# THE SEMIREGULAR VARIABLE STARS OF THE RV TAURI AND RELATED CLASSES 

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#### Abstract

Observations.-A spectroscopic survey of the F, G, and K semiregular variables was based on Mount Wilson spectrograms of thirty-eight stars.

Physical characteristics.-Strong ionized lines indicate that many of the stars are as bright as, or brighter than, the long-period cepheids. The mean spectral type is about G0 at maximum and K0 at minimum light. Titanium oxide bands occur in twenty-one stars and are seen on spectra as early as G4. The mean radial-velocity range during a cycle is $36 \mathrm{~km} / \mathrm{sec}$, but irregularities are so great that mean velocity-curves are impossible. The relation of velocity changes to light-variations is similar to that of the cepheids. Hydrogen emission is present in twenty-five stars at times of increasing light. The G band of CH becomes stronger with decreasing light and later spectral type.

Subdivisions.-If the stars are divided according to radial velocity, the fast and slow groups are found to differ also in mean luminosity, spectral type, intensity of carbon bands, and distribution in the sky. The fast-moving group is undoubtedly of type II population, but the exact relationship of the slow group to Baade's populations is uncertain.


In order to investigate the spectroscopic characteristics of the semiregular variablet with intermediate spectral types and periods, thirty-eight stars have been observed as Mount Wilson with low dispersion. Nearly all the observable RV Tauri variables and most of the irregular variables of types $\mathrm{F}, \mathrm{G}$, and K have been included.

Among variable-star observers there is general agreement as to the standard behavior of RV Tauri variables, but, unfortunately, few stars meet all the requirements over any considerable length of time. The changes and irregularities are often most confusing. Cyclic variations are seldom repeated exactly, and the statistical use of suggested periods is unsatisfactory.

The strange fluctuations of light of these variables have been investigated by numerous observers. Particularly valuable results have been obtained from the Harvard photographs covering periods of time sufficiently long to show the extreme irregularities at different epochs.The painstaking work of Payne-Gaposchkin, Brenton, and Gaposchkin ${ }^{1}$ giving light-curves for fourteen RV Tauri stars is most illuminating.

General data pertaining to the stars observed are in Table 1. The photographic magnitudes are mostly from Kukarkin and Parenago's Catalogue of Variable Stars. The classification according to Payne-Gaposchkin, Brenton, and Gaposchkin; Kukarkin and Parenago; and L. Rosino ${ }^{2}$ ("RV" = RV Tauri class, "SR" = semiregular, "LP" = long period) is indicated in the eighth to the tenth columns. From observations of the lightchanges, all three sources assign thirteen stars of the list to the RV Tauri class. Two place six other stars in this class, while for five stars the RV Tauri designation is from one only of these sources. The remaining thirteen stars are semiregular variables which are not recognized as RV Tauri stars, although in period, light-range, and spectroscopic characteristics they seem to be rather closely related to them. One star, AB Leonis ( $\mathrm{BD}+20^{\circ} 2337$ ), is the new variable whose light-changes were found by Miss D. Hoffleit ${ }^{3}$ to be of the RV Tauri type.

[^0]Five stars of the list-DF Cyg, SU Gem, U Mon, AI Sco, and RV Tau-have longperiod light-variations of 690-2320 days superposed upon the short-period ( $50-90$ days) light-curves. For U Mon, R. F. Sanford ${ }^{4}$ discovered a variation of $40 \mathrm{~km} / \mathrm{sec}$ in the $\gamma$ velocity in a period of 2320 days, and the same period was later found by E. Loreta ${ }^{5}$ in

TABLE 1
Data concerning Variables Observed

| Star | $\begin{aligned} & \text { Designa- } \\ & \text { tion } \end{aligned}$ | $l$ | $b$ | $m_{\text {ps }}$ |  | $\begin{aligned} & \text { Period } \\ & \text { (Days) } \end{aligned}$ | Class |  |  | $\begin{gathered} \text { No. } \\ \text { Plates } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Max. | Min. |  | Gap. | K. and P. | Rosino |  |
| WY And. | 233647 | $79^{\circ}$ | $-14^{\circ}$ | 9.5 | 10.6 | 109 |  | SR | SR | 10 |
| BL Aqr. | 210902 | 17 | -33 | 11.0 | 12.3 | 85 |  | SR |  | 8 |
| TW Aql. | 194613 | 20 | -8 | 10.6 | 12.7 | 96: |  | SR: |  | 5 |
| DY Aql. | 194111 | 357 | -19 | 10.2 | 12.9 | 131 | RV | RV |  | 7 |
| EZ Aql. | 193408 | 14 | -8 | 12.4 | 14.6 | 39 | RV | RV | RV | 3 |
| KK Aql. | 194314 | 20 | $-7$ | 11.5 | 12.8 | 89 | RV | SR |  | 7 |
| Z Aur. | 055353 | 127 | +16 | 9.7 | 12.9 | 111 |  | LP |  | 9 |
| AG Aur. | 062047 | 135 | +17 | 10.0 | 13.1 | 98 |  | RV | SR | 16 |
| TW Cam. | 041257 | 116 | + 6 | 10.4 | 11.5 | 86 |  | RV | RV | 6 |
| RX Cap... | 200913 | 358 | -26 | 11.6 | 13.7 | 68 | RV | RV | RV | 5 |
| RU Cep. | 010884 | 91 | +22 | 9.3 | 10.4 | 109 |  | SR |  | 7 |
| TZ Cep. | 001973 | 88 | +11 | 9.8 | 12.0 | 83 |  | SR |  | 6 |
| AV Cyg. | 191629 | 30 | + 6 | 11.2 | 13.0 | 90 | RV | SR |  | 7 |
| DF Cyg. | 194542 | 44 | +8 | 10.8 | 15.2 | 50 | RV | RV | RV | 10 |
| V360 Cyg. | 210630 | 45 | -12 | 10.8 | 13.3 | 63 | RV | RV | RV | 10 |
| SS Gem. | 060222 | 156 | +3 | 9.2 | 10.7 | 89 | RV | RV | RV | 13 |
| SU Gem. | 060727 | 152 | $+6$ | 10.7 | 13.2 | 50 |  | RV | RV | 5 |
| SX Her. | 160325 | 9 | +45 | 9.0 | 11.1 | 103 |  | SR | SR | 21 |
| UU Her. | 163238 | 28 | +41 | 8.5 | 10.6 | 71 | RV | SR | SR | 18 |
| AC Her. | 182621 | 18 | +13 | 7.1 | 9.4 | 75 | RV | RV | RV | 73 |
| AB Leo. | 092720 | 179 | +46 | 10.7 | 13.2 | 103 |  |  |  | 12 |
| W LMi. | 103926 | 176 | +63 | 11.3 | 14.5 | 117 |  | LP |  | 13 |
| UW Lib | 142516 | 303 | +39 | 10.4 | 11.0 | 85 |  | SR: |  | 17 |
| U Lup.. | 155429 | 313 | +16 | 10.8 | 13.2 | 87 |  | SR |  | 7 |
| U Mon. | 072609 | 194 | + 6 | 6.8 | 8.5 | 92 | RV | RV | RV | 68 |
| TT Oph. | 164403 | 349 | +27 | 9.8 , | 11.7 | 61 | RV | RV | RV | 14 |
| TX Oph. | 165905 | 352 | +25 | 9.8 | 12.1 | 138: | RV | RV: | SR | 11 |
| UZ Oph. | 171707 | 356 | +22 | 10.5 | 13.1 | 87 | R V | RV | RV | 9 |
| TX Per. | 024136 | 116 | -19 | 11.1 | 13.7 | 76 |  | SR |  | 10 |
| S Sge...... | 200916 | 26 | -11 | 9.0 | 11.5 | 71 | RV | RV | RV | 29 |
| AR Sgr. | 185323 | 340 | -14 | 9.6 | 11.5 | 88 | RV | RV |  | 8 |
| AI Sco. | 174933 | 325 | -6 | 9.4 | 12.6 | 72 |  | RV | RV |  |
| R Sct. | 184205 | 355 | -3 | 6.5 | 9.6 | 144 | RV | RV | RV | 12 |
| RV Tau. | 044025 | 143 | -11 | 9.8 | 13.3 | 79 | RV | RV | RV | 18 |
| WW Tau. | 035529 | 133 | -16 | 9.9 | 12.9 | 125: |  | SR |  | 6 |
| SV UMa... | 104055 | 119 | +55 | 9.8 | 11.3 | 76 |  | SR | SR | 11 |
| S Vul. | 194427 | 31 | 0 | 10.1 | 11.4 | 69 | RV | SR |  | 18 |
| V Vul. | 203226 | 37 | - 9 | 9.0 | 11.0 | 76 | RV | RV | RV | 31 |

[^1]the light-variations. On account of insufficient spectroscopic observations, this important correlation between light and velocity measures has not been traced in other stars. These five stars have a short mean double period of 69 days, and their mean total light-range is over 3 mag. They are high-luminosity stars with mean galactic latitude of $7^{\circ}$. Emission is weak or absent.

