THE SEMIREGULAR VARIABLE STARS OF THE RV TAURI AND RELATED CLASSES

Alfred H. Joy

MOUNT WILSON AND PALOMAR OBSERVATORIES CARNEGIE INSTITUTION OF WASHINGTON CALIFORNIA INSTITUTE OF TECHNOLOGY Received September 20, 1951

ABSTRACŢ

Observations.—A spectroscopic survey of the F, G, and K semiregular variables was based on Mount Wilson spectrograms of thirty-eight stars.

Physical characteristics.—Strong ionized lines indicate that many of the stars are as bright as, or brighter than, the long-period cepheids. The mean spectral type is about GO at maximum and KO at minimum light. Titanium oxide bands occur in twenty-one stars and are seen on spectra as early as G4. The mean radial-velocity range during a cycle is 36 km/sec, but irregularities are so great that mean velocity-curves are impossible. The relation of velocity changes to light-variations is similar to that of the cepheids. Hydrogen emission is present in twenty-five stars at times of increasing light. The G band of CH becomes stronger with decreasing light and later spectral type.

Subdivisions.—If the stars are divided according to radial velocity, the fast and slow groups are found to differ also in mean luminosity, spectral type, intensity of carbon bands, and distribution in the sky. The fast-moving group is undoubtedly of type II population, but the exact relationship of the slow group to Baade's populations is uncertain.

In order to investigate the spectroscopic characteristics of the semiregular variablet with intermediate spectral types and periods, thirty-eight stars have been observed as Mount Wilson with low dispersion. Nearly all the observable RV Tauri variables and most of the irregular variables of types F, G, and K have been included.

Among variable-star observers there is general agreement as to the standard behavior of RV Tauri variables, but, unfortunately, few stars meet all the requirements over any considerable length of time. The changes and irregularities are often most confusing. Cyclic variations are seldom repeated exactly, and the statistical use of suggested periods is unsatisfactory.

The strange fluctuations of light of these variables have been investigated by numerous observers. Particularly valuable results have been obtained from the Harvard photographs covering periods of time sufficiently long to show the extreme irregularities at different epochs. The painstaking work of Payne-Gaposchkin, Brenton, and Gaposchkin¹ giving light-curves for fourteen RV Tauri stars is most illuminating.

General data pertaining to the stars observed are in Table 1. The photographic magnitudes are mostly from Kukarkin and Parenago's *Catalogue of Variable Stars*. The classification according to Payne-Gaposchkin, Brenton, and Gaposchkin; Kukarkin and Parenago; and L. Rosino² ("RV" = RV Tauri class, "SR" = semiregular, "LP" = long period) is indicated in the eighth to the tenth columns. From observations of the lightchanges, all three sources assign thirteen stars of the list to the RV Tauri class. Two place six other stars in this class, while for five stars the RV Tauri designation is from one only of these sources. The remaining thirteen stars are semiregular variables which are not recognized as RV Tauri stars, although in period, light-range, and spectroscopic characteristics they seem to be rather closely related to them. One star, AB Leonis (BD+20°2337), is the new variable whose light-changes were found by Miss D. Hoffleit³ to be of the RV Tauri type.

¹ Harvard Ann., Vol. 113, No. 1, 1943. ² Ap. J., 113, 60, 1951.

³ Harvard Bull., No. 919, p. 11, 1949.

ALFRED H. JOY

Five stars of the list—DF Cyg, SU Gem, U Mon, AI Sco, and RV Tau—have longperiod light-variations of 690–2320 days superposed upon the short-period (50–90 days) light-curves. For U Mon, R. F. Sanford⁴ discovered a variation of 40 km/sec in the γ velocity in a period of 2320 days, and the same period was later found by E. Loreta⁵ in

TABLE 1

DATA CONCERNING VARIABLES OBSERVED

				m	pg			Class	<u></u>	
STAR	DESIGNA- TION	I	Ь	Max.	Min.	PERIOD (DAYS)	Gap.	K. and P.	Rosino	NO. Plates
WY And BL Aqr TW Aql DY Aql EZ Aql	233647 2109 <i>02</i> 194613 1941 <i>11</i> 193408	79° 17 20 357 14	-14° -33 - 8 -19 - 8	9.5 11.0 10.6 10.2 12.4	10.6 12.3 12.7 12.9 14.6	109 85 96: 131 39	RV RV	SR SR SR: RV RV	SR RV	10 8 5 7 3
KK Aql Z Aur AG Aur TW Cam RX Cap	194314 055353 062047 041257 2009 <i>13</i>	20 127 135 116 358	$ \begin{array}{r} - 7 \\ +16 \\ +17 \\ + 6 \\ -26 \end{array} $	$ \begin{array}{r} 11.5 \\ 9.7 \\ 10.0 \\ 10.4 \\ 11.6 \end{array} $	$12.8 \\ 12.9 \\ 13.1 \\ 11.5 \\ 13.7$	89 111 98 86 68	RV RV	SR LP RV RV RV	SR RV RV	7 9 16 6 5
R U Cep TZ Cep AV Cyg DF Cyg V360 Cyg	010884 001973 191629 194542 210630	91 88 30 44 45	+22 +11 + 6 + 8 -12	9.3 9.8 11.2 10.8 10.8	$10.4 \\ 12.0 \\ 13.0 \\ 15.2 \\ 13.3$	109 83 90 50 63	RV RV RV RV	SR SR SR RV RV	RV RV	7 6 7 10 10
SS Gem SU Gem SX Her UU Her AC Her	060222 060727 160325 163238 182621	156 152 9 28 18	+ 3 + 6 + 45 + 41 + 13	9.2 10.7 9.0 8.5 7.1	$10.7 \\ 13.2 \\ 11.1 \\ 10.6 \\ 9.4$	89 50 103 71 75	RV RV RV	RV RV SR SR RV	RV RV SR SR RV	13 5 21 18 73
AB Leo W LMi UW Lib U Lup U Mon	092720 1039 <i>26</i> 1425 <i>16</i> 1554 <i>29</i> 0726 <i>09</i>	179 176 303 313 194	+46 +63 +39 +16 + 6	$ \begin{array}{r} 10.7 \\ 11.3 \\ 10.4 \\ 10.8 \\ 6.8 \end{array} $	$13.2 \\ 14.5 \\ 11.0 \\ 13.2 \\ 8.5$	103 117 85 87 92	RV	LP SR: SR RV	 	12 13 17 7 68
TT Oph TX Oph UZ Oph TX Per S Sge	164403 165905 171707 024136 200916	349 352 356 116 26	+27 +25 +22 -19 -11	9.8 9.8 10.5 11.1 9.0	11.7 12.1 13.1 13.7 11.5	61 138: 87 76 71	RV RV ŘV RV	RV RV: RV SR RV	RV SR RV RV	14 11 9 10 29
AR Sgr AI Sco R Sct RV Tau WW Tau	1853 <i>23</i> 1749 <i>33</i> 184205 044025 035529	340 325 355 143 133	-14 - 6 - 3 -11 -16	9.6 9.4 6.5 9.8 9.9	$ \begin{array}{c} 11.5 \\ 12.6 \\ 9.6 \\ 13.3 \\ 12.9 \end{array} $	88 72 144 79 125:	RV RV RV	RV RV RV RV SR	RV RV RV	8 3 12 18 6
SV UMa S Vul V Vul	104055 194427 203226	119 31 37	$+55 \\ 0 \\ -9$	9.8 10.1 9.0	$11.3 \\ 11.4 \\ 11.0$	76 69 76	RV RV	SR SR RV	SR RV	11 18 31

⁴ Mt. W. Contr., No. 465; Ap. J., 77, 120, 1933.

⁵ A.N., 267, 399, 1938.

the light-variations. On account of insufficient spectroscopic observations, this important correlation between light and velocity measures has not been traced in other stars. These five stars have a short mean double period of 69 days, and their mean total light-range is over 3 mag. They are high-luminosity stars with mean galactic latitude of 7°. Emission is weak or absent.

SPECTROSCOPIC OBSERVATIONS

Our knowledge of the detailed spectroscopic behavior of the RV Tauri variables is based on the extensive studies of AC Herculis,⁶ U Monocerotis,⁴ R Sagittae,⁷ and V Vulpeculae⁸ by R. F. Sanford at Mount Wilson and of R Scuti⁹ by D. B. McLaughlin at Michigan. Their observations cover the whole period of light-variations and indicate that the fundamental behavior is related to that of the cepheids. Under the most favorable circumstances the double period is clearly seen in spectrographic and radial-velocity changes,¹⁰ as well as in the light-variations.

L. Rosino² has recently estimated the spectral type and luminosity class of thirteen of the stars of Table 1. McLaughlin and Rosino have added greatly to the value of their spectrographic data by determining simultaneous light-curves.

