars of luminosity classes III and IV have much higher mean rotational velocities than do those of class V . (3) There is no significant difference in the rotational velocities of the weak-and strong-line groups of F- and G-type stars. (4) The luminosity class I $a$ supergiants have considerably wider lines than do those of class Ib .


## I. INTRODUCTION

Most of our knowledge of the statistics of the rotational velocities of stars of spectral types F and later depends upon the work done by O. Struve and his colleagues at the Yerkes Observatory about 20 years ago and upon a recent contribution by Su-Shu Huang (1953). References to earlier work in the field will be found in the latter paper or in a review article by Struve (1945). Very briefly, the more extensive published studies of projected rotational velocities for stars of type F0 and later are the following: (1) Struve and C. T. Elvey (1931) estimated rotational velocities for 31 F0-K0 stars from the line widths on Yerkes spectrograms of dispersion $10 \mathrm{~A} / \mathrm{mm}$ at $\lambda 4500$; (2) Miss C. Westgate (1934) measured the width of $\operatorname{Sr}$ II $\lambda 4215$ with a micrometer microscope on Yerkes plates of dispersion $30 \mathrm{~A} / \mathrm{mm}$ at $\lambda 4500$ for 112 F-type stars and a limited number of later type; (3) Su-Shu Huang (1953) measured micrometrically the width of $M g$ II $\lambda 4481$ in 313 F-type and 10 G-type stars on plates of dispersions 10, 13, and $26 \mathrm{~A} / \mathrm{mm}$ at $\lambda 4481$ selected from the Lick collection of spectrograms.

Although the present investigation is, for the F-type stars, based on much of the same plate material as was used by Huang, it differs from his study in several ways. First, the present line widths (expressed here as rotational velocities) were determined, not from micrometer measures of line width but from careful visual comparison with the spectra of standard stars. The projected rotational velocities of the standard stars were determined from their line profiles. Second, only those stars were examined for which assignments of spectral type and luminosity class were available on the revised Atlas system (MK) of W. W. Morgan and P. C. Keenan (Johnson and Morgan 1953). Huang's types were taken from Pub. Lick Obs., Vol. 18, 1932, and are either HD assignments or types given by the radial-velocity observers; no distinction was made with respect to luminosity. Third, in our investigation, only plates taken with the "New" Mills spectrograph, of dispersion $11 \mathrm{~A} / \mathrm{mm}$ at $\lambda 4500$, were used; furthermore, a considerable number of new spectrograms were taken with this instrument of stars for which additional material seemed desirable. Fourth, the spectral interval covered was F0-K5. All known double-

[^0]line spectroscopic binaries in which the lines of the two components were not clearly separated and most unresolved visual binaries with $\Delta m \backsim 0$ were rejected. A number of unresolved visual binaries with small $\Delta m$, for which it is unlikely that line doubling contributes to the line width, were retained and are indicated in the notes to Table 2.

A preliminary report on this investigation was given by Herbig and Spalding (1953) at the Santa Barbara, California, meeting of the Astronomical Society of the Pacific in June, 1953. Not long after that paper was read, we learned of a parallel study of axial rotation in stars of type A7-G0 in progress by A. Slettebak, of the Perkins Observatory (1953, 1954). We wish to acknowledge the kindness of Dr. Slettebak in sending us in advance of publication a copy of his paper on "Axial Rotation in the F-Type Stars," which he prepared for the meeting of the American Astronomical Society in Boulder, Colorado, in August, 1953. The results of these two independent investigations are in substantial agreement.

## II. THE BASIC DATA: ROTATIONAL VELOCITIES AND SPECTRAL TYPES

The quantity actually observed in an investigation of this kind is the width of spectral lines. We have proceeded on the assumption that in the case of lines of $F e$ I, any broadening in excess of that observed in narrow-lined F- and G-type stars is due entirely to axial rotation in those stars less luminous than supergiants. Therefore, the results of the line-width estimates for individual stars (contained in Tables 1 and 2) are expressed as projected equatorial velocities of rotation, in kilometers per second. This assumption seems to be a reasonable one in the light of present knowledge, but we cannot furnish assurance that it is entirely correct.

In order to set up a system of comparison stars of known apparent rotational velocity, it was first assumed that narrow, unblended $F e$ I lines, as observed on Mills $11 \mathrm{~A} / \mathrm{mm}$ plates of the solar spectrum, contain in their profiles the effect of intrinsic line width in stars of that type, as well as the contribution of the finite resolution of the spectrograph. The lines chosen for profile determination were $\lambda 4472.7$ and $\lambda 4476.0$, both due mainly to $F e$ I. They were selected on the basis of their relative narrowness and their location in a spectral region where the position of the continuous spectrum is well defined on microphotometer tracings. In addition, $F e$ I $\lambda 4404.8$ was used for comparison with those stars in which large broadening rendered $\lambda 4472$ and $\lambda 4476$ excessively shallow and difficult to use.

The standards consisted of five stars of spectral types F5-G0, plus the sun, which were chosen after a preliminary survey of the plate material showed that they defined a wide range of line width without gaps that could not be spanned by visual interpolation. New spectrograms of photometric quality were obtained for the sun and for these standard stars with the Mills spectrograph. The slit-width projected on the plate was $19 \mu$, which corresponds to $14 \mathrm{~km} / \mathrm{sec}$ at $\lambda 4500$. The spectra were uniformly broadened by drifting to a width of $0.3-0.5 \mathrm{~mm}$. Kodak $\mathrm{II} a-\mathrm{O}$ plates were used throughout. The plates were traced in the modified Moll microphotometer of the Lick Observatory with a magnification of 424 times, and profiles were derived from a tube-sensitometer calibration in the usual manner. The differences in spectral type between some of the standard stars and the sun made it necessary to normalize the profiles in the stars of earliest type, in order that the increase in strength of the $F e$ I lines with spectral type should not confuse the determination of $v \sin i$. The profiles of the lines in the standard stars were then compared with sets of solar profiles as blurred by varying amounts of axial rotation. The method was the graphical one described by A. Unsöld (1938). A limb-darkening coefficient of $u=0.6$ was used. The value of $v \sin i$ (the projected equatorial velocity of axial rotation) was adopted that yielded the best fit between the computed and the observed line profiles. The adopted values of $v \sin i$, rounded off to the nearest $5 \mathrm{~km} / \mathrm{sec}$ for the stars with very broad lines, and other relevant data are given in Table 1.

Several spectrograms of different densities and slit widths were available for each standard star. With these at hand for ready reference, a survey of the entire collection of Mills spectrograms of stars with MK types between F0 and K5 was made with a hand magnifier. All stars having perceptibly wider lines than the sun were reserved for later examination. The second examination consisted of a careful comparison on a Hartmann spectrocomparator of the best spectrograms of each wide-lined star with those plates of the standard stars having the most comparable density and slit-width. It was necessary to exercise considerable judgment in the estimates of line width, on account of the large range in plate quality. Many of the older Mills spectrograms of fainter stars were taken with a slit-width of $38 \mu$ (or $28 \mathrm{~km} / \mathrm{sec}$ at $\lambda 4500$ ), which made them of limited value for the detection of small rotational velocities. The slit-width, therefore, had always to be taken into account in the assignment of $v \sin i$. The results for stars of luminosity classes II through V are contained in Table 2a. Because of the different character of the line broadening in supergiants, the data for the high-luminosity stars are given separately in Table $2 b$.

TABLE 1
Rotational Velocities of Standard Stars

| Star | ${ }_{1} 1900$ | $\delta_{1900}$ | $\begin{gathered} \text { MK Spectral } \\ \text { Type } \end{gathered}$ | $\begin{gathered} \text { Adopted } \\ v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Lines Used in Determination of $v \sin i$ <br> ( $\lambda$ ) | No. of Spectrograms |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sun*. |  |  | G2 V | <15 $\dagger$ |  | 4 |
| $\pi^{3}$ Ori | $4^{\text {b }} 44^{\text {m }}$. 4 | $+6^{\circ} 47^{\prime}$ | F6 V | 21 | 4472,4476 | $3 \ddagger$ |
| 11 Aql. | 1854.5 | +1329 | F8 IV | 27 | 4472,4476 | 2 |
| $\rho$ And. | 015.8 | +3725 | F5 IV | 45 | 4472,4476 | 2 |
| 31 Com . | 1246.8 | +2805 | G0 III | 85 | 4404,4476 | 2 |
| 18 Com. | 1224.4 | +24 40 | F5 IV | 115 | 4404,4476 | 2 |

* The sunlit sky and the moon were actually observed.
$\dagger$ Assumed.
$\ddagger \lambda 4476$ was utilized on all three plates of $\pi^{3}$ Ori, but $\lambda 4472$ on only one.
We believe that our estimates of $v \sin i$ are likely to be most uncertain, percentagewise, for those narrow-lined stars in which allowance for poor plate quality had to be made. The entries in the $v \sin i$ column of Tables $2 a$ and $2 b$ for narrow-lined stars are based on the following conventions. First, a star for which a plate or plates of good quality (i.e., narrow slit and proper exposure) were available and which exhibited weak absorption lines that were fully as sharp as those in the sun was assigned a $v \sin i$ of $<15 \mathrm{~km} / \mathrm{sec}$. For the best spectrograms, this value is probably too high a limit. Second, a star for which only poor plates were available but still showed no clear evidence of intrinsic line broadening was given a $v \sin i$ of $<20: \mathrm{km} / \mathrm{sec}$. Third, those stars for which the plate quality was so low that a rotational velocity of 25 or even $30 \mathrm{~km} / \mathrm{sec}$ would have been concealed were rejected. The choice between the second and third categories was sometimes difficult to make, and, although we have attempted always to err on the conservative side, it is not impossible that some stars of rotational velocity 20 or $25 \mathrm{~km} / \mathrm{sec}$ are listed as $<20: \mathrm{km} / \mathrm{sec}$ in Tables $2 a$ and $2 b$.

At the other extreme, for stars having $v \sin i$ of about $100 \mathrm{~km} / \mathrm{sec}$ or more, a dispersion of $11 \mathrm{~A} / \mathrm{mm}$ is inconveniently and unnecessarily large, at least when visual estimates are used for the determination of rotational velocity. We do not know whether the quality of our estimates of large $v \sin i$ 's has suffered for this reason, but it is certain that the work on such stars would have been less difficult at a lower dispersion.

TABLE $2 a$
Catalogue of Line Widths of 624 Stars between Spectral Types F0 and K 5 and of Luminosity Classes II-V, Expressed as Rotational Velocities

| No.* | Star | $a_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | 33 Psc | $0^{\mathrm{h}} 00^{\mathrm{m}} 2$ | $-6^{\circ} 16^{\prime}$ | K1 III | 2 | < 15 | SB1 |
| 2 | $\beta$ Cas | 003.8 | +58 36 | F2 IV | 1 | 85 |  |
| 3 | 22 And | 005.1 | +4531 | F2 II | 1 | 40 |  |
| 4. | 6 Cet | 006.2 | -16 01 | F6 V w | 2 | < 15 |  |
| 5. | HR 37 | 007.1 | -18 30 | K5 III | 2 | < 20: | VV |
| 6. | $\iota$ Cet | 014.3 | -923 | K2 III | 2 | < 15 |  |
| 7. | $\rho$ And | 015.8 | +3725 | F5 IV s | 4 | 45 |  |
| 8. | HR 152 | 031.3 | +43 56 | K5 III | 2 | $<15$ |  |
| 9 | $\epsilon$ And | 033.3 | +28 46 | G8 III | 2 | $<15$ |  |
| 10. | $\delta$ And | 034.0 | +30 19 | K3 III | 1 | < 15 | VV |
| 11. | $a \mathrm{Cas}$ | 034.8 | +55 59 | K0 II-III | 2 | < 15 | LV |
| 12. | 32 And | 035.7 | +38 55 | G8 III | 2 | $<15$ |  |
| 13 | $\beta$ Cet | 038.6 | -18 32 | K0 III | 2 | < 15 |  |
| 14 | $\phi^{1}$ Cet | 039.2 | -11 09 | K0 III | 2 | < 15 |  |
| 15* | $\zeta$ And | 042.0 | +23 43 | K1 II | 2 | 30 | SB1 |
| 16. | $\eta$ Cas | 043.0 | +5717 | G0 V w | 1 | $<15$ |  |
| 17. | $\delta$ Psc | 043.5 | + 702 | K5 III | 2 | < 20; |  |
| 18*. | 64 Psc | 043.7 | +16 24 | F8 V s | 2 | $\left\{\begin{array}{l}<15 \\ <15\end{array}\right\}$ | SB2 |
| 19. | $\phi^{2}$ Cet | 045.1 | -11 11 | F8 V s | 4 | $<15$ | - |
| 20. | HR 244 | 047.1 | +60 34 | F8 IV-V s | 4 | < 15 |  |
| 21. | $v^{1} \mathrm{Cas}$ | 049.1 | +58 26 | K2 III | 2 | $<15$ : |  |
| 22. | $v^{2} \mathrm{Cas}$ | 050.7 | +5838 | G8 III-IV |  | < 15 |  |
| 23. | $\eta$ And | 051.9 | +2253 | G8 III-IV | 2 | $\left\{\begin{array}{ll}<15 \\ <15\end{array}\right\}$ | SB2 |
| 24. | $\epsilon \mathrm{Psc}$ | 057.8 | + 721 | K0 III | 2 | < 15 |  |
| 25. | $\mu \mathrm{Cas}$ | 101.6 | +5426 | G5 Vp | 1 | < 15 |  |
| 26. | $\eta$ Cet | 103.6 | $-1043$ | K2 III | 2 | $<15$ |  |
| 27. | $\chi$ Psc | 106.1 | +2030 | K0 III | 2 | < 20: |  |
| 28. | $\tau$ Psc | 106.2 | +29 34 | K0 III-IV | 2 | < 15 | VV |
| 29. | $\phi$ Psc | 108.3 | +2403 | K0 III | 2 | < 15 | VV |
| 30. | $\xi$ And | 116.4 | +4500 | K0 III-IV | 2 | < 15 | VV? |
| 31. | $\psi$ Cas | 118.9 | +6736 | K0 III | 2 | < 15 |  |
| 32. | $\theta$ Cet | 119.0 | -842 | K0 III | 2 | < 15 |  |
| 33. | 46 Cet | 120.7 | -1507 | K3 III | 2 | $<15$ |  |
| 34. | $\omega$ And | 1221.7 | +4453 | F5 IV w | 4 | 75 $<$ |  |
| 35. | 49 And | 124.1 | +4630 | K0 III | 2 | $<20$ : |  |
| 36. | $\mu \mathrm{Psc}$ | 124.9 | + 538 | K4 III | 2 | < 15 |  |
| 37. | $\eta$ Psc | 126.1 | +1450 | G8 III | 1 | < 20: |  |
| 38. | $\chi$ Cas | 127.4 | +5843 | K0 III | 2 | < 20: |  |
| 39 | 40 Cas | 130.5 | +7232 | G8 II-III | 2 | < 20: |  |
| $40^{*}$ | $v$ And | 130.9 | +4054 | F8 V w | 1 | < 15 |  |
| 41. | 50 Cet | 131.1 | -15 54 | K2 III | 2 | < 20: |  |
| 42. | 51 And | 131.8 | +48 07 | K3 III | 1 | < 15 |  |
| 43. | $\chi$ x And | 133.4 | +4352 | G8 III | 2 | < 15 | VV |
| 44. | HR 483 | 135.7 | +4207 | G2 V s | 1 | < 15 |  |
| 45. | $\nu \mathrm{Psc}$ | 136.2 | + 459 | K3 III | 2 | $<20$ : |  |