## SPECTROSCOPIC OBSERVATIONS

Our knowledge of the detailed spectroscopic behavior of the RV Tauri variables is based on the extensive studies of AC Herculis, ${ }^{6}$ U Monocerotis, ${ }^{4}$ R Sagittae, ${ }^{7}$ and V Vulpeculae ${ }^{8}$ by R. F. Sanford at Mount Wilson and of R Scuti ${ }^{9}$ by D. B. McLaughlin at Michigan. Their observations cover the whole period of light-variations and indicate that the fundamental behavior is related to that of the cepheids. Under the most favorable circumstances the double period is clearly seen in spectrographic and radial-velocity changes, ${ }^{10}$ as well as in the light-variations.
L. Rosino ${ }^{2}$ has recently estimated the spectral type and luminosity class of thirteen of the stars of Table 1. McLaughlin and Rosino have added greatly to the value of their spectrographic data by determining simultaneous light-curves.

Spectra of two of the variables of Table 1 obtained at Mount Wilson have already been described. ${ }^{11}$ Data for the hitherto unpublished Mount Wilson observations are in Table 2, together with the spectrographic results for each plate. The photometric elements (mostly from the Variable Star Catalogue [1948], by Kukarkin and Parenago) used in computing the phases (fourth column) are in the notes following Table 3. The letters in the table indicate whether the phases are reckoned from maximum (M) or from minimum (m). In the last four columns are rough intensity estimates of the strongest emission lines, the titanium oxide bands, the general absorption effect of CH at the G band, and (M II) the relative strength of the lines of ionized metallic atoms as compared with those of neutral atoms. A dash is used to indicate that the photograph was not properly exposed to show the feature in question, but a zero indicates that the feature is not visible, even though the plate is competent to show it.

These observational results are summarized in Table 3, where the stars are separated into low- and high-velocity groups. In the last three columns are the mean or $\gamma$ velocity, the approximate velocity range, and the residual velocity, assuming the usual solar motion of $20 \mathrm{~km} / \mathrm{sec}$.

The spectral types generally vary from about G0 somewhat before maximum light to about K0 near minimum. Near minimum light the titanium oxide bands appear in spectra which otherwise would be classed as G or K . The classification on the basis of the TiO bands is given in parentheses. This peculiar phenomenon, which was first noticed in R Sct, ${ }^{11}$ seems to be characteristic of these stars and is especially outstanding among the members of group 2. In SV UMa an intensity of 4 in the titanium bands is observed on two spectrograms of types G5 and G8.

Rosino ${ }^{2}$ has noted the presence of carbon bands in AC Her. On the Mount Wilson plates, as reported by Sanford, ${ }^{6}$ the G band attains great strength as the light decreases to minimum. The $\lambda 4215 C N$ band and the $\lambda 4737 C_{2}$ bands are faintly visible for a few days preceding minimum. Doubtless the total carbon absorption is responsible for a part of the loss of light. The small change in color index ${ }^{1}$ at different phases indicates that the cyanogen absorption plays a minor role.

[^2]TABLE 2
Spectroscopic Observations of RV Tauri and Semiregular Variables

| Star | Plate | $\begin{aligned} & \text { Date } \\ & \text { JD } 24 \end{aligned}$ | Phase <br> (Days) | SpecTRUM | Velocity <br> (Km/SEC) | $\begin{gathered} \text { DISP. } \\ \mathrm{AT} H_{\gamma} \\ \left(\mathrm{A} / \mathrm{M}_{\mathrm{M}}\right) \end{gathered}$ | Intensity |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Em. | TiO | CH | M II |
| WY And. | $\gamma 19195$ | 26993 | M 108 | G6 | -176 | 70 | 0 | 0 | 2 | 1 |
|  | 19262 | 7021 | 27 | G8 | -191 | 70 | 0 | 0 | 2 | 1 |
|  | C 6348 | 7431 | 2 | -e | -192 | 35 | 4 | 0 | - | - |
|  | 6351 | 7432 | 3 | -e | -207 | 35 | 3 | 0 | - | - |
|  | $\gamma 23000$ | 9894 | 72 | K2 | -188 | 70 | 0 | 2 | 2 | 1 |
|  | 23144 | 9932 | 1 | G8e | -185 | 70 | 3 |  | 1 | 3 |
|  | Ce 3262 | 31038 | 19 | - | -197 | 20 | 1 | - | - | - |
|  | E 1455 | 1662 | 99 | G2e | -179 | 70 | 3 | 0 | 1 | 2 |
|  | 1492 | 1698 | 26 | G3e | -197 | 70 | 1 | 0 | 1 | 2 |
|  | $\gamma 27057$ | 1724 | 52 | K2 | -198 | 70 | 0 | 3 | 1 | 2 |
|  |  |  |  |  | -191 |  |  |  |  |  |
| BL Aqr . | ¢ 19769 | 27287 | M 17 | G4 | + 34 | 110 | 0 | 0 | , | 2 |
|  | C 7521 | 9826 | - 6 | G5 | + 46 | 110 | 0 | 0 | 2 | 2 |
|  | $\gamma 22856$ | 9857 | 37 | G4 | + 36 | 70 | 0 | 0 | 2 | 2 |
|  | E 209 | 30209 | 49 | K0 | + 52 | 110 | 0 | 1 | 3 | 1 |
|  | $\gamma 23640$ | 0220 | 60 | G5 | +39 $+\quad 51$ | 110 | 0 | 1 | 2 | 2 |
|  | E 1441 | 1638 | 33 | G8 | + 51 | 110 | 0 | 2 | 2 | 2 |
|  | - 1463 | 1665 | 60 | G8 | + 55 | 70 | 0 | 2 | 2 | 2 |
|  | r 27922 |  | 23 | G2 | + 47 | 110 | 0 | 0 | 1 | 2 |
|  |  |  |  |  | $+45$ |  |  |  |  |  |
| TW Aql. |  | 27018 | - | G5 |  | 110 |  |  |  |  |
|  | $\gamma 21862$ | 9413 | - - | G6 | + 34 | 70 | 0 | 0 | 3 | 3 |
|  | 22855 | 9857 | - | G0 | + 35 | 70 | 0 | 0 | 0 | 3 |
|  | 23639 | 30220 | - | G4 | + 2 | 110 | 0 | 0 | 3 | 3 |
|  | E 268 | 0266 | - | K0 | + 20 | 110 | 0 | 0 | 3 | 3 |
|  |  |  |  |  | $+21$ |  |  |  |  |  |
| DY Aql. | C 7490 | 29766 | m 109 | K0 | + 3 | 110 | 0 | 3 | 2 | 1 |
|  | r 22742 | 9804 | 15 | G8 | 0 | 110 | 0 | 0 | 3 | 2 |
|  | C 7520 | 9826 | 37 | K0 | + 30 | 110 | 0 | 2 | 3 | 2 |
|  | E 39 | 9896 | 107 | - | - | 110 | 0 | 2 | - | - |
|  |  | 9913 | 124 | G5e | + 14 | 110 | 5 | 0 | 2 | 3 |
|  | 146 | 30147 | 95 | G6 | + 24 | 110 | 0 | 2 | 2 | 3 |
|  | 259 | 0251 | 68 | K0 | + 25 | 110 | 0 | 1 | 4 | 2 |
|  |  |  |  |  | + 15 |  |  |  |  |  |
| EZ Aql. | C 734873517539 | 29452 | m 31 | G5 | - | 110 | 0 | 0 | 2 | 2 |
|  |  | 9471 |  | G8 | + 48 | 110 | 0 | 0 | 3 | 3 |
|  |  | 9853 | 7 | K0 | + 49 | 110 | 0 | 0 | 2 | 3 |
|  |  |  |  |  | + 48 |  |  |  |  |  |
| KK Aql. | $\begin{array}{r} \text { C } 6168 \\ 6445 \\ \gamma 21160 \\ \mathrm{E} \quad 255 \\ \gamma 27066 \\ 27703 \\ 27919 \end{array}$ |  | M 43 | G6 | -245 | 110 | 0 | 1 | 1 | 1 |
|  |  | 7611 | - 13 | - | -256 | 70 | 0 | 0 | - | 2 |
|  |  | 8734 | 72 | G2e | -280 | 110 | 4 | 0 | 1 | 2 |
|  |  | 30250 | 80 | G4 | -231 | 110 | 0 | 0 | 2 | 2 |
|  |  | 1727 | 49 | G6 | -246 | 110 | 0 | 2 | 1 | 2 |
|  |  | 1980 | 36 | G4 | -240 | 110 | 0 | 1 | 1 | 1 |
|  |  | 2052 | 19 | G6 | -262 | 110 | 0 | 0 | 0 | 1 |
|  |  |  |  |  | -252 |  |  |  |  |  |