Spectra of two of the variables of Table 1 obtained at Mount Wilson have already been described.¹¹ Data for the hitherto unpublished Mount Wilson observations are in Table 2, together with the spectrographic results for each plate. The photometric elements (mostly from the *Variable Star Catalogue* [1948], by Kukarkin and Parenago) used in computing the phases (fourth column) are in the notes following Table 3. The letters in the table indicate whether the phases are reckoned from maximum (**M**) or from minimum (**m**). In the last four columns are rough intensity estimates of the strongest emission lines, the titanium oxide bands, the general absorption effect of *CH* at the G band, and (**M** II) the relative strength of the lines of ionized metallic atoms as compared with those of neutral atoms. A dash is used to indicate that the photograph was not properly exposed to show the feature in question, but a zero indicates that the feature is not visible, even though the plate is competent to show it.

These observational results are summarized in Table 3, where the stars are separated into low- and high-velocity groups. In the last three columns are the mean or γ velocity, the approximate velocity range, and the residual velocity, assuming the usual solar motion of 20 km/sec.

The spectral types generally vary from about G0 somewhat before maximum light to about K0 near minimum. Near minimum light the titanium oxide bands appear in spectra which otherwise would be classed as G or K. The classification on the basis of the TiO bands is given in parentheses. This peculiar phenomenon, which was first noticed in R Sct,¹¹ seems to be characteristic of these stars and is especially outstanding among the members of group 2. In SV UMa an intensity of 4 in the titanium bands is observed on two spectrograms of types G5 and G8.

Rosino² has noted the presence of carbon bands in AC Her. On the Mount Wilson plates, as reported by Sanford,⁶ the G band attains great strength as the light decreases to minimum. The λ 4215 CN band and the λ 4737 C₂ bands are faintly visible for a few days preceding minimum. Doubtless the total carbon absorption is responsible for a part of the loss of light. The small change in color index¹ at different phases indicates that the cyanogen absorption plays a minor role.

⁶ Mt. W. Contr., No. 424; Ap. J., 73, 364, 1931.

⁷ Mt. W. Contr., No. 481; Ap. J., 79, 81, 1934.

⁸ Mt. W. Contr., No. 481; Ap. J., 79, 82, 1934.

⁹ Pub. Obs. U. Michigan, 7, 57, 1938.

¹⁰ D. B. McLaughlin, Ap. J., 94, 94, 1941.

¹¹ A. H. Joy. R Scuti, Pub. A.S.P., 34, 349, 1922; SX Herculis, Mt. W. Contr., No. 443; Ap. J., 75, 127, 1932.

TABLE	2
-------	---

SPECTROSCOPIC OBSERVATIONS OF RV TAURI AND SEMIREGULAR VARIABLES

	Ριλτε	Date	PHASE	Spec-	VELOCITY	Disp.		INTE	NSITY	
STAR	PLATE	JD 24	(DAYS)	TRUM	(Km/Sec)	$\begin{array}{c} \text{AT } H\gamma \\ (A/MM) \end{array}$	Em.	TiO	СН	мп
WY And	$\begin{array}{c} \gamma \ 19195 \\ 19262 \\ C \ 6348 \\ 6351 \\ \gamma \ 23000 \\ 23144 \\ Ce \ 3262 \\ E \ 1455 \\ 1492 \\ \gamma \ 27057 \end{array}$	26993 7021 7431 7432 9894 9932 31038 1662 1698 1724	M 108 27 2 3 72 1 19 99 26 52	$ \begin{array}{c} G6\\ G8\\e\\ K2\\ G8e\\e\\ G2e\\ G3e\\ K2\\ \end{array} $	$-176 \\ -191 \\ -192 \\ -207 \\ -188 \\ -185 \\ -197 \\ -179 \\ -179 \\ -197 \\ -198$	70 70 35 35 70 70 20 70 70 70	$ \begin{array}{c} 0 \\ 0 \\ 4 \\ 3 \\ 0 \\ 3 \\ 1 \\ 0 \\ \end{array} $	$ \begin{array}{c} 0 \\ 0 \\ 0 \\ 2 \\ \\ 0 \\ 0 \\ 3 \end{array} $	$ \begin{array}{c} 2\\ 2\\ -\\ -\\ 2\\ 1\\ -\\ 1\\ 1\\ 1 \end{array} $	$ \begin{array}{c} 1\\ 1\\ -\\ 1\\ 3\\ -\\ 2\\ 2\\ 2\\ 2 \end{array} $
					-191					
BL Aqr	$\begin{array}{c} \gamma \ 19769 \\ C \ 7521 \\ \gamma \ 22856 \\ E \ 209 \\ \gamma \ 23640 \\ E \ 1441 \\ 1463 \\ \gamma \ 27922 \end{array}$	$\begin{array}{c} 27287 \\ 9826 \\ 9857 \\ 30209 \\ 0220 \\ 1638 \\ 1665 \\ 2053 \end{array}$	M 17 6 37 49 60 33 60 23	G4 G5 G4 K0 G5 G8 G8 G2	$ \begin{array}{r} + 34 \\ + 46 \\ + 36 \\ + 52 \\ + 39 \\ + 51 \\ + 55 \\ + 47 \\ - \\ + 45 \\ \end{array} $	110 110 70 110 110 110 70 110	0 0 0 0 0 0 0 0	0 0 1 1 2 2 0	1 2 3 2 2 2 1	2 2 1 2 2 2 2 2 2 2
TW Aql	$\begin{array}{ccc} C & 5156 \\ \gamma & 21862 \\ & 22855 \\ & 23639 \\ E & 268 \end{array}$	27018 9413 9857 30220 0266		G5 G6 G0 G4 K0	$ \begin{array}{r} + 14 \\ + 34 \\ + 35 \\ + 2 \\ + 20 \\ \end{array} $	110 70 70 110 110	0 0 0 0	0 0 0 0 0	2 3 0 3 3	2 3 3 3 3
					+ 21					
DY Aql	$\begin{array}{c} {\rm C} & 7490 \\ \gamma & 22742 \\ {\rm C} & 7520 \\ {\rm E} & 39 \\ & 57 \\ & 146 \\ & 259 \end{array}$	29766 - 9804 9826 9896 9913 30147 0251	m 109 15 37 107 124 95 68	K0 G8 K0 G5e G6 K0	+ 3 0 + 30 + 14 + 24 + 25 - + 15	$ \begin{array}{c} 110\\ 110\\ 110\\ 110\\ 110\\ 110\\ 110\\ 110$	0 0 0 5 0 0	3 0 2 2 0 2 1	$ \begin{array}{c c} 2\\ 3\\ -\\ 2\\ 2\\ 4\\ \end{array} $	$\begin{array}{ c c }\hline 1\\2\\2\\\hline \hline 3\\3\\2\\\end{array}$
EZ Aql	C 7348 7351	29452 9471	m 31 11	G5 G8		110 110	000	000	23	23
	7539	9853	/	KU	+ 49	. 110	0	0	2	5
KK Aql	$\begin{array}{ccc} C & 6168 \\ & 6445 \\ \gamma & 21160 \\ E & 255 \\ \gamma & 27066 \\ & 27703 \\ & 27919 \end{array}$	27020 7611 8734 30250 1727 1980 2052	M 43 13 72 80 49 36 19	G6 G2e G4 G6 G4 G6	$ \begin{array}{c} -245 \\ -256 \\ -280 \\ -231 \\ -246 \\ -240 \\ -262 \\ -252 \\ \end{array} $	110 70 110 110 110 110 110	0 0 4 0 0 0 0	1: 0 0 2 1 0	$\begin{array}{ c c }\hline 1\\1\\2\\1\\1\\0\\\end{array}$	1 2 2 2 2 1 1