[^1]TABLE $2 a$-Continued

| No.* | Star | $\boldsymbol{\alpha}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 46. | 107 Psc | $1^{\text {b }} 37 \mathrm{~m} .1$ | $+19^{\circ} 47^{\prime}$ | K1 V | 1 | $<20$ : |  |
| 47. | HR 500 | 137.7 | -412 | K3 II-III | 2 | < 20: |  |
| 48. | $\tau$ Cet | 139.4 | $-1628$ | G8 Vp | 1 | < 15 |  |
| 49. | o Psc | 140.1 | +839 | K0 III | 2 | < 15 |  |
| 50. | $\zeta$ Cet | 146.5 | -10 50 | K2 III | 2 | < 20: | SB1 |
| 51 | a Tri | 147.4 | +29 06 | F6 IV w | 1 | 115 | SB1 |
| 52 | $\xi \mathrm{Psc}$ | 148.4 | + 242 | K0 III | 2 | < 15 | VV |
| 53 | ८ Ari | 151.9 | $+1720$ | K1 p | 2 | < 15: | SB1 |
| 54. | 49 Cas | 156.0 | +7538 | G8 III | 2 | $<15$ | VV? |
| 55. | $\gamma$ And A | 157.8 | +4151 | K2 III | 2 | < 15 |  |
| 56. | a Ari | 201.5 | +22 59 | K2 III | 1 | < 15 |  |
| 57. | 14 Ari | 203.7 | +25 28 | F2 III | 1 | $\geq 115$ |  |
| 58. | 60 And | 207.0 | +43 46 | K4 III | 2 | < 15 | SB1 |
| 59. | $\eta$ Ari | 207.2 | +2044 | F5 V s | 2 | < 20 |  |
| 60. | $\xi^{1}$ Cet | 207.7 | $+823$ | G8 II | 2 | < 15 | VV |
| 61. | $\delta$ Tri | 210.9 | +33 46 | G0 V w | 1 | < 15 | SB1 |
| 62. | 64 And | 217.8 | +49 33 | G8 III | 2 | < 15 |  |
| 63. | 65 And | 219.0 | +4950 | K4 III | 2 | < 15 |  |
| 64. | 14 Tri | 226.0 | +35 42 | K5 III | 2 | $<20$ : |  |
| 65. | HR 737 | 226.3 | $+150$ | K3 III | 2 | < 20: |  |
| 66. | $\sigma$ Cet | 227.4 | -15 41 | F5 IV-V s | 4 | 20 |  |
| 67. | HR 743 | 228.5 | +7223 | G8 III | 2 | < 20: |  |
| 68. | $\nu$ Cet | 230.6 | +509 | G8 III | 2 | < 15 |  |
| 69*. | $\theta$ Per | 237.4 | +48 48 | F7 V w | 1 | < 15 |  |
| 70. | $\mu \mathrm{Cet}$ | 239.5 | +942 | F0 IV | 1 | 45 | VV |
| 71. | $\tau^{1}$ Eri | 240.4 | -1900 +28 | F6 V s | 4 | 25 $<15$ |  |
| 72. | 39 Ari | 242.0 | +2850 | K1 III | 2 | < 15 |  |
| 73. | 16 Per | 244.3 | +3754 | F2 III | 1 | $>115$ |  |
| 74. | 17 Per | 245.4 | +34 39 | K5 III | 2 | $<15$ |  |
| 75*. | 20 Per | 247.4 | $+3756$ | F4 V | 2 | 85 | VB |
| 76. | $\eta$ Eri | 251.5 | -918 | K1 III-IV | 2 | < 15 |  |
| 77. | 24 Per | 252.9 | +34 47 | K2 III | 2 | < 15 |  |
| 78. | HR 918 | 258.0 | +5619 | K0 II-III | 2 | < 20: |  |
| 79. | $\iota$ Per | 301.8 | +49 14 | G0 V w | 1 | < 15 |  |
| 80. | $\kappa$ Per | 302.7 | +4429 | K0 III | 2 | < 15 | VV |
| 81. | $\omega$ Per | 304.8 | +39 14 | K1 III | 2 | $<20$ : |  |
| 82. | $\delta$ Ari | 305.9 | +1921 | K2 III | 2 | < 15 |  |
| 83. | 94 Cet | 307.7 | - 134 | F8 V s | 2 | < 15 |  |
| 84. | HR 969 | 309.0 | +5034 | G5 II | 2 | < 15 |  |
| 85. | HR 991 | 312.5 | +33 51 | K2 II | 2 | $<15$ |  |
| 86. | $\kappa$ Cet | 314.1 | + 300 | G5 V s | 1 | $<15$ |  |
| 87. | HR 999 | 314.3 | +2841 | K3 II-III | 2 | < 15 |  |
| 88. | 63 Ari | 317.0 | +20 23 | K3 III | 2 | < 20: |  |
| 89. | - Tau | 319.4 | + 841 | G8 III | 1 | $<15$ | SB1 |
| 90. | $\sigma$ Per | 323.6 | +4739 | K3 III | 2 | < 15 |  |
| 91. | 5 Tau |  | +1236 | K0 II-III |  | < 20: | SB1 |
| 92. | 36 Per | 325.5 3 | +4543 | F4 III | 1 | 40 $<$ |  |
| 93. | $\epsilon$ Eri | $\begin{array}{ll}3 & 28.2 \\ 3 & 31.8\end{array}$ | -948 | K 2 V | 1 | $<15$ |  |
| 94. | 10 Tau | 331.8 | +005 | F8 V w | 4 | < 15 |  |
| 95. | $\nu$ Per | 338.4 | +42 16 | F5 II | 1 | 45 | VV? |

TABLE $2 a$-Continued

| No.* | Star | $\boldsymbol{a}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 96. | $\delta$ Eri | $3^{\text {¢ }} 38.4$ | $-10^{\circ} 06^{\prime}$ | K0 IV | 1 | $<15$ |  |
| 97. | 43 Per | 349.2 | +50 24 | F5 V s | 4 | $\left\{\begin{array}{l}<15 \\ < \\ < \\ 15\end{array}\right\}$ | SB2 |
| 98. | 32 Eri A | 349.3 | - 315 | G8 III | 2 | < 15 |  |
| 99. | HR 1242 | 356.1 | +5853 | F0 II | 1 | < 20: |  |
| 100. | HR 1249 | 357.5 | $-033$ | F6 V s | 2 | 25 |  |
| 101. | 37 Tau | 358.8 | +2149 | K0 III | 2 | $<15$ |  |
| 102. | HR 1257 | 358.9 | + 233 | F6 IV w | 2 | 25 |  |
| 103* | 46 Tau | 408.2 | + 728 | F3 V | 1 | 65 | VB |
| 104. | 39 Eri | 409.6 | $-1030$ | K3 III | 2 | < 20: |  |
| 105. | HR 1327 | 411.3 | +64 54 | G5 III | 1 | < 20: |  |
| 106. | 54 Per | 413.9 | +34 20 | G8 III | 2 | $<20$ : |  |
| 107. | $\gamma$ Tau | 414.1 | +1523 | K0 III | 1 | < 15 |  |
| 108. | $\phi$ Tau | 414.2 | +2707 | K1 III | 2 | < 20: |  |
| 109. | $\delta$ Tau | 417.2 | +1718 | K0 III | 1 | < 15 |  |
| 110. | HR 1390 | 419.7 | +3113 | K1 III | 2 | < 20: |  |
| 111. | ${ }^{\pi}$ Tau | 421.0 | +1429 | G8 III | 2 | < 15 |  |
| 112. | 75 Tau | 422.7 | +1608 | K2 III | 2 | $<20$ : |  |
| 113. | $\epsilon \mathrm{Tau}$ | 422.8 | +1858 | K0 III | 1 | < 15 |  |
| 114. | $\theta^{1}$ Tau | 422.8 | +1544 | K0 III | 1 | < 20: | VV |
| 115. | 45 Eri | 426.8 | -016 | K3 II-III | 2 | < 15 |  |
| 116. | HR 1452 | 429.4 | - 911 | K4 II-III | 2 | < 20: |  |
| 117. | a Tau | 430.2 | +1619 | K5 III | 1 | < 15 |  |
| 118. | 3 Cam | 432.0 | +5253 | K0 III | 2 | < 15 | SB1 |
| 119. | 53 Eri | 433.6 | -1430 | K2 III | 2 | < 15 | SB1 |
| 120. | HR 1523 | 441.6 | +81 02 | K3 III | 2 | < 15 | VV? ${ }^{\text {d }}$ |
| 121. | HR 1533 | 443.2 | +37 19 | K4 II | 2 | < 20: |  |
| 122. | $\pi^{3}$ Ori | 444.4 | + 647 | F6 V s | 1 | 20 |  |
| 123. | 2 Aur | 445.9 | +3632 | K3 III | 2 | < 15 |  |
| 124. | ८ Aur | 450.5 | +3300 | K3 II | 1 | < 15 |  |
| 125. | $0^{2}$ Ori | 450.8 | +1321 | K2 III | 2 | < 15 |  |
| 126. | $\pi^{6}$ Ori | 453.4 | + 134 | K2 II | 5 | < 15 |  |
| 127. | 68 Eri | 503.8 | -435 | F5 V w | 2 | < 15 |  |
| 128. | HR 1684 | 506.0 | +1555 | K5 III | 2 | < 20: |  |
| 129. | HR 1686 | 506.1 | +7907 | F6 V w | 2 | < 20: |  |
| 130. | $\rho$ Ori | 508.1 | + 245 | K3 III | 2 | < 15 | SB1 |
| 131*. | a Aur | 509.3 | +45 54 |  |  |  | SB2 |
| 132. | 16 Aur | 511.6 | +3316 | K3 III | 2 |  | SB1 |
| 133*. | $\lambda$ Aur | 512.1 | +4001 | G0 V w | 1 | < 15: |  |
| 134. | 109 Tau | 513.3 | +2200 | G8 III | 2 | < 15 |  |
| 135. | 21 Ori | 514.0 | +230 | F5 II | 2 | 85 |  |
| 136. | $\sigma$ Aur | 517.8 |  | K4 III |  | < 20, |  |
| 137. | 111 Tau | 518.6 | +1717 | F8 V s | 2 | 25 |  |
| 138. | 29 Ori | 519.1 | -754 | G8 III | 2 | < 15 |  |
| 139. | 27 Ori | 519.4 | - 059 | K0 III | 2 | < 20: |  |
| 140. | $\phi$ Aur | 521.0 | +3424 | K3p | 2 | < 15 |  |
| 141. | ${ }_{31}^{\beta}$ Lep | 524.0 524.6 | -20 50 $-\quad 110$ | G2 II | 6 | < 20: | IV |
| 143. | 51 Ori | 537.3 | + 126 | K1 III | 2 | < 15 |  |
| 144. | $\tau$ Aur | 542.2 | +39 09 | G8 III | 2 | < 15 |  |
| 145. | 132 Tau | 542.9 | +24 32 | G8 III | 2 | < 20 |  |