TABLE 2-Continued

| Star | Plate | $\begin{aligned} & \text { Date } \\ & \text { JD } 24 \end{aligned}$ | Phase <br> (Days) | Spectrom | Velocity <br> (Km/Sec) | $\begin{gathered} \text { Disp. } \\ \text { AT } H_{\gamma} \\ \left(\mathrm{A} / \mathrm{Mm}_{\mathrm{M}}\right) \end{gathered}$ | Intensity |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Em. | TiO | CH | M II |
| Z Aur. | $\gamma 23030$ | 29898 | M 46 | G4e | -155 | 70 | 5 | 0 | 2 | 1 |
|  | 23163 | 9945 | 93 | G6e | -187 | 110 | 4 | 0 | 2 | 2 |
|  | 23339 | 30071 | 8 | G2 | -157 | 110 | 0 | 0 | 1 | 1 |
|  | E 258 | 0251 | 65 | G2e | -152 | 110 | 3 | 0 | 1 | 1 |
|  | r 23842 | 0302 | 5 | G0e | -154 | 70 | 3 | 0 | 1 | 1 |
|  | - 23929 | 0334 | 37 | G0 | -160 | 110 | 0 | 0 | 1 | 1 |
|  | 27176 | 1755 | 17 | G5e | -157 | 110 | 5 | 1 | 1 | 1 |
|  | 27503 | 1894 | 45 | G4e | -168 | 110 | 4 | 2 | 1 | 1 |
|  | E 1688 | 1922 | 73 | G3e | -170 | 110 | 2 | 0 | 2 | 2 |
|  |  |  |  |  | -165 |  |  |  |  |  |
| AG Aur. | C 4695 | 25305 | M 30 | G6 | +182 | 70 | 0 | 0 | 1 | 2 |
|  | - 4717 | 5342 | 67 | - | - | 70 | 0 | 2 | - | 1 |
|  | 4729 | 5344 | 69 | - | +196 | 70 | 0 | 2 | - | 1 |
|  | 5364 | 5956 | - 92 | G8e | +199 | 70 | 2 | 0 | 2 | 2 |
|  | 5568 | 6256 | 97 | G4e | +190 | 70 | 1 | 0 | 2 | 2 |
|  | 5584 | 6267 | 10 | G4e | +190 | 70 | 1 | 0 | 1 | 2 |
|  | 5602 | 6283 | 26 | G4 | +192 | 70 | 0 | 1 | 1 | 1 |
|  | 5624 | 6311 | 54 | G8 | +206 | 70 | 0 | 3 | 1 | 1 |
|  | 5664 | 6340 | 83 | G2e | +197 | 35 | 5 | 0 | 2 | 1 |
|  | V 5665 | 6340 | 83 | G2e | +195 | 70 | 5 | 0 | 1 | 1 |
|  | V 94 | 6647 | 95 | G5e | +195 | 35 | 2 | 0 | 2 | 2 |
|  | C 6347 | 7403 | 82 | - | +201 | 35 | 4 | - | - |  |
|  | 6349 | 7431 | 12 | G4e | +186 | 70 | 4 | 0 | 1 | 2 |
|  | $\gamma 27177$ | 31756 | 12 | G4e | +183 | 110 | 4 | 0 | 1 | 2 |
|  | 27504 | 1894 | 53 | K0 | +189 | 110 | 0 | 1 | 2 | 1 |
|  | E 1689 | 1922 | 81 | G8 | +200 | 110 | 0 | 2 | 2 | 1 |
|  |  |  |  |  | +193 |  |  |  |  |  |
| TW Cam. | $\gamma 23137$ | 29927 | m 82 | G8 | - 69 | 110 | 0 | 0 | 0 | 3 |
|  | 23197 | 9957 | 27 | G8 | - 44 | 110 | 0 | 0 | 1 | 3 |
|  | C 7642 | 9971 | 41 | G5 | - 51 | 70 | 0 | 0 | 1 | 3 |
|  | E 257 | 30250 | 63 | G2 | - 59 | 110 | 0 | 0 | 1 | 3 |
|  | $\gamma 27171$ | 1754 | 26 | G3 | - 61 | 70 | 0 | 0 | 0 | 3 |
|  | 27971 | 2076 | 6 | G4 | - 40 | 110 | 0 | 0 | 1 | 3 |
|  |  |  |  |  | - 55 |  |  |  |  |  |
| RX Cap. |  |  |  |  | -135 | 110 | 0 | 0 | 0 | 1 |
|  | $\gamma 22848$ | 9856 | 10 | G0 | -122 | 110 | 0 | 0 | 1 | 2 |
|  | 23132 | 9927 | 13 | G3 | -148 | 110 | 0 | 0 | 1 | 2 |
|  | 23509 | 30180 | 62 | G2 | -156 | 110 | 0 | 0 | 1 | 1 |
|  | 26939 | 1696 | 15 | G0 | -135 | 110 | 0 | 0 | 0 | 2 |
|  |  |  |  |  | -135 |  |  |  |  |  |
| RU Cep. | $\gamma 22107$ | 29505 | M 62 | - | - 13 |  |  |  |  | 1 |
|  | 22199 | 9560 | 7 | - | - 18 | 70 | 0 | 0 | - | 2 |
|  | 22415 | 9647 | 94 | K0 | - 4 | 70 | 0 | 1 | 1 | 2 |
|  | 23027 | 9898 | 16 | - | - 17 | 70 | 0 | 2 | - | 2 |
|  | 23029 | 9898 | 16 | K2 | - 17 | 70 | 0 | 2 | 2 | 1 |
|  | 27170 | 31754 | 11 | K0 | -18 | 35 | 0 | 1 | 1 | 2 |
|  | 27924 | 2053 | 91 | G6 | - 8 | 70 | 0 | 2 | 2 | 1 |
|  |  |  |  |  | - 12 |  |  |  |  |  |
| TZ Cep. | $\gamma 19188$ | 26992 | $\text { M } 74$ | K0e |  |  |  | 0 | 3 |  |
|  | 21971 | 9450 | $42$ | G6 | - 5 | 110 | 0 | 2 | 2 | 3 |

