# THE SPECTRA OF THE BRIGHT STARS OF TYPES F5-K5 

Nancy G. Roman<br>Yerkes Observatory<br>Received March 1, 1952


#### Abstract

Spectral types and luminosity classes have been obtained for 641 stars in the spectral range F5-K5 brighter than 5.50 visual magnitude and north of declination $-20^{\circ}$. These types show the well-known absence of subgiants later than K1 and, in addition, show that the stars near zero absolute magnitude become plentiful extremely abruptly between G5 and G8. In the range G0-G5 we have 4 giants; at G8 we have 67 . Color-magnitude diagrams show that this change occurs in a very small range of temperature.

New calibrations of the absolute magnitudes are made for all spectral types and luminosity classes which contain enough stars to yield significant results. For the most part these agree well with older determinations. A surprising result is that the K0 III-K2 III stars are about 0.8 mag. fainter, on the average, than the giants at G8 and in the classes K3-K5. That this is not merely a systematic effect in the classification is shown by the fact that the mean absolute magnitudes for all stars of luminosity classes II-IV show the same phenomenon.

Space velocities corrected for the solar motion have been computed for each star fainter than luminosity class II. In the spectral range G8-K1 it is found that spectroscopic differences exist among stars of the same spectral type and luminosity class. If these stars are separated spectroscopically, it is found that the velocity distributions within the different groups are also different. The two groups which contain 85 per cent of the stars are about equally numerous. They are separated by the fact that the $G$ band and $\lambda 4226$ of CaI are stronger relative to the remainder of the spectrum in one group than they are in the other. The velocity distributions indicate that the group with the stronger G band and $\lambda 4226$ is dynamically related to the group of weak-line stars in the earlier types and that the other group is dynamically related to the strong-line stars. In addition, two other groups exist which are characterized by peculiarities in the cyanogen absorption. One of these has fairly strong cyanogen which is characterized by a peculiar appearance of the region near $\lambda 4150$ and by a strengthening of the absorption in this region compared to that near $\lambda 4120$. Dynamically, these stars cannot be distinguished from the weak-line group. The fourth group is characterized by unusually weak cyanogen absorption. As has been known for some time, these stars are the "high-velocity" stars. Although some members of this group have fairly low velocities and some members of the weak-line group have fairly high ones, the mean velocities of the stars with weak $C N$ is $95 \mathrm{~km} / \mathrm{sec}$, as compared to a mean of $41 \mathrm{~km} / \mathrm{sec}$ for the weak-line group.


## I. INTRODUCTION

As part of a program instigated some years ago by Dr. W. W. Morgan, covering all spectral types, spectra have been obtained of all nonvariable stars brighter than visual magnitude 5.50 , north of declination $-20^{\circ}$, and with Henry Draper spectral types in the range F0 to Ma. The revised types of 693 of these stars are in the interval F5-K5 inclusive. These spectra form an important collection of data for statistical studies of stars in this spectral range, both alone and combined with the large amount of additional data available for these stars. The majority have measured trigonometric parallaxes, all but a few binaries without orbits have published radial velocities, and all the stars have wellobserved proper motions.

Of the 693 stars, 41 probably have composite spectra either because they are unresolved binaries or because they are visual binaries too close to separate on the slithead of the Yerkes 40 -inch spectrograph. These have been omitted from this discussion. In addition, 11 of the stars do not appear to belong anywhere on the normal Hertz-sprung-Russell diagram. These will be discussed individually in the notes to Table 4. For each of the remaining 641 stars a spectral type, luminosity class, spectroscopic parallax and absolute magnitude, and, except for the supergiants, a space velocity have been determined. In addition, new calibrations have been made of the absolute magnitudes in many parts of the spectral type-luminosity class diagram, and the distributions of the stellar speeds have been discussed.

## II. SPECTRAL TYPES

Each of the stars has been classified on the system of the Yerkes spectral atlas, ${ }^{1}$ except that two minor changes in that system have been suggested recently by Dr. Morgan. ${ }^{2}$ The stars of types F5-F8, such as $\beta$ Del and $v$ Peg, which were previously assigned to luminosity class III, have now been assigned to luminosity class IV, and the former class IV stars, such as a CMi, have been included in class IV-V. The reason for this change is the fact that spectra of the stars of the older class III resemble the stars of class V more closely than those of class Ib. The class III stars of types G2-K1 have been reclassified using new criteria and a system of types for the standard stars which provides a better correlation of spectral type with color. Dr. Morgan prepared a new list of standards for the types G8-K1 about a year and a half ago, basing his classification primarily on the appearance of the G-band region and, to a lesser extent, on the strength of $\lambda 4226$ of Ca r. For reasons mentioned below, the present author has also considered the strength of the hydrogen lines as an indicator of spectral type at G8 and K0 after the luminosity class of the star has been accurately determined. The use of this additional criterion does not change the spectral type assigned to any of the standard stars, nor does it lessen the correlation of spectral type with color.
Figure 1 illustrates the correlation between the Henry Draper and the revised spectral types. On the average, the agreement is good. The most notable features are the concentration of the HD G5 stars at G8 on the present system, the widespread and almost uniform distribution of the HD type K0 stars over the revised range G8-K3, and the sparing use of the types F8 and K2 in the Henry Draper Catalogue. Also, the mean revised type for the stars which were classified K2 in this catalogue is almost as late as K4. As mentioned in the preceding paragraph, the colors confirm the revised type G8 for most of the HD G5 stars. The mean color for the G8 giants is very nearly fourfifths of the way from that of the G0 giant to that of the K0 giants, and a smooth progression in color from class V to class II is preserved for each spectral type on the revised system. The relative scarcity of K 1 stars in the revised types is probably a systematic effect in the present classifications, since the decision to use this type was not made until after the preliminary classifications were finished. However, the accuracy possible in the classification seems to warrant the use of this type.

Figure 2 shows the number of stars in each region of the spectral type-luminosity class array as well as the divisions in luminosity used at each spectral type. Two supergiants have been omitted, HR 8752 at G0 I $a$ and $\psi^{1}$ Aur at K5 I $a b$. The supergiants are distributed uniformly in spectral type, and the low-luminosity stars show their expected behavior. The latter are plentiful at F5 and gradually diminish in number toward later spectral types and, hence, toward lower absolute magnitudes. This behavior is due to the selection effect introduced by the bright limiting apparent magnitude. However, other features of the diagram cannot be explained this easily. The most striking of these is the very sudden onset of giants at G8. Even on the older system the onset was fairly sudden at G5 but the new classifications have sharpened the boundary appreciably. Between G0 and G5 we have 4 stars in luminosity class III (i.e., as we shall see later, with absolute magnitudes near 0.0 mag.), while at G8 we have 67 . The strong concentration of giants persists to later spectral types also, thinning out only gradually by K5. The stars in luminosity classes III-IV, II-III, and even II indicate the existence of the same phenomenon. An equally striking feature is the lack of stars fainter than the class III stars and later than K1. This cannot be due solely to selection effect, since the absolute magnitudes of these stars would be no greater than those of the F dwarfs and certainly not sufficiently lower

[^0]than the absolute magnitudes of the stars of the same luminosity class at G8 to account for their complete disappearance at K2.

## III. ABSOLTUTE MAGNITUDES

The existence of good proper motions and trigonometric parallaxes for the stars brighter than 5.5 mag. makes these stars useful for calibrating the luminosity classes in terms of absolute magnitude. For this reason new values of the mean absolute magni-


Fig. 1.-The correlations between the HD spectral type and the types on the system of the Yerkes spectral atlas. The area of each block represents the number of stars at that point on the diagram.
tudes have been determined for those classes which contain a sufficient number of stars brighter than this limit to make the new calibration useful.

For stars with appreciable trigonometric parallaxes, i.e., for stars in luminosity classes with mean absolute magnitudes fainter than -0.5 mag., the mean trigonometric parallax was computed for each group. For each star with more than one determination of its trigonometric parallax, individual values from Allegheny, Cape, Greenwich, McCormick, and Yale Observatories were averaged with equal weight, unless the probable
errors of the individual determinations differed considerably. These values were taken from the back of the General Catalogue of Stellar Parallaxes (Yale, 1935). The resulting value was then reduced to the parallax which the star would have if it had the apparent magnitude 5.00 instead of its actual apparent magnitude. Negative parallaxes were divided by the same factor by which they would have had to be multiplied if they had been positive. These values were then averaged, weighting the value for each star according to the number of independent determinations. Although the parallaxes of most of the stars are too small to be of any use individually, the agreement among the reduced parallaxes is surprisingly good. If anything, the mean errors given in Table 1, which


Fig. 2.-The spectral type-luminosity class array for the bright northern stars. Each circle represents one star. The lines indicate the number of types usually distinguished. Circles centered on a line indicate stars with in-between types.
have been computed on the assumption that one good determination of a trignonometric parallax has a mean error of 0 ". 010 , is overestimated. After this work had been completed, Dr. Strömgren pointed out ${ }^{3}$ that it would be preferable to use the observed parallaxes directly. If an estimate is made of the mean absolute magnitude of a group of stars and is used to compute spectroscopic parallaxes, then a comparison of the mean unreduced trigonometric and the mean spectroscopic parallaxes will indicate the correction which must be applied to the assumed absolute magnitude. For three groups in different parts of the spectral type-luminosity diagram, this method was used. The results agreed with the first results within the mean errors of the determinations.

For groups with mean absolute magnitudes brighter than +3.0 the mean parallax was also computed from the proper motions. The observed motion for each star was also reduced to the value it would have if the star were actually of apparent magnitude 5.00. The sky north of declination $-20^{\circ}$ was divided into nine regions of approximately equal