		Date	PHASE	SPEC-	VELOCITY	Disp.		Inte	NSITY	
STAR	Plate	JD 24	(Dayš)	TRUM	(Km/Sec)	ат <i>Н</i> γ (А/Мм)	Em.	TiO	СН	мп
Z Aur	$\begin{array}{c} \gamma \ 23030 \\ 23163 \\ 23339 \\ \text{E} \ 258 \\ \gamma \ 23842 \\ 23929 \\ 27176 \\ 27503 \\ \text{E} \ 1688 \end{array}$	29898 9945 30071 0251 0302 0334 1755 1894 1922	M 46 93 8 65 5 37 17 45 73	G4e G6e G2 G2e G0e G0 G5e G4e G3e	$-155 \\ -187 \\ -157 \\ -152 \\ -154 \\ -160 \\ -157 \\ -168 \\ -170$	70 110 110 110 10 10 110 110 110	5 4 0 3 3 0 5 4 2	0 0 0 0 0 0 1 2 0	2 2 1 1 1 1 1 1 2	1 2 1 1 1 1 1 1 2
					-165					
AG Aur	$\begin{array}{c} C & 4695 \\ 4717 \\ 4729 \\ 5364 \\ 5568 \\ 5584 \\ 5602 \\ 5624 \\ 5664 \\ 5665 \\ V & 94 \\ C & 6347 \\ 6349 \\ \gamma & 27177 \\ 27504 \\ E & 1689 \end{array}$	$\begin{array}{c} 25305\\ 5342\\ 5344\\ 5956\\ 6256\\ 6267\\ 6283\\ 6311\\ 6340\\ 6340\\ 6647\\ 7403\\ 7431\\ 31756\\ 1894\\ 1922 \end{array}$	M 30 67 69 92 97 10 26 54 83 83 95 82 12 12 53 81	G6 G8e G4e G4e G4e G2e G2e G2e G5e G4e G4e K0 G8	$\begin{array}{c} +182 \\ \\ +196 \\ +199 \\ +190 \\ +190 \\ +192 \\ +206 \\ +197 \\ +195 \\ +201 \\ +186 \\ +183 \\ +189 \\ +200 \end{array}$	70 70 70 70 70 70 70 70 35 35 70 110 110 110	$ \begin{array}{c} 0 \\ 0 \\ 0 \\ 2 \\ 1 \\ 1 \\ 0 \\ 5 \\ 5 \\ 2 \\ 4 \\ 4 \\ 0 \\ 0 \end{array} $	$ \begin{array}{c} 0 \\ 2 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 2 \end{array} $	$ \begin{array}{c} 1 \\ - \\ 2 \\ 2 \\ 1 \\ 1 \\ 2 \\ - \\ 1 \\ 2 \\ - \\ 1 \\ 2 \\ 2 \\ 2 \\ 2 \\ 2 \\ 2 \\ 2 \\ 2 \\ 2 \\ 2$	$ \begin{array}{c} 2 \\ 1 \\ 1 \\ 2 \\ 2 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 1 \\ 1 \\ 1 \\ 2 \\ 1 \\ 1 \\ 1 \\ 2 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1$
					+193					
TW Cam	$\begin{array}{c} \gamma \ 23137 \\ 23197 \\ C \ 7642 \\ E \ 257 \\ \gamma \ 27171 \\ 27971 \end{array}$	29927 9957 9971 30250 1754 2076	m 82 27 41 63 26 6	G8 G8 G5 G2 G3 G4	$ \begin{array}{r} - 69 \\ - 44 \\ - 51 \\ - 59 \\ - 61 \\ - 40 \\ \end{array} $	110 110 70 110 70 110	0 0 0 0 0 0	0 0 0 0 0 0	0 1 1 1 0 1	3 3 3 3 3 3 3
RX Cap	$\begin{array}{c} C & 7515 \\ \gamma & 22848 \\ & 23132 \\ & 23509 \\ & 26939 \end{array}$	29825 9856 9927 30180 1696	m 47 10 13 62 15	G3 G0 G3 G2 G0	$ \begin{array}{r} -33 \\ -135 \\ -122 \\ -148 \\ -156 \\ -135 \\ \hline \end{array} $	110 110 110 110 110 110	0 0 0 0 0	0 0 0 0 0	0 1 1 1 0	1 2 2 1 2
R U Cep	γ 22107 22199 22415 23027 23029 27170 27924	29505 9560 9647 9898 9898 31754 2053	•M 62 7 94 16 16 11 91	— K0 — K2 K0 G6	$ \begin{array}{r} -133 \\ -133 \\ -13 \\ -13 \\ -13 \\ -17 \\ -17 \\ -17 \\ -18 \\ -8 \\ -12 \\ \end{array} $	70 70 70 70 70 35 70	0 0 0 0 0 0 0	0 0 1 2 2 1 2	$\begin{array}{c} - \\ 1 \\ 2 \\ 1 \\ 2 \\ 1 \\ 2 \end{array}$	1 2 2 1 2 1
TZ Cep	γ 19188 21971	26992 9450	M 74 42	K0e G6	- 12 - 15 - 5	70 110	1 0	02	3 2	33

TABLE 2—Continued

TABLE 2-Continued

G _	Da	DATE	PHASE	Spec-	VELOCITY	Disp.		Inte	NSITY	
STAR	PLATE	JD 24	(Days)	TRUM	(Km/Sec)	АТ <i>Н</i> ү (А/Мм)	Em.	TiO	СН	мп
TZ Cep	γ 23028 23136 23636 27974	29898 9927 30219 2077	M 75 21 64 13	G8e K1 K2e K0	$ \begin{array}{r} - 7 \\ 0 \\ + 4 \\ + 6 \end{array} $	70 110 110 110	4 0 3 0	1 2 1 0	$\begin{array}{c}3\\2\\3\\0\end{array}$	3 2 1 1
AV Cyg	γ 18899 C 7305 7549 γ 23453 E 1416 γ 26744 C 7708	26878 9410 9855 30151 1600 1633 1958	M 77 8 4 31 45 78 44	G4 G3e G2e G6 G0e G3 G2e	$ \begin{array}{r} - & 5 \\ - & 28 \\ - & 16 \\ - & 30 \\ - & 11 \\ - & 32 \\ - & 19 \\ - & 28 \\ \hline \hline - & 28 \\ \hline \end{array} $	70 110 110 110 110 70 110	0 3 3 0 1 0 2	0 0 0 0 0 0	3 3 3 3 2 2 3	1 3 2 3 2 2 2 2
DF Cyg	$\begin{array}{c} \gamma \ 18070 \\ C \ 5751 \\ 5758 \\ 5841 \\ 7064 \\ 7086 \\ 7100 \\ \gamma \ 21218 \\ 21231 \\ C \ 7193 \end{array}$	26401 6495 6516 6606 8702 8731 8763 8793 8821 9144	m 12 7 28 18 23 2 34 14 42 16	K0 K2 G6 K2 K4 K0 G6 G8 G8 G8 G5	$ \begin{array}{r} - 5 \\ + 4 \\ - 10 \\ - 35 \\ - 7 \\ + 8 \\ - 9 \\ - 4 \\ + 7 \\ - 16 \\ \hline - 5 \\ \end{array} $	$ \begin{array}{c} 110\\ 70\\ 10\\ 110\\ 110\\ 110\\ 110\\ 110\\ 1$	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0	2 1 3 3 1 2 3 4 3	3 3 3 3 3 3 2 3 3 3 3 3
V360 Cyg	$\begin{array}{c} C & 7507 \\ \gamma & 22758 \\ C & 7540 \\ E & 40 \\ & 313 \\ 1417 \\ 1433 \\ \gamma & 27056 \\ 27173 \\ 27920 \end{array}$	29806 9824 9853 9896 30297 1600 1635 1724 1755 2052	m 57 11 40 20 41 16 51 13 44 25	F5 F8e G0 G0e F8 F5 G0 F8e G0e F5	$ \begin{array}{r} -260 \\ -247 \\ -238 \\ -238 \\ -264 \\ -258 \\ -255 \\ -240 \\ -264 \\ -281 \\ \hline -250 \\ \end{array} $	110 110 110 110 110 110 110 110 110 110	0 1 0 2 0 0 0 1 1 0	0 0 0 0 0 0 0 0 0	0 1 0 1 0 1 0 0 0 0	1 1 2 1 1 2 1 1 2 1 1 2 1 1 2
SS Gem	$\begin{array}{c} C 1677 \\ 3238 \\ 3661 \\ 4221 \\ 4560 \\ 4740 \\ 5610 \\ 5630 \\ 5647 \\ \gamma 17978 \\ C 5652 \\ 5674 \\ \gamma 18035 \end{array}$	23179 4249 4539 4984 5217 5347 6285 6312 6316 6322 6338 6342 6346	m 36 35 57 55 20 61 17 44 48 54 70 74 78	G5 G5 G4 G8 G4 G5 G2 G0 G2 G0 G2 G0 G2	$\begin{array}{r} +23\\ +30\\ -19\\ +9\\ -17\\ -14\\ -14\\ -19\\ -15\\ -8\\ -7\\ -5\\ -23\\ \hline -6\\ \end{array}$	70 70 70 70 35 70 70 70 70 70 70 70	0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0	$\frac{3}{2}$ $\frac{3}{4}$ $\frac{3}{1}$ $\frac{1}{2}$ $\frac{2}{1}$ $\frac{1}{1}$	2 2 3 2 2 2 2 3 2 3 2 3 2 2 2 2 2 2 2 2