TABLE $2 a$-Continued

| No.* | Star | $a_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} 0 \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 146 | ${ }_{\nu}$ Aur | $5^{\text {b }} 44^{\text {m }} 6$ | $+39^{\circ} 07^{\prime}$ | K0 III | 2 | < 15 |  |
| 147. | 56 Ori | 547.2 | +150 | K2 II | 1 | < 20: |  |
| 148 | $\chi^{1}$ Ori | 548.5 | +20 16 | G0 V s | 2 | < 20: |  |
| 149 | $\delta$ Aur | 551.3 | +5417 | K0 III | 1 | < 15 |  |
| 150. | 1 Mon | 554.3 | -924 | F2 II | 7 | 25: |  |
| 151. | HR 2113 | 555.0 | $-305$ | K2 III | 2 | < 15 |  |
| 152 | 37 Cam | 601.2 | +5857 | G8 III | 2 | $<20$ : |  |
| 153. | 36 Cam | 602.8 | +6544 | K2 II-III | 2 | < 15 |  |
| 154 | 71 Ori | 609.0 | +19 12 | F6 V s | 2 | < 15 |  |
| 155. | $\kappa$ Aur | 609.0 | +29 32 | G8 III | 2 | < 20: |  |
| 156. | 74 Ori | 610.8 | +12 18 | F5 IV-V w | 2 | 20 |  |
| 157. | 45 Aur | 613.6 | +5330 | F5 III s | 2 | 20 | SB1 |
| 158. | 5 Lyn | 618.1 | +5828 | K4 III | 2 | < 20: |  |
| 159. | HR 2305 | 619.5 | -1128 | K3 III | 2 | < 20: |  |
| 160. | HR 2379 | 626.7 | -12 19 | K3 III | 2 | < 20: |  |
| 161. | $\psi^{2}$ Aur | 632.2 | +4235 | K3 III | 2 | < 15 |  |
| 162. | $\nu^{2} \mathrm{CMa}$ | 632.3 | -19 10 | K1 IV | 2 | < 15 |  |
| 163. | $\nu^{3} \mathrm{CMa}$ | 633.5 | -18 09 | K1 III | 2 | < 15 |  |
| 164. | HR 2450 | 634.7 | -14 03 | K2 II | 2 | < 15 |  |
| 165. | $\psi^{4}$ Aur | 635.8 | +44 37 | K5 III | 2 | < 15 |  |
| 166. | 13 Lyn | 638.3 | +5716 | K0 III | 2 | < 20: |  |
| 167. | 30 Gem | 638.4 | +1320 | K1 III | 2 | < 20: |  |
| 168. | $\psi^{5}$ Aur | 639.5 | +43 41 | G0 V s | 2 | < 15 |  |
| 169. | $\xi$ Gem | 639.7 | +1300 | F5 IV s | 4 | 95 |  |
| 170. | $\psi^{6}$ Aur | 640.0 | +4854 | K1 III | 2 | < 20: |  |
| 171. | 17 Mon | 641.9 | + 809 | K4 III | 2 |  |  |
| 172. | 18 Mon | 642.6 | + 231 | K0 III | 2 | < 15 | VV |
| 173. | $\psi^{7}$ Aur | 643.7 | +4154 | K3 III | 2 | < 20: |  |
| 174. | HR 2527 | 645.5 | +7706 | K4 III | 2 | < 15 | VV |
| 175. | $\theta \mathrm{CMa}$ | 649.6 | -1155 | K4 III | 2 | < 20: |  |
| 176. | $\omega$ Gem | 656.3 | +24 21 | G5 II | 1 | $<20$ : |  |
| 177. | HR 2649 | 658.1 | +1106 | K3 III | 2 | < 20: |  |
| 178. | $\tau$ Gem | 704.8 | +30 25 | K2 III | 2 | < 15 |  |
| 179. | 63 Aur | 704.8 | +3929 | K4 II-III | 2 | < 15 |  |
| 180. | 20 Mon | 705.3 | $-405$ | K0 III | 2 | $<20$ : |  |
| 181. | 18 Lyn | 707.2 | +59 49 | K2 III | 2 | < 20: |  |
| 182. | $\delta$ Gem | 714.2 | +22 10 | F2 IV-V | 6 | 115 | VV? |
| 183. | 65 Aur | 715.4 | +3657 | K0 III | 2 | $<15$ |  |
| 184. | 66 Aur | 717.2 | +40 52 | K0 III | 2 | < 20: |  |
| 185. | 57 Gem | 717.4 | +25 15 | G8 III | 2 | $<20$ : |  |
| 186. | $\iota$ Gem | 719.5 | +28 00 | K0 III | 2 | $<15$ |  |
| 187. | $\epsilon \mathrm{CMi}$ | 720.2 | + 928 | G8 III | 2 | < 15 |  |
| 188 | 22 Lyn | 722.3 | +49 53 | F6 V s | 2 | < 20: |  |
| 189. | $\gamma \mathrm{CMi}$ | 722.7 | +908 | K3 III | 2 | < 15 | SB1 |
| 190. | $\rho$ Gem | 722.7 | +3159 | F0 V | 1 | 85 |  |
| 191*. | 65 Gem | 723.6 | +28 07 | K2 III | 2 | $\left\{\begin{array}{ll}\ll & 15 \\ < & 15\end{array}\right\}$ | SB2 |
| 192. | 6 CMi | 724.2 | +12 13 | K2 III | 2 | $<20$ : |  |
| 193. | HR 2896 | 728.8 | +3111 | K0 III | 2 | < 20: |  |
| 194. | $v$ Gem | 729.8 | +2707 | K5 III | 2 | < 20: |  |
| 195. | 25 Mon | 732.3 | - 353 | F5 III w | 2 | 30 |  |

TABLE 2a-Continued

| No.* | Star | $\boldsymbol{\alpha}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} 0 \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 196. | a CMi | 7 h 34 m . | $+5^{\circ} 29^{\prime}$ | F5 IV-V s | 1 | $<15$ | VB |
| 197. | a Mon | 736.5 | - 919 | K0 III | 2 | $<15$ |  |
| 198* | $\sigma$ Gem | 737.1 | +2908 | K1 III | 2 | 25 | SB1 |
| 199. | 76 Gem | 738.0 | +2601 | K5 III | 2 | < 20: |  |
| 200. | $\kappa$ Gem | 738.4 | +24 38 | G8 III | 1 | < 15 |  |
| 201. | $\beta$ Gem | 739.2 | +28 16 | K0 III | 1 | < 15 |  |
| 202 | 81 Gem | 740.3 | +1845 | K 5 III | 2 | < 15 | VV |
| 203* | 9 Pup | 747.1 | -13 38 | G1 V s | 4 | $<15$ | VB |
| 204. | 11 Pup | 752.6 | -22 37 | F8 II | 7 | 25 |  |
| 205. | 14 CMi | 753.2 | + 229 | K0 III | 2 | < 20, |  |
| 206. | 27 Mon | 754.7 | - 324 | K2 III | 2 | $<20$ : |  |
| 207. | 28 Mon | 756.1 | -107 | K4 III | 2 | < 20: |  |
| 208. | HR 3145 | 757.1 | $+237$ | K2 III | 2 | < 20: |  |
| 209. | $\chi$ Gem | 757.4 | +2804 | K2 III | 2 | < 20: | VV |
| 210. | $\mu \mathrm{Cnc}$ | 801.9 | $+2152$ | G2 IV s | 4 | < 20: |  |
| 211. | HR 3182 | 802.9 | +6846 | G8 II | 2 | < 20: |  |
| 212. | $\rho$ Pup | 803.3 | $-2401$ | F6 II | 7 | 15 | VV |
| 213 | 19 Pup | 806.6 | -12 38 | K0 III | 2 | $<15$ |  |
| 214 | HR 3212 | 806.7 | -728 | G8 III | 2 | < 20: |  |
| 215 | $\beta$ Cnc | 811.1 | $+930$ | K4 III | 1 | < 15 |  |
| 216. | $\chi \mathrm{Cnc}$ | 814.0 | +2732 | F6 V w | 4 | $<20$ : |  |
| 217. | 31 Lyn | 816.0 | +43 31 | K5 III | 2 | $<20$ : |  |
| 218 . | HR 3306 | 820.6 | + 753 | G8 II | 2 | < 20: |  |
| 219* | o UMa | 822.0 | +6103 | G2 II-III |  | 15 |  |
| 220 | $\pi^{2} \mathrm{UMa}$ | 831.5 | +64 41 | K2 III | 2 | < 15 |  |
| 221. | $\sigma$ Hya | 833.5 | + 342 | K2 III | 2 | $<15$ |  |
| 222. | 6 Hya | 835.3 | $-1207$ | K4 III | 2 | < 20: |  |
| 223. | 9 Hya | 837.1 | -15 35 | K1 III | 2 | $<20$ : |  |
| 224. | $\delta$ Cnc | 839.0 | +18 31 | K0 III | 2 | < 15 |  |
| 225. | $\iota$ Cnc | 840.6 | +2908 | G8 II | 2 | < 20: |  |
| 226*. | $\epsilon$ Hya AB | 841.5 | + 647 | G |  | $<15$ |  |
| 227. | 12 Hya | 841.7 | -1311 | G8 III | 2 | < 15 | SB1 |
| 228. | 35 Lyn | 845.2 | +44 06 | K0 III | 2 | < 15 |  |
| 229 | $\rho^{2} \mathrm{Cnc}$ | 849.7 | +28 19 | G8 II-III | 2 | $<20$ : |  |
| 230. | $\zeta$ Hya | 850.1 | + 620 | K0 III | 2 | $<15$ |  |
| 231*. | HR 3579 | 854.2 | +42 11 | F5 V w | 1 | 25 | VB |
| 232. | $\sigma^{1} \mathrm{UMa}$ | 859.6 | +67 17 | K5 III | 2 | $<20$ : |  |
| 233. | $\omega$ Hya | 900.7 | +530 +67 | K2 II-III | 2 | < 20: |  |
| 234* | $\sigma^{2} \mathrm{UMa}$ | 901.6 | +6732 | F7 IV-V s | 1 | $<15$ |  |
| 235. | $\tau$ Cnc | 902.0 | $+3003$ | G8 III | 2 | $<20$ : |  |
|  | $\tau \mathrm{UMa}$ | 902.7 | +6355 | A7 m | 2 | $<15$ | VV |
| 237. | $\xi \mathrm{Cnc}$ | 903.6 | +22 27 | K0 III | 2 | < 15 | SB1 |
| 238. | 17 UMa | 908.4 | +5710 | K5 III | 2 | < 20: |  |
| 239. | 23 Hya | 911.7 | - 556 | K2 III | 2 | < 20: | SB1 |
| 240. | 26 Hya | 915.0 | -1133 | G8 III | 2 | < 20: |  |
| 241. | 27 Hya | 915.6 | -908 | G8 III-IV | 2 | < 20: |  |
| 242. | $\kappa$ Leo | 918.8 | +26 37 | K2 III | 2 | < 20: |  |
| 243. | $a \mathrm{Hya}$ | 922.7 | -814 | K3 III | 2 | < 15 |  |
| 244. | HR 3750 | 922.8 | - 538 | G2 V s | 4 | < 15 | VV? |
| 245. | HR 3751 | 922.8 | +8146 | K3 III | 2 | $<20$ : |  |

TABLE $2 a$-Continued

| No.* | Star | $\alpha_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 246. | $\tau^{1} \mathrm{Hya}$ | $9^{\mathrm{h}} 24^{\mathrm{m}} 1$ | $-2^{\circ} 20^{\prime}$ | F6 V w | 4 | 45 | VV? |
| 247. | 24 UMa | 925.6 | +70 16 | G5 IV s | 2 | < 20: |  |
| 248. | $\lambda$ Leo | 926.0 | +2325 | K5 III | 2 | < 15 | VV? |
| 249. | $\theta \mathrm{UMa}$ | 926.2 | +5208 | F6 IV w | 1 | < 15 |  |
| 250. | 6 Leo | 926.6 | +10 09 | K3 III | 2 | < 15 |  |
| 251. | $\xi$ Leo | 926.6 | +1145 | K0 III | 2 | $<20$ : |  |
| 252. | 10 LMi | 928.1 | +36 51 | G8 III | 2 | < 20: |  |
| 253. | HR 3809 | 928.8 | +40 04 | K0 III | 2 | < 20: |  |
| 254. | 11 LMi | 929.7 | +3616 | G8 IV-V | 1 | < 15 |  |
| 255. | 10 Leo | 931.9 | + 717 | K1 III | 2 | $<15$ | VV |
| 256. | HR 3834 | 933.2 | + 506 | K3 III | 2 | $<20$ : |  |
| 257. | 27 UMa | 933.8 | +7242 | K0 III | 2 | < 20: |  |
| 258. | $\iota$ Hya | 934.8 | -041 | K3 III | 2 | < 15 |  |
| 259. | 43 Lyn | 935.8 | +40 13 | G8 III | 2 | < 20: |  |
| 260. | $\epsilon$ Leo | 940.2 | +2414 | G0 II | 1 | < 15 |  |
| 261 | HR 3881 | 942.1 | +4629 | G2 V s | 4 | < 15 |  |
| 262. | $v$ UMa | 943.9 | +5931 | F2 IV | 1 | 115 |  |
| 263. | $v^{1} \mathrm{Hya}$ | 946.7 | -1423 | G8 III | 2 | < 20: |  |
| 264. | $\mu$ Leo | 947.1 | +2629 | K2 III | 2 | < 15 |  |
| 265. | 19 LMi | 951.6 | +4132 | F5 V s | 4 | < 20: | SB1 |
| 266. | 31 Leo | 1002.6 | +1029 | K4 III | 2 | < 20: |  |
| 267. | HR 3991 | 1005.2 | -1219 | F5 V s | 2 | $\geq 115$ |  |
| 268. | $\lambda$ Hya | 1005.7 | -11 52 | K0 III | 2 | < 20: | SB1 |
| 269. | $\zeta$ Leo | 1011.1 | +23 55 | F0 III | 1 | 85 | VV |
| 270* | 40 Leo | 1014.3 | +19 59 | F6 IV w | 1 | 20 |  |
| 271. | $\gamma$ Leo A | 1014.5 | $+2021$ | K0 III | 2 | < 15 |  |
| 272* | HR 4084 | 1018.9 | +8304 | F5 IV w | 4 | 115 |  |
| 273. | $\mu$ Hya | 1021.2 | -1620 | K4 III | 2 | < 20: |  |
| 274. | 31 LMi | 1022.1 | +3713 | G8 III-IV | 2 | < 20: |  |
| 275. | 36 UMa A | 1024.2 | $+5630$ | F8 V w | 1 | < 15 |  |
| 276. | HR 4126 | 1026.6 | +7614 | K0 III | 2 | < 20: |  |
| 277. | 48 Leo | 1029.6 | + 728 + | G8 II-III | 2 | < 20: |  |
| 278. | 37 LMi | 1033.1 | +32 30 | G2 II | 2 | < 20: |  |
| 279. | $\phi$ Hya | 1033.7 | -16 21 | K0 III | 2 | < 15 | SB1 |
| 280. | 38 UMa | 1035.1 | +6614 | K2 III | 2 | < 20: |  |
| 281. | HR 4181 | 1035.9 | +69 36 | K3 III | 2 | < 20: |  |
| 282 | $\nu$ Hya | 1044.7 | -1540 | K2 III | 2 | < 15 |  |
| 283 | 44 UMa | 1047.5 | +5507 | K3 III | 2 | < 20: |  |
| 284 | 46 LMi | 1047.7 | +34 45 | K0 III-IV | 1 | < 20: |  |
| 285. | HR 4251 | 1048.6 | -19 36 | F6 V s | 4 | 20 |  |
| 286. | 46 UMa | 1050.2 | +34 02 | K1 III | 2 | < 20: |  |
| 287. | 47 UMa | 1053.9 | +4058 | G0 V s | 4 | < 20: |  |
| 288. | $a \mathrm{Crt}$ | 1054.9 | -1746 | K0 11 I | 2 | < 20: |  |
| 289. | 58 Leo | 1055.4 | +409 | K1 III | 2 | < 20: |  |
| 290. | 61 Leo | 1056.7 | $-157$ | K5 III | 2 | < 20: | VV |
| 291. | $a \mathrm{UMa}$ | 1057.6 | +62 17 | K0 III | 1 | < 15 | VB |
| 292. | \% UMa | 1104.0 | +4502 | K1 III | 1 | < 20: |  |
| 293. | 73 Leo | 1110.6 | $+1351$ | K3 III | 2 | < 20: | VV |
| 294. | $\xi \mathrm{UMa}$ | 1112.8 | +3206 | G0 V w | 4 | $\left\{\begin{array}{l}<15 \\ <120\end{array}\right.$ | $\left.\begin{array}{l} \text { A(btr.) } \\ \underset{B(f \text { ftr. })}{ } \\ \text { SB1 } \end{array}\right\} \text { VB }$ |
| 295. | $\nu \mathrm{UMa}$ | 1113.1 | +33 38 | K3 III | 1 | < 20: |  |