[^1]TABLE 1
Mean Parallaxes

| Spectral Type | Method | Num- <br> ber of <br> Stars | $\bar{\pi}(m=5.00)$ |  | $10+5 \log \bar{\pi}$ |  | Adopted $\bar{M}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| F5 IV-F8 IV. | $\pi_{t r}$ | 14 | $0^{\prime \prime} .0227 \pm 0.00018 \text { m.e. }$ |  | $+1.8 \pm 0.2$ m.e. $\}$+2.3 .2 |  | +1.9 |
| F5 IV-F8 IV. | $\mu$ | 19 |  |  |  |  |  |
| F5 IV-V-G2 IV-V | $\mu$ | 26 | . 0357 . 0025 |  | $\begin{array}{ll}+2.8 & .2 \\ +3.0 & .1\end{array}$ |  | $\begin{aligned} & +2.8 \\ & +2.9^{*} \end{aligned}$ |
| F5 IV-V-F6 IV-V. | $\bar{\pi}_{t r}$ | 15 | . 0390 | . 0020 |  |  |  |
| F8 IV-V; G0 IV-G2 IV | $\bar{\pi}_{t r}$ | 9 | . 0421 | . 0023 | +3.1 | . 1 |  |
| F5 V. | $\bar{\pi}_{t r}$ | 13 |  | . 0020 | +3.3 . 1 |  | +3.3+3.6 |
| F6 V | $\frac{\bar{\pi}_{t r}}{\bar{\pi}_{t r}}$ | 15 | . 0554.0021 |  | +3.7 . 1 |  |  |
| F8 V. |  | 17 | . 0546 | . 0016 | +3.7 | . 1 | +3.6 +3.9 |
| G0 V-G2 V. | $\bar{\pi}_{t r}$ | 19 | . 0786 | . 0016 | +4.5 . 0 |  | +4.4* |
| G5 II-K5 II. | $\bar{\mu}$ | 34 | . 0032 | . 0005 | -2.5 . 3 |  | $-2.6$ |
| G8, K0 II-III | $\mu$ | 914 | $\begin{aligned} & .0069 \\ & .0066 \end{aligned}$ | $.0015$ | -0.8 . 5 |  | $\begin{aligned} & -0.9^{*} \\ & -0.9^{*} \end{aligned}$ |
| K1 II-III-K5 II-III |  |  |  | $.0018$ | -0.8 | . 6 |  |
| G8 III. | $\underline{\mu}$ | 65 | . 0088 | . 0010 | -0.2 1.2 |  | 0.0 |
| G8 III. | $\stackrel{\nu}{v}_{\bar{\pi}}^{\text {m }}$ | 65 | . 0057 | $\begin{aligned} & .003: \\ & .0012 \end{aligned}$ | $\left.\begin{array}{rr}-1.1 & . . \\ +0.3 & .2\end{array}\right\}$ |  |  |
| G8 III. |  | 49 | . 0114 |  |  |  |  |
| K0 III. | $\underline{\mu}$ | 86 | . 0162 | . 0014 | +1.0 |  | +0.7 |
| K0 III. | $\bar{\pi}_{t r}$ | 71 | . 0136 | . 0010 | +0.7 |  |  |
| K1 III. | $\stackrel{\mu}{\bar{\pi}}_{\text {tr }}$ | 3222 | $\begin{aligned} & .0148 \\ & .0155 \end{aligned}$ | $.0009$ | $\left.\begin{array}{ll}+0.9 & 1 \\ +1.0\end{array}\right\}$ |  | +0.8 |
| K1 III. |  |  |  | $.0017$ | +1.0 | . 2$\}$ |  |
| K2 III | $\mu$ | 61 | . 0147 | . 0015 | +0.8 . 2$\}$ |  | +0.9 |
| K2 III | $\widetilde{\pi}_{t r}$ | 46 | . 0166 | . 0012 | +1.1 | . 25 |  |
| K3 III. | $\overline{\bar{\mu}}_{\bar{\mu}}^{\text {er }}$ | 59 | .0114.0106 | $\begin{aligned} & .0016 \\ & .0012 \end{aligned}$ | +0.3 . 3$\}$ |  | +0.1 |
| K3 III. |  | 42 |  |  | +0.1 | . 2 \} |  |
| K4 III. | $\bar{\pi}_{t r}$ | 31 | .0098.0106 | $\begin{aligned} & .0019 \\ & .0015 \end{aligned}$ | +0.0 0.4$\}$ |  | -0.1 |
| K4 III. |  | 25 |  |  | +0.1 | . 35 |  |
| K5 III | $\bar{\pi}_{t r}$ | 3126 | .0090.0095 | $\begin{aligned} & .0007 \\ & .0016 \end{aligned}$ | -0.2 . 2 \} |  | -0.2 |
| K5 III. |  |  |  |  | -0.1 |  |  |
| G5-K0 III-IV. | $\overline{\bar{\mu}}_{\bar{\pi}_{t r}}$ | 2219 | $\begin{aligned} & .0193 \\ & .0187 \end{aligned}$ | $\begin{array}{r} .0029 \\ .0019 \end{array}$ | $\left.\begin{array}{ll}+1.4 & .3 \\ +1.4 & .2\end{array}\right\}$ |  | +1.3* |
| G5-K1 III-IV. |  |  |  |  |  |  |  |
| G5-K0 IV. | $\bar{\pi}_{t r}$ | 6 | . 0526 | . 0044 | +3.6 . 2 |  | +3.5* |
| K1 IV. | $\bar{\pi}_{t r}$ | 3 | 0.038 | 0.004 | +2.9 0.2 |  | +2.9 |

* Individual mean absolute magnitudes were adopted as shown below.

| F8 IV-V.......... +3.0 | G8 II-III. . . . . . . . . . . . . 1.0 | K1 III-IV........ +1.3 |
| :---: | :---: | :---: |
| G0 IV. . . . . . . . . . . +2.6 | K0 II-III-K2 II-III . . . . . -0.8 | G5 IV . . . . . . . . . ${ }^{\text {a }}$ + 3.2 |
| G2 IV.............. +2.9 | K3 II-III-K5 II-III . . . . . -1.0 | G8 IV. . . . . . . . . . . +3.5 |
| G0 V............. +4.3 | G8 III-IV.............. +1.3 | K0 IV. . . . . . . . . . +3.5 |
| G2 V............. +4.6 | K0 III-IV............... . +1.4 | K1 IV. . . . . . . . . . . +2.9 |

area, and the mean proper motion was determined in each region. These mean motions were then used to compute mean parallaxes according to the formulae given by Smart. ${ }^{4}$ These formulae involve the assumptions that the two-stream picture of stellar motions is valid and that there are an equal number of stars in each stream. In addition, the amount of the solar motion and the stream constants are required for their application. A solar motion of $20 \mathrm{~km} / \mathrm{sec}$ was adopted. ${ }^{5}$ For the stream constants the values found by Smart and Tannahill ${ }^{6}$ in their study of the Cape proper motions were used. These formulae have the advantage that they make use of the total proper motion rather than just one component of this motion. As the observational errors in the proper motions are relatively small, each star was given equal weight in the solution. The mean error of the results is computed from the agreement of the results from individual regions of the sky.

The results of the solutions for the mean parallaxes are given in Table 1. In this table, $\pi$ denotes parallax; $\mu$, the total proper motion; $v$, the component of the proper motion parallel to the solar motion; $m$, the visual apparent magnitude of a star; and $M$, the visual absolute magnitude of a star. It is evident that where the two methods of determining the mean parallax overlap the agreement between them is good. This table also gives the absolute magnitudes, found by assuming that all stars in each group have the same absolute magnitude, together with the approximate mean error of these values as indicated by the mean errors of the mean parallaxes. To obtain the true mean absolute magnitude, the correction $0.23 \sigma_{M}^{2}$ must be applied where $\sigma_{M}$ is the standard deviation of the absolute magnitudes of the stars in the group. It was estimated that this correction is about +0.1 mag., except for the dwarfs earlier than G0 for which the correction was ignored. This correction has been included in the adopted visual absolute magnitudes given in the final column of Table 1. A few values in this column, for the F stars and the class II-III stars in the range G8-K5, have been smoothed somewhat.

Figure 3 shows a plot of the adopted visual absolute magnitudes in this region of the H-R diagram. The points connected by dotted lines are from an article by Keenan and Morgan. ${ }^{7}$ The remainder are from the new solutions. Of particular note is the sharp drop in absolute magnitude for the giants between G8 and K0, followed by the equally steep rise between K2 and K3. The results in Table 1 leave little doubt that this behavior is real. In addition, the second method of employing the trigonometric parallaxes mentioned above also supports the sharp drop between G8 and K0. Finally, at G8, an additional solution was made, using the upsilon components of the proper motion. This solution has decidedly less weight than that using the total proper motions, both because of the loss of one component of the motion and because of the varying weights in different parts of the sky and, hence, the low weight in some regions. However, it supports the high luminosity at G8 III. The point at K1 IV is uncertain, but it is definitely above the point for K0 IV.

Table 2 gives the mean absolute magnitude for each spectral type for all luminosity classes except class I and, for stars later than the sun, class V. The stars omitted are too few to have much real influence on the mean, but they lie far enough from the mean to cause spurious fluctuations from one spectral type to the next. Although these mean absolute magnitudes refer only to the stars in this study and may not be valid for other groups of stars, such as those in a particular galactic latitude or with fainter apparent magnitudes, they do illustrate the characteristics of this material. The mean absolute magnitudes for the stars earlier than G5 behave as one would expect. Among the latertype stars the same behavior can be noted as was found in the giants of these classes.

[^2]Hence this behavior is not a product of the classification system. If we omit the dwarfs, the K $0-\mathrm{K} 2$ stars are definitely fainter as a group than are those stars either at G8 or later than K2.
The data shown in Figures 2 and 3 are combined in Figure 4, which illustrates a schematic color-magnitude diagram for the stars included in this study. The mean color for each spectral type and luminosity class was determined from the $B-V$ colors measured by H. L. Johnson. ${ }^{8}$ The area of the color-magnitude diagram was then divided


Fig. 3.-Mean absolute magnitudes for stars in the range F5-K5. Roman numerals indicate the main luminosity classes. The remaining lines are for luminosity classes II-III, III-IV, and IV-V. The dotted lines connect values given by Keenan and Morgan. The remaining points are based on new results.

TABLE 2
Mean Absolute Magnitudes to Limiting Magnitude 5.50 for Mixed Luminosity Classes

| Spectral Type | $\bar{M}$ | Spectral Type | $\bar{M}$ |
| :---: | :---: | :---: | :---: |
| Classes II-V: |  | Classes II-IV: |  |
| F5 | +2.2 | G5. | $+0.7$ |
| F6. | +3.0 | G8. | +0.1 |
| F8. | +3.5 | K0. | +0.6 |
| G0. | +3.2 | K1 | +0.6 |
| G2 | +2.1 | K2 | +0.5 |
|  |  | K3 | -0.3 |
|  |  | K4. | -0.4 |
|  |  | K5 | -0.3 |

${ }^{8} A p . J$. (in press).
into cells, each centered on the mean $B-V$ and mean absolute magnitude, on the HRP system, for the stars in a given cell in the spectral type-luminosity class diagram and with the boundaries approximately midway between adjacent centers. In each of the cells constructed in this way, a circle was drawn for each star found to have the corresponding spectral type and luminosity class. Hence no circle on the diagram represents a particular star, but the result should be similar to that which we would obtain if we knew the color and absolute magnitude for each star individually. However, the width of the giant sequence for the late-type stars is indeterminate. Figure 4, again, shows the same features


Fig. 4.-A schematic color-magnitude diagram for the bright northern stars. Each circle represents one star, but not a particular star.
as Figure 2. Stars with absolute magnitudes greater than +2.0 are entirely absent for colors greater than 1.4 mag., and stars with absolute magnitudes between -1.0 and +1.0 are scarce for colors between 0.45 and 0.82 mag . On this diagram the spectra merely form an intermediate step in obtaining the position of a given star. Hence the sharp onset for the late-type giants is probably real. If it is not real, then the giants are even more crowded at the color 0.85 or 0.86 mag., since the mean color of the stars cannot be changed appreciably.
The general features shown in Figure 4 are not new. In 1913 H. N. Russell made the statement: "It is further noteworthy that all the stars of classes K 5 and M which appear on our diagram are either very bright or very faint. There are none comparable with the

Sun in brightness." ${ }^{\prime 9}$ In 1922 H. D. Curtis ${ }^{10}$ published an H-R diagram, based on all parallaxes available at the time and on the HD spectral types, which is surprisingly similar to the color-magnitude diagram shown in Figure 4. In the same year Hertzsprung ${ }^{11}$ called attention to the fact that, if the quantity $m+5 \log \mu$, where $m$ is the apparent magnitude and $\mu$ is the total proper motion, is plotted against the reciprocal color temperature, then, for stars about 5 mag. brighter than the sun, there is a "marked gap" on the diagram between the red stars and the blue stars. Comparing his diagram with his table of the colors corresponding to each spectral type, we see that the gap is between stars of spectral type A5 and stars slightly later than G2 on the HD system. During the succeeding thirty years the edges of this gap have tended to become less well defined in the literature, and the red edge of the gap has progressed steadily toward the violet, until some modern authors have placed this edge near F5 or even earlier. Further evidence that the giants actually start abruptly near G8 is furnished in Figure 5, which shows two diagrams similar to Figure 4 but derived from independent sets of data. Figure $5 a$ is a plot of the colors measured by Bottlinger ${ }^{12}$ against the absolute magnitudes computed from the trigonometric parallaxes. Figure $5 b$ is a plot of the infrared colors measured by J. S. Hall ${ }^{13}$ against the absolute magnitudes which the stars would have if each had a tangential motion of $20 \mathrm{~km} / \mathrm{sec}$. That is, $P=m_{v}+5$ $\log \mu+1.87$. Both figures contain all the stars plotted in Figure 4 for which the necessary data are available, and the mean colors of G0 V and G8 III stars have been indicated on each. Since these diagrams are very similar to Figure 4, we may conclude that the Hertzsprung gap extends through G5 and has a very sharp boundary at a temperature between that of a G5 giant and a G8 giant.

## IV. VELOCITY DISTRIBUTIONS

Nearly two years ago it was shown that among the late F- and early G-type stars two groups of stars could be distinguished in the same spectral type and luminosity class by small spectroscopic differences. ${ }^{14}$ It was also shown that the members of these two groups, which occur in nearly equal numbers among the bright northern stars, have different velocity distributions. The stars in one of these groups have systematically weaker lines than those in the other group, and the two groups have been identified accordingly as the strong-line and the weak-line stars. $\beta$ Vir is representative of the strongline group, and $\iota$ Psc of the weak-line group.