ψ,

TABLE 2-Continued

		Date	Phase	Spec-	Velocity	Disp.		Intel	NSITY	
STAR	PLATE	JD 24	(Days)	TRUM	(Km/Sec)	ат <i>Н</i> ү (А/Мм)	Em.	TiO	СН	мп
SU Gem	$\begin{array}{c} \gamma \ 21440 \\ 23159 \\ C \ 7661 \\ E \ 339 \\ \gamma \ 26392 \end{array}$	29176 9944 30029 0324 1463		G2 G4 G2 F5 G6	$ \begin{array}{r} + 16 \\ + 2 \\ - 7 \\ + 7 \\ - 26 \\ \hline - 2 \end{array} $	110 70 110 110 110	0 0 0 0 0	0 0 0 0 0	1 1 2 0 2	3 2 3 2 3
UU Her	$\begin{array}{c} C & 2742 \\ 2766 \\ 2796 \\ 3512 \\ 3980 \\ 4197 \\ 4224 \\ 4225 \\ 4285 \\ 4308 \\ 4370 \\ 5205 \\ 5234 \\ 5390 \\ 5415 \\ 5464 \\ 5740 \\ 5756 \end{array}$	$\begin{array}{c} 23889\\ 3916\\ 3926\\ 4417\\ 4750\\ 4956\\ 4984\\ 5011\\ 5040\\ 5048\\ 5079\\ 5777\\ 5809\\ 6018\\ 6048\\ 6135\\ 6493\\ 6516\end{array}$		F5 F6 F8 F5 G0 F5 F7 F4 G0 F6 F5 F6 F8 F7 F7 F6	$\begin{array}{c} -128\\ -142\\ -137\\ -121\\ -130\\ -132\\ -130\\ -127\\ -132\\ -139\\ -126\\ -131\\ -117\\ -141\\ -139\\ -144\\ -125\\ -125\\ -125\\ \end{array}$	$\begin{array}{c} 70\\ 70\\ 70\\ 70\\ 70\\ 70\\ 70\\ 70\\ 70\\ 70\\$	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	$\begin{array}{c} 0 \\ 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\$	2 2 2 2 2 2 2 2 2 2 2 1 2 2 2 1 2 2 2 1 2 2 2 1 2 2 2 1 2
AB Leo	E 1681 1690 Ce 4231 γ 27603 27651 E 1707 γ 27705 29272 E 1951 γ 29383 E 1969 γ 29524	$\begin{array}{c} 31919\\ 1923\\ 1929\\ 1930\\ 1952\\ 1976\\ 1981\\ 2555\\ 2582\\ 2611\\ 2636\\ 2671 \end{array}$	M 47 51 57 58 80 1 6 64 91 17 42 77	G0e G0e F5e G3e G0 F8 G0e F5e G2e F5e	$-131 \\ +208 \\ +188 \\ +182 \\ +166 \\ +163 \\ +194 \\ +172 \\ \\ +180 \\ +189 \\ +178 \\ +182 \\ +182 \\$	110 110 20 70 110 110 110 110 110 110 110	4 5 4 3 1 0 0 5 1 1 6	0 0 0 0 0 0 0 0 0 0 0 0 0	$ \begin{array}{c} 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \\ 1 \\ 1 \\ 0 \\ \end{array} $	$ \begin{array}{c} 2 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 1 \\ 1 \end{array} $
W LMi	$\begin{array}{c} C & 7176 \\ \gamma & 21784 \\ C & 7664 \\ \gamma & 23340 \\ E & 87 \\ \gamma & 23450 \\ 24024 \\ E & 422 \\ \gamma & 26394 \\ E & 1354 \\ 1397 \\ 1595 \\ C & 7715 \end{array}$	$\begin{array}{c} 29379\\ 9380\\ 30030\\ 0071\\ 0090\\ 0151\\ 0397\\ 0443\\ 1464\\ 1546\\ 1568\\ 1844\\ 1960\\ \end{array}$	M 101 102 48 90 109 53 64 110 76 41 63 104 104	— K0e G6e G2e G2e K0e G4e G5e G3e K2e K0e	$ \begin{array}{c} \\ + 57 \\ + 55 \\ + 94 \\ + 48 \\ + 64 \\ + 96 \\ + 71 \\ + 41 \\ + 46 \\ \\ + 90 \\ + 66 \\ \end{array} $	110 70 110 110 110 110 110 110 110 110 1	3 3 10 3 2 6 8 3 4 5 5 0 1	1 1 2 0 1 0 0 1 0 2 0 3 2	0 2 1 2 3 2 1 3 2 2 2 2 2 1	

 $\ensuremath{\textcircled{}^{\odot}}$ American Astronomical Society $\ \bullet$ Provided by the NASA Astrophysics Data System

2

	BLATE	DATE	PHASE	SPEC-	VELOCITY	DISP.		Intensity			
STAR	PLATE	JD 24	(DAYS)	TRUM	(Km/Sec)	AT $H\gamma$ (A/Mm)	Em.	TiO	СН	M II	
UW Lib	$\begin{array}{c} \gamma \ 22735 \\ 22756 \\ C \ 7538 \\ \gamma \ 23341 \\ E \ 106 \\ 151 \\ \gamma \ 23510 \\ 24025 \\ 24054 \\ E \ 423 \\ 442 \\ 1396 \\ \gamma \ 26612 \\ 26742 \\ 27642 \\ C \ 7707 \\ \gamma \ 27706 \end{array}$	29803 9824 9853 30071 0119 0149 0181 0398 0423 0443 0443 04471 1567 1595 1633 1948 1958 1981		G7e G8 G6e G4 G7e G2e G8 K0 G6 G6e G6e G5e G6e G8e G6e G8 G6e G8	$\begin{array}{r} +155\\ +186\\ +164\\ +169\\ +194\\ +155\\ +142\\ +176\\ +179\\ +136\\ +161\\ +169\\ +171\\ +174\\ +146\\ +145\\ \hline\end{array}$	70 110 110 110 110 110 110 110 110 110 1	0 0 4 0 2 1 0 0 0 4 2 2 1 1 2 1 0	0 1 0 1 2 0 1 0 2 3 0 0 1 0 0 0 1 0 0 0 0	$ \begin{array}{c} 1\\1\\1\\2\\2\\1\\2\\2\\1\\1\\2\\2\\2\\1\\1\\1\\2\\2\\2\end{array} $	1 1 2 1 2 1 2 1 2 1 2 1 2 1 2 2 1 1	
U Lup	C 7485 7502 E 93 107 171 1428 C 7716	29765 9806 30091 0119 0178 1634 1960		K0 K0e K0 G2 G6e	$-134 \\ -134 \\ -141 \\ -124 \\ -109 \\ -141 \\ -130$	110 110 110 110 110 110 110	0 0 2 1 0 0 4	2 1 0 2 0 0	$\begin{array}{c} 2\\ \hline 2\\ 2\\ 2\\ 2\\ 2\\ 2\\ 2\\ 2\end{array}$	1 1 1 1 2 1	
TT Oph	$\begin{array}{ccc} \gamma & 6870 \\ C & 340 \\ & 386 \\ & 441 \\ & 476 \\ & 504 \\ 1075 \\ 1114 \\ & 1218 \\ 1265 \\ & 1367 \\ & 1640 \\ & 2297 \\ & 3881 \end{array}$	$\begin{array}{c} 21711\\ 2414\\ 2443\\ 2473\\ 2483\\ 2507\\ 2866\\ 2882\\ 2918\\ 2940\\ 2970\\ 3136\\ 3592\\ 4715 \end{array}$	m 13 43 12 42 52 15 8 24 59 20 50 33 0 24	G4e G6e K0 G4e G5 K0 G5 K0 G6 G8 K0 G8 G8 G7	$ \begin{array}{r} - & 64 \\ - & 43 \\ - & 41 \\ - & 62 \\ - & 53 \\ - & 53 \\ - & 57 \\ - & 58 \\ - & 57 \\ - & 67 \\ - & 81 \\ - & 39 \\ - & 34 \\ - & 61 \\ \hline \\ - & 50 \\ \end{array} $	70 35 35 35 35 70 35 70 35 70 70 70 70 70	$ \begin{array}{c} 1\\2\\3\\1\\0\\2\\0\\0\\0\\0\\0\\0\\0\\0\\0\\0\\0\\0\\0\\0\\0\\0\end{array} \end{array} $	0- 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2 3 3 3 2 3 2 3 2 3 3 2 2 3 3 2	$ \begin{array}{c} 2 \\ 3 \\ 3 \\ 3 \\ 2 \\ 3 \\ 3 \\ 3 \\ 2 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3$	
TX Oph	$\begin{array}{c} C & 4225 \\ & 4251 \\ & 4399 \\ & 4739 \\ & 4928 \\ & 5227 \\ & 5435 \\ & 7 \ 24129 \\ & 24151 \\ & 26613 \\ E & 1683 \end{array}$	24984 5010 5129 5346 5458 5786 6078 30484 0504 1595 1919		G2e G0 G2 G3 G6e G4e G0e F8 G3 G6 F5e	-50 -157 -166 -172 -170 -158 -161 -155 -165 -178 -164 -177 -165	70 70 70 70 70 70 110 110 110	1 0 0 1 1 1 1 0 0 0 1	0 0 0 0 0 0 0 0 0 0 0	$ \begin{array}{c} 1 \\ 0 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 0 \\ \hline 1 \\ 0 \\ \hline 1 \\ 0 \\ 0 \end{array} $	3 3 3 3 2 2 3 3 2 2 2 2	