TABLE $2 a$-Continued

| No.* | Star | $\boldsymbol{a}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 296 | $\delta \mathrm{Crt}$ | $11^{\text {h }} 14 \mathrm{~m} 3$ | $-14^{\circ} 14^{\prime}$ | G8 III-IV | 2 | $<20$ : | VV |
| 297. | 56 UMa | 1117.4 | +44 02 | G8 II | 1 | < 20: |  |
| 298. | $\lambda \mathrm{Crt}$ | 1118.4 | -1814 | F5 IV s | 2 | 25 | VV |
| 299. | $\epsilon \mathrm{Crt}$ | 1119.6 | -10 19 | K5 III | 2 | < 20: |  |
| 300. | $\tau$ Leo | 1122.8 | + 324 | G8 II-III | 2 | < 20: |  |
| 301. | 87 Leo | 1125.2 | $-2.27$ | K4 III | 2 | < 20: |  |
| 302. | HR 4439 | 1126.7 | +6138 | F6 V w | 4 | < 20: |  |
| 303. | 2 Dra | 1130.2 | +6953 | K0 III | 2 | < 20: |  |
| 304. | $v$ Leo | 1131.8 | -016 | G9 III | 2 | < 20: |  |
| 305. | 92 Leo | 1135.6 | $+2154$ | K0 III | 2 | < 15 |  |
| 306. | 61 UMa | 1135.8 | +34 46 | G8 V | 1 | < 15 |  |
| 307. | 3 Dra | 1136.9 | +6718 | K3 III | 2 | < 15 |  |
| 308. | $\zeta \mathrm{Crt}$ | 1139.7 | -1748 | G8 III | 2 | < 20: |  |
| 309. | $\chi$ UMa | 1140.8 | +4820 | K0 III | 2 | < 20: |  |
| 310. | HR 4521 | 1141.6 | +5611 | K3 III | 2 | < 20: |  |
| 311. | $\beta$ Vir | 1145.5 | + 220 | F8 V s | 1 | < 15 |  |
| 312. | $o \mathrm{Vir}$ | 1200.1 | + <br> + | G8 III | 2 | < 20: |  |
| 313. | 7 Com | 1211.3 | +24 30 | K0 III | 2 | < 15 |  |
| 314. | HR 4668 | 1211.5 | +33 37 | K1 III | 2 | < 15 | SB1 |
| 315. | 16 Vir | 1215.3 | + 352 | K0 III | 2 | $<20$ : |  |
| 316. | 11 Com | 1215.7 | +1821 | G8 III | 2 | < 20: |  |
| 317. | HR 4699 | 1215.8 | $-1301$ | K1 III | 2 | < 20: |  |
| 318. | 5 CVn | 1219.2 | +5207 | G7 III | 2 | < 15 |  |
| 319. | 6 CVn | 1220.9 | +3934 | G8 III-IV | 2 | < 20: |  |
| 320. | 15 Com | 1222.0 | +28 49 | K1 III-IV | 2 | < 15 |  |
| 321. | 18 Com | 1224.4 | +24 40 | F5 IV s | 4 | 115 |  |
| 322. | HR 4783 | 1228.7 | +33 48 | K0 III | 2 | < 20: |  |
| 323. | $\beta \mathrm{CVn}$ | 1229.0 | +4154 | G0 V w | 1 | < 15 |  |
| 324. | $\beta \mathrm{Crv}$ | 1229.1 | $-2251$ | G5 II | 6 | $<15$ |  |
| 325. | $\chi$ Vir | 1234.1 | $-727$ | K2 III | 2 | $<15$ |  |
| 326*. | $\gamma$ Vir | 1236.6 | - 054 | F0 V | 1 | $\left\{\begin{array}{l}25 \\ 40\end{array}\right.$ | $\mathrm{np}_{\mathrm{sf}}{ }^{\text {d }} \mathrm{VB}$ |
| 327. | HD 110628 | 1238.4 | +26 40 | F2n IV | 7 | 110: |  |
| 328. | 27 Com | 1241.6 | +1707 | K3 III | 2 | < 15 |  |
| 329. | 31 Com | 1246.8 | +2805 | G0 III s | 1 | 85 |  |
| 330. | 35 Com | 1248.4 | +2147 | G8 III | 2 | $<15$ |  |
| 331. | $a^{1} \mathrm{CVn}$ | 1251.3 | +3851 | F0 V | 1 | 20: |  |
| 332. | 37 Com | 1255.5 | +3120 | K1p | 2 | < 20: |  |
| 333. | 9 Dra | 1256.1 | +6708 | G8 III | 2 | < 15 |  |
| 334. | 78 UMa | 1256.4 | +5654 | F2 V | 1 | 105: |  |
| 335. | $\epsilon$ Vir | 1257.2 | +1130 | G9 III | 2 | < 15 |  |
| 336. | 41 Com | 1302.4 | +28 10 | K5 III | 2 | $<15$ |  |
| 337. | $49 . \mathrm{Vir}$ | 1302.6 | -10 12 | K1 III | 2 | < 20: |  |
| 338. | 53 Vir | 1306.7 | -15 40 | F6 IV s | 4 | < 15 |  |
| 339 | $\beta$ Com | 1307.2 | +28 23 | G0 V s | 1 | < 20: |  |
| 340. | HR 4997 | 1309.2 | +40 41 | K0 III | 2 | < 20: |  |
| 341. | 59 Vir | 1311.8 | +957 | G0 V s | 4 | < 15 |  |
| 342. | HR 5013 | 1312.3 | +14 12 | K3 III | 2 | < 20: |  |
| $343 *$. | 61 Vir | 1313.2 | $-1745$ | G6 V w | 1 | $<15$ |  |
| 344. | ${ }_{\sim}^{\gamma} \mathrm{Hya}$ | 1313.5 | -22 39 | G5 III | 6 | $<15$ |  |
| 345. | 70 Vir | 1323.5 | +14 19 | G5 V w | 1 | < 15 |  |

TABLE $2 a$-Continued

| No.* | Star | $\boldsymbol{a}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 346: | 76 Vir | 1327.7 | -939 | K0 III | 2 | < 20: |  |
| 347* | $\tau$ Boo | 1342.5 | +1757 | F7 V w | 1 | < 15 |  |
| 348. | 89 Vir | 1344.4 | -1738 | K1 III | 2 | < 20: |  |
| 349. | $v$ Boo | 1344.6 | +1618 | K5 III | 2 | < 15 |  |
| 350. | 6 Boo | 1345.0 | +2146 | K4 III | 2 | $<20$ : |  |
| 351. | 90 Vir | 1349.6 | - 101 | K2 III | 2 | < 15 |  |
| 352. | $\eta$ Boo | 1349.9 | +1854 | G0 IV s | 1 | 20 | SB1 |
| 353. | 9 Boo | 1352.0 | +2759 | K3 III | 2 | $<20$ : |  |
| 354. | $\kappa \mathrm{Vir}$ | 1407.6 | -948 | K3 III | 2 | < 20: |  |
| 355. | 4 UMi | 1409.2 | +7801 | K3 III | 2 | < 15 | SB1 |
| 356. | 15 Boo | 1410.0 | +10 34 | K0 III | 2 | $<20$ : |  |
| 357. | $\iota$ Vir | 1410.8 | - 531 | F6 IV s | 4 | 20 |  |
| 358. | a Boo | 1411.1 | +19 42 | K2 IIIp | 1 | < 15 |  |
| 359. | HR 5361 | 1413.8 | +3558 | K1 III | 2 | < 15 | SB1 |
| 360. | $v$ Vir | 1414.4 | -148 | G8 III | 2 | $<20$ : |  |
| 361. | 18 Boo | 1414.4 | +1328 | F5 IV-V s | 4 | 45 |  |
| 362. | 20 Boo | 1415.0 | +1646 | K3 III | 2 | < 15 |  |
| 363* | $\theta$ Boo | 1421.8 | +5219 | F7 V w | 1 | 40 |  |
| 364. | $\phi$ Vir | 1423.0 | -147 | G2 III | 2 | $<20$ : |  |
| 365. | $\rho$ Boo | 1427.5 | +3049 | K3 III | 1 | $<15$ | VV? |
| 366. | 5 UMi | 1427.7 | +7608 | K4 III | 2 | $<15$ |  |
| 367 | $\sigma$ Boo | 1430.3 | +3011 | F2 V | 1 | $<15$ |  |
| 368 | 31 Boo | 1436.7 | + 835 | G8 III | 2 | < 15 |  |
| 369 | $\mu \mathrm{Vir}$ | 1437.8 | - 513 | F5 IV w | 4 | -85 | VV |
| 370 | - Boo | 1440.6 | +1723 | K0 III | 2 | $<15$ |  |
| 371. | $a^{1} \mathrm{Lib}$ | 1445.2 | -15 35 | F5 IV-V w | 4 | < 20: |  |
| 372. | 11 Lib | 1445.8 | -153 | G8 III-IV | 2 | $<15$ |  |
| 373. | HR 5541 | 1446.6 | +3741 | K0 III-IV | 2 | < 15 |  |
| 374. | $\beta$ UMi | 1451.0 | +74 34 | K4 III | 1 | < 15 |  |
| 375 | $\omega$ Boo | 1457.7 | +25 24 | K4 III | 2 | < 15 |  |
| 376. | 110 Vir | 1457.8 | + 229 | K0 III | 2 | $<15$ |  |
| 377. | $\beta$ Boo | 1458.2 | +4047 | G8 II-III | 2 | < 15 |  |
| 378. | $\psi$ Boo | 1500.2 | +2720 | K2 III | 2 | $<15$ |  |
| 379 | 45 Boo | 1502.9 | +2516 | F5 V w | 1 | 75 |  |
| 380 | HR 5635 | 1503.4 | +5456 | G8 III | 2 | $<20$ : |  |
| 381. | ${ }_{\delta}^{\delta} \mathrm{Boo}$ | 1511.5 | +3341 | G8 III | 1 | < 20: |  |
| 382. | HR 5691 | 1513.5 | +6744 | F8 V s | 2 | < 20: |  |
| 383. | 5 Ser | 1514.2 | + 209 | F8 IV-V w | 1 | < 15 |  |
| 384. | 6 Ser | 1516.0 | + 104 | K3 III | 2 | < 15 |  |
| 385. | 11 UMi | 1517.2 | +72 11 | K4 III | 2 | $<15$ |  |
| 386. | $\epsilon \cdot \operatorname{Lib}$ | 1518.8 | - 958 | F5 V s | 4 | $<20$ : | SB1 |
| 387. | ${ }^{\text {¢ D }}$ Dra | 1522.7 | +5919 +4110 | K2 III | 1 | < 15 |  |
| 388. | $\nu^{1} \mathrm{Boo}$ | 1527.3 | +4110 | K5 III | 2 | $<15$ |  |
| 389. | 37 Lib | 1528.7 | -943 | K1 III | 2 | < 20: |  |
| 390. | $\gamma$ Lib | 1529.9 | -14 27 | G8 III-IV | 2 | < 15 |  |
| 391. | 16 Ser | 1531.7 | +1021 | K0p | 2 |  | VV |
| 392. | $\phi$ Boo | 1534.2 | +40 41 | G8 IV | 2 | < 20: |  |
| 393. | $\theta$ UMi | 1534.4 | +7741 | K5 III | 2 | < 15 |  |
| 394. | a Ser | 1539.3 | +644 | K2 III | 1 | $<15$ |  |
| 395. | $\lambda$ Ser | 1541.6 | +740 | G0 V w | 1 | < 15 |  |