In the course of classifying the remainder of the stars, it was found that spectroscopic differences also exist among stars of the same luminosity class and spectral type in the range G8-K1. Eighty-five per cent of these stars belong to one of two groups. In one of these, both the G band and $C a$ I 4226 are stronger than in stars of the same type in the other group. The two K0 III stars, HR 4126 and 2 Dra, are examples of the members of each group, and the differences between these stars are typical. Relative to the strength of Fe r 4045, $\lambda 4226$ is stronger in the spectrum of 2 Dra than it is in the spectrum of HR 4126. This alone might be explained if 2 Dra were later in type or lower in luminosity. However, the G band is also stronger in 2 Dra, and this would indicate an earlier type; the strength of the cyanogen and the ratio of $\lambda 4077$ to $\lambda 4063$ indicate that 2 Dra cannot be appreciably fainter than HR 4126. Figure 6 illustrates the velocity distributions for the stars in the two groups together with the velocity distributions

[^3]

Fig. 5.-Color-magnitude diagrams for the bright northern stars: $a$, a plot of the visual absolute magnitudes determined from trigonometric parallaxes and the colors measured by Bottlinger; $b$, a plot of visual magnitudes determined from hypothetical parallaxes (i.e., the assumption that each star has a tangential velocity of $20 \mathrm{~km} / \mathrm{sec}$ ) and the colors measured by Hall.
for the strong- and weak-line groups in the earlier types for comparison. (Thirty-seven stars have been added to the diagrams shown in the earlier paper.) Table 3 contains, for each group, the number of stars, the mean velocity, and the standard deviation of the velocities. These show that one group of the late-type stars can be identified dynamically with the strong-line group in the earlier stars and the other with the weak-line group. For this reason, although the names are no longer descriptive, the group of stars resembling HR 4126, which appears similar dynamically to the strong-line stars of earlier type,


Fig. 6.-The frequency distributions of the speeds in the strong- and weak-line groups in the spectral ranges F5-G5 and G8-K1.
has been called the strong-line group and the group of stars resembling 2 Dra has been called the weak-line group.

The remaining 15 per cent of the stars of types G8-K1 appear to belong to neither of these groups spectroscopically but to one of the groups represented by the K0 III stars illustrated in Figure 7. Stars in these groups seem to share the characteristics of the weakline group to the extent that the G band and $\lambda 4226$ tend to be strong compared with the remainder of the spectrum, but, in addition, the $C N$ band is peculiar. In stars like


Fig. 7.-Two K0 III stars with peculiar $C N$. HR 645 belongs to the 4150 group. $\phi^{2}$ Ori belongs to the group with weak $C N$. Both stars are high-velocity stars, and the two must be fairly similar in temperature and luminosity.

HR 645, not only is the absorption in the region between $\lambda 4145$ and $\lambda 4175$ stronger than in the region between $\lambda 4175$ and $\lambda 4215$, but also the appearance is different. Similar stars have been found on objective-prism plates at the Case Observatory by Dr. Nassau and his associates. They are recognized on low dispersion by the fact that the $\lambda 4150$ region of $C N$ is too strong compared with the region more to the red. Hence they have been called " 4150 stars." In addition, the entire $C N$ band appears too strong for the strength of the hydrogen lines and of $\lambda 4077$. On the other hand, in stars like $\phi^{2}$ Ori, the

TABLE 3
Characteristics of the Velocity Distributions

| Group | Number of Stars | $\begin{gathered} \text { Mean Speed } \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | Standard <br> Deviation <br> (Km/Sec) |
| :---: | :---: | :---: | :---: |
| Strong-line Weak-line. | F5-G5 (except G2 and G5 III and IV) |  |  |
|  | 70 | $28.4 \pm 1.7$ | 14.5 |
|  | 61 | $42.7 \pm 2.8$ | 22.2 |
|  | G5-K1, II-III to IV |  |  |
| Strong-line. | 91 | $24.7 \pm 1.3$ | 12.6 |
| Weak-line: | 113 | $40.9 \pm 2.3$ | 24.1 |
| 4150. | 25 | $42.1 \pm 8.3$ | 41.6 |
| Weak CN | 12 | $95.6 \pm 13.7$ | 47.4 |



Fig. 8.-The frequency distributions of the speeds of the 4150 stars and of the stars with weak $C N$
$C N$ is too weak for the strength of $\lambda 4077$ and for the luminosities indicated by trigonometric parallaxes.
Table 3 also gives the characteristics of the velocity distributions for these groups of stars, and Figure 8 illustrates these distributions. It is seen that the velocity distribution for the 4150 stars is similar to that for the weak-line stars, although spectroscopically they form a distinct group. The dispersion is higher, but for such a small number of stars this difference may not be significant. On the other hand, the stars with weak $C N$ definitely form a separate group dynamically. The mean velocity is decidedly higher than that for the other groups, and the distribution of the velocities also appears differ-
ent, although it should be remembered that Figure 8 contains very few stars. This is definitely a high-velocity group of stars, and it has been recognized for some time both in globular clusters ${ }^{15}$ and among the high-velocity stars. ${ }^{1}$ More recently, both stars in globular clusters and the high-velocity stars have been recognized as objects belonging to Baade's population II, and the weak $C N$ has been identified as a characteristic of this population. ${ }^{16}$ It should be noted, however, not only that some members of this group have velocities lower than the $63 \mathrm{~km} / \mathrm{sec}$ limit but also that stars in the weak-line and in the 4150 groups have velocities which are above this limit. For example, the velocity of HR 645 is $143 \mathrm{~km} / \mathrm{sec}$.
Spectroscopic differences exist also among stars later than K1. The 4150 stars seem to be fairly numerous at K2, and the stars with weak $C N$ are also certainly present at this type (for example, a Boo).

Several lines of evidence support the above conclusions. The addition of 37 stars to the 98 previously discussed with spectral types in the range F5-G5 has had no appreciable effect on the velocity characteristics of the strong- and weak-line groups. Among the later-type stars, the velocity characteristics of each group show clearly in each spectral type separately. Hence the divisions are almost certainly real. Throughout the region of the $\mathrm{H}-\mathrm{R}$ diagram included in this investigation, the mean reduced trigonometric parallaxes for the strong- and weak-line stars of the same spectroscopic absolute magnitude agree within their mean errors. In addition, in each group, the mean radial velocity agrees with the mean velocity from one component of the tangential motion in both the earlier and later spectral types. Thus the higher mean velocities for some groups cannot result from the use of values of the spectroscopic absolute magnitudes which are too high for these groups. The galactic concentration tells us nothing: all the stars seem to be fairly uniformly distributed in a direction perpendicular to the galactic plane up to the relatively small distances reached in this investigation.

Table 4 lists the stars brighter than 5.50 mag., north of declination $-20^{\circ}$, with revised spectral types between F5 and K5, with the exception of variable stars, stars with composite spectra, and stars in three lists which have been published recently. ${ }^{14,17}$ The table includes the name or HR number of each star, its 1900 position, the visual apparent magnitude corrected for the light of the fainter component in close visual double stars and two-line spectroscopic binaries, the spectral type, the spectroscopic parallax and absolute magnitude, the group (strong-line, weak-line, 4150 , or weak $C N$ ) to which the star belongs, and its space velocity corrected for the usual solar motion of $20 \mathrm{~km} / \mathrm{sec}$ toward $a=18^{\mathrm{h}} 04^{\mathrm{m}}$ and $\delta=+28^{\circ}$. The abbreviations "st-l," "wk-1," and "wk CN" stand for "strong-line," "weak-line," and "weak $C N$," respectively; an " $n$ " at the end of a line indicates a note on that star at the end of the table. The remaining symbols have their usual meanings.

I am indebted to Dr. W. W. Morgan not only for the use of a large number of plates but also for many helpful discussions and for lists of revised spectral types for the standard stars.

[^4]Spectroscopic Results

| Name |  | 8 | m | $\begin{gathered} \text { Spoctral } \\ \text { Type } \end{gathered}$ | M | Group | \% ${ }^{\text {sp }}$ | $\begin{gathered} \text { Speed } \\ (\mathrm{Km} / \mathrm{Sec} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 33 Psc | $0^{\mathrm{h}} 0^{\mathrm{m}}$ 2 | $-6^{\circ} 161$ | 4.68 | KI III | +0.8 | 4150 | 0.017 | 40 |
| 6 Cot | 06.2 | -16 1 | 5.05 | F6 ${ }^{\text {V }}$ | +3.6 | wk-1 | . 051 | 52 |
| HR 37 | 07.1 | -1830 | 5.47 | 15 III | -0.2 |  | . 0073 | 26 |
| $\bigcirc$ Cet | 014.3 | - 923 | 3.75 | L2 III | +0.9 |  | . 027 | 26 |
| 13 Cet | 030.1 | -49 | 5.75 | F8 ${ }^{\text {P }}$ | +3.9 | wk-1 | . 043 | 32 |
| HR 152 | 051.3 | +4356 | 5.44 | L5 III | -0.2 |  | . 0074 | 50 |
| $\epsilon$ and | 033.3 | +2846 | 4.52 | G8 III | +0.0 | we CN | . 0125 | 156 |
| 8 and | 034.0 | +30 19 | 3.49 | K3 III* | +0.1 |  | . 021 | 18 |
| a Cas | 034.8 | +5559 | 2.47 | S0 II-III | -0.8 | st-1 | . 022 | 6 |
| 32 and | 035.7 | +3855 | 5.42 | G8 III | ,0.0 | st-1 | . 0082 | 22 |
| $\beta$ cet | 038.5 | -18 32 | 2.24 | K0 III | +0.7 | st-1 | . 049 | 15 |
| $\phi^{\prime}$ Cet | 039.2 | -11 9 | 4.93 | KO III | +0.7 | st-1 | . 014 | 34 |
| \% and | 042.0 | +23 43 | 4.30 | K1 II | -2.6 |  | . 0042 |  |
| 8 Psc | 043.5 | +72 | 4.55 | K5 III | -0.2 |  | . 011 | 39 |
| 64 Psc | 043.7 | +1624 | 5.23 | F8 ${ }^{\text {V }}$ | + 3.9 | st-1 | . 054 | 19 |
| $v^{\prime}$ Cas | 049.1 | +5826 | 4.95 | L2 III | +0.9 |  | . 0155 | 32 |
| $\nu^{2}$ Cas | 050.7 | +58 38 | 4.83 | 68 III-IV | +1.5 | wk-1 | . 020 | 56 |
| $\phi^{3} \mathrm{Cet}$ | 051.0 | -11 49 | 5.49 | K4 III | -0.1 |  | . 0076 | 42 |
| $\eta$ And | 051.9 | +22 53 | 4.62 | G8 III-IV | +1.3 | st-1 | . 022 | 24 |
| HR 285 | 055.0 | +8543 | 4.52 | K2 II-III | -0.8 |  | . 0886 | 34 |
| Psc | 057.8 | + 721 | 4.45 | K0 III. | +0.7 | wic-1 | . 018 | 41 |
| $\mu \mathrm{Cas}$ | 11.6 | +5426 | 5.26 | G5 Vp* |  |  |  |  |
| $\eta$ Cet | 13.6 | $-1043$ | 3.60 | K2 III | +0.9 |  | . 029 | 27 |
| $\chi \mathrm{Psc}$ | 16.1 | +2030 | 4.89 | KO III | +0.7 | st-1 | . 0145 | 17 |
| $\tau$ Psc | 16.2 | +29 34 | 4.70 | KO III-IV | +1.4 | st-1 | . 022 | 31 |
| $\phi$ Psc | 18.3 | +24 3 | 4.64 | K0 III | +0.7 | st-1 | . 016 | 12 |
| $\xi$ and | 116.5 | +450 | 4.99 | Ko III-IV | +1.4 | st-1 | . 019 | 17 |
| $\psi^{4}$ Cas | 118.9 | +6736 | 4.96 | KO III | +0.7 | 4150 | . 014 | 20 |
| $\theta$ Cot | 119.0 | -842 | 3.83 | K0 III | +0.7 | -k-1 | . 024 | 48 |
| 46 Cot | 120.7 | -15 7 | 5.19 | K3 III | +0.1 |  | . 0095 | 51 |
| 49 and | 124.1 | +4630 | 5.38 | K0 III | +0.7 | 4150 | . 011 | 17 |
| $\mu \mathrm{Psc}$ | 124.9 | + 538 | 5.12 | L4 III | -0.1 |  | . 0090 | 144 |
| $\eta \mathrm{Psc}$ | 126.1 | +1450 | 3.72 | G8 III* | 0.0 | st-1 | . 018 | 16 |
| $X$ Сав | 127.4 | +5843 | 4.83 | KO III | +0.7 | mk-1 | . 0145 | 30 |
| 40 Cas | 130.5 | +7232 | 5.50 | G8 II-III | -1.0 | wk-1 | . 060 | 25 |
| 50 Cet | 151.1 | -15 54 | 5.48 | K2 III | +0.9 |  | . 012 | 22 |
| 51 And | 151.9 | +48 7 | 3.77 | [3 III* | +0.1 |  | . 019 | 26 |
| $X$ and | 138.4 | +4352 | 5.17 | G8 III | 0.0 | wk-1 | . 0092 | 32 |
| HR 485 | 135.7 | +42 7 | 5.10 | G2 ${ }^{\text {b }}$ | +4.6 | st-1 | . 079 | 32 |
| $\nu \mathrm{Psc}$ | 136.2 | + 459 | 4.68 | E3 III | +0.1 |  | . 012 | 26 |
| 107 Psc | 137.1 | +19 47 | 5.32 | K1 ${ }^{\text {* }}$ | +6.2 |  | . 151 | 46 |
| HR 500 | 137.7 | -412 | 5.27 | K3 II-III | -1.0 |  | . 0056 | 48 |
| $\tau$ Cet | 139.4 | -16 28 | 3.65 | G8 ${ }^{\text {* }}$ | +5.6 |  | . 245 | 60 |
| - Psc | 140.1 | + 839 | 4.50 | KO III | +0.7 | st-1 | . 017 | 26 |
| 5 Cet | 146.5 | -10 50 | 3.92 | K2 III | +0.9 |  | . 025 | 9 |
| a Tri | 147.4 | +29 6 | 3.58 | F5 IV* | +1.9 | wik-1 | . 046 | 24 |
| $\xi$ Psc | 148.4 | + 242 | 4.84 | K0 III | +0.7 | nk-1 | . 015 | 30 |
| 6 Ari | 151.9 | +1720 | 5.16 | K1 p |  |  |  |  |
| 49 cas | 156.0 | +75 38 | 5.30 | G8 III | 0.0 | mk-1 | . 0086 | 26 |
| $\gamma$ and $A$ | 157.3 | +4151 | 2.28 | K2 III | +0.9 |  | . 053 | 18 |
| $\alpha$ Ari | 21.5 | +22 59 | 2.25 | K2 III* | +0.9 |  | . 054 | 18 |
| 60 and | 27.0 | +4346 | 5.08 | K4 III | -0.1 |  | . 0092 | 52 |
| HR 645 | 27.0 | +50 36 | 5.40 | KO III | +0.7 | 4150 | . 0115 | 143 |
| $\eta$ Ari | 27.2 | +20 44 | 5.35 | P5 ${ }^{\text {P }}$ | +3.3 | st-1 | . 039 | 13 |
| $\xi^{\prime}$ cet | 27.7 | + 823 | 4.54 | G8 II | -2.5 |  | . 0038 |  |
| 64 and | 217.3 | +4933 | 5.49 | G8 III | 0.0 | st-1 | . 0080 | 16 |
| 65 and | 218.9 | +4950 | 4.96 | K4 III | -0.2 |  | . 010 | 7 |
| 14 Tri | 226.0 | + 3542 | 5.35 | K5 III | -0.2 |  | . 0077 | 48 |
| HR 737 | 226.3 | +150 | 5.44 | K3 III | +0.1 |  | . 0085 | 17 |
| HR 743 | 228.5 | +7223 | 5.34 | G8 III | 0.0 | wk-1 | . 0085 | 37 |