TABLE 2-Continued

		Date	PHASE	Spec-	VELOCITY	Disp.		Inte	NSITY	
STAR	PLATE	JD 24	(Days)	TRUM	(Km/Sec)	$\begin{array}{c} \text{AT } H\gamma \\ (A/MM) \end{array}$	Em.	TiO	СН	M II
UZ Oph	$\begin{array}{c} C & 4899 \\ & 5149 \\ 5460 \\ \gamma & 21968 \\ 23345 \\ 23637 \\ E & 443 \\ \gamma & 24130 \\ E & 1415 \end{array}$	25439 5688 6133 9450 30087 0220 0471 0484 - 1600	m 24 11 19 15 41 86 75 1 68	G6e G6 G4e G5e G4 G8 G2 G8 G2e	$ \begin{array}{r} - & 99 \\ - & 58 \\ - & 99 \\ - & 80 \\ - & 87 \\ - & 76 \\ - & 120 \\ - & 90 \\ - & 92 \end{array} $	$\begin{array}{c} 70 \\ 70 \\ 70 \\ 70 \\ 110 \\ 110 \\ 110 \\ 110 \\ 110 \\ 110 \end{array}$	$ \begin{array}{c} 1 \\ 0 \\ 1 \\ 2 \\ 0 \\ 0 \\ 0 \\ 0 \\ 2 \\ \end{array} $	$ \begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 2 \\ 0 \\ 1 \\ 0 \end{array} $	2 2 0 1 2 2 3 2 2	3 3 2 2 2 2 2 2 2 2 2 2 2 2
					- 85					
TX Per	$\begin{array}{c} \gamma \ 19263 \\ 22109 \\ C \ 7432 \\ E \ 43 \\ 54 \\ 261 \\ 1493 \\ \gamma \ 27174 \\ 27251 \\ E \ 1762 \end{array}$	$\begin{array}{c} 27021\\ 9506\\ 9646\\ 9896\\ 9912\\ 30251\\ 1698\\ 1755\\ 1786\\ 2082\\ \end{array}$	M 6 48 36 58 74 31 28 9 40 31	K2 G7 K0e K0 G8e K2 G6 G5 G6e	$ \begin{array}{r} - 15 \\ - 7 \\ + 7 \\ - 6 \\ - 13 \\ + 21 \\ - 2 \end{array} $	70 110 110 110 70 110 70 110 110 110	0 0 1 0 2 0 0 0 3	1 0 2 1 2 1 3 1 0 1	$ \begin{array}{c} 4 \\ 3 \\ 2 \\ - \\ 4 \\ 1 \\ 3 \\ 2 \\ 2 \end{array} $	2 2 1 2 2 2 2 2 2 2 1 1
					0			,		
AR Sgr	$\begin{array}{ccc} C & 4995 \\ & 5487 \\ & 5557 \\ E & 50 \\ \gamma & 23508 \\ & 23634 \\ & 26616 \\ E & 1430 \end{array}$	25518 6164 6242 9912 30180 0219 1596 1634	m 31 62 52 •31 36 75 46 84	G6 G2 F8 G0 G0 G2 G3e F5e	$ \begin{array}{r} -101 \\ -101 \\ -90 \\ -101 \\ -108 \\ -102 \\ -105 \\ -88 \\ \end{array} $	70 70 70 70 70 110 70 70	0 0 1 0 0 0 2 1	0 0 0 0 0 0 0 0 0	1 1 0 1 1 1 0 1	2 1 2 2 2 2 1 1
					-100					
AI Sco	C 6261 6268 E 274	27254 7256 30267	 	K2 G0 G5	$ \begin{array}{r} - 3 \\ - 40 \\ - 8 \end{array} $	110 110 110	0 0 0	0 0 0	$\begin{vmatrix} 1\\2\\2 \end{vmatrix}$	$\frac{3}{2}$
DUT	0 4511	05102	62	V 1	- 15	- 70				2
ку тац	$\begin{array}{c} 4311\\ 5150\\ 5329\\ 5617\\ 5658\\ 5702\\ 5843\\ \gamma\ 19122\\ 19199\\ C\ 6173\\ E\ 47\\ 279\\ 1498\\ \gamma\ 27059\\ E\ 1524\\ \gamma\ 27175\\ \end{array}$	23183 5690 5875 6310 6339 6431 6606 6964 6993 7020 9897 30267 1710 1724 1744 1755	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} K1 \\ G4 \\ K0e \\ G8e \\ G8 \\ G5e \\ G6 \\ G6 \\ G6 \\ G6 \\ G4 \\ G6 \\ G4 \\ G6 \\ G4 \\ G6 \\ G4 \\ G6 \\ G6$	$\begin{array}{r} + 40 \\ + 39 \\ + 34 \\ + 48 \\ + 44 \\ + 33 \\ + 41 \\ + 32 \\ + 18 \\ + 33 \\ + 39 \\ + 28 \\ + 25 \\ + 41 \\ + 22 \\ + 5 \end{array}$	70 70 70 70 70 70 70 70 70 70 10 110 110 110 110 110	0 1 2 0 1 0 0 1 0 0 0 1 0 0 0 0 0 0 0 0	0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	4 2 3 1 3 2 3 2 2 4 2 2 4 2 2 4 2 3 2 3 2 3 <t< td=""><td>3 2 3 2 3 1 3 <t< td=""></t<></td></t<>	3 2 3 2 3 1 3 <t< td=""></t<>

33

.

TABLE 2—Continued

_	_	Date	PHASE	Spec-	VELOCITY	Disp.		Intel	NSITY	
STAR	PLATE	JD 24	(Days)	TRUM	(Km/Sec)	AT $H\gamma$ (A/MM)	Em.	TiO	СН	M II
RV Tau	γ 27347 Ε 1908	31831 2496	m 29 66	G5 G4e	+ 25 + 24	70 110	0 1	0 0	3 3	3 2
					+ 35					
WW Tau	$egin{array}{ccc} \gamma & 22473 \ { m E} & 48 \ \gamma & 23161 \ & 23196 \ { m E} & 284 \ \gamma & 27068 \end{array}$	29678 9897 9945 9957 30268 1727		G5 G4e K2 K0 K0 G4e	$ \begin{array}{r} - & 99 \\ - & 113 \\ - & 102 \\ - & 109 \\ - & 109 \\ - & 120 \end{array} $	110 110 110 110 110 110 110	0 5 0 0 0 2	$\begin{array}{c} 0\\ 2\\ 3\\ 3\\ \hline 1 \end{array}$	2 1 2 1 1 2	2 2 1 2 2 2 2
					-110			-		
SV UMa	$\begin{array}{c} C & 4667 \\ & 4738 \\ & 4761 \\ & 4764 \\ & 4804 \\ & 4822 \\ & 4841 \\ & 4850 \\ & 5148 \\ & 5164 \\ & 5393 \end{array}$	25278 5346 5353 5362 5380 5394 5410 5422 5688 5723 6018		G5e G4e G5e G8 G5 G8 G6 G8 G6 G8 G2e G3	$ \begin{array}{r} -80 \\ -86 \\ -99 \\ -101 \\ -97 \\ -85 \\ -90 \\ -85 \\ -101 \\ -90 \\ -85 \\ -101 \\ -90 \\ \end{array} $	70 70 70 70 70 70 70 70 70 70	6 3 1 0 0 0 0 0 0 0 1 0	$\begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 4 \\ 4 \\ 3 \\ 1 \\ 0 \\ 0 \\ \end{array}$	$ \begin{array}{c} 1 \\ 2 \\ 1 \\ 1 \\ 3 \\ 2 \\ \hline 3 \\ 2 \\ 2 \\ 2 \\ 2 \end{array} $	2 3 2 2 3 3 2 2 2 2 2 1 3
S Vul	C 2937 3950 4400 4983 5180 5211 5237 γ 16781 17544 17545 17576 C 5556 γ 17855 C 5615 5801 5819 5846 6046	$\begin{array}{c} 24377\\ 4744\\ 5129\\ 5515\\ 5751\\ 5779\\ 5809\\ 5836\\ 6154\\ 6155\\ 6169\\ 6241\\ 6285\\ 6310\\ 6554\\ 6580\\ 6607\\ 6879\\ \end{array}$	M 56 28 35 14 47 7 37 64 44 45 59 62 39 62 39 63 37 63 22 23	G6• G6 K2 K0 G0 G8 G4 G6 G6 G6 G6 G2 K0 G6 G8 G5 G6 G4 G4	$ \begin{array}{r} - 14 \\ + 1 \\ + 10 \\ - 5 \\ - 1 \\ - 13 \\ + 6 \\ - 10 \\ - 3 \\ - 3 \\ - 2 \\ - 9 \\ + 4 \\ - 5 \\ + 8 \\ - 4 \\ - 13 \\ - 6 \\ \hline - 2 \\ \end{array} $	70 70 70 70 70 70 70 70 70 70 70 70 70 7		$\begin{array}{c} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\$	$ \begin{array}{c} 1\\ 1\\ 4\\ 3\\ 1\\ 3\\ 2\\ 3\\ -1\\ -3\\ 1\\ 2\\ 1\\ 2\\ 1\\ 2\\ 1 \end{array} $	2 2 3 3 3 2 2 2 2 2 2 3 2 2 3 2 3 3 3 3