TABLE 2-Continued

| Star | Plate | $\begin{aligned} & \text { Date } \\ & \text { JD } 24 \end{aligned}$ | $\begin{aligned} & \text { Phase } \\ & \text { (Days) } \end{aligned}$ | $\begin{aligned} & \text { Spec- } \\ & \text { TRUM } \end{aligned}$ | Velocity <br> (Km/Sec) | $\begin{gathered} \text { Disp. } \\ \text { AT } H \gamma \\ \left(\mathrm{~A} / \mathrm{M}_{\mathrm{M}}\right) \end{gathered}$ | Intensity |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Em. | TiO | CH | M II |
| TZ Cep. | $\gamma 23028$ | 29898 | M 75 | G8e | - 7 | 70 | 4 | 1 | 3 | 3 |
|  | 23136 | 9927 | - 21 | K1 | 0 | 110 | 0 | 2 | 2 | 2 |
|  | 23636 | 30219 | 64 | K2e | + 4 | 110 | 3 | 1 | 3 | 1 |
|  | 27974 | 2077 | 13 | K0 | + 6 | 110 | 0 | 0 | 0 | 1 |
|  |  |  |  |  | - 5 |  |  |  |  |  |
| AV Cyg. | $\gamma 18899$ | 26878 | M 77 | G4 | - 28 | 70 | 0 | 0 | 3 | 1 |
|  | C 7305 | 9410 | 8 | G3e | - 16 | 110 | 3 | 0 | 3 | 3 |
|  | 7549 | 9855 | 4 | G2e | - 30 | 110 | 3 | 0 | 3 | 2 |
|  | र 23453 | 30151 | 31 | G6 | - 11 | 110 | 0 | 0 | 3 | 3 |
|  | E 1416 | 1600 | 45 | G0e | - 32 | 110 | 1 | 0 | 2 | 2 |
|  | $\gamma 26744$ | 1633 | 78 | G3 | - 19 | 70 | 0 | 0 | 2 | 2 |
|  | C 7708 | 1958 | 44 | G2e | - 28 | 110 | 2 | 0 | 3 | 2 |
|  |  |  |  |  | --23 |  |  |  |  |  |
| DF Cyg. |  | 26401 | m 12 | K0 | - 5 | 110 | 0 |  |  |  |
|  | C 5751 | 6495 | 7 | K2 | + <br> +4 | 70 | 0 | 0 | 1 | 3 |
|  | 5758 | 6516 | 28 | G6 | - 10 | 70 | 0 | 0 | 1 | 3 |
|  | 5841 | 6606 | 18 | K2 | - 35 | 110 | 0 | 0 | 3 | 3 |
|  | 7064 | 8702 | 23 | K4 | - 7 | 110 | 0 | 0 | 3 | 3 |
|  | 7086 | 8731 | 2 | K0 | + 8 | 110 | 0 | 0 | 1 | 3 |
|  | 7100 | 8763 | 34 | G6 | - 9 | 110 | 0 | 0 | 2 | 2 |
|  | $\gamma 21218$ | 8793 | 14 | G8 | - 4 | 110 | 0 | 0 | 3 | 3 |
|  | 21231 | 8821 | 42 | G8 | + 7 | 110 | 0 | 0 | $4$ | 3 |
|  | C 7193 |  | 16 | G5 | - 16 | 110 | 0 | 0 | 3 | 3 |
|  |  |  |  |  | - 5 |  |  |  |  |  |
| V360 Cyg. | C 7507 | 29806 | m 57 | F5 | -260 | 110 | 0 | 0 | 0 |  |
|  | r 22758 | 9824 |  | F8e | -247 | 110 | 1 | 0 | 1 | 1 |
|  | C 7540 | 9853 | 40 | G0 | -238 | 110 | 0 | 0 | 0 | 1 |
|  | E 40 | 9896 | 20 | G0e | -238 | 110 | 2 | 0 | 0 | 2 |
|  | 313 | 30297 | 41 | F8 | -264 | 110 | 0 | 0 | 1 | 1 |
|  | 1417 | 1600 | 16 | F5 | -258 | 110 | 0 | 0 | 0 | 1 |
|  | 1433 | 1635 | 51 | G0 | -255 | 70 | 0 | 0 | 1 | 2 |
|  | r 27056 | 1724 | 13 | F8e | -240 | 110 | 1 | 0 | 0 | 1 |
|  | 27173 | 1755 | 44 | G0e | -264 | 110 | 1 | 0 | 0 | 1 |
|  | 27920 | 2052 | 25 | F5 | -281 | 110 | 0 | 0 | 0 | 2 |
|  |  |  |  |  | -250 |  |  |  |  |  |
| SS Gem. | C 1677 | 23179 | m 36 | G5 | + 23 | 70 | 0 | 0 | 3 | 2 |
|  | C 3238 | 4249 | - 35 | - | + 30 | 70 | 0 | 0 | - | 2 |
|  | 3661 | 4539 | 57 | G5 | - 19 | 70 | 0 | 0 | 2 | 3 |
|  | 4221 | 4984 | 55 | G4 | $+\quad 9$ | 70 | 0 | 0 | 3 | 2 |
|  | 4560 | 5217 | 20 | G8 | - 17 | 70 | 0 | 0 | 4 | 2 |
|  | 4740 | 5347 | 61 | G4 | - 14 | 70 | 0 | 0 | - | 2 |
|  | 5610 | 6285 | 17 | G5 | - 14 | 35 | 0 | 0 | 3 | 2 |
|  | 5630 | 6312 | 44 | G2 | - 19 | 70 | 0 | 0 | 1 | 3 |
|  | 5647 | 6316 | 48 | G0 | -15 | 70 | 0 | 0 | 2 | 2 |
|  | r 17978 | 6322 | 54 | G2 | - 8 | 70 | 0 | $0$ |  | 3 |
|  | C 5652 | 6338 | 70 | G0 | - 7 | 70 | $0$ | $0$ | $\begin{aligned} & 2 \\ & 1 \end{aligned}$ | 2 |
|  | $5674$ | $6342$ | $74$ | G0 | - 5 | $70$ | $0$ | $0$ | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ | 2 |
|  | $\gamma 18035$ | 6346 | 78 | G2 | - 23 | 70 | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ | $0$ | 1 | 2 |
|  |  |  |  |  | - 6 |  |  |  |  |  |

TABLE 2-Continued

| Star | Plate | $\begin{aligned} & \text { Date } \\ & \text { JD } 24 \end{aligned}$ | Phase <br> (Days) | Spectrum | Velocity <br> (Km/Sec) | $\begin{gathered} \text { DISP. } \\ \text { AT } H_{\gamma} \\ \left(\mathrm{A} / \mathrm{MM}_{\mathrm{M}}\right) \end{gathered}$ | Intensity |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Em. | TiO | CH | M II |
| SU Gem. | $\gamma 21440$ | 29176 | - | G2 | + 16 | 110 | 0 | 0 | 1 | 3 |
|  | 23159 | 9944 | - | G4 | + 2 | 70 | 0 | 0 | 1 | 2 |
|  | C 7661 | 30029 | - | G2 | - 7 | 110 | 0 | 0 | 2 | 3 |
|  | E 339 | 0324 | - | F5 | + 7 | 110 | $0$ | 0 | 0 | 2 |
|  | r 26392 |  | - | G6 | - 26 | 110 | 0 |  | 2 | 3 |
|  |  |  |  |  | - 2 |  |  |  |  |  |
| UU Her. | C 2742 | 23889 | - | F5 | -128 | 70 | 0 | 0 | 0 | 2 |
|  | 2766 | 3916 | - | F6 | -142 | 70 | 0 | 0 | 0 | 2 |
|  | 2796 | 3926 | - | F8 | -137 | 70 | 0 | 0 | 0 | 2 |
|  | 3512 | 4417 | - | F5 | -121 | 70 | 0 | 0 | 0 | 2 |
|  | 3980 | 4750 | - | G0 | -130 | 70 | 0 | 0 | 1 | 2 |
|  | 4197 | 4956 | - | F2 | -132 | 70 | 0 | 0 | 0 | 2 |
|  | 4224 | 4984 | - | F5 | -130 | 70 | 0 | 0 | 0 | 1 |
|  | 4254 | 5011 | - | F7 | -127 | 70 | 0 | 0 | 0 | 2 |
|  | 4285 | 5040 | - | F4 | -132 | 70 | 0 | 0 | 0 | 2 |
|  | 4308 | 5048 | - | G0 | -139 | 70 | 0 | 0 | 0 | 1 |
|  | 4370 | 5079 | - | F6 | -126 | 70 | 0 | 0 | 0 | 2 |
|  | 5205 | 5777 | - | F5 | -131 | 70 | 0 | 0 | 0 | 2 |
|  | 5234 | 5809 | - | F6 | -117 | 70 | 0 | 0 | 0 | 1 |
|  | 5390 | 6018 | - | F8 | -141 | 70 | 0 | 0 | 0 | 2 |
|  | 5415 | 6048 | - | F8 | -139 | 70 | 0 | 0 | 0 | 2 |
|  | 5464 | 6135 | - | F7 | -144 | 35 | 0 | 0 | 0 | 2 |
|  | 5740 | 6493 | - | F7 | -125 | 70 | 0 | 0 | 0 | 1 |
|  | 5756 | 6516 | - | F6 | -125 | 70 | 0 | 0 | 0 | 1 |
|  |  |  |  |  | -131 |  |  |  |  |  |
| AB Leo. |  |  |  |  |  |  |  |  |  |  |
|  | $1690$ | 1923 | - 51 | G0e | +188 | 110 | 5 | 0 | 1 | 1 |
|  | Ce 4231 | 1929 | 57 | - | +182 | 20 | 4 | - | - |  |
|  | $\gamma 27603$ | 1930 | 58 | F6e | +166 | 70 | 3 | 0 | 0 | 1 |
|  | 27651 | 1952 | 80 | F5e | +163 | 70 | 3 | 0 | 0 | 1 |
|  | E 1707 | 1976 | 1. | G3e | +194 | 110 | 1 | 0 | 1 | 1 |
|  | $\gamma 27705$ | 1981 | 6 | G0 | +172 | 110 | 0 | 0 | 1 | 1 |
|  | 29272 | 2555 | 64 | F8 | - | 110 | 0 | 0 | 1 | 1 |
|  | E 1951 | 2582 | 91 | G0e | +180 | 110 | 5 | 0 | 1 | 2 |
|  | - 29383 | 2611 | 17 | F5e | +189 | 110 | 1 | 0 | 1 | 2 |
|  | E 1969 | 2636 | 42 | G2e | +178 | 110 | 1 | 0 | 1 | 1 |
|  | $\gamma 29524$ | 2671 | 77 | F5e | +182 | 110 | 6 | 0 | 0 | 1 |
|  |  |  |  |  | +182 |  |  |  |  |  |
| W LMi. | C 7176 | 29379 | M 101 | - | - | 110 | 3 | 1 | 0 |  |
|  | $\gamma 21784$ | 9380 | 102 | K0e | - | 70 | 3 | 1 | 2 | 1 |
|  | C 7664 | 30030 | 48 | G4e | + 57 | 110 | 10 | 2 | 1 | 1 |
|  | $\gamma 23340$ | 007.1 | 90 | G6e | + 55 | 110 | 3 | 0 | 2 | 1 |
|  | E 87 | 0090 | 109 | K0e | + 94 | 110 | 2 | 1 | 3 | 1 |
|  | $\gamma 23450$ | 0151 | 53 | G2e | + 48 | 110 | 6 | 0 | 2 | 1 |
|  | 24024 | 0397 | 64 | G2e | + 64 | 110 | 8 | 0 | 1 | 1 |
|  | E 422 | 0443 | 110 | K0e | + 96 | 110 | 3 | 1 | 3 | 1 |
|  | r 26394 | 1464 | 76 | G4e | + 71 + | 110 | 4 | 0 | 2 | 1 |
|  | E 1354 | 1546 | 41 | G5e | + 41 | 110 | 5 | 2 | 2 | 1 |
|  | - 1397 | 1568 | 63 | G3e | + 46 | 70 | 5 | 0 | 2 | 1 |
|  | $1595$ | 1844 | 104 | K2e |  | 110 | 0 | $3$ | 2 | 1 |
|  | C 7715 | 1960 | 104 | K0e | +90 | 110 | 1 | 2 | 1 | 1 |
|  |  |  |  |  | $+66$ |  |  |  |  |  |