Table 4 (continued)

| Name | $a$ | 8 | III | Spectral Type | M | Group | Tsp | $\begin{gathered} \text { Speed } \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\nu$ Cet | $2^{\mathrm{h}_{3}}{ }^{\text {ma }} 6$ | + $5^{\circ} 91$ | 5.02 | G8 III | 0.0 | st-1 | 080099 | 28 |
| $\epsilon$ Cet | 234.7 | -12 18 | 5.01 | F5 IV-V | +2.8 | Wk-1 | . 936 | 25 |
| 39 Ari | 242.0 | +2850 | 4.62 | K1 III | +0.8 | st-1 | . 017 | 42 |
| 17 Per | 245.4 | +34 39 | 4.67 | K5 III | -0.2 |  | . 0105 | 19 |
| 20 Per | 247.4 | +57 56 | 5.32 | F4 V | +3.3 |  | . 039 | 9 |
| $\eta$ Eri | 251.5 | - 918 | 4.05 | K1 III-IV | +1.3 | wik-1 | . 028 | 44 |
| 24 Per | 252.9 | +34 47 | 4.97 | K2 III | +0.9 |  | . 0155 | 51 |
| HR 918 | 258.0 | +5619 | 5.08 | KO II-III | -0.8 | wk-1 | . 0066 | 83 |
| $\boldsymbol{k}$ Per | 32.7 | +44 29 | 4.00 | KO III | +0.7 | wk-1 | . 022 | 42 |
| $\omega$ Per | 34.8 | +39 14 | 4.82 | K1 III | +0.8 | st-1 | . 016 | 24 |
| $\delta$ Ari | $3 \quad 5.9$ | +19 21 | 4.53 | K2 III | +0.9 |  | . 019 | 32 |
| 94 Cet | 37.7 | - 134 | 5.14 | F8 V | +3.9 | st-1 | . 057 | 8 |
| HR 969 | 39.1 | +50 34 | 5.29 | G5 II | -2.3 |  | . 0030 |  |
| HR 991 | 312.5 | +33 51 | 4.92 | K2 II | -2.6 |  | . 0031 |  |
| HR 999 | 314.3 | +28 41 | 4.72 | K3 II-III | -1.0 |  | . 0072 | 15 |
| 63 Ari | 317.0 | +20 23 | 5.25 | K3 III | +0.1 |  | . 0093 | 32 |
| - Tau | 319.4 | + 841 | 3.80 | G8 III* | 0.0 | st-1 | . 017 | 45 |
| $\sigma$ Per | 323.6 | +4739 | 4.55 | K3 III | +0.1 |  | . 013 | 29 |
| 5 Tau | 325.4 | +1236 | 4.28 | KO II-III | -0.8 | st-1. | . 8095 | 13 |
| 36 Per | 325.5 | +4543 | 5.35 | F4 III* | +0.2 |  | . 0093 | 63 |
| $\delta$ Eri | 388.5 | -10 6 | 3.72 | KO IV* | +3.5 | wik-1 | . 091 | 53 |
| 32 Eri A | 349.3 | - 315 | 4.95 | G8 III | 0.0 | st-1 | . 010 | 17 |
| HR 1249 | 357.5 | -0 33 | 5.42 | F6 V | +3.6 | st-1 | . 043 | 19 |
| 57 Tau | 358.3 | +21 49 | 4.50 | KO III | +0.9 | st-1 | . 019 | 13 |
| HR 1257 | 358.9 | $+233$ | 5.39 | F6 IV | +1.9 | wk-1 | . 020 | 46 |
| 39 Eri | 49.5 | -10 30 | 5.13 | K3 III | +0.1 |  | . 0098 | 74 |
| HR 1327 | 411.3 | +64 54 | 5.40 | G5 III | 0.0 | wk-1 | . 0082 | 35 |
| 54 Per | 413.9 | +3420 | 5.10 | G8 III | 0.0 | 4150 | . 0095 | 41 |
| $\gamma$ Tau | 414.1 | +15 23 | 3.36 | KO III* | +0.7 | st-1 | . 023 | 30 |
| ¢ Tau | 414.2 | +27 7 | 5.06 | K1 III | +0.8 | wk-1 | . 014 | 20 |
| 8 Tau | 417.2 | +1718 | 3.93 | KO III* | +0.7 | st-1 | . 023 | 31 |
| HR 1390 | 419.7 | +31 13 | 5.33 | K1 III | +0.8 | wik-1 | . 012 | 42 |
| T Tau | 421.0 | +1429 | 4.94 | G8 III | 0.0 | st-1 | . 010 | 20 |
| 75 Tau | 422.7 | +168 | 5.29 | K2 III | +0.9 |  | . 013 | 25 |
| $\boldsymbol{\epsilon}$ Tau | 422.8 | +1858 | 3.63 | KO III* | +0.7 | wk-1 | . 026 | 31 |
| $\theta^{\prime}$ Tau | 422.9 | +15 44 | 4.04 | KO III* | +0.7 | st-1 | . 022 | 32 |
| 45 Eri | 426.8 | - 016 | 4.97 | K3 II-III | -1.0 |  | . 0064 | 6 |
| HR 1452 | 429.4 | -911 | 5.50 | K4 II-III | -1.0 |  | . 0050 | 116 |
| a Tau | 430.2 | +1619 | 1.06 | K5 III* | -0.2 |  | . 056 | 41 |
| 3 Can | 432.0 | +5253 | 5.31 | KO III | -0.7 | st-1 | . 012 | 44 |
| 53 Eri | 433.5 | -1430 | 3.98 | K2 III | -0.9 |  | . 024 | 41 |
| HR 1523 | 441.6 | +81 2 | 5.32 | K3 III | +0.1 |  | . 0090 | 32 |
| HR 1533 | 443.2 | +3719 | 5.10 | K4 II | -2.6 |  | . 0029 |  |
| 60 Eri | 445.7 | -16 23 | 5.1 .6 | KO III | +0.7 | wk-1 | . 018 | 34 |
| 2 Aur | 445.9 | +36 32 | 5.04 | K3 III | +0.1 |  | . 010 | 33 |
| $\mathrm{o}^{2}$ Ori | 450.7 | +13 21 | 4.28 | K2 III | +0.9 |  | . 021 | 26 |
| 104 Tau | 51.5 | +1831 | 5.79 | G4 V | +4.9 | stm1 | . 066 | 36 |
| 68 ErL | $5 \quad 3.8$ | - 435 | 5.23 | F5 V | $+3.3$ | wis-1 | . 041 | 13 |
| HR 1684 | 56.0 | +15 55 | 5.36 | K5 III | -0.2 |  | . 0077 | 26 |
| HR 1686 | 56.1 | +79 7 | 5.16 | F6 V | +3.6 | wic-1. | . 049 | 36 |
| $p$ Ori | 58.8 .1 | + 245 | 4.64 | K3 III | +0.1 |  | . 0125 | 24 |
| 16 Aur | 511.6 | +3316 | 4.81 | K3 III | +0.1 |  | . 0115 | 64 |
| 109 Tau | 513.3 | +220 | 5.14 | G8 III | 0.0 | wk-1 | . 0093 | 27 |
| 21 Ori | 514.0 | + 230 | 5.45 | F5 II | -2.0 |  | . 0032 |  |
| $\sigma$ Aur | 517.9 | + 3718 | 5.22 | K4 III | -0.1 |  | . 0086 | 30 |
| 111 Tau | 518.6 | +1717 | 5.14 | F8 V | +3.9 | st-2 | . 057 | 33 |
| 29 Ori | 519.1 | -754 | 4.21 | G8 III | 0.0 | wk-1 | . 014 | 58 |
| 27 Ori | 519.4 | - 059 | 5.15 | KO III | +0.7 | wk-1 | . 013 | 58 |
| $\phi$ Aur | 521.0 | +3424 | 5.26 | K3 p |  |  |  | n |