TABLE 3

SUMMARY OF SPECTROSCOPIC RESULTS

		MAX. Emis-	СН	Max.		Velocity	
STAR	Spectrum (Atomic Lines <i>TiO</i>)	SION INT.	G BAND Int.	M II Int.	Meas. (Km/Sec)	Range (Km/Sec)	Resid. (Km/Sec)
		Gr	oup 1: Veloc	ities<70	Km/Sec		
BL Aqr. TW Aql. DY Aql. DY Aql. EZ Aql. TW Cam RU Cep. TZ Cep. AV Cyg. DF Cyg. SS Gem. SU Gem. SX Her. AC Her. U Mon. TT Oph. UZ Oph. TX Per. R Sge. AI Sco. R V Tau. S Vul. V Vul.	$\begin{array}{c} G2 & -K0 & (M2) \\ G0 & -K0 \\ G5e-K0 & (M3) \\ G5 & -K0 \\ G2 & -G8 \\ G6 & -K2 & (M2) \\ G6 & -K2e & (M2) \\ G0e-G6 \\ G5 & -K4 \\ G0 & -G8 \\ F5 & -G6 \\ G3e-K0 & (M3) \\ F1 & -K4e \\ F8e-K2 & (M2) \\ G2e-K0 \\ G2e-G8 & (M2) \\ G5e-K2 & (M3) \\ G2 & -K0 \\ G0 & -K2 \\ G5e-K2 & (M3) \\ G4e-K1 & (M1) \\ G0 & -K2 & (M1) \\ G4 & -K3 & (M2) \\ \end{array}$	$ \begin{array}{c} 0\\0\\5\\0\\0\\4\\3\\0\\0\\0\\8\\4\\5\\3\\2\\3\\0\\0\\3\\2\\0\\1\end{array} $	$1-3 \\ 0-3 \\ 1-3 \\ 2-3 \\ 0-1 \\ 1-2 \\ 0-3 \\ 2-3 \\ 1-4 \\ 0-4 \\ 0-2 \\ 0-3 \\ 0-4 \\ 1-4 \\ 1-4 \\ 1-2 \\ 2-3 \\ 1-4 $	2 3 3 3 2 3 3 3 2 3 3 3 2 3 3 3 2 3	$\begin{array}{r} + 45 \\ + 21 \\ + 15 \\ + 48 \\ - 55 \\ - 12 \\ - 23 \\ - 5 \\ - 23 \\ - 5 \\ - 2 \\ - 20 \\ - 30 \\ + 35 \\ - 50 \\ - 85 \\ 0 \\ + 10 \\ - 15 \\ + 40 \\ + 35 \\ - 2 \\ - 15 \end{array}$	$\begin{array}{c} 20\\ 35\\ 30\\\\ 30\\ 15\\ 20\\ 20\\ 45\\ 55\\ 40\\ 15\\ 60\\ 45\\ 45\\ 70\\ 40\\ 40\\ 35\\ 35\\ 45\\ 25\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 35\\ 35\\ 45\\ 25\\ 40\\ 40\\ 40\\ 35\\ 35\\ 45\\ 25\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 40\\ 35\\ 40\\ 40\\ 40\\ 40\\ 40\\ 40\\ 40\\ 40\\ 40\\ 40$	$\begin{array}{r} + 57 \\ + 39 \\ + 29 \\ + 66 \\ - 3 \\ + 4 \\ + 13 \\ - 13 \\ + 38 \\ - 10 \\ + 38 \\ - 17 \\ - 56 \\ + 24 \\ - 56 \\ + 17 \\ - 56 \\ + 17 \\ - 56 \\ + 17 \\ - 56 \\ + 17 \\ - 56 \\ + 17 \\ - 56 \\ - 56 \\ + 17 \\ - 56$
		Gre	oup 2: Veloc	ities>70	Km/Sec	<u>. </u>	
WY And KK Aql Z Aur AG Aur RX Cap V360 Cyg UU Her AB Leo W LMi UW Lib UW Lib UU Lup TX Oph AR Sgr WW Tau SV UMa	$\begin{array}{c} G2e-K2 & (M3)\\ G2e-G6 & (M2)\\ G0e-G6e & (M1)\\ G2e-K0 & (M3)\\ G0 & -G3\\ F5 & -G0e\\ F2 & -G0\\ F5e-G3e\\ G2e-K2e & (M3)\\ G2e-K0 & (M3)\\ G2 & -K0e & (M2)\\ F5e-G6e\\ F5e-G6\\ G4e-K2 & (M3)\\ G2e-G8 & (M4)\\ \end{array}$	4 4 5 5 0 2 0 6 10 4 1 2 5 6	$1-2 \\ 1-2 \\ 1-2 \\ 1-2 \\ 0-1 \\ 0-1 \\ 0-1 \\ 0-1 \\ 1-3 \\ 1-2 \\ 2-2 \\ 0-1 \\ 0-1 \\ 1-2 \\ 1-3 $	3 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	$\begin{array}{r} -191 \\ -252 \\ -165 \\ +193 \\ -135 \\ -250 \\ -131 \\ +182 \\ +66 \\ +163 \\ -130 \\ -165 \\ -100 \\ -110 \\ -90 \end{array}$	55 50 35 25 35 45 25 50 55 60 30 20 10 20 20	$\begin{array}{r} -183 \\ -234 \\ -167 \\ +188 \\ -123 \\ -235 \\ -114 \\ +175 \\ +70 \\ +176 \\ -122 \\ -147 \\ -88 \\ -119 \\ -86 \end{array}$

NOTES TO TABLES 2 AND 3

WY And	Max. = JD 2428408.9 + 108 d8E. On plates C 6348, C 6351, and Ce 3262 the stellar
	D1 and D2 sodium lines are well separated by velocity from the interstellar lines.
	Ce 3262 was taken and measured by R. F. Sanford. On this plate the Ha emission is
	symmetrically divided by a strong, deep absorption line.
BL Aqr	$Max. = JD 2430160 + 85^{d}E.$
TW Aql	P = 96? days. Sharp lines.
DY Aql	$Min_{\cdot} = JD_{\cdot}^{2428344} + 131^{\cdot}42E.$

35

.