TABLE 2-Continued

| Star | Plate | Date <br> JD 24 | $\begin{aligned} & \text { Phase } \\ & \text { (Days) } \end{aligned}$ | Spectrum | Velocity <br> (Km/Sec) | $\begin{gathered} \text { Disp. } \\ \mathrm{AT}_{\mathrm{AT}} \\ \mathrm{~A} / \mathrm{MM}) \end{gathered}$ | Intensity |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Em. | TiO | CH | M II |
| UW Lib. | $\gamma 22735$ | 29803 | - | G7e | +155 | 70 | 0 | 0 | 1 | 1 |
|  | 22756 | 9824 | - | G8 | +186 | 110 | 0 | 1 | 1 | 1 |
|  | C 7538 | 9853 | - | G6e | +164 | 110 | 4 | 0 | 1 | 2 |
|  | r 23341 | 30071 | - | G4 | +146 | 110 | 0 | 1 | 2 | 1 |
|  | E 106 | 0119 | - | G7e | +169 | 110 | 2 | 2 | 2 | 2 |
|  | 151 | 0149 | - | G2e | +194 | 110 | 1 | 0 | 2 | 2 |
|  | $\gamma 23510$ | 0181 | - | G8 | +155 | 110 | 0 | 1 | 1 | 1 |
|  | 24025 | 0398 | - | K0 | +142 | 110 | 0 | 0 | 2 | 2 |
|  | 24054 | 0423 | - | G6 | +176 | 110 | 0 | 2 | 2 | 1 |
|  | E 423 | 0443 | - | G7e | +179 | 110 | 4 | 3 | 2 | 2 |
|  | 442 | 0471 | - | G6e | +136 | 110 | 2 | 0 | 2 | 1 |
|  | 1396 | 1567 | - | G4e | +161 | 70 | 2 | 0 | 1 | 2 |
|  | $\gamma 26612$ | 1595 | - | G6e | +169 | 110 | 1 | 1 | 1 | 1 |
|  | 26742 | 1633 | - | G5e | +171 | 70 | 1 | 0 | 1 | 2 |
|  | 27642 | 1948 | - | G8e | +174 | 110 | 2 | 0 | 2 | 2 |
|  | C 7707 | 1958 | - | G6e | +146 | 110 | 1 | 0 | 2 | 2 |
|  | r 27706 | 1981 | - | G8 | +145 | 110 | 0 | 0 | 2 | 1 |
|  |  |  |  |  | +163 |  |  |  |  |  |
| U Lup. |  | 29765 | - | K0 | -134 | 110 | 0 |  | 2 | 1 |
|  | 7502 | 9806 | - | - | - | 110 | 0 | 1 | 2 | 1 |
|  | E 93 | 30091 | - | G6e | -134 | 110 | 2 | 0 | 2 | 1 |
|  | 107 | 0119 | - | K0e | -141 | 110 | 1 | 0 | 2 | 1 |
|  | 171 | 0178 | - | K0 | -124 | 110 | 0 | 2 | 2 | 1 |
|  | 1428 | 1634 | - | G2 | -109 | 110 | 0 | 0 | 2 | 2 |
|  | C 7716 | 1960 | - | G6e | -141 | 110 | 4 | 0 | 2 | 1 |
|  |  |  |  |  | -130 |  |  |  |  |  |
| TT Oph. | $\gamma 6870$ | 21711 | m 13 | G4e | - 64 | 70 | 1 | 0. | 2 | 2 |
|  | C 340 | 2414 | - 43 | G6e | -43 | 35 | 2 | 0 | 3 | 3 |
|  | 386 | 2443 | 12 | - | - | 35 | 3 | 0 |  | - |
|  | 441 | 2473 | 42 | G5e | - 41 | 35 | 1 | 0 | - | 3 |
|  | 476 | 2483 | 52 | K0 | - 62 | 35. | 0 | 0 | 3 | 3 |
|  | 504 | 2507 | 15 | G4e | - 53 | 70 | 2 | 0 | 3 | 3 |
|  | 1075 | 2866 | 8 | G8 | - 49 | 35 | 0 | 0 | 3 | 2 |
|  | 1114 | 2882 | 24 | G5 | - 58 | 70 | 0 | 0 | 2 | 3 |
|  | 1218 | 2918 | 59 | K0 | - 57 | 35 | 0 | 0 | 3 | 3 |
|  | 1265 | 2940 | 20 | G6 | - 67 | 70 | 0 | 0 | 2 | 3 |
|  | 1367 | 2970 | 50 | G8 | -81 | 70 | 0 | 0 | 2 | 3 |
|  | 1640 | 3136 | 33 | K0 | - 39 | 70 | 0 | 0 | 3 | 2 |
|  | 2297 | 3592 | 0 | G8 | - 34 | 70 | 0 | 0 | 3 | 3 |
|  | 3881 | 4715 | 24 | G7 | - 61 | 70 | 0 | 0 | 2 | 3. |
|  |  |  |  |  | - 50 |  |  |  |  |  |
| TX Oph. | C 4225 |  | - |  |  |  |  | 0 |  |  |
|  | 4251 | 5010 | - | G0 | -166 | 70 | 0 | 0 | 0 | 3 |
|  | 4399 | 5129 | - | G2 | -172 | 70 | $0$ | 0 | 1 | 3 |
|  | 4739 | 5346 | - | G3 | -170 | 70 | $0$ | 0 | 1 | 3 |
|  | 4928 | 5458 | - | G6e | -158 | 70 | 1 | 0 | 1 | 3 |
|  | 5227 | 5786 | - | G4e | -161 | 70 | 1 | 0 | 1 | 2 |
|  | 5435 | 6078 | - | G0e | -155 | 70 | 1 | 0 | 1 | 2 |
|  | $\gamma 24129$ | 30484 | - | F8 | -165 | 110 | 0 | 0 | 0 | 3 |
|  | 24151 | 0504 | - | G3 | -178 | 110 | 0 | 0 | - | 3 |
|  | 26613 | $1595$ | - | G6 | $-164$ | 110 | 0 | 0 | 1 | 2 |
|  | E 1683 | 1919 | - | F5e | -177 | 110 | 1 | 0 | 0 | 2 |
|  |  |  |  |  | -165 |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |

TABLE 2-Continued


TABLE 2-Continued


TABLE 3
Summary of Spectroscopic Results

| Star | $\begin{gathered} \text { Spectrum } \\ \text { (Atomic Lines } T i O \text { ) } \end{gathered}$ | Max. <br> Emis- <br> sion <br> Int. | $\begin{gathered} C H \\ \text { G bAND } \\ \text { Int. } \end{gathered}$ | Max. <br> M II <br> Int. | Velocity |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Meas. ( $\mathrm{Km} / \mathrm{Sec}$ ) | $\begin{gathered} \text { Range } \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ | $\begin{gathered} \text { Resid. } \\ (\mathrm{Km} / \mathrm{Sec}) \end{gathered}$ |
|  | Group 1: Velocities $<70 \mathrm{Km} / \mathrm{Sec}$ |  |  |  |  |  |  |
| BL Aqr. | G2 -K0 (M2) | 0 | 1-3 | 2 | + 45 | 20 | + 57 |
| TW Aql. | G0 -K0 | 0 | 0-3 | 3 | + 21 | 35 | + 39 |
| DY Aql. | G5e-K0 (M3) | 5 | 1-3 | 3 | +15 | 30 | + 29 |
| EZ Aql. | G5 -K0 | 0 | 2-3 | 3 | + 48 | - | + 66 |
| TW Cam. | G2-G8 | 0 | 0-1 | 3 | - 55 | 30 | - 56 |
| RU Cep. | G6-K2 (M2) | 0 | 1-2 | 2 | - 12 | 15 | - 3 |
| TZ Cep. | G6 -K2e (M2) | 4 | 0-3 | 3 | - 5 | 20 | + 4 |
| AV Cyg | G0e-G6 | 3 | 2-3 | 3 | - 23 | 20 | - 4 |
| DF Cyg | G5 -K4 | 0 | 1-4 | 3 | - 5 | 45 | + 13 |
| SS Gem. | G0-G8 | 0 | 0-4 | 3 | - 6 | 55 | - 19 |
| SU Gem. | F5-G6 | 0 | 0-2 | 3 | - 2 | 40 | - 13 |
| SX Her. | G3e-K0 (M3) | 8 | 0-3 | 2 | + 20 | 15 | + 38 |
| AC Her | F1-K4e | 4 | 0-4 | 3 | - 30 | 60 | - 10 |
| U Mon | F8e-K2 (M2) | 5 | 1-4 | 3 | +35 | 45 | + 17 |
| TT Oph | G2e-K0 | 3 | 2-3 | 3 | - 50 | 45 | - 33 |
| UZ Oph | G2e-G8 (M2) | 2 | 1-3 | 3 | -85 | 70 | - 67 |
| TX Per. | G5e-K2 (M3) | 3 | 1-4 | 2 | 0 | 40 | - 3 |
| R Sge. | G2 -K0 | 0 | 1-4 | 3 | + 10 | 40 | + 27 |
| AI Sco | G0-K2 | 0 | 1-2 | 3 | - 15 | 35 | - 6 |
| R Sct. | G5e-K2 (M3) | 3 | 2-3 | 3 | + 40 | 35 | + 56 |
| RV Tau | G4e-K1 (M1) | 2 | 1-4 | 3 | + 35 | 45 | + 24 |
| S Vul. | G0-K2 (M1) | 0 | 1-4 | 3 | - 2 | 25 | +17 |
| V Vul. | G4-K3 (M2) | 1 | 1-4 | 3 | - 15 | 40 | + 2 |
|  | Group 2: Velocities $>70 \mathrm{Km} / \mathrm{Sec}$ |  |  |  |  |  |  |
| WY And | G2e-K2 (M3) | 4 | 1-2 | 3 | -191 | 55 | -183 |
| KK Aql. | G2e-G6 (M2) | 4 | 1-2 | 2 | -252 | 50 | -234 |
| Z Aur.. | G0e-G6e (M1) | 5 | 1-2 | 2 | -165 | 35 | -167 |
| AG Aur. | G2e-K0 (M3) | 5 | 1-2 | 2 | +193 | 25 | +188 |
| RX Cap. | G0-G3 | 0 | 0-1 | 2 | -135 | 35 | -123 |
| V360 Cyg | F5-G0e | 2 | 0-1 | 2 | -250 | 45 | -235 |
| U H Her. | F2-G0 | 0 | 0-1 | 2 | -131 | 25 | -114 |
| AB Leo. | F5e-G3e | 6 | 0-1 | 2 | +182 | 50 | +175 |
| W LMi | G2e-K2e (M3) | 10 | 1-3 | 1 | + 66 | 55 | + 70 |
| UW Lib | G2e-K0 (M3) | 4 | 1-2 | 2 | +163 | 60 | +176 |
| ULup. | G2-K0e (M2) | 4 | 2-2 | 2 | -130 | 30 | -122 |
| TX Oph. | F5e-G6e | 1 | 0-1 | 3 | -165 | 20 | -147 |
| AR Sgr. | F5e-G6 | 2 | 0-1 | 2 | -100 | 10 | - 88 |
| WW Tau | G4e-K2 (M3) | 5 | 1-2 | 2 | -110 | 20 | -119 |
| SV UMa | G2e-G8 (M4) | 6 | 1-3 | 3 | - 90 | 20 | - 86 |

NOTES TO TABLES 2 AND 3
WY And $\quad$ Max. $=$ JD $2428408.9+108 \mathrm{~d} 8 E$. On plates C 6348, C 6351 , and Ce 3262 the stellar D1 and D2 sodium lines are well separated by velocity from the interstellar lines. Ce 3262 was taken and measured by R. F. Sanford. On this plate the $H a$ emission is symmetrically divided by a strong, deep absorption line.
BL Aqr $\quad$ Max. $=\mathrm{JD} 2430160+85 \mathrm{~d} E$.
TW Aql
$P=96$ ? days. Sharp lines.
DY Aql $\quad$ Min. $=$ JD $2428344+131$ d $42 E$.

## NOTES TO TABLES 2 AND 3-Continued

| EZ Aql | Min. $=$ JD $2428611.05+3861 E$. Extensive light-observations by Taylor and Olivier (Pub.Obs. U. Pennsylvania, Vol. 6, Part 5, 1941). The spectrum is much like that of DF Cyg. |
| :---: | :---: |
| KK Aql |  |
| Z Aur | Max. $=$ JD $2432072+110$ |
| AG Aur | Max. $=$ JD $2425766.5+98$ d26E (Schneller, 1939) |
| TW Cam | Min. $=$ JD $2428647+85 \mathrm{~d} 6 E$ |
| RX Cap | Min. $=$ JD $2420741.4+67$ d95E. Only maximum phase was observ |
| RU Cep | Max. $=$ JD $2430649+109$ d5E. Observed by P. C. Keenan, M0 III (Ap. J., 95, 462, 1942). The Mount Wilson observations are poorly distributed and do not cover the minimum phases. |
| TZ Cep | Max. $=$ JD $2425840+83 \mathrm{~d} 0 \mathrm{E}$. |
| AV Cyg | Max. $=$ JD $2430659+89 \mathrm{~d} 7 E$. Except for $\lambda 4077$ and $\lambda 4215 S r$ m, the lines are weak. |
| DF Cyg | Min. $=$ JD $2414883.5+49$ d. $808 E$. The spectrograms were all obtained at the brighter phases of the long-period variation of 782 days. The remarkable light-variations of this star were discovered and extensively observed by Miss M. Harwood (Harvard Ann., 105, 521, 1937). |
| V360 Cyg | Min. $=$ JD $2426967+63 \mathrm{~d} 26 E$. The emission lines are double, with shortward component stronger; separation $160 \mathrm{~km} / \mathrm{sec}$. The absorption lines are weak. |
| SS |  |
| SU Gem | $P=50.12$ days, with an additional long-period variation of 689.6 days. The absorption lines show large changes in intensity. |
| SX Her | The spectroscopic behavior of this star resembles that of the Mira stars in some particulars. Hydrogen emission occurs for about 30 days before and after maximum light. TiO bands attain considerable strength at minimum light. |
| UU Her | Alternating periods of 90.40 and 71.06 days have been found. The G band is usually absent. Spectral changes and velocity variations are small and uncertain. The star is unlike other stars of the group. The mean of the Mount Wilson and McCormick trigonometric parallaxes is $0^{\prime \prime} 010$. The observations were made at the times when the period of 90 days prevailed. |
| AC Her | Sanford (Mt.W.Contr., No. 424; Ap. J., 73, 364, 1931) found that during increasing light the hydrogen lines have emission edges. The velocity-curve shows a double maximum corresponding to the double minimum of the light-curve. The spectral type at maximum is earlier than that of any other star in the list and has a large range (F1-K4), although no $T i O$ bands appear. The $G$ band shows remarkable changes with phase. L. Rosino ( $A p . J ., 113,60,1951$ ) calls attention to the strength of the carbon bands during decreasing light and classifies the star as Rp at this phase. |
| $\begin{aligned} & \mathrm{AB} \text { Leo }= \\ & \mathrm{BD}+20^{\circ} 2337 \end{aligned}$ | Max. $=$ JD $2428880+103 \mathrm{~d} 2 E$. A. Vyssotsky found emission lines of hydrogen in ob-jective-prism spectra of this star. From Harvard plates Miss Hoflleit discovered lightchanges which resemble those of the semiregular or RV Tauri variables. She determined theelements used here. The light-curve seldom shows alternating bright and faint minima, but the period seems to hold, even though the epoch may shift. At times the light-fluctuations become irregular and of small range. The bright lines are strong and persistent, showing slow decrement shortward, but the type is too early to permit TiO bands. The star is evidently one of the semiregular variables of high velocity and moderate luminosity. <br> Plate Ce 4231 was taken by R. F. Sanford. On this plate the emission at $H a$ is symmetrically divided by a narrow central reversal. In general, the absorption lines are sharp, and the spectrum resembles that of UU Her, but, on the plates showing the earliest estimated spectral type, the lines seem weak, although no certain veiling effect is observable. |
| W LMi | Max. $=$ JD $2428303+117 \mathrm{~d} 2 E$. The light-changes and period are poorly determined. The range of light-variation is large. The hydrogen emission lines are strong and persistent, but the enhanced lines are weak. This star should certainly be placed among the high-velocity stars. |
| UW Lib | $P=84.73$ days. No epoch. This period does not seem to satisfy the velocity and spectral variations. Small light-range. |
| U Lup | The period is variable between 75 and 95 days, according to D. J. K. O'Connell (Harvard Bull., No. 893, 1933). |
| U Mon | Sanford (Mt.W.Contr., No. 465; Ap.J., 77, 120, 1933) found that the velocity-curve shows a double minimum, corresponding to the double maximum of the light-curve. Hydrogen emission and TiO bands were observed. |
| TT Oph | Min. $=$ JD $2428723+61$ d $08 E$. This star, which was at first thought to be an eclipsing binary, is one of the best examples of the RV Tauri type of variation. The light- |