Table 4 (continued)

| Name | $a$ | 8 | m | $\begin{gathered} \text { Spectral } \\ \text { Type } \end{gathered}$ | M | Group | $\pi \mathrm{sp}$ | $\begin{gathered} \text { Speed } \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 310 Ori | $5^{\mathrm{h}} 24 .{ }^{\text {m.7 }}$ | $-10101$ | 4.97 | K5 III | -0.2 |  | 050092 | 9 |
| $\phi^{2} 0 \mathrm{Ori}$ | 531.4 | + 914 | 4.39 | KO III | +0.7 | wik Can | . 018 | 109 |
| 51 Ori | 537.3 | + 126 | 5.24 | KI III | +0.8 | WK-1 | . 013 | 74 |
| T Aur | 542.3 | +39 9 | 4.64 | G8 III | 0.0 | wk-1 | . 012 | 31 |
| 132 Tau | 542.9 | +24 32 | 5.02 | G8 III | 0.0 | 4150 | . 0099 | 4 |
| $\nu$ Aur | 544.6 | +39 7 | 4.18 | KO III | +0.7 | st-1 | . 020 | 21 |
| $X^{\prime}$ Ori | 548.5 | +20 16 | 4.62 | GO V | +4.3 | st-1 | . 086 | 30 |
| 8 Aur | 551.5 | +5417 | 3.88 | KO III* | +0.7 | wk-1 | . 023 | 19 |
| HR 2113 | 555.1 | - 35 | 4.68 | K2 III | +0.9 |  | . 0175 | 14 |
| 37 Cam | 61.2 | +58 57 | 5.42 | G8 III | 0.0 | wk-1 | . 0082 | 47 |
| 36 Cam | 62.8 | +6544 | 5.59 | K2 II-III | -0.8 |  | . 0058 | 9 |
| $k$ Aur | 69.0 | +29 32 | 4.45 | G8 III | 0.0 | wk-1 | . 013 | 83 |
| 71 Ori | 69.0 | +19 12 | 5.18 |  | +3.6, | st-1 | . 048 | 25 |
| $\gamma$ Mon | 610.0 | - 615 | 4.09 | K3 III | +0.1 |  | . 016 | 23 |
| 74 Ori | 610.8 | +12 18 | 5.11 | P5 IV-V | +2.8 | wic-1 | . 034 | 41 |
| HR 2260 | 613.3 | -16 47 | 5.28 | K5 III | +0.1 |  | . 0091 | 29 |
| 45 Aur | 613.7 | +53 30 | 5.41 | F5 III | +0.2 | 8t-1 | . 0091 | 35 |
| 5 Lgn | 618.1 | +5828 | 5.43 | K4 III | -0.1 |  | . 0077 | 15 |
| HR 2305 | 619.5 | -11 28 | 5.59 | K3 III | +0.1 |  | . 0088 | 55 |
| HR 2379 | 626.7 | -12 19 | 5.33 | KJ III | +0.1 |  | . 0090 | 25 |
| $\psi^{2} \mathrm{Aur}$ | 632.2 | +42 35 | 5.09 | K3 III | +0.1 |  | . 010 | 15 |
| $\nu^{2} \mathrm{Cua}$ | 632.3 | -19 10 | 4.14 | K1 IV | +2.9 | st-1 | . 057 | 20 |
| $\nu^{3} \mathrm{CaNa}$ | 633.5 | -18 9 | 4.85 | K1 III | +0.8 | st-1 | . 017 | 22 |
| HR 2450 | 634.7 | -14 | 4.97 | K2 II | -2.6 |  | . 0031 |  |
| $\psi^{4}$ Aur | 635.8 | +44 37 | 5.17 | K5 III | -0.2 |  | . 0084 | 83 |
| 13 Lyn | 658.3 | +5716 | 5.47 | KO III | +0.7 | Wix-1 | . 011 | 20 |
| 30 Gem | 638.4 | +1320 | 4.65 | K1 III | +0.8 | st-1 | . 017 | 4 |
| 56 Aur | 639.5 | +43 41 | 5.34 | 60 V | +4.3 | st-1 | .062 | 43 |
| $\psi^{6}$ Aur | 640.0 | +4854 | 5.28 | K1 III | +0.8 | st-1 | . 013 | 25 |
| 17 Mon | 641.9 | + 89 | 5.00 | K4 III | -0.1 |  | . 0104 | 33 |
| 18 Mon | 642.7 | $+231$ | 4.70 | KO III | +0.7 | st-1 | . 016 | 9 |
| $\psi^{7}$ Aur | 645.7 | +4154 | 5.04 | K3 III | +0.1 |  | . 0102 | 69 |
| HR 2527 | 645.5 | +77 6 | 4.75 | K4 III | -0.1 |  | . 0107 | 43 |
| $\theta$ cma | 649.6 | -11 55 | 4.25 | K4 III | -0.1 |  | . 0135 | 90 |
| HR 2649 | 658.1 | +11 6 | 5.25 | KS III | +0.1 |  | . 0092 | 7 |
| 63 Aur | 74.8 | + 3929 | 5.07 | K4 II-III | -1.0 |  | . 0061 | 57 |
| $T$ Gem | 74.8 | +30 25 | 4.48 | K2 III | +0.9 |  | . 019 | 14 |
| 20 Mon | 75.3 | -45 | 5.02 | KO III | +0.7 | wk-1 | . 014 | 101 |
| 18 Lyn | 77.2 | +59 49 | 5.33 | K2 III | +0.9 |  | . 013 | 83 |
| 65 Aur | 715.4 | +3657 | 5.21 | KO III | +0.7 | wk-1 | . 0125 | 33 |
| 66 Aur | 717.2 | +40 52 | 5.28 | K0 III | +0.7 | 4150 | . 012 | 18 |
| 57 Gem | 717.4 | +25 15 | 5.08 | G8 III | 0.0 | wk-1 | . 0096 | 28 |
| 6 Gem | 719.5 | +2800 | 3.89 | KO III | +0.7 | wk-1 | . 023 | 19 |
| c CMi | 720.2 | + 928 | 5.07 | G8 III | 0.0 | st-1 | . 0097 | 24 |
| 63 Gem | 721.8 | +21 39 | 6.01 | P5 IV-V | +2.8 | st-1 | . 023 | 17 |
| 22 Lyn | 722.3 | +4953 | 5.36 | F6 V | +3.6 | st-1 | . 944 | 36 |
| $\gamma$ cai | 722.7 | +98 | 4.60 | KS III | +0.1 |  | . 013 | 41 |
| 65 Gean | 723.6 | +28 7 | 5.09 | K2 III | +0.9 |  | . 015 | 23 |
| 6 Cai | 724.2 | +12 13 | 4.85 | K2 III | +0.9 |  | . 016 | 31 |
| HR 2896 | 728.8 | +31 11 | 5.33 | KO III | +0.7 | Wk-1 | . 0094 | 28 |
| $v$ Gem | 729.8 | +27 7 | 4.22 | K5 III | -0.2 |  | . 015 | 38 |
| 25 Mon | 732.3 | - 353 | 5.17 | F5 III | +0.2 | wk-1 | . 010 | 41 |
| HR 2959 | 735.8 | -15 2 | 5.15 | K3 II | -2.6 |  | . 0028 |  |
| a Mon | 736.5 | -919 | 4.07 | KO III | +0.7 | wis-1 | . 021 | 11 |
| $\boldsymbol{\sigma}$ Gem | 737.1 | +29 8 | 4.26 | K1 III | +0.8 | st-1 | . 020 | 58 |
| 78 Gem | 738.0 | +26 1 | 5.40 | K5 III | -0.2 |  | . 0075 | 10 |
| $K$ Gea | 738.4 | +24 38 | 3.68 | G8 III* | 0.0 | st-1 | . 018 | 9 |
| $\beta$ Gem | 739.2 | +28 16 | 1.21 | KO III* | +0.7 | WK-1 | . 079 | 33 |
| 81 Gem | 740.3 | +18 45 | 5.02 | K5 III | -0.2 |  | . 0090 | 77 |
| 6 Pup | 745.2 | -16 59 | 5.54 | KS III | +0.1 |  | . 0081 | 76 |

Table 4 (continued)

| Name | a | 8 | a | Spectral Type | M | Group | $\pi \mathrm{sp}$ | $\begin{gathered} \text { Speed } \\ (\mathrm{K} \mathrm{~m} / \mathrm{Sec}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HR 3075 |  | $+74^{\circ} 11$ | 5.56 | K3 III | +0.1 |  | 0:0081 | 41 |
| 14 cmi | 753.2 | + 229 | 5.40 | KO III | +0.7 | wk-1 | . 0115 | 83 |
| 27 Mon | 754.7 | - 324 | 5.06 | K2 III | +0.9 |  | . 015 | 47 |
| 28 Mon | 756.1 | - 17 | 4.38 | K4 III | -0.1 |  | . 0103 | 46 |
| HR 3145 | 757.1 | + 237 | 4.52 | K2 III | +0.3 |  | . 019 | 58 |
| $X$ Gem | 757.4 | +28 4 | 5.04 | K2 III | +0.9 |  | . 015 | 20 |
| 55 Cam | 82.9 | +68 46 | 5.48 | G8 II | -2.5 |  | . 0024 |  |
| 19 Pup | 86.6 | -12 38 | 4.68 | Ko III | +0.7 | wk-1 | . 016 | 21 |
| HR 3212 | 6.7 | -728 | 5.36 | G8 III | 0.0 | st-1 | . 0084 | 30 |
| 20 Pup | 88.7 | -15 29 | 5.05 | G5 II | -2.3 |  | . 0034 |  |
| $\beta$ Cnc | 811.1 | +930 | 3.76 | K4 III | -0.1 |  | . 017 | 10 |
| 31 Lyn | 818.0 | +43 51 | 4.43 | K5 III | -0.2 |  | . 012 | 30 |
| HR 3306 | 820.6 | + 753 | 5.25 | G8 II | -2.8 |  | . 0027 |  |
| $\eta$ Cnc | 826.9 | +2047 | 5.52 | K3 III | +0.1 |  | . 0082 | 24 |
| $\pi^{2} \mathrm{Ma}$ | 831.5 | +6441 | 4.76 | K2 III | +0.9 |  | . 017 | 30 |
| $\sigma$ Hya | 833.5 | + 542 | 4.54 | K2 III | +0.9 |  | . 019 | 14 |
| 6 Hya | 835.3 | -12 7 | 5.15 | K4 III | -0.1 |  | . 0089 | 41 |
| 9 нуa | 837.1 | -15 35 | 4.98 | Kl III | +0.8 | st-1 | . 0145 | 34 |
| 8 cac | 839.0 | +1831 | 4.17 | KO III | +0.7 | wk-1 | . 020 | 42 |
| $\bigcirc$ Cnc | 840.7 | +29 8 | 4.20 | G8 II | -2.6 |  | . 0044 |  |
| 12 Hya | 841.7 | -13 11 | 4.44 | G8 III | 0.0 | wk-1 | . 013 | 31 |
| 35 Lyn | 845.3 | +44 6 | 5.24 | KO III | +0.7 | wk-1 | . 012 | 37 |
| $\rho^{2} \mathrm{Cnc}$ | 849.7 | +2819 | 5.25 | G8 II-III | -1.0 | st-1 | . 0056 | 17 |
| $\zeta$ Hya | 850.1 | + 620 | 3.30 | KO III | +0.7 | 4150 | . 030 | 17 |
|  | 859.6 | +67 17 | 5.33 | K5 III | -0.2 |  | . 0079 | 20 |
| HR 3612 | 0.2 | +38 51 | 4.71 | G8 Ib-II | -5.6 |  | . 0022 |  |
| $\omega$ Hya | 90.7 | + 530 | 5.41 | K2 II-III | -0.3 |  | . 0058 | 16 |
| $\tau$ cac | 92.0 | +30 ${ }^{3}$ | 5.38 | G8 III | 0.0 | wk-1 | . 0083 | 24 |
| ${ }_{\text {c }}$ OMa | 92.7 | +63 55 | 4.74 | A7 m |  |  |  | n |
| $\varepsilon$ cac | 93.5 | +22 27 | 5.22 | KO III | +0.7 | st-1 | . 0125 | 27 |
| 17 UMa | 98.4 | +57 10 | 5.48 | K5 III | -0.2 |  | . 0073 | 29 |
| 23 нya | 911.7 | - 556 | 5.40 | K2 III | +0.9 |  | . 0125 | 32 |
| 26 нуa | 915.0 | -11 33 | 4.94 | G8 III | 0.0 | st-1 | . 010 | 18 |
| 27 Hya | 915.6 | -98 | 4.97 | G8 III-IV | +1.3 | st-1 | . 018 | 16 |
| $\kappa$ Leo | 918.8 | +26 37 | 4.51 | K2 III | +0.9 |  | . 018 | 23 |
| a Hya | 922.7 | -814 | 2.16 | K3 III | +0.1 |  | . 039 | 24 |
| HR 3751 | 922.9 | +81 46 | 4.58 | K3 III | +0.1 |  | . 013 | 9 |
| 24 UTa | 925.6 | +70 16 | 4.57 | G5 IV | +3.2 | st-1 | . 053 | 31 |
| $\lambda$ Leo | 926.0 | +23 25 | 4.48 | K5 III | -0.2 |  | . 0115 | 21 |
| 6 Leo | 926.6 | +10 9 | 5.28 | Kร III | +0.1 |  | . 0092 | 17 |
| $\boldsymbol{\xi}$ Leo | 926.6 | +11 45 | 5.12 | ko III | +0.7 | nk-1 | . 013 | 34 |
| 10 Lui | 928.1 | +3651 | 4.52 | G8 III | 0.0 | st-1 | . 012 | 24 |
| HR 3809 | 928.8 | +40 4 | 4.99 | Ko III | +0.7 | wk-1 | . 014 | 25 |
| 11 LMi | 929.7 | +3618 | 5.48 | G8 IV-V | +4.5 |  | . 067 | 37 |
| 10 Leo | 931.9 | + 717 | 5.14 | KI III | +0.8 | wk-1 | . 014 | 17 |
| HR 3834 | 933.3 | + 56 | 4.78 | K3 III | +0.1 |  | . 012 | 60 |
| 27 UMa | 935.8 | +72 42 | 5.39 | KO III | +0.7 | st-1 | . 012 | 12 |
| 6 时a | 934.8 | -0 41 | 4.10 | K3 III | +0.1 |  | . 016 | 33 |
| 43 Ly | 935.8 | +40 13 | 5.50 | G8 III | +0.0 | wk-1 | . 0079 | 34 |
| $v^{\prime}$ Hya | 946.7 | -14 23 | 4.29 | G8 III | 0.0 | st-1 | . 014 | 36 |
| $\mu \mathrm{Leo}$ | 947.1 | +26 29 | 4.10 | K2 III | +0.9 |  | . 025 | 31 |
| 31 Leo | 102.6 | +10 29 | 4.58 | K4 III | -0.1 |  | . 0115 | 40 |
| HR 3991 | 105.2 | -12 19 | 5.42 | F5 V | +3.3 | st-1 | . 058 | 14 |
| $\lambda$ нya | 105.7 | -11 52 | 3.83 | K0 III | +0.7 | 4150 | . 024 | 27 |
| $\gamma$ Leo | 1014.5 | +20 21 | 2.61 | KO III | +0.7 | wis Cas | . 042 | 65 |
|  | 1021.3 | -1620 | 4.06 | K4 III | -0.1 |  | . 015 | 42 |
| $\beta$ Lui | 1022.1 | +37 13 | 4.51 | G8 III-IV | +1.3 | st-1 | . 025 | 14 |
| HR 4126 | 1026.6 | +7614 | 5.04 | K0 III | +0.7 | st-1 | . 014 | 26 |
| 48 Leo | 1029.6 | + 728 | 5.17 | G8 II-III | -1.0 | wk-1 | .0059 | 87 |
| 37 LMi | 1035.1 | +32 30 | 4.77 | G2 II | -2.0 |  | .0044 |  |