TABLE $2 a$-Continued

| No.* | Star | $\boldsymbol{a}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} 0 \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 396 | $\omega \mathrm{Ser}$ | $15^{\mathrm{h}} 45^{\text {m }}$. 2 | $+2^{\circ} 30^{\prime}$ | G8 III | 2 | < 15 |  |
| 397. | $\delta \mathrm{CrB}$ | 1545.4 | +26 23 | G5 III-IV | 2 | < 15 |  |
| 398. | $\rho \mathrm{Ser}$ | 1546.9 | +21 17 | K5 III | 2 | $<15$ |  |
| 399. | $\kappa \mathrm{CrB}$ | 1547.5 | +35 58 | K0 III-IV | 2 | < 15 |  |
| 400. | $\theta \mathrm{Lib}$ | 1548.1 | -1626 | G8 III-IV | 2 | < 20: |  |
| 401*. | $\chi$ Her | 1549.2 | +42 44 | F9 V w | 1 | < 15 |  |
| 402*. | $\gamma$ Ser | 1551.8 | +15 59 | F6 V w | 1 | < 20: | VV |
| 403. | $\epsilon \mathrm{CrB}$ | 1553.4 | +2710 | K3 III | 1 | < 15 |  |
| 404. | 5 Her | 1556.8 | +1806 | K0 III | 2 | < 15 |  |
| 405. | $\rho \mathrm{CrB}$ | 1557.2 | $+3337$ | G2 V w | 2 | < 20: |  |
| 406. | $\theta$ Dra | 1600.0 | +5850 | F8 IV-V s | 1 | 30 | SB1 |
| 407. | $\kappa$ Her A | 1603.6 | +1719 | G8 III | 2 | < 20: |  |
| 408. | $\tau \mathrm{CrB}$ | 1605.3 | +3645 | K0 III | 1 | < 15 | VV? |
| 409. | $\chi$ Sco | 1608.3 | -1135 | K3 III | 2 | < 15 |  |
| 410. | $\epsilon$ Oph | 1613.0 | $-427$ | G8 III | 2 | < 15 |  |
| 411. | $\gamma$ Her | 1617.5 | +19 23 | F0 III | 6 | 115 | VV |
| 412. | $\psi$ Oph | 1618.2 | -19 48 | K0 III | 2 | < 15 |  |
| 413. | $\xi \mathrm{CrB}$ | 1618.2 | +3107 | K0 III | 2 | < 15 |  |
| 414. | $\nu^{2} \mathrm{CrB}$ | 1618.7 | +3356 | K5 III | 2 | < 15 |  |
| 415. | HR 6126 | 1622.0 | +6920 | K2 III | 2 | < 20: |  |
| 416. | $\eta$ Dra | 1622.6 | +6144 | G8 III | 1 | < 15 |  |
| 417. | HR 6136 | 1623.5 | + 053 | K4 IIIp | 2 | < 20: |  |
| 418 | $\phi$ Oph | 1625.4 | -16 24 | G8 III | 2 | < 20: |  |
| 419. | $\beta$ Her | 1625.9 | +2142 | G8 III | 1 | < 20: | SB1 |
| 420. | HR 6152 | 1626.2 | $+2042$ | G8p | 2 | < 15 |  |
| 421. | 29 Her | 1627.9 | +1142 | K5 III | 2 | $<20$ : |  |
| 422. | HR 6196 | 1635.8 | $-1733$ | G8 II | 2 | < 20: |  |
| 423. | HR 6199 | 1636.0 | +5613 | K1 III | 2 | < 15 |  |
| 424. | $\zeta$ Her | 1637.5 | +3147 | G0 IV w | 1 | < 15 | VB |
| 425. | $\eta$ Her | 1639.5 | +39 07 | G8 III-IV | 2 | $<15$ | VV? |
| 426. | 18 Dra | 1640.2 | +64 47 | K1p | 2 | < 20: |  |
| 427 | 43 Her | 1641.0 | + 846 | K5 III | 2 | < 15 |  |
| 428. | 20 Oph | 1644.3 | -10 36 | F6 IV w | 4 | < 20: |  |
| 429 | 51 Her | 1647.6 | +2450 | K2 II-III | 2 | < 15 |  |
| 430. | 23 Oph | 1649.2 | -600 | K2 III | 2 | $<20$ : |  |
| 431 | HR 6287 | 1650.6 | +2107 | G8 III | 2 | $<15$ |  |
| 432. | $\kappa$ Oph | 1652.9 | +932 | K2 III | 1 | < 15 | LV |
| 433. | 19 Dra | 1655.5 | +6517 | F6 V w | 4 | < 20: | SB1 |
| 434. | 30 Oph | 1655.8 | -404 | K4 III | 2 | < 20: |  |
| 435. | $\epsilon \mathrm{UMi}$ | 1656.2 | +82 12 | G5 III s | 2 | 25 | SB1 |
| 436. | HR 6388 | 1706.3 | +4054 | K3 III | 2 | $<15$ | VV |
| 437 | 41 Oph | 1711.5 | -020 | K2 III | 2 | < 15 |  |
| 438. | $\pi \mathrm{Her}$ | 1711.6 | $+3655$ | K3 II | 1 | $<15$ |  |
| 439. | HR 6433 | 1713.9 | +1058 | K4 II-III | 2 | $<15$ |  |
| 440*. | 72 Her | 1716.9 | $+3236$ | G0 V w | 1 | < 15 |  |
| 441. | $\sigma$ Oph | 1721.6 | + 414 | K3 II | 2 |  |  |
| 442. | $\lambda$ Her | 1726.7 | +2611 | K4 III | 2 | $<15$ |  |
| 443. | $\beta$ Dra | 1728.2 | +52 23 | G2 II | 1 | $<15$ |  |
| 444. | 27 Dra | 1732.4 | +68 12 | K0 III | 2 | $<15$ |  |
| 445*. | 26 Dra | 1734.0 | +6157 | G1 V w | 1 | < 20, |  |

TABLE $2 a$-Continued

| No.* | Star | $\boldsymbol{a}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} 0 \sin i \\ (\mathrm{~K} \mathrm{~m} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 446. | $\omega$ Dra | 17437m 5 | $+68^{\circ} 48^{\prime}$ | F5 V w | 4 | $<20$ : | SB1 |
| 447. | $\beta$ Oph | 1738.5 | + 437 | K2 III | 1 | < 15 |  |
| 448. | $\mu \mathrm{Her}$ | 1742.6 | +27 47 | G5 IV | 1 | < 15 |  |
| 449 | $\psi$ Dra A | 1743.7 | +72 12 | F5 V s | 4 | 15 |  |
| 450 | 87 Her | 1744.8 | +2539 | K2 III | 2 | < 15 |  |
| 451. | 90 Her | 1750.0 | +4001 | K3 III | 2 | $<20$ : |  |
| 452. | $\xi$ Dra | 1751.8 | +5653 | K2 III | 1 | < 15 |  |
| 453 | $\theta$ Her | 1752.8 | +3716 | K1 II | 1 | < 20: |  |
| 454. | $\nu \mathrm{Oph}$ | 1753.5 | -946 | K0 III | 2 | < 15 |  |
| 455. | $\xi$ Her | 1753.9 | +29 16 | K0 III | 2 | $<20$ : |  |
| 456. | 35 Dra | 1753.9 | +7659 | F6 IV-V s | 4 | $<20$ : |  |
| 457. | $\gamma$ Dra | 1754.3 | +5130 | K5 III | 1 | < 15 |  |
| 458. | $\nu$ Her | 1754.7 | +3012 | F2 II | 1 | 30 |  |
| 459. | $\zeta \mathrm{Ser}$ | 1755.2 | - 341 | F3 V | 1 | 110: | VV? |
| 460. | 93 Her | 1755.6 | +16 46 | K0 II-III | 2 | < 15 |  |
| 461. | 70 Oph A | 1800.4 | +231 | K0 V | 1 | $<20$ : | SB1, VB |
| 462. | 71 Oph | 1802.5 | + 843 | G8 III-IV | 2 | < 20: |  |
| 463* | 99 Her | 1803.2 | +30 33 | F7 V w | 1 | < 20: |  |
| 464. | HR 6791 | 1804.5 | +4327 | K0p | 2 | < 15 | VV? |
| 465. | 36 Dra | 1813.3 | +6422 | F5 V w | 2 | < 15 |  |
| 466. | 74 Oph | 1815.9 | + 320 | G8 III | 2 | < 20: |  |
| 467. | $\eta$ Ser | 1816.1 | $-255$ | K0 III-IV | 1 | < 20: |  |
| 468. | $\kappa$ Lyr | 1816.4 | +3601 | K2 III | 2 | < 15 |  |
| 469. | $\zeta$ Sct | 1818.2 | -859 | K0 III | 2 | < 15 | SB1 |
| 470. | HR 6885 | 1818.4 | +1746 | K3 III | 2 | < 15 |  |
| 471. | 109 Her | 1819.4 | +2143 | K2 III | 2 | < 15 |  |
| 472. | $\chi$ Dra | 1822.9 | +7241 | F7 V | 1 | < 15 | SB1 |
| 473. | 60 Ser | 1824.5 | -203 | K0 III | 2 | < 15 | SB1 |
| 474. | 42 Dra | 1825.7 | +65 30 | K2 III | 2 | < 15 |  |
| 475. | HR 6970 | 1829.5 | -1103 | G8 III | 2 | < 20: |  |
| 476. | $a \mathrm{Sct}$ | 1829.8 | $-819$ | K3 III | 2 | < 15 |  |
| 477. | HR 6983 | 1831.7 | +5216 | K0 III | 2 | < 15 | VB |
| 478. | $\epsilon$ Sct | 1838.1 | -822 | G8 II | 2 | < 20: |  |
| 479* | 110 Her | 1841.4 | +20 27 | F6 V w | 1 | < 20: |  |
| 480. | $\beta$ Sct | 1841.9 | -451 | G5 II | 1 | < 15 | SB1 |
| 481. | HR 7064 | 1842.0 | +2633 | K3 III | 2 | $<15$ |  |
| 482. | HR 7117 | 1848.3 | +7358 | K0 II-III | 2 | < 15 |  |
| 483. | o Dra | 1849.7 | +5916 | K0 II-III | 2 | < 20: | SB1 |
| 484. | HR 7137 | 1850.8 | +5035 | G8 III | 2 | < 20: |  |
| 485. | $\eta$ Sct | 1851.7 | - 558 | K2 III | 2 | < 20: |  |
|  | HR 7162 | 1853.3 |  | G0 V w |  |  |  |
| 487*. | 11 Aql | 1854.5 | +1329 | F8 IV w | 4 | 25 |  |
| 488. | $\epsilon$ Aql | 1855.1 | +1456 | K2 III | 2 | $<15$ |  |
| 489. | $v$ Dra | 1855.6 | +7110 | K0 III | 2 | < 15 | VV |
| 490. | HR 7181 | 1855.7 | +2605 | K2 III | 2 | < 15 | VV |
| 491. | $\lambda \mathrm{Lyr}$ | 1856.2 | +3200 | K3 III | 2 | < 20: |  |
| 492. | 12 Aql | 1856.3 | - 553 | K1 III | 2 | < 15 |  |
| 493. | $\pi \mathrm{Sgr}$ | 1903.8 | -21 11 | F2 II | 7 | 30 |  |
| 494. | 53 Dra | 1909.8 | +5641 | G8 III | 2 | < 20: |  |
| 495. | 43 Sgr | 1911.8 | -19 08 | G8 II | 2 | < 20: |  |

TABLE $2 a$-Continued

| No.* | Star | $\boldsymbol{a}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 496 | 54 Dra | $19^{\mathrm{h}} 12^{\mathrm{m}} .1$ | $+57^{\circ} 32^{\prime}$ | K2 III | 2 | < 20: |  |
| 497 | $\delta$ Dra | 1912.5 | +6729 | G9 III | 2 | < 15 |  |
| 498 | $\theta$ Lyr | 1912.9 | +3757 | K0 II | 1 | < 20: |  |
| 499. | 23 Aql | 1913.4 | +054 | K2 II-III | 2 | < 20: |  |
| 500 | $\kappa$ Cyg | 1914.8 | +5311 | K0 III | 1 | < 15 | VV |
| 501. | 26 Aql | 1915.2 | - 536 | G8 III-IV | 2 | $<15$ | SB1 |
| 502 | $\tau$ Dra | 1917.5 | +7310 | K3 III | 2 | $<15$ | VV |
| 503. | 31 Aql | 1920.2 | +1144 | G8 IV | 2 | < 15 |  |
| 504. | $\delta \mathrm{Aql}$ | 1920.4 | $+255$ | F0 IV-V | 8 | 85 | VV |
| 505. | 4 Vul | 1921.1 | +19 36 | K0 III | 2 | < 20, |  |
| 506. | $\mu \mathrm{Aql}$ | 1929.2 | +710 +69 | K3 III | 2 | < 20: |  |
| 507. | $\sigma$ Dra | 1932.6 | +69 29 | K0 V | 1 | < 15 |  |
| 508. | HR 7468 | 1933.5 | +4428 | K0 III | 2 | < 20: |  |
| 509. | $\theta$ Cyg | 1933.8 | +4959 | F5 IV-V s | 4 | < 20: |  |
| 510. | a Sge | 1935.6 | +1747 | G0 II | 1 | < 15 |  |
| 511. | $\beta$ Sge | 1936.6 | +1715 | G8 II | 2 | < 20: |  |
| 512 | 10 Vul | 1939.6 | +25 32 | G8 III | 2 | < 15 |  |
| 513 | 15 Cyg | 1940.7 | +3707 | G8 III | 2 | < 20: |  |
| 514 | $\gamma \mathrm{Aql}$ | 1941.5 | +1022 | K3 II | 1 | < 15 |  |
| 515. | 17 Cyg A | 1942.6 | $+3330$ | F5 V w | 1 | < 20: | VV? |
| 516. | o Aql | 1946.2 | +10 10 | F8 V s | 2 | < 15 |  |
| 517. | 20 Cyg | 1948.1 | +5244 | K3 III | 2 | < 20: |  |
| 518. | $\epsilon$ Dra | 1948.5 | +7001 | G8 III | 2 | < 20: |  |
| 519 | $\xi \mathrm{Aql}$ | 1949.4 | + 812 | K0 III | 2 | < 20: |  |
| 520. | $\beta$ Aql | 1950.4 | + 609 | G8 IV | 1 | < 20: |  |
| 521. | 7 Cyg | 1952.6 | +34 49 | K0 III | 2 | < 20: |  |
| 522. | HR 7633 | 1954.0 | $+5835$ | K5 II-III | 2 | < 20: |  |
| 523 | $\gamma$ Sge | 1954.3 | +19 13 | K5 III | 2 | $<15$ |  |
| 524. | 26 Cyg | 1958.5 | +4950 | K1 II-III | 2 | < 20: |  |
| 525. | $\eta$ Sge | 2000.7 | +19 42 | K2 III | 2 | < 20: |  |
| 526. | $\rho$ Dra | 2002.4 | +6735 | K3 III | 2 | < 20: |  |
| 527. | 23 Vul | 2011.6 | +2730 | K3 III | 2 | < 20: |  |
| 528. | $a^{2}$ Cap | 2012.5 | $-1251$ | G9 III | 2 | $<15$ |  |
| 529. | 24 Vul | 2012.5 | +2422 | G8 III | 2 | < 20: |  |
| 530. | HR 7759 | 2013.4 | +40 03 | K4 II | 2 | < 20: |  |
| 531. | HR 7794 | 2018.2 | + 501 | G8 III-IV | 2 | < 20: |  |
| 532. | 39 Cyg | 2019.9 | +3152 | K3 III | 2 | < 20: |  |
| 533. | $\rho$ Cap | 2023.2 | $-1809$ | F2 IV | 7 | 115: |  |
| 534. | 41 Cyg | 2025.3 | +30 02 | F5 II | 1 | < 15 |  |
| 535*. | $\beta$ Del | 2032.9 | +1415 | F5 IV s | 4 | 55 | VB |
| 536. | 71 Aql | 2033.2 | -127 | G8 III | 2 | < 20: | SB1 |
| 537. | 1 Aqr | 2034.3 | + 008 | K1 III | 2 | < 20: |  |
| 538. | $\kappa$ Del | 2034.3 | + 944 | G5 IV | 2 | < 20: |  |
| 539. | 30 Vul | 2040.6 | $+2455$ | K2 III | 2 | $<15$ | VV |
| 540. | 52 Cyg | 2041.5 | $+3021$ | K0 III | 2 | < 15 |  |
| 541. | $\epsilon \mathrm{Cyg}$ | 2042.2 | $+3336$ | K0 III | 1 | < 15 | VV |
| 542. | HR 7955 | 2042.9 | +5713 | F8 IV-V w | 4 | < 20: |  |
| 543. | HR 7956 | 2043.2 | +3400 | K3 III | 2 | < 20: |  |
| 544. | ${ }^{\eta} \mathrm{Cep}$ | 2043.2 | +6127 | K0 IV | 1 | < 15 |  |
| 545. | 31 Vul | 2047.8 | +26 43 | G8 III | 2 | < 20: |  |