Fig. 1.-Spectra of semiregular variables. $a$, K2 (M3), TX Persei; $b$, F4, UU Herculis; $c$, G5 (M4), SV Ursae Majoris, strong titanium bands on G5 spectrum; $d$, G8e, RV Tauri, $C H$ weak; $e$, KO, RV Tauri, $C H$ strong; $f$, G6, TW Camelopardalis, ionized metallic lines strong; g, G2e, WY Andromedae, ionized metallic lines weak, slow decrement of bright lines, $H \epsilon$ weakened; $h$, G5e (M2), W Leonis Minoris, all absorption lines weak, $H \epsilon$ absent; $i$, G0e, AB Leonis, lines weak.

## NOTES TO TABLES 2 AND 3-Continued

minima are usually well defined and of nearly equal depth. Emission lines of hydrogen appear during increasing light and reach greatest intensity 2 days before maximum light. The velocity-curve shows definite correlation with the light-curve. No TiO bands have been observed. The enhanced lines are strong.

| TX Oph | $P=138$ ? days. The range in velocity and spectral type is small. The enhanced lines are strong and indicate the highest luminosity of the high-velocity stars. |
| :---: | :---: |
| UZ Oph | Min. $=$ JD $2422531.84+87 \mathrm{~d} 39 E$. This star may belong to the high-velocity group. |
| TX Per | Max. $=$ JD $2428466+76 \mathrm{~d} 3 E$. |
| R Sge | Sanford found (Mt.W.Contr., No. 481; Ap.J., 79, 81, 1934) that the radial velocities show little correlation with the light-curve, but D. B. McLaughlin (Ap.J., 94, 94, 1941) discovered that, by omitting velocities obtained when light-variations were irregular, a reasonable correlation could be determined. No TiO bands or emission lines were found. The G band strengthens at minimum light. |
| AR Sgr | Min. $=$ JD $2426103+87$ d87E (Harvard Ann., 113, 39, 1943). Observed minimum. |
| AI Sco | $P=71.78$ days, with superposed period of 960 days. |
| R Sct | The appearance of $T i O$ bands at spectral type G9 was noted (Pub. A.S.P., 34, 349, 1922) in 1922. This fine example of RV Tauri variation has been thoroughly studied by D. B. McLaughlin (Pub. Obs. U. Michigan, 7, 57, 1938). |
| RV Tau | Min. $=$ JD $2429290+786 E$ (Harvard Ann., 113, 49, 1943). Observed minimum. A superposed period of 1227 days has been suggested. The G band and the enhanced lines are strong, but the emission lines and $T i O$ bands are weak and rarely seen. |
| WW Tau | The period varies from 113 to 138 days. The velocity range is small, but there is considerable variation in spectral type. |
| SV UMa | $P=76$ days. The light-variations are quite irregular, and the period is variable. The star was spectroscopically observed in 1930 by R. O.. Redman (M.N., 92, 116, 1931) at Victoria. A series of seventeen spectrograms covering more than a cycle failed to show, at that time, the strong emission lines of hydrogen and the TiO bands observed later at Mount Wilson. A McDonald spectrogram in 1941 by P. C. Keenan was classi- |
| S Vul | fied as K3p: $\mathrm{I} a(A p . J ., 95,463,1942)$ with weak lines. <br> Max. $=$ JD $2423671.7+67$ d $77 E$ (Schneller, 1939). The period is variable. Velocity and spectral variations are small, but the strength of the $G$ band shows large fluctua- |
| V Vul | Sanford (Mt.W.Contr., No. 481; Ap.J., 79, 82, 1934) reported weak TiO bands but no emission. |

The CH absorption is an outstanding feature of the stars of group 1 , reaching its greatest strength at the times of later spectral type. At other phases the band becomes weak or disappears. In group 2, $C H$ seldom attains great intensity. In all the stars, marked changes in the bands take place in a few days' time. The $\lambda 4215 C N$ band has also been found for a short period preceding minimum in the luminous stars DF Cyg, SS Gem, U Mon, RV Tau, and SV UMa.

Emission lines of hydrogen occur, especially at times of increasing light, in a majority of the stars of both groups. The bright lines are stronger and more persistent in group 2. The decrement toward the violet is usually gradual. The bright hydrogen line $H \epsilon$ is often greatly reduced-in intensity by the absorption of the H line of calcium (Fig. 1, $g, h$, and $i$.

With further observation, hydrogen emission or titanium bands may yet be found at favorable phases in some of the stars in which these features were not observed.

The irregular behavior of the stars makes it impossible to draw useful velocity-curves from scattered observations. The mean measured velocity range of $36 \mathrm{~km} / \mathrm{sec}$ is somewhat less than that of the most luminous cepheids, but this may be due to periods of inactivity which occur from time to time among the semiregular variables. The mean velocity range is the same for both groups of Table 3.

In studies of variable stars the period of variation has usually been an important factor in the discussion. This parameter has rendered little help with the irregular stars discussed in this paper. Various correlations with period have been tried, but they have not seemed significant.

## SUBGROUPS

Since the stars of the present list were included largely on the basis of their spectral characteristics, considerable study was given to their spectroscopic behavior, in order to detect the presence of physically defined subgroups. Such an analysis points to a division (Table 3 and Fig. 3) into high- and low-velocity groups as the most natural and fruitful means of bringing together the stars of like physical characteristics. Only five stars of the list have residual velocities between 57 and $114 \mathrm{~km} / \mathrm{sec}$, and none are found between 70 and $86 \mathrm{~km} / \mathrm{sec}$. A value of $70 \mathrm{~km} / \mathrm{sec}$ was set as the lower limit of the velocities of group 2. It is near the minimum frequency of velocities and corresponds well with the values used by Oort and others in separating stars of low and high velocity. If the maximum strength of the ionized lines (fifth column of Table 3) or that of the G band (fourth column) had been taken as criteria, the grouping would have been practically the same,