Table 4 (continued)

| Name | a | 8 | m | $\begin{gathered} \text { Spectral } \\ \text { Type } \end{gathered}$ | M | Group | T sp | $\begin{gathered} \text { Speed } \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\phi$ Hуa | $10^{\mathrm{h}} 33.7$ | $-16^{\circ} 21^{\prime}$ | 5.11 | K0 III | +0.7 | st-1 | 08013 | 25 |
| 38 UMa | 1035.1 | +6614 | 5.17 | K2 III | +0.9 |  | . 014 | 42 |
| HR 4181 | 1035.9 | +69 36 | 5.23 | K3 III | +0.1 |  | . 0094 | 16 |
| $\nu$ Hya | 1044.7 | -15 40 | 3.32 | K2 III | +0.9 |  | . 033 | 49 |
| 44 0Ma | 1047.5 | +557 | 5.36 | K3 III | +0.1 |  | . 0089 | 20 |
| 46 LMi | 1047.7 | + 3445 | 3.92 | K1 III | +0.8 | wk-1 | . 024 | 59 |
| 46 UMa | 1050.2 | +34 2 | 5.23 | K1 III | +0.8 | wk-1 | . 024 | 30 |
| a Crt | 1054.9 | -1746 | 4.20 | KO III | +0.7 | 4150 | . 020 | 105 |
| 58 Leo | 1055.1 | + 49 | 5.05 | K1 III | +0.8 | wk-1 | . 014 | 25 |
| 61 Leo | 1056.7 | - 157 | 4.97 | K5 III | -0.2 |  | . 0092 | 34 |
| a oma | 1057.6 | +6217 | 1.95 | KO III* | +0.8 | st-1 | . 055 | 8 |
| $\boldsymbol{\psi}$ UMa | 114.0 | +45 2 | 3.15 | K1 III | +0.8 | wik-1 | . 054 | 11 |
| HR 4365 | 1110.6 | +13 51 | 5.48 | K3 III | +0.1 |  | . 0084 | 21 |
| $\nu \mathrm{UMa}$ | 1113.1 | +53 38 | 3.71 | K3 III | +0.1 |  | . 019 | 22 |
| 8 Crt | 1114.3 | -14 14 | 3.82 | G8 III-IV | +1.3 | wk-1 | . 051 | 41 |
| $\lambda$ Crt | 1118.4 | -18 14 | 5.15 | F5 IV | +1.9 | st-1 | . 022 | 48 |
| $\boldsymbol{\epsilon C r t}$ | 1119.6 | -10 19 | 5.07 | K5 III | -0.2 |  | . 0088 | 22 |
| $\tau$ Leo | 1122.8 | + 324 | 5.18 | G8 II-III | -1.0 | st-1 | . 0058 | 40 |
| 87 Leo | 1125.2 | -227 | 5.07 | K4 III | -0.1 |  | . 0092 | 34 |
| 2 Dra | 1130.2 | +6953 | 5.36 | KO III | +0.7 | wk-1 | . 012 | 75 |
| $v$ Leo | 1131.8 | - 016 | 4.47 | G9 III | +0.3 | wik-1 | . 015 | 31 |
| 92 Leo | 1135.5 | +2154 | 5.43 | KO III | +0.7 | wk-1 | . 012 | 13 |
| 3 Dra | 1156.9 | +6718 | 5.48 | K3 III | +0.1 |  | . 0084 | 31 |
| $\zeta$ Crt | 1139.7 | -17 48 | 4.90 | G8 III | 0.0 | st-1 | . 0105 | 39 |
| $\chi$ UMa | 1140.8 | +4820 | 3.85 | KO III* | +0.7 | wk-1 | . 024 | 17 |
| HR 4521 | 1141.6 | +56 11 | 5.41 | K3 III | +0.1 |  | . 0087 | 28 |
| - Vir | 120.1 | + 917 | 4.24 | G8 III* | 0.0 | wk-1 | . 014 | 67 |
| 7 Com | 1211.3 | +2430 | 5.08 | K0 III | +0.7 | wk-1 | . 013 | 26 |
| HR 4668 | 1211.5 | +33 37 | 5.08 | K1 III | +0.8 | st-1 | . 014 | 47 |
| 16 Vir | 1215.3 | + 352 | 5.10 | KO III | +0.7 | wis CN | . 013 | 96 |
| 11 Com | 1215.7 | +1821 | 4.91 | G8 III | 0.0 | wk-1 | . 0105 | 73 |
| HR 4699 | 1215.8 | -13 1 | 5.36 | K1 III | +0.3 | st-1 | . 012 | 30 |
| 5 CVn | 1219.2 | +527 | 4.97 | G7 III | 0.0 | st-1 | . 010 | 28 |
| 6 CVn | 1220.9 | +39 34 | 5.22 | G8 III-IV | +1.3 | wk-1 | . 017 | 5 |
| 15 Com | 1222.0 | +2849 | 4.58 | K1 III-IV | +1.3 | 4150 | . 022 | 14 |
| HR 4783 | 1228.7 | +33 48 | 5.43 | KO III | +0.7 | wk-I | . 0115 | 31 |
| $X$ Vir | 1234.1 | - 727 | 4.78 | K2 III | +0.9 |  | . 017 | 19 |
| 27 Com | 1241.7 | +17 7 | 5.33 | K3 III | +0.1 |  | . 0089 | 63 |
| 35 Com | 1248.4 | +2147 | 5.10 | G8 III | 0.0 | st-1 | . 0095 | 6 |
| 37 Com | 1255.5 | + 3120 | 5.08 | K1 p |  |  |  | n |
| 9 Dra. | 1256.1 | +67 8 | 5.50 | G8 III | 0.0 | wic CN | . 0079 | 69 |
| $\epsilon$ Vir | 1257.2 | +1130 | 2.95 | G9 III | $+0.3$ | st-1 | . 030 | 29 |
| 41 Com | $13 \quad 2.4$ | +2810 | 4.30 | K5 III | -0.2 |  | . 0094 | 46 |
| 49 Vir | $13 \quad 2.7$ | -10 12 | 5.28 | K1 III | +0.8 | st-1 | . 013 | 27 |
| HR 4997 | 139.2 | +40 41 | 5.05 | Ko III | +0.7 | st-1 | . 0135 | 14 |
| 57 Vir | 1310.6 | -19 25 | 5.32 | K1 IV | +2.9 | 4150 | . 033 | 72 |
| HR 5013 | 1312.3 | +1412 | 5.45 | K3 III | +0.2 |  | . 0085 | 43 |
| 63 Vir | 1317.7 | -1713 | 5.45 | Ko III | +0.7 | wix-1 | . 011 | 24 |
| 69 Vir | 1322.1 | -15 27 | 4.39 | K1 III | +0.8 | 4150 | . 015 | 29 |
| 76 Vir | 1327.7 | -939 | 5.43 | KO III | +0.7 | wk-1 | . 011 | 8 |
| 89 Vir | 1344.4 | -17 38 | 5.11 | K1 III | +0.8 | st-1 | . 014 | 40 |
| $v$ Boo | 1344.7 | +1618 | 4.28 | K5 III | -0.2 |  | . 0126 | 29 |
| 6 Boo | 1345.0 | +2146 | 5.06 | K4 III | -0.2 |  | . 0093 | 32 |
| 90 Vir | 1349.6 | -1 1 | 5.30 | K2 III | +0.9 |  | . 013 | 12 |
| 9 Boo | 1352.0 | +2759 | 5.18 | K3 III | +0.1 |  | . 0096 | 45 |
| $k$ Vir | 147.6 | -948 | 4.31 | K3 III | +0.1 |  | . 014 | 61 |
| 4 OMi | 14 9.2 | +78 1 | 5.00 | K3 III | +0.1 |  | . 0104 | 23 |
| 15 Boo | 1410.0 | +1034 | 5.36 | K0 III | +0.7 | wh-1 | . 012 | 59 |
| a Boo | 1411.1 | +19 42 | 0.24 | K2 III | +0.9 |  | . 135 | 69 |
| HR 5361 | 1413.3 | +3558 | 4.83 | K1 III | +0.3 | st-1 | . 016 | 21 |

Table 4 (continued)