TABLE $2 a$-Continued

| No.* | Star | $\boldsymbol{a}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ \left(\mathrm{~K}_{\mathrm{m}} / \mathrm{Sec}\right) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 546 | 32 Vul |  | $+27^{\circ} 41^{\prime}$ | K4 III | 2 | < 15 |  |
| 547 | 17 DeJ | 2050.9 | +1320 | K0 III | 2 | < 20: |  |
| 548* | 1 Equ | 2054.1 | +355 +38 | F5 IV w | 4 | 75 | VB |
| 549 | 61 Cyg A | 2102.4 | +3815 | K5 V | 1 | $<15$ |  |
| 550 | $\nu \mathrm{Aqr}$ | 2104.2 | -1147 | G8 III | 2 | < 15 |  |
| 551 | $\zeta$ Cyg | 2108.7 | +29 49 | G8 II | 1 | < 15 | VV |
| 552 | $\iota$ Cap | 2116.7 | $-1716$ | G8 III | 2 | < 15 |  |
| 553 | 1 Peg | 2117.5 | +1923 | K1 III | 1 | < 15 |  |
| 554 | 71 Cyg | 2125.8 | +4606 | K0 III | 2 | < 20: |  |
| 555. | $\rho$ Cyg | 2130.2 | +4509 | G8 III | 2 | < 20: |  |
| 556. | 72 Cyg | 2130.7 | +38 05 | K1 III | 2 | < 15 |  |
| 557 | 25 Aqr | 2134.5 | + 148 | K0 III | 2 | < 20: |  |
| 558* | 42 Cap | 2136.1 | -14 30 | G2 IV s | 2 | 15 | SB1 |
| 559. | $\kappa$ Сар | 2137.1 | -19 19 | G8 III | 2 | $<20$ : |  |
| 560. | 46 Cap | 2139.7 | $-932$ | G8 II-III | 2 | < 15 | VV |
| 561. | $\mu$ Cyg A | 2139.7 | +28 17 | F6 V w | 4 | < 15 |  |
| 562. | 11 Cep | 2140.4 | +7051 | K0 III | 2 | < 15 |  |
| 563. | HR 8324 | 2141.8 | +7152 | K1 III | 2 | < 15 | VV? |
| 564. | 16 Cep | 2157.8 | +7242 | F5 V s | 2 | 35 |  |
| 565. | $\nu \mathrm{Peg}$ | 2200.6 | $+434$ | K4 III | 2 | < 15 | VV |
| 566. | HR 8424 | 2202.0 | +44 32 | K5 III | 2 | < 15 |  |
| 567. | 20 Cep | 2202.0 | +6218 | K4 III | 2 | < 15 |  |
| 568 | $\iota \mathrm{Peg}$ | 2202.4 | +2451 | F5 V s | 1 | < 20: | SB1 |
| $569 *$ | $\pi \mathrm{Peg}$ | 2205.6 | +3241 | F5 III s | 4 | 115: |  |
| 570. | 24 Cep | 2207.9 | +7151 | G8 III | 2 | < 20, | VV? |
| 571. | HR 8472 | 2208.2 | +5620 | F8 V s | 2 | < 20: |  |
| 572. | HR 8475 | 2208.4 | +3407 | K2 III | 2 | < 20: | VV? |
| 573. | HR 8485 | 2209.6 | +39 13 | K3 III | 2 | < 15 | VV? |
| 574. | $\epsilon$ Cep | 2211.4 | +5633 | F0 IV | 1 | 110 | VV |
| 575. | $\theta$ Aqr | 2211.6 | $-817$ | G8 III-IV | 2 | < 15 |  |
| 576. | 1 Lac | 2211.6 | +3715 | K3 II-III | 2 | < 20: |  |
| 577. | 3 Lac | 2219.6 | +5144 | G9 III | 2 | < 15 |  |
| 578. | 35 Peg | 2222.8 | +412 | K0 III | 2 | $<20$ : |  |
| 579. | $\zeta$ Aqr | 2223.7 | - 032 | F5 IV w | 4 | $\left\{\begin{array}{l}75 \\ 75\end{array}\right.$ | $\left.\mathrm{np}_{\text {sf }}\right\}_{\text {VB }}$ |
| 580. | 37 Peg | 2224.9 | $+355$ | F5 IV s | 4 | - 85 | VB |
| 581 | $\kappa$ Aqr | 2232.6 | $-445$ | K2 III | 2 |  |  |
| 582* | 31 Cep | 2233.3 | +7307 | F4 III | 7 | 100 |  |
| 583. | 11 Lac | 2236.1 | +43 45 | K3 III | 2 | $<15$ |  |
| 584. | 66 Aqr $\eta \mathrm{Peg}$ | 2238.2 22 | 1921 +2942 | K4 III | 2 1 | < 20 $<15$ |  |
| 585. | $\eta$ Peg | 2238.3 | +29 42 | G2 II-III | 1 | < 15 | SB1 |
| 586. | 13 Lac | 2239.6 | +4118 | K0 III | 2 | < 20: |  |
| 587* | $\xi \mathrm{Peg}$ | 2241.7 | +1140 | F7 V w | 1 | < 15 |  |
| 588. | $\lambda \mathrm{Peg}$ | 2241.7 | +2302 | G8 II-III | 2 | < 20: |  |
| 589. | $\mu \mathrm{Peg}$ | 2245.2 | +2404 | K0 III | 2 | < 15 |  |
| 590. | $\iota$ Cep | 2246.1 | +6540 | K1 III | 2 | $<20$ : |  |
| 591*. | $\sigma$ Peg | 2247.3 | + 918 | F7 IV s | 1 | < 15 |  |
| 592. | HR 8702 | 2247.9 | +8237 | K3 III | 2 | < 20: |  |
| 593. | HR 8748 | 2255.2 | +83 49 | K4 III | 2 | < 15 |  |
| 594. | 3 And | 2259.7 | +4930 | K0 III | 2 | < 15 |  |
| 595. | HR 8779 | 22.59 .7 | +6640 | K3 III | 2 | < 15 |  |

TABLE $2 a$-Continued

| No.* | Star | $\boldsymbol{a}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Remarks $\ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 596. | 56 Peg | $23^{\mathrm{h}} 02^{\mathrm{m}} 2$ | $+24^{\circ} 56^{\prime}$ | K0 IIp | 2 | < 15 | VV |
| $597 *$ | $\pi$ Cep | 2304.7 | +7451 | G2 III | 6 | $\leqq 15$ | SB1, VB |
| 598. | $\psi^{1}$ Aqr | 2310.6 | -938 | K0 III | 2 | $<15$ |  |
| 599. | $\gamma \mathrm{Psc}$ | 2312.0 | + 244 | G8 III | 2 | < 15 |  |
| 600. | 94 Aqr | 2313.8 | $-1400$ | G5 IV | 2 | $\leqq 15$ | VV |
| 601. | o Cep | 2314.5 | +6734 | K0 III | 2 | < 15 |  |
| 602. | 11 And | 2314.8 | +48 05 | K0 III | 2 | < 20: |  |
| 603. | 7 Psc | 2315.2 | + 450 | K2 III | 2 | < 20: |  |
| 604. | 66 Peg | 2318.0 | +1146 | K3 III | 2 | < 20: |  |
| 605. | $v \mathrm{Peg}$ | 2320.4 | +2251 | F8 IV s | 1 | 95 |  |
| 606. | $\theta$ Psc | 2322.9 | + 550 | K1 III | 2 | < 15 |  |
| 607. | 70 Peg | 2324.1 | +1213 | G8 III | 2 | < 20, | VV? |
| 608 | 14 And | 2326.4 | +3841 | K0 III | 2 | < 20: |  |
| 609* | 72 Peg | 2329.0 | $+3046$ | K4 III | 2 | < 20: | VB |
| 610. | $\lambda$ And | 2332.7 | $+4555$ | G8 III-IV | 1 | < 20: | SB1 |
| 611*. | $\iota$ Psc | 2334.8 | + 505 | F7 V w | 1 |  |  |
| 612. | ${ }_{\gamma}$ Cep | 2335.2 | +7704 | K1 IV | 1 | < 15 |  |
| 613. | 104 Aqr | 2336.6 | -1822 | G0 II | 7 | 15 |  |
| 614. | HR 8987 | 2337.3 | -1600 | K4 III | 2 | < 15 | VV? |
| 615. | 78 Peg | 2339.0 | +28 48 | K0 III | 2 | $<20$ : | VV? |
| 616. | $\tau$ Cas | 2342.2 | +5806 | K1 III | 2 | < 15 |  |
| 617. | 27 Psc | 2353.6 | -407 | G9 III | 2 | < 20: |  |
| 618. | $\omega$ Psc | 2354.2 | +619 | F4 IV s | 4 | 55 | VV? |

NOTES TO TABLE $2 a$

| $15 \zeta$ And: | Spectroscopic binary with $P=17.8$ days. See the discussion by L. Gratton, $A p . J ., 111,31,1950 ; M c D o n a l d$ Contr., No. 185. |
| :---: | :---: |
| 1864 Psc: | Double-line spectroscopic binary with $P=14$ days. |
| 40 v And: | Miss Roman (1950) gives F8 IV on the MKK system. |
| 69 日 Per: | Miss Roman (1950) classifies this star as F6 V. |
| 7520 Per: | The $\Delta m$ is about 0.4 mag . |
| 10346 Tau: | The $\Delta m$ is about 0.3 mag . |
| 131 a Aur: | See text. |
| $133 \lambda$ Aur: | Miss Roman (1950) gives G2 IV-V. |
| 19165 Gem: | Double-line spectroscopic tinary with a period of several years. |
| $198 \sigma$ Gem: | Spectroscopic binary with $P=19.6$ days. The line width is presumably due to rapid axial rotation associated with the orbital motion. |
| 2039 Pup: | The $\Delta m$ is about 0.7 mag . |
| 219 o UMa: | The type is given as G5 V in the Yerkes Atlas. |
| 226 є Нуa AB: | The type is given as G0 III in the Yerkes Atlas but does not appear in later lists. According to W. P. Bidelman, the brighter component of this close binary belongs to a later subdivision of class G. |
| 231 HR 3579: | This star ( $=10 \mathrm{UMa}$ ) is a visual binary with a period of about 21 years. The line width was estimated on spectrograms that were taken in the interval February 8-March 23, 1953. |
| $234 \sigma^{\mathbf{2}}$ UMa: | Miss Roman (1950) gives F6 IV on the MKK system. |
| 27040 Leo: | Miss Roman (1950) classifies this star as F6 V. |
| 272 HR 4084: | The type is given as F2 V by Bidelman (1951). |
| 326 \% Vir: | The difference in line width between the two components has been noted by Struve and Mrs. Gould (Pub. A.S.P., 64, 183, 1952; A.J., 57, 160, 1952). |
| 34361 Vir: | The type is given as G5 V by Miss Roman (1950). |
| 347 т Boo: | Miss Roman (1950) gives F6 IV on the MKK system. |
| 363 ө Boo: | Miss Roman (1950) classifies this star as F6 IV on the MKK system. |
| 401 x Her: | The type is given as F8 V by Miss Roman (1950). |
| $402 \gamma$ Ser: | Miss Roman (1950) gives F6 IV on the MKK system. |
| 44072 Her: | The type is given by Miss Roman (1950) as G2 V. |
| 44526 Dra: | Miss Roman (1950) gives G2 V. |
| 46399 Her: | The type is given as F8 V by Miss Roman (1950). |
| 479110 Her: | Miss Roman (1950) classifies this star as F5 IV on the MKK system. |
| 48711 Aql: | The type on the MKK system is F8 III-IV, according to Miss Roman. We have assumed that this corresponds to F8 IV on the MK system. |
| 535 B Del: | The $\Delta m$ is about 0.6 mag. |
| 5481 Equ: | The $\Delta m$ is only about 0.2 mag . |
| 55842 Cap: | The line widening is only marginally visible. |
| $569 \pi$ Peg: | No good Mills plates are available. The type is F5 II-III on the MKK system (Miss Roman 1950), and we have assumed that this is equivalent to F5 III on the MK system. |
| 58231 Cep: | A type of F4 II-III on the MKK system was assigned by Bidelman. We have assumed that this is equivalent to F4 III on the MK system. |
| 587 ¢ Peg: | Miss Roman (1950) assigned a type of F6 III-IV on the MKK system. |
| 591 б Peg: | A type of F6 V was assigned by Miss Roman (1950). |
| 597 т Cep: | This star is a single-line spectroscopic binary ( $P=556$ days) and the brighter component of a visual binary with $\Delta m$ about 2 mag. We are unable to explain the discrepancy between our value of $v \sin i(\leq 15 \mathrm{~km} / \mathrm{sec})$ and the value of $70 \mathrm{~km} / \mathrm{sec}$ reported by Slettebak (1953). |
| 60972 Peg: | The $\Delta m$ is very small. |
| 611 ィ Psc: | Miss Roman's (1950) type is F8 V. |