ALFRED H. JOY

NOTES TO TABLES 2 AND 3-Continued

EZ Aql	Min. = JD 2428611.05 + 38 ^d 61E. Extensive light-observations by Taylor and Olivier (<i>Pub. Obs. U. Pennsylvania</i> , Vol. 6, Part 5, 1941). The spectrum is much like that of DF Cyg
KK Aql Z Aur	Max. = JD 2428308.4 + 8847E. $Max = JD 2432072 + 110496E$
AG Aur	$Max = JD 2457665 \pm 0.8426F$ (Schneller 1939)
TW Cam	$Min. = ID 2428647 + 85^{d}6E$
RX Cap	Min. = JD 2420741.4 + $67 d95E$. Only maximum phase was observed.
RU Cep	Max. = JD 2430649 + 109 $^{4}5E$. Observed by P. C. Keenan, M0 III ($Ap. J., 95, 462$, 1942). The Mount Wilson observations are poorly distributed and do not cover the
TZ Cen	Max = ID 2425840 + 83 dOE
AV Cvg	Max. = ID 2430659 + 89 $^{\circ}7E$. Except for λ 4077 and λ 4215 Sr II, the lines are weak.
DF Cyg	Min. = JD 2414883.5 + 49 4808 <i>E</i> . The spectrograms were all obtained at the brighter phases of the long-period variation of 782 days. The remarkable light-variations of this star were discovered and extensively observed by Miss M. Harwood (<i>Harvard</i> 1027)
V360 Cyg	Ann., 105, 521, 1937). Min - ID 2426067 \perp 63d26F. The emission lines are double with shortward com-
SS Com	ponent stronger; separation 160 km/sec. The absorption lines are weak.
SU Gem	P = 50.12 days with an additional long-period variation of 680.6 days. The absorp-
SU dem	T = 50.12 days, with an automational long-period variation of 009.0 days. The absorption lines show large changes in intensity.
SX Her	The spectroscopic behavior of this star resembles that of the Mira stars in some par-
	ticulars. Hydrogen emission occurs for about 30 days before and after maximum light.
	TiO bands attain considerable strength at minimum light.
UU Her	Alternating periods of 90.40 and 71.06 days have been found. The G band is usually
	absent. Spectral changes and velocity variations are small and uncertain. The star is
	nometric parallaxes is 0^{μ} (10). The observations were made at the times when the pe-
	riod of 90 days prevailed.
AC Her	Sanford (Mt. W. Contr., No. 424; Ap. J., 73, 364, 1931) found that during increasing
	light the hydrogen lines have emission edges. The velocity-curve shows a double maxi-
	mum corresponding to the double minimum of the light-curve. The spectral type at
	maximum is earlier than that of any other star in the list and has a large range $(FI-K4)$,
	although no $I i U$ bands appear. The G band shows remarkable changes with phase. L. Rosino ($A = 113, 60, 1051$) calls attention to the strength of the carbon bands
	during decreasing light and classifies the star as Rn at this phase
AB Leo =	Max. = ID 2428880 + $103^{d}2E$, A. Vyssotsky found emission lines of hydrogen in ob-
BD+20°2337	jective-prism spectra of this star. From Harvard plates Miss Hoffleit discovered light-
	changes which resemble those of the semiregular or RV Tauri variables. She deter-
	mined the elements used here. The light-curve seldom shows alternating bright and faint
	minima, but the period seems to hold, even though the epoch may shift. At times the
	ngnt-nuctuations become irregular and of small range. The bright lines are strong and persistent showing slow decrement shortward, but the type is too early to permit <i>TiO</i>
	bands. The star is evidently one of the semiregular variables of high velocity and mod-
	erate luminosity.
	Plate Ce 4231 was taken by R. F. Sanford. On this plate the emission at Ha is sym-
*	metrically divided by a narrow central reversal. In general, the absorption lines are
	sharp, and the spectrum resembles that of UU Her, but, on the plates showing the earli-
	est estimated spectral type, the lines seem weak, although no certain veiling effect is
W LMi	$Max = ID 2428303 + 117^{d}2E$ The light-changes and period are poorly determined
	The range of light-variation is large. The hydrogen emission lines are strong and per-
	sistent, but the enhanced lines are weak. This star should certainly be placed among
	the high-velocity stars.
UW Lib	P = 84.73 days. No epoch. This period does not seem to satisfy the velocity and spec-
III	trai variations. Small light-range.
U Lup	nard Bull. No 893 1933)
U Mon	Sanford (<i>Mt. W. Contr.</i> , No. 465; <i>Ap. J.</i> , 77, 120, 1933) found that the velocity-curve
	shows a double minimum, corresponding to the double maximum of the light-curve.
TT 0 1	Hydrogen emission and <i>TiO</i> bands were observed.
TT Oph	Min. = $JD 2428723 + 61^{\circ}08E$. This star, which was at first thought to be an eclipsing
	omary, is one of the best examples of the KV fauri type of variation. The light-



FIG. 1.—Spectra of semiregular variables. a, K2 (M3), TX Persei; b, F4, UU Herculis; c, G5 (M4), SV Ursae Majoris, strong titanium bands on G5 spectrum; d, G8e, RV Tauri, CH weak; e, KO, RV Tauri, CH strong; f, G6, TW Camelopardalis, ionized metallic lines strong; g, G2e, WY Andromedae, ionized metallic lines weak, slow decrement of bright lines, $H\epsilon$ weakened; h, G5e (M2), W Leonis Minoris, all absorption lines weak, $H\epsilon$ absent; i, G0e, AB Leonis, lines weak.

NOTES TO TABLES 2 AND 3-Continued

1 1 - 41 75 - 1 - 1

	minima are usually well defined and of nearly equal depth. Emission lines of hydrogen appear during increasing light and reach greatest intensity 2 days before maximum light. The velocity-curve shows definite correlation with the light-curve. No <i>TiO</i> bands have been observed. The enhanced lines are strong.
TX Oph	P = 138? days. The range in velocity and spectral type is small. The enhanced lines are strong and indicate the highest luminosity of the high-velocity stars.
UZ Oph TX Per	Min. = \overline{JD} 2422531.84 + 87 ⁴ 39 <i>E</i> . This star may belong to the high-velocity group. Max. = \overline{JD} 2428466 + 76 ⁴ 3 <i>E</i> .
R Sge	Sanford found (Mt . W . Contr., No. 481; $Ap. J.$, 79, 81, 1934) that the radial velocities show little correlation with the light-curve, but D. B. McLaughlin ($Ap. J.$, 94, 94, 1941) discovered that, by omitting velocities obtained when light-variations were irregular, a reasonable correlation could be determined. No <i>TiO</i> bands or emission lines were found. The G band strengthens at minimum light.
AR Sgr	Min. = JD 2426103 + 87487E (Harvard Ann., 113, 39, 1943). Observed minimum.
AI Sco	P = 71.78 days, with superposed period of 960 days.
R Sct	The appearance of <i>TiO</i> bands at spectral type G9 was noted (<i>Pub. A.S.P.</i> , 34, 349, 1922) in 1922. This fine example of RV Tauri variation has been thoroughly studied by D. B. McLaughlin (<i>Pub. Obs. U. Michigan</i> , 7, 57, 1938).
RV Tau	$\dot{Min.} = JD \ 2429290 + 7846E \ (Harvard Ann., 113, 49, 1943).$ Observed minimum. A superposed period of 1227 days has been suggested. The G band and the enhanced lines are strong, but the emission lines and TiO bands are weak and rarely seen.
WW Tau	The period varies from 113 to 138 days. The velocity range is small, but there is con- siderable variation in spectral type.
SV UMa	P = 76 days. The light-variations are quite irregular, and the period is variable. The star was spectroscopically observed in 1930 by R. O. Redman (<i>M.N.</i> , 92, 116, 1931) at Victoria. A series of seventeen spectrograms covering more than a cycle failed to show, at that time, the strong emission lines of hydrogen and the <i>TiO</i> bands observed later at Mount Wilson. A McDonald spectrogram in 1941 by P. C. Keenan was classified as K3p: Ia (<i>A p. J.</i> , 95, 463, 1942) with weak lines.
S Vul	Max. = JD 2423671.7 + 67 477E (Schneller, 1939). The period is variable. Velocity and spectral variations are small, but the strength of the G band shows large fluctua- tions with phase. The spectrum resembles that of cepheids of intermediate period.
V Vul	Sanford ($Mt.W.Contr.$, No. 481; $Ap. J.$, 79, 82, 1934) reported weak TiO bands but no emission.

The CH absorption is an outstanding feature of the stars of group 1, reaching its greatest strength at the times of later spectral type. At other phases the band becomes weak or disappears. In group 2, CH seldom attains great intensity. In all the stars, marked changes in the bands take place in a few days' time. The λ 4215 CN band has also been found for a short period preceding minimum in the luminous stars DF Cyg, SS Gem, U Mon, RV Tau, and SV UMa.

Emission lines of hydrogen occur, especially at times of increasing light, in a majority of the stars of both groups. The bright lines are stronger and more persistent in group 2. The decrement toward the violet is usually gradual. The bright hydrogen line $H\epsilon$ is often greatly reduced in intensity by the absorption of the H line of calcium (Fig. 1, g, h, and i).

With further observation, hydrogen emission or titanium bands may yet be found at favorable phases in some of the stars in which these features were not observed.

The irregular behavior of the stars makes it impossible to draw useful velocity-curves from scattered observations. The mean measured velocity range of 36 km/sec is somewhat less than that of the most luminous cepheids, but this may be due to periods of inactivity which occur from time to time among the semiregular variables. The mean velocity range is the same for both groups of Table 3.

In studies of variable stars the period of variation has usually been an important factor in the discussion. This parameter has rendered little help with the irregular stars discussed in this paper. Various correlations with period have been tried, but they have not seemed significant.

ALFRED H. JOY

SUBGROUPS

Since the stars of the present list were included largely on the basis of their spectral characteristics, considerable study was given to their spectroscopic behavior, in order to detect the presence of physically defined subgroups. Such an analysis points to a division (Table 3 and Fig. 3) into high- and low-velocity groups as the most natural and fruitful means of bringing together the stars of like physical characteristics. Only five stars of the list have residual velocities between 57 and 114 km/sec, and none are found between 70 and 86 km/sec. A value of 70 km/sec was set as the lower limit of the velocities of group 2. It is near the minimum frequency of velocities and corresponds well with the values used by Oort and others in separating stars of low and high velocity. If the maximum strength of the ionized lines (fifth column of Table 3) or that of the G band (fourth column) had been taken as criteria, the grouping would have been practically the same,



FIG. 2.—Galactic latitude and longitude of semiregular variables. Circles are high-velocity stars (Group 1); crosses, low-velocity stars (Group 2); and filled circles, cepheids with period > 20 days.

except that it might have been necessary to place TW Cam in group 2 with the highvelocity stars.