Table 4 (continued)

| Name | a | 8 | m | Spectral Type | ¢ | Group | T sp | $\begin{gathered} \text { Speed } \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 54 Her | $16^{\text {h }} 51{ }^{\text {m }} 0$ | $+18^{\circ} 36{ }^{\prime}$ | 5.56 | K4 III | -0.1 |  | 010074 | 72 |
| $\kappa$ Oph | 1652.9 | + 932 | 3.42 | K2 III* | +0.9 |  | . 031 | 63 |
| 30 Oph | 1655.3 | -4 4 | 5.00 | K4 III | -0.1 |  | . 0096 | 34 |
| $\boldsymbol{\epsilon}$ UMi | 1656.2 | +8212 | 4.40 | G5 III | +0.0 | st-1 | . 013 | 18 |
| HR 6388 | 17 6.3 | + 4054 | 5.12 | K3 III | +0.1 |  | . 0099 | 41 |
| 41 Oph | 1711.5 | - 020 | 4.82 | K2 III | +0.9 |  | . 016 | 18 |
| HR 6433 | 1713.9 | +1058 | 5.28 | K4 II-III | -1.0 |  | . 0053 | 94 |
| $\sigma \mathrm{Oph}$ | 1721.6 | + 414 | 4.44 | K3 II | -2.6 |  | . 0039 |  |
| HR 6516 | 1725.3 | - 053 | 5.34 | G8 IV-V | +4.6 |  | . 071 | 60 |
| $\lambda$ Her | 1726.7 | +2611 | 4.48 | K4 III | -0.1 |  | . 012 | 15 |
| 27 Dra | 1732.4 | +6812 | 5.21 | Kо III | +0.7 | wk-1 | . 0125 | 72 |
| $\beta$ Oph | 1738.5 | + 437 | 2.94 | K2 III* | +0.9 |  | . 039 | 28 |
| $\mu \mathrm{Her}$ | 1742.6 | +2747 | 3.48 | G5 IV | +3.2 | Wk-1 | . 088 | 43 |
| 87 Her | 1744.8 | +2539 | 5.34 | K2 III | +0.9 |  | . 013 | 13 |
| 90 Her | 1750.1 | +40 1 | 5.12 | K3 III | +0.1 |  | . 0099 | 28 |
| $\xi$ Dra | 1751.8 | +5653 | 3.90 | K2 III* | +0.9 |  | . 025 | 23 |
| $\boldsymbol{\nu}$ Oph | 1753.5 | -946 | 3.50 | KO III | $+0.7$ | st-1 | . 028 | 29 |
| \% Her | 1753.9 | + 2916 | 3.82 | KO III | +0.7 | st-1 | . 024 | 26 |
| $\gamma$ Dra | 1754.3 | +5130 | 2.42 | K5 III* | -0.2 |  | . 030 | 14 |
| 93 Her | 1755.6 | +1646 | 4.71 | KO II-III | -0.8 | 4150 | . 0090 | 5 |
| 70 Oph | $18 \quad 0.4$ | $+231$ | 4.28 | KO ${ }^{*}$ | +6.0 |  | . 220 | 24 |
| 71 Oph | 182.5 | + 843 | 4.73 | G8 III-IV | +1.3 | st-1 | . 021 | 21 |
| HR 6791 | 184.5 | +4327 | 5.11 | KO p |  |  |  |  |
| 36 Dra | 1813.3 | +64 22 | 5.03 | F5 V | $+3.3$ | wk-I | . 045 | 41 |
| 105 Her | 1815.1 | +2424 | 5.49 | K4 II | -2.6 |  | . 0024 |  |
| 74 Oph | 1815.9 | + 320 | 4.92 | G8 III | 0.0 | st-1 | . 010 | 27 |
| $\eta$ Ser | 1816.1 | -255 | 3.42 | G8 IV | + 3.5 | Wk-1 | . 105 | 42 |
| $k$ Lyr | 1816.4 | +36 1 | 4.34 | K2 III | $+0.9$ |  | . 020 | 8 |
| 5 Sct | 1818.2 | -859 | 4.83 | KO III | $+0.7$ | wik-1 | . 015 | 29 |
| HR 6885 | 1818.4 | +1746 | 5.48 | K3 III | +0.1 |  | . 0083 | 44 |
| 109 Her | 1813.4 | +2143 | 3.92 | K2 III | $+0.9$ |  | . 025 | 67 |
| $X$ Dra | 1822.9 | +7241 | 3.69 | F6 ** | +3.6 | st-1 | . 096 | 62 |
| 60 Ser | 1824.5 | -2 3 | 5.44 | KO III | $+0.7$ | 4150 | . 011 | 45 |
| 42 Dra | 1825.7 | +6530 | 4.99 | K2 III | +0.9 |  | . 015 | 62 |
| HR 6970 | 1829.5 | -11 3 | 5.25 | G8 III | 0.0 | st-1 | . 0088 | 34 |
| a sct | 1829.8 | -819 | 4.06 | K3 III | +0.1 |  | . 016 | 96 |
| HR 6983 | 1831.7 | +5216 | 5.42 | K0 III | $+0.7$ | st-1 | . 0115 | 7 |
| $\boldsymbol{\epsilon}$ Sct | 1838.0 | -822 | 5.03 | G8 II | -2.6 |  | . 0329 |  |
| HR 7064 | 1842.1 | +26 33 | 4.92 | K3 III | +0.1 |  | . 011 | 13 |
| HR 7117 | 1848.3 | +7358 | 5.33 | KO II-III | -0.8 | wk-1 | . 0076 | 57 |
| - Dra | 1849.7 | +5916 | 4.78 | KO II-III | -0.8 | wx-Cid | . 0076 | 53 |
| HR 7137 | 1850.8 | +50 35 | 4.97 | G8 III | 0.0 | st-1 | . 010 | 32 |
| $\boldsymbol{\eta}$ Sct | 1851.7 | -5 58 | 5.04 | K2 III | $+0.9$ |  | . 015 | 81 |
| HR 7162 | 1853.3 | +3246 | 5.21 | GO V | +4.3 | wk-1 | . 056 | 34 |
| $\epsilon \mathrm{Aql}$ | 1855.1 | +1456 | 4.22 | K2 III | +0.3 |  | . 022 | 54 |
| $\nu$ Dra | 1855.6 | +7110 | 4.91 | KO III | $+0.7$ | Wk-1 | . 014 | 15 |
| HR 7181 | 1855.7 | +26 5 | 5.23 | K2 III | +0.9 |  | . 013 | 28 |
| $\lambda$ Lyr | 1856.2 | +320 | 5.112 | K3 II | -2.6 |  | .0029 |  |
| 12 Aql | 1856.3 | -5 53 | 4.15 | Kl III | +0.8 | *k-1 | . 021 | 30 |
| 53 Dra | 199.8 | +5641 | 5.24 | G8 III | 0.0 | 4150 | . 0089 | 25 |
| 43 Sgr | 1911.8 | -19 8 | 5.03 | G8 II | -2.6 |  | . 0030 |  |
| 54 Dra | 1912.1 | +5732 | 5.28 | K2 III | +0.9 |  | . 013 | 35 |
| 8 Dra | 1912.5 | +67 29 | 3.24 | G9 III | $+0.3$ | wk-1 | . 026 | 17 |
| 23 Aql | 1913.5 | + 054 | 5.32 | K2 II-III | -0.8 |  | . 0060 |  |
| K Cyg | 1914.8 | +53 11 | 3.98 | KO III* | +0.7 | st-1 | . 022 | 28 |
| 26 AqI | 1915.2 | -536 | 5.10 | G8 III-IV | $+1.3$ | wk-1 | . 017 | 35 |
| 5 Dra | 1917.5 | +7310 | 4.63 | K3 III | +0.2 |  | . 0125 | 66 |
| 31 Aql | 1920.2 | +1144 | 5.23 | G8 IV | $+3.5$ | 4150 | . 045 | 130 |
| 4 Vul | 1921.1 | +1936 | 5.31 | KO III | $+0.7$ | wic-1 | . 012 | 43 |
| $\mu \mathrm{Aql}$ | 1929.2 | + 710 | 4.65 | K3 III | +0.1 |  | . 012 | 95 |

Table 4 (continued)

|  | Same | $\boldsymbol{a}$ | 8 | m | Spectral Type | M | Group | \% sp | $\begin{gathered} \text { Speed } \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 37 |  | $19^{\mathrm{h}} 29^{\text {m. }} 6$ | $-10^{\circ} 471$ | 5.24 | G8 III | 0.0 | 4150 | 080089 | 20 |
| $\sigma$ | Dra | 1932.6 | +69 29 | 4.73 | KO $\mathrm{V}^{*}$ | +6.0 |  | . 175 | 74 |
|  |  | 1932.3 | +1614 | 5.67 | G8 III | 0.0 | 8t-1 | . 0074 | 22 |
| HR | 7468 | 1933.5 | +4428 | 5.15 | Ko III | +0.7 | wix-1 | . 013 | 60 |
|  |  | 1935.0 | -16 31 | 5.45 | K2 III | +0.9 |  | . 012 | 50 |
|  | Cyg | 1935.4 | +2955 | 4.79 | G8 III-IV | $+1.3$ | st-1 | . 020 | 27 |
|  | Sge | 1936.6 | +1715 | 4.45 | G8 II | -2.5 |  | . 0039 |  |
|  |  | 1939.6 | +2532 | 5.45 | G8 III | 0.0 | wk-1 | . 0080 | 17 |
|  | Sgr | 1940.5 | -20 0 | 5.05 | KI III | +0.8 | - k -1 | . 014 | 62 |
|  |  | 1940.7 | +37 7 | 5.02 | G9 III | 0.0 | st-1 | . 0099 | 33 |
|  |  | 1946.2 | +10 10 | 5.22 | F8 $V$ | +3.9 | st-1 | . 054 | 22 |
| 20 |  | 1943.1 | +5244 | 5.17 | K3 III | +0.1 |  | . 0096 | 39 |
| $\epsilon$ | Dra | 1948.5 | +70 1 | 3.99 | G8 III* | 0.0 | wk-1 | . 016 | 43 |
|  | Aql | 1949.4 | + 812 | 4.86 | KO III | +0.7 | wk-1 | . 015 | 38 |
|  |  | 1950.4 | + 69 | 3.90 | G8 ID* | +3.5 | wk-1 | . 083 | 31 |
| $\boldsymbol{\eta}$ | Cyg | 1952.6 | +34 49 | 4.03 | KO III | +0.7 | wk-1 | . 021 | 18 |
|  | 7633 | 1954.0 | +58 35 | 5.13 | K5 II-III | -1.0 |  | . 0060 | 32 |
|  | Sge | 1954.3 | +19 13 | 3.71 | K5 III | -0.2 |  | . 017 | 22 |
| 26 | Cyg | 1958.5 | +4950 | 5.28 | KI II-III | -0.8 | 4150 | . 0061 | 21 |
| $\boldsymbol{\eta}$ | Sge | 200.7 | +19 42 | 5.28 | K2 III | +0.9 |  | . 013 | 41 |
| $\boldsymbol{p}$ | Dra | $20 \quad 2.4$ | +6735 | 4.68 | K3 III | +0.1 |  | . 012 | 11 |
| 66 | Dra | 204.0 | +6142 | 5.57 | K3 III | +0.1 |  | . 0081 | 79 |
| 23 | Vul | 2011.6 | +2730 | 4.73 | K3 III | +0.1 |  | . 012 | 30 |
|  |  | 2012.5 | +2422 | 5.45 | G8 III | 0.0 | wk-I | . 0080 | 34 |
|  | Cap | 2012.5 | -12 51 | 3.77 | G9 III | +0.3 | Wk-1 | . 021 | 18 |
| HR | 7759 | 2013.4 | +40 3 | 5.50 | K4 II | -2.6 |  | . 0024 |  |
| $\sigma$ |  | 2013.5 | -1926 | 5.46 | K3 II | -2.6 |  | . 0024 |  |
| HR | 7794 | 2018.2 | $+51$ | 5.41 | G8 III-IV | +1.3 | wis-1 | . 015 | 18 |
| 39 | Cyg | 2019.9 | + 3152 | 4.60 | K3 III | +0.1 |  | . 0125 | 8 |
| 69 | AqI | 2024.4 | - 313 | 5.11 | K2 III | +0.9 |  | . 014 | 18 |
| 70 |  | 2031.5 | -254 | 5.22 | K5 II | -2.6 |  | . 0027 |  |
| 71 | Aql | 2033.2 | - 127 | 4.51 | G8 III | 0.0 | st-1 | . 0125 | 8 |
| K | Del | 2034.3 | + 944 | 5.23 | G5 IV | +3.2 |  | . 039 | 48 |
| 1 | Aqr | 2034.3 | + 08 | 5.39 | KI III | +0.3 | wk-1 | . 012 | 42 |
| 30 | Vul | 2040.6 | +2455 | 5.13 | K2 III | +0.9 |  | . 014 | 76 |
| 52 | Cyg | 2041.5 | +3021 | 4.34 | KO III | +0.7 | wix-1 | . 019 | 22 |
| $\epsilon$ | Cyg | 2042.0 | +33 36 | 2.64 | KO III* | +0.7 | st-1 | . 041 | 49 |
| HR | 7956 | 2043.2 | +34 0 | 5.20 | K3 III | +0.1 |  | . 0095 | 13 |
| $\eta$ | Cep | 2043.3 | +6127 | 3.59 | KO III-IV | +1.4 | Wk CN | . 056 | 124 |
| 31 | Vul | 2047.9 | +2643 | 4.76 | G8 III | 0.0 | st-1 | . 011 | 47 |
| 32 | Vul | 2050.3 | +27 41 | 5.24 | K4 III | -0.1 |  | . 0085 | 26 |
| 17 | Del | 2050.9 | +1320 | 5.39 | KO III | +0.7 | wk-1 | . 0115 | 7 |
| 63 | Cyg | 21 3.? | +4715 | 4.88 | K4 II | -2.6 |  | . 0032 |  |
| $\nu$ | Aqr | 21 4.2 | -1147 | 4.52 | G8 III | 0.0 | st-1 | . 0125 | 25 |
| $\bullet$ | Cap | 2116.7 | -17 16 | 4.30 | G8 III | 0.0 | 8t-1 | . 014 | 25 |
|  |  |  |  | 4.24 |  | $+0.8$ | wic-1 | . 021 | 66 |
| 71 | Cyg | 2125.3 | +46 6 | 5.34 | KO III | +0.7 | wk-1 | . 012 | 41 |
| P | Cyg | 2130.2 | +45 9 | 4.22 | G8 III | 0.0 | wk Cas | . 014 | 41 |
| 72 | Cyg | 2130.7 | + 385 | 4.98 | K1 III | +0.3 | 4150 | . 015 | 67 |
| 25 | Aqr | 2154.5 | + 148 | 5.33 | KO III | +0.7 | Wc-1 | . 012 | 40 |
| 42 | Cap | 2136.1 | -14 30 | 5.23 | G2 IV | +2.9 | st-1 | . 033 | 46 |
| $K$ | Cap | 2137.1 | -19 19 | 4.32 | G8 III | 0.0 | wk-1 | . 011 | 51 |
| 46 | Cap | 2139.7 | -932 | 5.29 | G8 II-III | -1.0 | 4150 | . 0055 | 7 |
|  | Cep | 2140.5 | +70 51 | 4.35 | KO III | +0.7 | wik-1 | . 015 | 44 |
|  | Peg | 2141.5 | +22 29 | 5.45 | KO Ib | -4.5 |  |  |  |
|  | 8324 | 2141.9 | +7152 | 5.40 | K1 III | +0.8 | 4150 | . 012 | 43 |
|  | Cep | 2157.8 | +7242 | 5.15 | F5 V | $+3.3$ | st-1 | . 043 | 33 |
|  | Peg | 220.6 | + 434 | 4.90 | K4 III | -0.1 |  | . 010 | 70 |
| HR | 8424 | 22.0 | +4432 | 5.32 | K5 III | -0.2 |  | . 0078 | 17 |
| 20 | Cep | 22.0 | +62 18 | 5.39 | K4 III | -0.1 |  | . 0080 | 33 |