TABLE $2 b$
Catalogue of Line Widths of 32 High-Luminosity Stars between Spectral Types F0 and K5, Expressed as Rotational Velocities

| No.* | Star | $\boldsymbol{a}_{1900}$ | $\delta_{1900}$ | Spectral Type | Source $\dagger$ | $\begin{gathered} v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | $\begin{gathered} \text { Re- } \\ \text { marks } \ddagger \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 619. | ${ }_{\phi}$ Cas | $1^{\text {b }} 13 \mathrm{~m}$ m | $+57^{\circ} 42^{\prime}$ | F0 Ia | 1 | 35 | VV |
| 620 | $\eta$ Per | 243.4 | +55 29 | K3 Ib | 1 | <20: |  |
| 621. | a Per | 317.2 | +4930 | F5 Ib | 1 | 20 |  |
| 622. | $\mu$ Per | 407.6 | +48 09 | G0 Ib | 1 | <15 | SB1 |
| 623* | 10 Cam | 454.5 | +6018 | G0 Ib | 1 | 15 |  |
| 624*. | $\epsilon$ Aur | 454.8 | +43 40 | F0p Ia | 8 | 30 | SB1 |
| 625. | $a \mathrm{Lep}$ | 528.3 | -1754 | F0 Ib | 1 | 15 |  |
| 626. | $\epsilon$ Gem | 637.8 | +2514 | G8 Ib | 1 | <15 |  |
| 627. | $o^{1} \mathrm{CMa}$ | 650.0 | -24 04 | K3 Iab | 1 | $\leq 20$ |  |
| 628. | $\delta \mathrm{CMa}$ | 704.3 | -26 14 | F8 Ia | 1 | 25 |  |
| 629. | $\zeta$ Mon | 803.6 | - 242 | G2 Ib | 1 | <15: |  |
| 630 | HR 3459 | 838.8 | - 652 | G2 Ib | 5 | <15 |  |
| 631. | HR 3612 | 900.2 | +3851 | G8 Ib-II | 2 | <20: |  |
| 632 | 89 Her | 1751.4 | +2604 | F2 Ia | 1 | 25 | VV |
| 633. | 45 Dra | 1830.8 | +5658 | F7 Ib | 7 | $<20$ : |  |
| 634. | $\nu$ Aql | 1921.4 | + 008 | F2 Ib | 1 | $<20$ : |  |
| 635. | 22 Vul | 2011.2 | +2312 | G2 Ib | 1 | 15: | SB1 |
| 636. | $a^{1} \mathrm{Cap}$ | 2012.1 | -1249 | G3 Ib | 5 | <15 | VV |
| 637. | 35 Cyg | 2014.8 | +3440 | F5 Ib | 1 | <15 | VV |
| 638. | $\gamma \mathrm{Cyg}$ | 2018.6 | +3956 | F8 Ib | 1 | <15 |  |
|  | $\underset{\xi}{\underline{C l y g}}$ | 2101.3 | +4332 | K5 Ib | 1 | $<15$ | VV |
| 640* | DT Cyg | 2102.3 | +3047 |  | 1 | $<15$ | LV |
| 641. | $\zeta$ Cap | 2121.0 | -22 51 | G4 Ib pec. | 6 | $<20$ | VV |
| 642. | $\beta$ Aqr | 2126.3 | - 601 +925 | G0 Ib | 1 | <15 |  |
| 643. | $\epsilon \mathrm{Peg}$ | 2139.3 | +925 | K 2 Ib | 1 | <15 |  |
| 644. | 9 Peg | 2139.8 | +1653 | G5 Ib |  |  |  |
| 645. | a Aqr | 2200.6 | - 048 | G2 Ib | 1 | <15 |  |
| 646. | $\zeta$ Cep | 2207.4 | +5742 | K 1 Ib | 1 | <15 |  |
| 647. | HR 8752 | 2255.9 | +56 24 | G0 Ia | 1 | 35 | VV? |
| 648. | $\psi$ And | 2341.1 | +45 52 | G5 Ib | 2 | <20: |  |
| $649 *$ | $\rho$ Cas | 2349.4 2359 | +5657 -1104 | F8 Ia pec. | 6 | 20: | LV |
| 650. | 3 Cet | 2359.4 | -1104 | K3 Ib | 2 | <15 |  |

* Additional remarks for stars noted by asterisks:

62310 Cam : The weak lines are slightly wider than those in the sun.
624 є Aur: The type has been given by Bidelman (1951) as A8 I $a$; the spectrum may be slightly variable, even outside eclipse.
640 DT Cyg: A cepheid variable with $P=2.5$ days. The range in spectral type is given by A. D. Code ( $A$ p. $J ., 106,309,1947$ ) as F5.5 I-II to F7 I-II. The upper limit to $v \sin i$ quoted in the table was assigned on the basis of a plate exposed at phase 0.609 period (see W. H. Grasberger and G. H. Herbig, Pub. A.S.P., 64, 28, 1952).
$649 \rho$ Cas: $\quad$ The value of $v \sin i=20: \mathrm{km} / \mathrm{sec}$ was estimated on a spectrogram taken on November 19, 1953. An examination of the width of weak lines on Mills plates of $\rho$ Cas exposed in 1906, 1907, 1908, 1910, and 1923 yielded essentially the same result.
$\dagger$ The sources are identified in the text (see pp. 135 and 136).
$\ddagger$ See note to Table $2 a$.

The estimates of line width were not made directly in kilometers per second but in units of an arbitrary scale in which the solar line width was set at $1.0, \pi^{3}$ Orionis 1.3, 11 Aquilae 2.0, $\rho$ Andromedae 3.0, 31 Comae 4.0, and 18 Comae 5.0. The conversion of estimates on this scale to $v \sin i$ in $\mathrm{km} / \mathrm{sec}$ by means of a correlation diagram led to a spurious grouping of the $v \sin i$ values around certain rotational velocities, especially at those of the standard stars. The concentration of velocities around values ending in 5 is due to the same reason. No attempt has been made to correct the data in Tables $2 a$ and $2 b$ for this effect. All values of $v \sin i$ in those tables have, however, been rounded off to the nearest multiple of $5 \mathrm{~km} / \mathrm{sec}$.

For the supergiants, the turbulence-widened profiles of the strong lines made these lines unsuitable for estimating $v \sin i$, so that only weak lines were used for this purpose in stars of luminosity class I. Because of the marked difference in line character between the supergiants and the standard stars, it is entirely possible that determinations of $v \sin i$ for supergiants by some more appropriate method might differ systematically from the values in Table $2 b$. It should be emphasized that $v \sin i$ is used in that table only as a numerical index of the width of weak lines; its use is not intended to imply that the line-broadening agent in such stars is necessarily axial rotation.

Because of the manner in which the $v \sin i$ 's in Tables $2 a$ and $2 b$ were determined, it is difficult to make any general statement as to their probable uncertainties. It is possible, however, to gain a limited idea of their reliability by comparing them with rotational velocities obtained for the same stars by other investigators. Such a comparison is shown in Table 3, in which the published $v \sin i$ 's have all been obtained with dispersions comparable with that of the present work. The stars are identified by their numbers in Tables $2 a$ and $2 b$. The main conclusions to be drawn are, first, that the present results for stars with narrow lines seem to be in good agreement with other work and, second, that the $v \sin i$ 's for the supergiants are in reasonable agreement with rotational velocities assigned to those stars from detailed studies of their line profiles. However, the material in Table 3 is too scanty to furnish a good check on the accuracy of the data of this paper for stars with $v \sin i$ greater than about $25 \mathrm{~km} / \mathrm{sec}$.

A more detailed comparison is possible with the results of Huang (1953), which were obtained from micrometer measures of many of these same spectrograms. Figure 1 shows the correlation of Huang's rotational velocities ( $\xi_{r} \sin i$, computed from his eqs. [1] and [2] with the parameter $\gamma=2$, its compromise value) as determined from Mills plates, with the values of $v \sin i$ for the same stars given in this paper. For this comparison, 115 stars are available. The supergiants have been excluded because of the special nature of their line profiles. The points plotted in Figure 1 show the existence of a scale difference between the two series. Approximately the same difference in scale seems to be present in a comparison of Huang's velocities for stars with strong $\lambda 4481$ (i.e., stars of types late A, F, and G) with those determined by Elvey (see Fig. 3 of Huang's paper). As was suggested by Huang, this effect probably arises from a visual overestimation, when the micrometer settings were made, of the width of a strong, rotationally broadened line. Formally, Huang's series of rotational velocities of F- and G-type stars that are plotted in Figure 1 can be reduced to the scale of the present paper by using $\gamma \cong$ 1.4.

The spectral types used in this paper are on or near the revised Atlas system of Morgan and Keenan. Other lists of spectral types in the Yerkes systems were also drawn upon, so that in Tables $2 a$ and $2 b$ the type is accompanied by a number that identifies the source. The sources and their designations are as follows.

1. H. L. Johnson and W. W. Morgan (1953): a list of standards for the MK system.
2. N. G. Roman (1952a): a list of types and luminosity classes for F5-K5 stars, expressed on the MK system.
3. N. G. Roman (1952b) : classifications of a number of F- and G-type stars on the MK system.
4. N. G. Roman (1950): a list of the types and luminosity classes of F5-G5 stars, expressed on the MKK system of the Atlas of Stellar Spectra by W. W. Morgan, P. C. Keenan, and E. Kellman (1943). These classifications have been converted to the MK system as follows (see Johnson and Morgan 1953, p. 319, and Roman 1952a, p. 123): (a) all F2-F8 luminosity class III stars have been moved to class IV, and (b) all F2-F8 class IV stars have been changed to class IV-V.

TABLE 3
Stars for Which $v$ Sin $i$ Has Been Measured from Line Profiles by Another Investigator

| Tables $2 a, 2 b$ No. | Star | $\begin{gathered} \text { Tables } 2 a, 2 b \\ v \sin i \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Published $v \sin i$ (Km/Sec) | Reference* |
| :---: | :---: | :---: | :---: | :---: |
| 3 | 22 And | 40 | 65 | 4 |
| 156 | 74 Ori | 20 | 20 | 3 |
| 182. | $\delta$ Gem | 115 | 70; 70 | 1 |
| 196. | a CMi | < 15 | 0; 0 | 1 |
| 270. | 40 Leo | 20 | 15 | 3 |
| 326. | $\gamma \mathrm{Vir}\left\{\begin{array}{l}\text { np } \\ \text { sf }\end{array}\right.$ | 25 40 | 25; 50 | 1 |
| 329 | 31 Com | 85 | 75 | 4 |
| 338. | 53 Vir | < 15 | 10 | 3 |
| 383. | 5 Ser | < 15 | 0 | 3 |
| 428. | 20 Oph | $<20$ : | 10 | 3 |
| 463. | 99 Her | $<20$ : |  | 3 |
| 504. | $\delta \mathrm{Aql}$ | 85 | 100; 100 | 1 |
| 534 | 41 Cyg | < 15 | 0; 0 | 1 |
| 569. | $\pi \mathrm{Peg}$ | 115: | $\left\{\begin{array}{c}\text { about } 100 \\ 125\end{array}\right.$ | 2 |
| 611. | ${ }_{\iota} \mathrm{Psc}$ | < 15 | 0; 0 | 1 |
| 621. | $a \mathrm{Per}$ | 20 | 0; 0 | 1 |
| 624. | $\epsilon$ Aur | 30 | $\left\{\begin{array}{c}0 ; 0 \\ 30\end{array}\right.$ | 1 |
| 628. | $\delta \mathrm{CMa}$ | 25 | $\approx 30$ | 5 |

[^2]5. W. W. Morgan and N. G. Roman (1950): a list of supergiant standards. These types have been used without change unless there is a conflict with a classification given in source 1, above, in which case the latter type has been used.
6. W. W. Morgan, P. C. Keenan, and E. Kellman, Atlas of Stellar Spectra (1943): this work defines the MKK system. The changes described under source 4 have been made for F2-F8 stars taken from this work. Other types have not been changed.
7. W. P. Bidelman (1951): a list of classifications of Miss Payne's c-stars, expressed on the MKK system. The treatment was the same as described under source 4, above.
8. P. C. Keenan and W. W. Morgan in Astrophysics (Hynek 1951), chap. 1.

## III. DISCUSSION

The early Yerkes work on the spectral-type dependence of stellar rotation among stars less luminous than supergiants indicated that, in general, appreciable line broadening disappears among single stars ${ }^{1}$ later than type F5. The results of the present paper demonstrate the existence of appreciable line widths in main-sequence stars as late as type F8. The slight difference between this and the Yerkes value of F5 is undoubtedly due to the higher dispersion that was used in this work. Among stars of somewhat higher luminosity, it has been known for many years that a few single objects of types later than F5 showed lines of appreciable width: for example, W. W. Campbell and J. H. Moore (1928) noted that the determination of the radial velocities of 31 Comae and


Fig. 1.-The scatter diagram relating rotational velocities measured by Su-Shu Huang ( $\left.\xi_{r} \sin i\right)$ and those of this paper $(v \sin i)$, both in $\mathrm{km} / \mathrm{sec}$. The scales of the ordinates and abscissae differ by a factor of 2 , so the slope of the usual $45^{\circ}$ regression line is decreased accordingly. Open circles with horizontal arrows represent stars for which only an upper or lower limit on $v \sin i$ was determined in the present investigation. A horizontal line through a filled circle indicates that the value of $v \sin i$ for that star is somewhat uncertain. In order to avoid congestion near the origin, 29 stars for which $\xi_{r} \sin i=0$ and $v \sin i<15 \mathrm{~km} /$ sec , and 17 stars for which $\xi_{r} \sin i=0$ and $v \sin i<20: \mathrm{km} / \mathrm{sec}$ have not been plotted. Furthermore, only stars of luminosity classes II through V are represented in the diagram.

[^3]$v$ Pegasi, both of HD type G0, was difficult because of the poor quality of their spectral lines. More recently, J. L. Greenstein (1952, 1953), Slettebak (1953, 1954), Herbig and Miss Turner (1953), and others have noted that broad lines are very common among giant stars of types as late as early G.