The evidence for two physical groups among these semiregular variables is strong in several respects: (1) The mean galactic latitudes of groups 1 and 2 (13° and 27°) indicate a difference in distribution (Fig. 2), although in neither group is the concentration toward the galactic equator as marked as in the δ Cephei variables, for which the average distance from the equator is less than 5° . (2) Mean proper motions determined by R. E. Wilson are 0".018 for thirteen stars of group 1 and 0".035 for seven stars of group 2. Since these values are, respectively, two and three times the mean proper motions of cepheids with periods greater than 20 days, it seems unlikely that either group has close kinetic relationship with the long-period cepheids. (3) Mean residual radial velocities (Table 3) without regard to sign: group 1, 28 km/sec; group 2, 154 km/sec. (4) A plot of radial velocities according to galactic longitude (Fig. 3) shows a distinct difference in the distribution of velocities in the two groups. The high velocities of group 2 are widely separated from those of group 1. A solar-motion solution for group 2 from the radial velocities indicates a group motion of 263 km/sec in nearly the same direction as that of RR Lyrae

stars¹² and the high-velocity R-type stars.¹³ The smaller velocities of group 1, unlike those of the δ Cephei stars, show little galactic-rotation effect. (5) The average spectral type of group 2 is slightly earlier than that of group 1: at maximum F9 for group 2, G2 for group 1; at minimum G7 and K0, respectively. (6) The ionized lines of metals are distinctly stronger in group 1, and the absorption spectrum is more clearly defined, indicating higher luminosity. (7) The G band (*CH*) reaches greater intensity in group 1, but this may be, in part, due to the effect of later spectral type in the low-velocity stars. (8) Emission lines of hydrogen are often found in both groups at certain phases but occur more frequently and in greater strength among the high-velocity stars (eleven of twentythree stars in group 1; thirteen of fifteen stars in group 2). (9) The double period with two unequal minima of light, typical of the more regular RV Tauri stars, seldom occurs in group 2.



FIG. 3.—Radial velocity and galactic longitude of semiregular variables. Circles are high-velocity stars (Group 1); crosses, low-velocity stars (Group 2). The solid curve shows the radial velocity of Group 2 with reference to the sun; the dashed curve is the theoretical galactic rotation effect having a maximum of 25 km/sec.

The stars of group 2 are doubtless of type II population and might be expected to resemble those of groups 4 and 5 of the globular clusters.¹⁴ This similarity prevails with regard to luminosity, period, and the occasional appearance of emission lines in our group 2 as compared with group 5 of the clusters. On the other hand, in the clusters the mean range of light-variation is smaller, 0.8 mag. compared to 2.2 mag. Also, in the clusters the G band is stronger and the spectral type somewhat later, although the *TiO* bands apparently are less frequent.

High-luminosity variables such as those of group 4 in the clusters seem to be few or absent among the high-velocity stars of the galaxy. Perhaps TX Oph may be an exception. Several of the low-velocity stars of our group 1 are similar to those of group 4 in the

- ¹² J. H. Oort, B.A.N., 8, 337, 1939; O. Struve, Pub. A.S.P., 62, 217, 1950.
- ¹³ N. W. McLeod, Ap. J., 105, 390, 1947.
- ¹⁴ A. H. Joy, Ap. J., 110, 105, 1949.

clusters, except that the group 1 stars are later in spectral type and have strong G bands, while CH in group 4 of the clusters is weak or absent.

From these considerations it seems evident that these semiregular variables may well comprise two groups based on distribution, motions, luminosity, or the intensity of the G band of *CH*. The relationship of these two groups to the variables of the δ Cephei class, on the one hand, and to the red M-type variables, on the other, is yet uncertain. Group 2 definitely should be included in population II, but the place of group 1 is not clear. Since the peculiar motions of group 1, which includes many of the best-known RV Tauri variables, such as U Mon, R Sct, and V Vul, are large as compared with the long-period cepheids but yet are much smaller than is generally found for type II stars, and their galactic latitude agrees with neither, it seems best, at present, to consider these stars as an anomalous group of population I stars. Possibly they may be related to the widely scattered giant K stars whose rapid velocities were first found by W. W. Campbell.

Most of the stars of group 2 are irregular variables which cannot meet the rigid requirements usually set up for the RV Tauri class. TX Oph and RX Cap have most of the RV Tauri characteristics and may correspond to the RV Tauri group in the clusters.

ABSOLUTE MAGNITUDE AND DISTANCE

On account of the great distances, trigonometric parallaxes of these stars are few and unreliable. Spectroscopic estimates of the visual absolute magnitude have been published for SX Her¹¹ (-1.5) and U Mon¹⁵ (-2.0), and comparisons with the spectra of cepheids of the same spectral type indicate clearly that the luminosity of the brightest stars is as high as, or perhaps higher than, that of any of the cepheids. This conclusion is confirmed by the distances determined from the strength of the interstellar lines of sodium¹⁶ in three of the less luminous stars (WY And, AG Aur, and UU Her), from which absolute magnitudes brighter than -2.2 may be deduced. In the globular clusters the absolute photographic magnitudes of the RV Tauri and semiregular groups are -3.0 and -1.5, respectively. Using the proper motions of sixteen stars (eleven belonging to these groups), P. P. Parenago¹⁷ found a mean absolute visual magnitude of -0.4, but this value is of low weight on account of the small proper motions (mean about 0".02) involved.

Rosino² has classified eleven of the stars (eight of group 1 and three of group 2) and assigned the luminosity class Ia or Ib, indicating visual absolute magnitudes as high as -4 or -5 according to the Yerkes system.

While none of these methods of determining absolute magnitude are precise, they indicate that the RV Tauri and related stars are among the most highly luminous stars and that they are comparable with the cepheids of similar spectra and periods of from 20 to 40 days for which Shapley's period-luminosity curve gives photographic absolute magnitudes as bright as -3.0.

Judging by the strength of their ionized lines, many of the stars of group 1 appear to be somewhat more luminous than the brightest cepheids. Absolute photographic magnitudes -3.0 for group 1 and -1.5 for group 2 seem to be reasonable mean values.

Neglecting space absorption, the distances of the stars of group 1, as determined from this value of the absolute magnitude and their median apparent magnitudes, average about 7 kpc. Since only twelve stars of this group are within 10° of the galactic equator, large corrections to their apparent magnitudes on account of interstellar absorption are probably limited to a few stars of the group. Some of the stars, such as BL Aql, SX Her, TT Oph, and UZ Oph are distant 2.5–5 kpc from the galactic plane. With these assumptions, the mean distance of the stars of group 2 is about 4 kpc.

¹⁵ W. S. Adams et al., Mt. W. Contr., No. 511; Ap. J., 81, 225, 1935.

¹⁶ A. H. Joy, Pub. A.S.P., 46, 51, 1934.

¹⁷ A.J.U.S.S.R., 11, 95, 1934.

SEMIREGULAR VARIABLE STARS

CONCLUSIONS

As a result of spectroscopic observations it is evident that the semiregular variables with pseudo-periods between 39 and 144 days and spectral types F, G, and K do not form a homogeneous group. In motion, luminosity, and spectral behavior no standard pattern is rigorously followed. The RV Tauri stars, well known to observers of variable stars for their irregular light-changes, are the accepted models for the group, but wide deviations in the behavior and characteristics of the individual stars are present.

On the basis of velocity, of absolute magnitude as determined by the strength of the ionized lines, and of the maximum intensity of the G band (CH), the thirty-eight stars observed may be separated into two groups, group 1 having velocities less than 70 km/sec, brighter absolute magnitudes, and greater maximum intensities of the G band. Within these two groups marked differences among the stars are found.

The stars of group 2 evidently belong to the type II population and correspond closely with the semiregular variables of the globular clusters. In luminosity and in radialvelocity variations the members of group 1 are similar to the long-period cepheids, but they are more scattered with reference to the plane of the galaxy and fail to show clearly the effect of galactic rotation. Also, these stars frequently have hydrogen emission and titanium oxide bands which have not been found in the cepheids. The place of the group 1 stars with reference to Baade's population types is not yet clear.

The veiling and absorption effects of titanium and carbon bands must contribute toward dimming the light of the semiregular stars at certain phases. On the other hand, increases in light may be, in part, due to flare effects, which are accompanied by hydrogen emission and a marked diminution in the visibility of the absorption spectrum at times in many of the stars. Such outbursts must be quite different in size and duration from those encountered in the faint dwarfs of extremely low temperatures.