Fig. 2.-Galactic latitude and longitude of semiregular variables. Circles are high-velocity stars (Group 1); crosses, low-velocity stars (Group 2); and filled circles, cepheids with period $>20$ days.
except that it might have been necessary to place TW Cam in group 2 with the highvelocity stars.
The evidence for two physical groups among these semiregular variables is strong in several respects: (1) The mean galactic latitudes of groups 1 and $2\left(13^{\circ}\right.$ and $\left.27^{\circ}\right)$ indicate a difference in distribution (Fig. 2), although in neither group is the concentration toward the galactic equator as marked as in the $\delta$ Cephei variables, for which the average distance from the equator is less than $5^{\circ}$. (2) Mean proper motions determined by R. E. Wilson are 0 ". 018 for thirteen stars of group 1 and 0.035 for seven stars of group 2. Since these values are, respectively, two and three times the mean proper motions of cepheids with periods greater than 20 days, it seems unlikely that either group has close kinetic relationship with the long-period cepheids. (3) Mean residual radial velocities (Table 3) without regard to sign: group $1,28 \mathrm{~km} / \mathrm{sec}$; group $2,154 \mathrm{~km} / \mathrm{sec}$. (4) A plot of radial velocities according to galactic longitude (Fig. 3) shows a distinct difference in the distribution of velocities in the two groups. The high velocities of group 2 are widely separated from those of group 1. A solar-motion solution for group 2 from the radial velocities indicates a group motion of $263 \mathrm{~km} / \mathrm{sec}$ in nearly the same direction as that of RR Lyrae
stars ${ }^{12}$ and the high-velocity R-type stars. ${ }^{13}$ The smaller velocities of group 1, unlike those of the $\delta$ Cephei stars, show little galactic-rotation effect. (5) The average spectral type of group 2 is slightly earlier than that of group 1: at maximum F9 for group 2, G2 for group 1; at minimum G7 and K0, respectively. (6) The ionized lines of metals are distinctly stronger in group 1, and the absorption spectrum is more clearly defined, indicating higher luminosity. (7) The G band ( CH ) reaches greater intensity in group 1, but this may be, in part, due to the effect of later spectral type in the low-velocity stars. (8) Emission lines of hydrogen are often found in both groups at certain phases but occur more frequently and in greater strength among the high-velocity stars (eleven of twentythree stars in group 1 ; thirteen of fifteen stars in group 2). (9) The double period with two unequal minima of light, typical of the more regular RV Tauri stars, seldom occurs in group 2.


Fig. 3.-Radial velocity and galactic longitude of semiregular variables. Circles are high-velocity stars (Group 1); crosses, low-velocity stars (Group 2). The solid curve shows the radial velocity of Group 2 with reference to the sun; the dashed curve is the theoretical galactic rotation effect having a maximum of $25 \mathrm{~km} / \mathrm{sec}$.

The stars of group 2 are doubtless of type II population and might be expected to resemble those of groups 4 and 5 of the globular clusters. ${ }^{14}$ This similarity prevails with regard to luminosity, period, and the occasional appearance of emission lines in our group 2 as compared with group 5 of the clusters. On the other hand, in the clusters the mean range of light-variation is smaller, 0.8 mag. compared to 2.2 mag . Also, in the clusters the G band is stronger and the spectral type somewhat later, although the TiO bands apparently are less frequent.

High-luminosity variables such as those of group 4 in the clusters seem to be few or absent among the high-velocity stars of the galaxy. Perhaps TX Oph may be an exception. Several of the low-velocity stars of our group 1 are similar to those of group 4 in the

[^3]clusters, except that the group 1 stars are later in spectral type and have strong G bands, while $C H$ in group 4 of the clusters is weak or absent.

From these considerations it seems evident that these semiregular variables may well comprise two groups based on distribution, motions, luminosity, or the intensity of the G band of $C H$. The relationship of these two groups to the variables of the $\delta$ Cephei class, on the one hand, and to the red M-type variables, on the other, is yet uncertain. Group 2 definitely should be included in population II, but the place of group 1 is not clear. Since the peculiar motions of group 1, which includes many of the best-known RV Tauri variables, such as U Mon, R Sct, and V Vul, are large as compared with the long-period cepheids but yet are much smaller than is generally found for type II stars, and their galactic latitude agrees with neither, it seems best, at present, to consider these stars as an anomalous group of population I stars. Possibly they may be related to the widely scattered giant K stars whose rapid velocities were first found by W. W. Campbell.

Most of the stars of group 2 are irregular variables which cannot meet the rigid requirements usually set up for the RV Tauri class. TX Oph and RX Cap have most of the RV Tauri characteristics and may correspond to the RV Tauri group in the clusters.

## ABSOLUTE MAGNITUDE AND DISTANCE

On account of the great distances, trigonometric parallaxes of these stars are few and unreliable. Spectroscopic estimates of the visual absolute magnitude have been published for SX Her ${ }^{11}(-1.5)$ and $\mathrm{U} \mathrm{Mon}^{15}(-2.0)$, and comparisons with the spectra of cepheids of the same spectral type indicate clearly that the luminosity of the brightest stars is as high as, or perhaps higher than, that of any of the cepheids. This conclusion is confirmed by the distances determined from the strength of the interstellar lines of sodium ${ }^{16}$ in three of the less luminous stars (WY And, AG Aur, and UU Her), from which absolute magnitudes brighter than -2.2 may be deduced. In the globular clusters the absolute photographic magnitudes of the RV Tauri and semiregular groups are -3.0 and -1.5 , respectively. Using the proper motions of sixteen stars (eleven belonging to these groups), P. P. Parenago ${ }^{17}$ found a mean absolute visual magnitude of -0.4 , but this value is of low weight on account of the small proper motions (mean about 0.102 ) involved.

Rosino ${ }^{2}$ has classified eleven of the stars (eight of group 1 and three of group 2) and assigned the luminosity class $\mathrm{I} a$ or $\mathrm{I} b$, indicating visual absolute magnitudes as high as -4 or -5 according to the Yerkes system.

While none of these methods of determining absolute magnitude are precise, they indicate that the RV Tauri and related stars are among the most highly luminous stars and that they are comparable with the cepheids of similar spectra and periods of from 20 to 40 days for which Shapley's period-luminosity curve gives photographic absolute magnitudes as bright as -3.0 .

Judging by the strength of their ionized lines, many of the stars of group 1 appear to be somewhat more luminous than the brightest cepheids. Absolute photographic magnitudes -3.0 for group 1 and -1.5 for group 2 seem to be reasonable mean values.

Neglecting space absorption, the distances of the stars of group 1, as determined from this value of the absolute magnitude and their median apparent magnitudes, average about 7 kpc . Since only twelve stars of this group are within $10^{\circ}$ of the galactic equator, large corrections to their apparent magnitudes on account of interstellar absorption are probably limited to a few stars of the group. Some of the stars, such as BL Aql, SX Her, TT Oph, and UZ Oph are distant $2.5-5 \mathrm{kpc}$ from the galactic plane. With these assumptions, the mean distance of the stars of group 2 is about 4 kpc .

[^4]
## CONCLUSIONS

As a result of spectroscopic observations it is evident that the semiregular variables with pseudo-periods between 39 and 144 days and spectral types $\mathrm{F}, \mathrm{G}$, and K do not form a homogeneous group. In motion, luminosity, and spectral behavior no standard pattern is rigorously followed. The RV Tauri stars, well known to observers of variable stars for their irregular light-changes, are the accepted models for the group, but wide deviations in the behavior and characteristics of the individual stars are present.

On the basis of velocity, of absolute magnitude as determined by the strength of the ionized lines, and of the maximum intensity of the G band $(\mathrm{CH})$, the thirty-eight stars observed may be separated into two groups, group 1 having velocities less than 70 $\mathrm{km} / \mathrm{sec}$, brighter absolute magnitudes, and greater maximum intensities of the G band. Within these two groups marked differences among the stars are found.

The stars of group 2 evidently belong to the type II population and correspond closely with the semiregular variables of the globular clusters. In luminosity and in radialvelocity variations the members of group 1 are similar to the long-period cepheids, but they are more scattered with reference to the plane of the galaxy and fail to show clearly the effect of galactic rotation. Also, these stars frequently have hydrogen emission and titanium oxide bands which have not been found in the cepheids. The place of the group 1 stars with reference to Baade's population types is not yet clear.

The veiling and absorption effects of titanium and carbon bands must contribute toward dimming the light of the semiregular stars at certain phases. On the other hand, increases in light may be, in part, due to flare effects, which are accompanied by hydrogen emission and a marked diminution in the visibility of the absorption spectrum at times in many of the stars. Such outbursts must be quite different in size and duration from those encountered in the faint dwarfs of extremely low temperatures.


[^0]:    ${ }^{1}$ Harvard Ann., Vol. 113, No. 1, 1943.
    ${ }^{2}$ Ap.J., 113, 60, $1951 . \quad{ }^{3}$ Harvard Bull., No. 919, p. 11, 1949.

[^1]:    ${ }^{4}$ Mt. W. Contr., No. 465; Ap.J., 77, 120, 1933.
    ${ }^{5}$ A.N., 267, 399, 1938.

[^2]:    ${ }^{6}$ Mt. W. Contr., No. 424; Ap. J., 73, 364, 1931.
    ${ }^{7}$ Mt. W. Contr., No. 481; Ap. J., 79, 81, 1934.
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[^4]:    ${ }^{15}$ W. S. Adams et al., Mt. W. Contr., No. 511; Ap. J., 81, 225, 1935.
    ${ }^{16}$ A. H. Joy, Pub. A.S.P., 46, 51, 1934.
    ${ }^{17}$ A.J.U.S.S.R., 11, 95, 1934.