The luminosity dependence of $v \sin i$ for the spectral interval F0-G5, as indicated by the data of this paper, is shown in Table 4. In this, as in the other collections of data that follow, each component of a visual binary or double-line spectroscopic binary has

TABLE 4

## Luminosity Dependence of Rotational Velocity for Spectral Types F0-G5

|  | Types F0-F4 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Luminosity class. <br> No. stars with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. <br> Total no. stars. <br> Fraction with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. | II | III | IV | IV-V | V |
|  | 4 | 6 | 7 | 2 | 7 |
|  | 5 | 6 | 7 | 2 | 9 |
|  | 0.8 | 1.0 | 1.0 | 1.0 | 0.8 |
|  | Types F5-F7 |  |  |  |  |
| Luminosity class. <br> No. stars with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. <br> Total no. stars <br> Fraction with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. | II240.5 | III230.7 | IV14200.7 | IV-V180.1 | $\begin{gathered} \mathrm{V} \\ 87 \\ 37 \\ 0.2 \end{gathered}$ |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Fraction with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. | Types F8-G0 |  |  |  |  |
| Luminosity class. <br> No. stars with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. <br> Total no. stars $\qquad$ | II | III | IV | IV-V | V |
|  | 4 | 1 | 2 | 1 | 1 |
|  |  |  | 4 | 4 |  |
|  | 0.2 | 1.0 | 0.5 | 0.2 | 0.04 |
| Fraction with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. | Types G1-G5 |  |  |  |  |
| Luminosity class <br> No. stars with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. <br> Total no. stars <br> Fraction with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. | II | III* | IV | IV-V | V |
|  | 0 | 0 | 0 |  | 0 |
|  | 7 | 5 | 6 | 0 | 10 |
|  | 0.0 | 0.0 | 0.0 |  | 0.0 |

* Includes one star of type G5 III-IV.
been entered with the integrated spectral type of the system, if the individual types are unknown. The last line of Table 4 gives the fraction of stars of each luminosity class that have projected rotational velocities greater than $20 \mathrm{~km} / \mathrm{sec}$. The entries in this line show that the tendency for a given star to have a $v \sin i>20 \mathrm{~km} / \mathrm{sec}$ weakens rapidly through spectral type $F$ but that rotation persists to later types in luminosity classes III and IV than in classes II or V. Rotation may be somewhat more common among the later F-type stars of luminosity class II than in those of class V, but the small sample of class II objects makes this point quite uncertain.

One type G5 star ( $\epsilon$ Ursae Minoris) and two of type K ( $\zeta$ Andromedae and $\sigma$ Gemi-
norum) in Table $2 a$ show broadened lines, very probably due to the fact that all are spectroscopic binaries of relatively short periods (39, 18, and 20 days, respectively) for such large stars. No other stars of types later than G5 have been found to have perceptibly wide lines. The line broadening observed in a few other objects of types G2-G5 is marginal ( $v \sin i=15 \mathrm{~km} / \mathrm{sec}$ ). If these three binaries are rejected, then the latest spectral type at which at least one star with $v \sin i \geq 20 \mathrm{~km} / \mathrm{sec}$ is known is G0 for luminosity classes III and IV, and type F8 for classes II, IV-V, and V.

The dependence of rotational velocity upon luminosity class is shown also in Table 5, which has been obtained by combining the first three parts of Table 4 . Table 5 gives the fractions of F0-G0 stars with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$ for each luminosity class from II to V. It must be emphasized, however, that the presentation of the data in the compressed form of Table 5 gives a somewhat misleading impression, because the mean spectral type is not the same for each luminosity class. For example, in the class III stars, 9 of the 10 objects between F0 and G0 are of types F0-F5, where the rotational velocities for any luminosity are fairly high. On the other hand, the bulk of the F0-G0 stars of class V represented in these statistics are of type F5 or later, where the average

TABLE 5
Fractions of F0-G0 Stars with $v$ SIn $i>20 \mathrm{Km} / \mathrm{SEC}$ as a Function of Luminosity Class*

| Luminosity class | II | III | IV | IV-V | V |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. stars with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. | 7 | 9 | 23 | 4 | 16 |
| Total no. stars | 13 : | 10 | 31 | 14 | 74 |
| Fraction with $v \sin i>20 \mathrm{~km} / \mathrm{sec}$. | 0.5 | 0.9 | 0.7 | 0.3 | 0.2 |

* See the text for a caution regarding the interpretation of the data in this Table.
$v \sin i$ is small. A much fairer picture of the situation is shown by the same data in Table 4, where an effort was made to minimize the effect present in Table 5 by combining stars over a spectral-type range no larger than was necessary to obtain a reasonably significant number of stars.

The variation of the mean rotational velocities ( $\bar{v}$, not $\bar{v} \sin i$ ) of groups of stars over the spectrum-luminosity class diagram between types F0 and G5 is shown in Table 6, which was constructed from the data of Tables $2 a$ and $2 b$. The blocks indicate the regions of the diagram from which stars were drawn in order to form the mean velocities. ${ }^{2}$ The mean $v \sin i$ 's for stars of luminosity classes II-V were multiplied by the factor $4 / \pi$ in order to obtain mean $v$ 's freed of the effect of an assumed random distribution in direction of the axes of rotation (Chandrasekhar and Münch 1950). This correction was applied throughout, although the number of stars in many of the groups is too small for it to be very meaningful. No allowance of this type was made for the supergiants (luminosity classes $\mathrm{I} a$ and $\mathrm{I} b$ ), and so the mean velocities entered in Table 6 for these objects are straight averages of the velocities listed in the $v \sin i$ column of Table $2 b$. The figures in parentheses beneath the mean velocities in Table 6 are the numbers of stars used in forming the means.

Although the samples in many of the regions of Table 6 are very small, the observational data, when presented in this form, lead to the same conclusions with regard to the luminosity dependence of rotation as were drawn on the basis of Table 4. The arrangement of the material in Table 6 may be the more useful for theoretical workers.

We have assumed throughout the present work that the assignment of spectral type

[^4]
and luminosity class is unaffected by the presence or absence of line width, since such classifications are generally made at a dispersion (about $125 \mathrm{~A} / \mathrm{mm}$ ) where line broadening of the magnitude found in stars of types F0 and later would be expected to be imperceptible. Nevertheless, the point is important enough to deserve a closer examination than we are in a position to make.

Among the stars of spectral types F5-G5 Miss Roman (1950, 1952a) has distinguished two groups, one characterized by weak and the other by strong lines. The space-velocity distribution of the weak-line stars has a larger dispersion than does that of the strongline stars. In Table $2 a$ the spectral types of stars between types F5 and G5 which have been assigned by Miss Roman to one group or the other, are followed by a " w " or an "s," even though the spectral type and luminosity class quoted there have been drawn from another source. Between types F5 and G0, there are available about 50 stars in each group. It is important to know whether axial rotation is correlated with membership in these groups. The answer is negative: there is no indication that the apparent rotational velocities of the two groups of stars differ in any significant way. There are about the same fractions of slowly rotating (or rapidly rotating) stars in each luminosity class for both weak- and strong-line objects.

As might be expected, the data of Table $2 b$ indicate that the supergiants of luminosity class $\mathrm{I} a\left(M_{v} \sim-7\right)$ have systematically greater line widths than those of class $\mathrm{I} b$ ( $M_{v} \sim-4.5$ ). In the spectral interval F0-G5, for which the data are probably most reliable for such spectra, the mean $v \sin i$ is $28 \mathrm{~km} / \mathrm{sec}$ for 6 class $I a$ stars, and $<15$ $\mathrm{km} / \mathrm{sec}$ for 17 class $\mathrm{I} b$ supergiants. A comparable result has been obtained by Huang and Struve (1954).

We have not included our results for the components of a Aurigae in the statistical results, because no accurate spectral types are available. The Yerkes Atlas (Morgan, Keenan, and Kellman 1943) gives MKK types of G5 and F6 for the primary and secondary components, respectively, but states that "the separate values for the two components are very uncertain and may be in error by a considerable fraction of their separation." K. O. Wright (1954) gives spectral types of approximately G5 III and G0 III for the

## NOTES TO TABLE 6

The entries in the table are $4 / \pi$ times $\overline{v \sin i}$ for luminosity classes II through V , and $\overline{v \sin i}$ for classes $\mathrm{I} a$ and $\mathrm{I} b$. It was sometimes necessary to combine the results for stars having definitely determined values of $v \sin i$ with those for which only an upper limit was available. This was done by assuming that it was permissible to use a value of $10 \mathrm{~km} / \mathrm{sec}$ in those cases where $v \sin i<15$ or $<20: \mathrm{km} / \mathrm{sec}$, always provided that the resulting mean was not unrealistically small. The values contained in the table were computed in this way. So that one may judge the effect of this assumption upon the means, the notes below give for a number of tabular entries the extreme limits on the value of $4 \bar{v} \sin i / \pi$ arising from error in this assumption. This range was obtained by regarding all stars for which $v \sin i$ has been observed to be $<15$ or $<20$ : $\mathrm{km} / \mathrm{sec}$ as having, first, $v \sin i=0$ and, second, $v \sin i$ values equal to their upper limits. In cases where lower limits have been set on $v \sin i$ in Table 2, it was assumed that a value of $\geq 115 \mathrm{~km} / \mathrm{sec}$ corresponds to $120 \mathrm{~km} / \mathrm{sec}$ and that $>115 \mathrm{~km} / \mathrm{sec}$ may be replaced by $140 \mathrm{~km} / \mathrm{sec}$ in order to compute the mean. The numbers in parentheses are the numbers of stars used in computing the corresponding value of $\bar{v}=$ $4 \overline{v \sin i} / \pi$.

The ranges are as follows:
F0-F2 II: the range of $\bar{v}$ is $32-37 \mathrm{~km} / \mathrm{sec}$. F5-F8 II: the range of $\bar{v}$ is $43-47 \mathrm{~km} / \mathrm{sec}$. F6-F8 IV: the range of $\bar{v}$ is $36-44 \mathrm{~km} / \mathrm{sec}$. F5 IV-V: the range of $\bar{v}$ is $18-30 \mathrm{~km} / \mathrm{sec}$. F0-F2 V: the range of $\bar{v}$ is $58-62 \mathrm{~km} / \mathrm{sec}$. F5 V: the range of $\bar{v}$ is $22-38 \mathrm{~km} / \mathrm{sec}$.
F6 V: the range of $\bar{v}$ is $11-27 \mathrm{~km} / \mathrm{sec}$.
One of the three stars entered under G5 III is actually of type G5 III-IV.
two components; the G5 star is usually regarded as the primary. The Lick spectrograms that we examined were taken in 1938-1939 on Process emulsion, but with a somewhat greater slit-width than we consider optimum. There is no difficulty, however, in assigning a value of $v \sin i<15 \mathrm{~km} / \mathrm{sec}$ to the primary star. The lines of the earlier-type star are much wider. It is our impression from examining a number of our best spectrograms that the narrow features often seen flanking strong lines of the primary, which seem to shift from one side to the other in phase with the secondary spectrum, are frequently not lines of the fainter component at all. In many cases they seem to be only weak lines in the spectrum of the primary star, which strengthen or become faint, depending upon the position of the underlying, wide-lined spectrum of the secondary. In speaking of the line width of the secondary star, therefore, we refer not to these narrow components but to the hazy, ill-defined features that underlie the rich, sharp-lined spectrum of the G5 star. It is difficult to estimate the width of these wide lines, but it is our impression that the line breadth of the earlier-type component of a Aurigae is comparable to that of 31 Comae ( $v \sin i=85 \mathrm{~km} / \mathrm{sec}$ ). If our interpretation of the spectrum is correct, it is interesting that the components of this binary, which lie on either side of the rotational "cutoff" slightly later than type G0 for stars of intermediate luminosity, have rotational velocities consistent with those of single stars of the same types.

The spectral interval F0-G5 is a region in which the transition from rapidly rotating to slowly rotating stars takes place, and for this reason it may be particularly important to have representative (i.e., extensive) data for stars of these types. The very small numbers of stars in some regions of the spectral-type luminosity-class diagram between F0 and G5 raises the question of how representative such small samples may be. The deterrent to the accumulation of more data is not the fact that somewhat fainter stars would have to be observed with moderately high dispersion but is the lack of accurate spectral-type and luminosity classifications for any significant number of additional objects. A systematic spectral classification of F0-G5 stars down to visual magnitude 6.5 or 7.0 would be very valuable. It not only would make possible a more thorough study of the matters discussed in this paper but might also render practical an examination of aspects of the phenomenon of rotation at which the present data only hint.

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[^0]:    * Contributions from the Lick Observatory, Ser. II, No. 56.

[^1]:    * Additional remarks for stars noted by asterisks are given in "Notes to Table 2a."
    $\dagger$ The sources are identified in the text (pp. 135 and 136).
    $\ddagger$ The abbreviations in the "Remarks" column have the following meanings:
    $\begin{array}{ll}\text { SB1: single-line spectroscopic binary. } & \text { SB2: double-line spectroscopic binary. } \\ \text { VV: variable velocity. } & \text { VV?: possibly variable velocity. } \\ \text { LV: light variable. } & \text { VB: visual binary. }\end{array}$

[^2]:    * The published $v \sin i$ 's were drawn from the following sources:

    1. C.T. Elvey, Ap.J., 71, 221, 1930. The two entries in the "Published $v \sin i$ " column are independent estimates by Elvey and by O. Struve, respectively.
    J. L. Greenstein, Ap. J., 117, 269, 1953.
    M. and B. Schwarzschild, AP. J., 112, 248, 1950.
    A. Slettebak, A.J., 58, 228, 1953.
    A. Unsöld and O. Struve, Ap.J., 110, 455, 1949; McDonald Contr., No. 177.
    2. K. O. Wright and E. Van Dien, J.R.A.S.Canada, 43, 15, 1949; Contr. Dom. Ap. Obs. Victoria, No. 17.
[^3]:    ${ }^{1}$ In addition to close binaries, we do not consider in the present discussion peculiar objects with broad lines, such as the T Tauri stars (G. H. Herbig, J.R.A.S. Canada, 46, 222, 1952; Contr. Dom. Ap. Obs. Victoria, No. 27 [part 3]) and HD 117555 (P. W. Merrill, Pub. A.S.P., 60, 382, 1948).

[^4]:    ${ }^{2}$ The remark appended to Table 6 discusses the convention used in computing these means.