Table 4 (continued)

| Name |  | $a$ | 8 | m | Spectral Type | M | Group | T sp | Speed $(\mathrm{Km} / \mathrm{Sec})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 24 Cep | $22^{\text {h }}$ | $7{ }^{(19} 9$ | $+71^{\circ} 511$ | 4.99 | G8 III | 0.0 | st-1 | 01010 | 5 |
| HR 8472 | 22 | 8.2 | +5621 | 5.42 | F8 V | + 3.9 | st-1 | . 050 | 14 |
| HR 8475 | 22 | 8.4 | +34 7 | 5.42 | K2 III | +0.9 |  | . 0125 | 16 |
| HR 8485 | 22 | 9.5 | + 5913 | 4.64 | K3 III | +0.1 |  | . 012 | 7 |
| 1 Lac |  | 11.6 | +3715 | 4.22 | K3 II-III | -0.3 |  | . 0090 | 6 |
| $\theta \mathrm{Aqr}$ |  | 11.6 | $-817$ | 4.32 | G8 III-IV | +1.3 | st-I | . 025 | 12 |
| $\beta$ Lac | 22 | 19.5 | +51 44 | 4.58 | G9 III | +0.3 | wk-1 | . 014 | 67 |
| 35 Peg | 22 | 22.8 | + 412 | 4.93 | KO III | +0.7 | wk-1 | . 015 | 110 |
| $\kappa \mathrm{Aqr}$ | 22 | 32.5 | -445 | 5.33 | K2 III | +0.9 |  | . 013 | 53 |
| 11 Lac | 22 | 36.1 | +43 45 | 4.64 | K3 III | +0.1 |  | . 0125 | 23 |
| 66 Aqr | 22 | 38.2 | -19 21 | 4.38 | K4 III | -0.1 |  | . 010 | 38 |
| 13 Lac | 22 | 39.5 | +4118 | 5.24 | KO III | +0.7 | wic-1 | . 012 | 50 |
| $\lambda \mathrm{Peg}$ | 22 | 41.7 | +23 22 | 4.14 | 68 II-III | -1.0 | st-1 | . 0093 | 16 |
| $\mu \mathrm{Peg}$ | 22 | 45.2 | +24 4 | 3.67 | KO III | +0.7 | st-1 | . 326 | 26 |
| ${ }_{6} \mathrm{Cep}$ | 22 | 46.1 | +6540 | 3.68 | K1 III | +0.8 | st-1 | . 027 | 35 |
| HR 8702 | 22 | 47.9 | +82 37 | 4.97 | K3 III | +0.1 |  | . 0105 | 29 |
| HR 8748 | 22 | 55.2 | +83 49 | 4.96 | K4 III | -0.1 |  | . 0097 | 37 |
| HR 8779 | 22 | 59.7 | +6640 | 5.50 | K3 III | +0.2 |  | .0082 | 8 |
| 3 and | 22 | 59.7 | +4930 | 4.91 | KO III | $+0.7$ | wik-1 | . 014 | 76 |
| 56 Peg | 23 | 2.2 | +2456 | 4.98 | KO IIp* |  |  |  | n |
| $\psi^{\prime}$ Aqr |  | 10.7 | - 938 | 4.48 | KO III | +0.7 | wik-1 | . 018 | 86 |
| $\gamma$ Psc | 23 | 12.0 | $+244$ | 3.85 | 68 III* | 0.0 | wk CN | . 017 | 197 |
| 94 Aqr | 23 | 13.9 | -14 0 | 5.27 | G5 IV | +3.2 |  | . 038 | 24 |
| - Cep | 23 | 14.5 | + 8734 | 4.90 | K0 III | +0.7 | wk-1 | . 0145 | 11 |
| 11 And | 23 | 14.8 | +48 5 | 5.42 | KO III | +0.7 | wk-1 | . 011 | 35 |
| 7 Psc |  | 15.3 | $+450$ | 5.18 | K2 III | +0.9 |  | . 014 | 46 |
| 66 Peg | 23 | 18.0 | +1146 | 5.28 | K3 III | +0.1 |  | . 0091 | 2 |
| $\theta$ Psc | 23 | 22.9 | + 550 | 4.45 | K1 III | $+0.3$ | 4150 | . 019 | 48 |
| 70 Peg | 23 | 24.1 | +1213 | 4.67 | G8 III | 0.0 | wk-1 | . 012 | 25 |
| 14 And | 23 | 26.4 | +38 41 | 5.34 | KO III | $+0.7$ | Wk CA | . 012 | 114 |
| 72 Peg | 23 | 29.0 | + 3046 | 5.21 | K4 III | -0. 1 |  | . 0087 | 23 |
| $\lambda$ and | 23 | 32.7 | + 4555 | 4.00 | G8 III-IV | +1.3 | Wk CNT | . 029 | 80 |
| $\gamma \mathrm{Cep}$ | 23 | 35.2 | +77 4 | 3.42 | K1 IV* | +2.9 | 4150 | . 105 | 39 |
| HR 8987 | 23 | 37.3 | -16 0 | 5.44 | K4 III | -0.1 |  | . 0078 | 8 |
| 78 Peg | 23 | 39.0 | +2848 | 4.98 | KO III | +0.7 | wk-1 | . 014 | 10 |
| $\psi$ and |  | 41.1 | +45 52 | 5.09 | G5 Ib -- | -4.5 |  |  |  |
| $t$ Cas | 23 | 42.2 | +58 6 | 5.09 | K1 III | +0.8 | wk-1 | . 014 | 26 |
| 27 Psc | 23 | 53.5 | -47 | 5.07 | G9 III | $+0.3$ | st-1 | . 0115 | 40 |
| 3 Cet | 23 | 59.4 | -114 | 5.16 | K 3 Ib | -4.5 |  |  |  |

* $\boldsymbol{\mu}$

6 Ari
$\phi$ Aur
$\tau$ 37 C

16 Ser HF 6136

HR 6152
18 Dra
$18 \mathrm{Dra} \quad \mathrm{CN}$ and CH are weak. Otherwise, the star appears to be a normal giant.
HR $6791 \quad \mathrm{CN}$ and Sr II are weak. The hydrogen lines are strong enough to indicat
56 Peg
These stars have been classified by Dr. W. W. Morgan und have been used as standards in this study.
This star shows spectroscopic evidence of being fainter than other G5 V stars, such as $K$ Cet. The large trigonometric parallax supports this conclusion.
The hydrogen lines and $\lambda 4290$ are strong enough to indicate a class II star, but the CN is berely strong enough for class III, and the Sr II line is not auch stronger than tiis mould require. CN is very strong, but Sr II is only slightly stronger than in class III stars, and the hydrogen lines are quite weak.
A metallic-line star. See Koman, Morgan, and Eggen, Ap. J., 107, 107, 1948.
The hydrogen lines are strong, but the strontium line indicates that the star is no brighter than class II, and the CN indicates an even lower luminosity. $C H$ is very weak. The remainder of the spectrum shows no evidence that it is composite.
Sr II is very strong, but CN is only moderate in intensity, and the hydrogen lines are weak.
CN is too strong for a star later than K 2 or K 3 , but the Ca I line, $\lambda 4226$, is as strong as it is at K5 III.
The hydrogen lines and Sr II indicate that this is a class II star, but CN is very weak or absent. CH is probably too strong for class II.

The hydrogen lines are too weak for the strength of Sr II and CN .


[^0]:    ${ }^{1}$ Morgan, Keenan, and Kellman, An Atlas of Stellar Spectra (Chicago: University of Chicago Press, 1943).
    ${ }^{2}$ Private communication.

[^1]:    ${ }^{3}$ Private conversation.

[^2]:    ${ }^{4}$ Stellar Dynamics (Cambridge: At the University Press, 1938).
    ${ }^{5}$ Based on the results of Nordström, Lund Medd., Ser. II, No. 79, 1936.
    ${ }^{6}$ M.N., 100, 30, 1939.
    ${ }^{7}$ Astrophysics, ed. J. A. Hynek (New York: McGraw-Hill Book Co., 1951).

[^3]:    ${ }^{9}$ Pop. Astr., 22, 275, 1914. The giant and dwarf sequences had been recognized by Hertzsprung nine years earlier, but Russell seems to have been the first to emphasize that there were no stars of intermediate absolute magnitude among the late K- and M-type stars, although such stars existed in earlier types.
    $\begin{array}{ll}{ }^{10} \text { Pub. A.S.P., 34, 33, } 1922 . & { }^{11} \text { Leiden Ann., 14, Pt. 1, } 1922 . \\ { }^{12} \text { Veröff. u. Sternw Berlin-Babelsberg, Vol. 3, No. 4, } 1923 . \\ { }^{13} \text { Ap.J. 79, 145, } 1934 . & { }^{14} \text { N. G. Roman, Ap.J., 112, 554, } 1950 .\end{array}$

[^4]:    ${ }^{15}$ B. Lindblad, $A p . J ., 55,85,1922$, and D. M. Popper, Ap. J., 105, 204, 1947.
    ${ }^{16}$ W. Baade, Ap. J., 100, 137, 1944, and Keenan, Morgan, and Münch, A.J., 53, 194, 1948.
    ${ }^{17}$ Morgan and Roman, Ap. J., 112, 362, 1950, and W. P. Bidelman, Ap. J., 113, 304, 1951.

