# THE RADIAL VELOCITIES OF THE STARS OF SPECTRAL CLASSES R AND N* 

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#### Abstract

The catalogue.-An attempt is made to bring together in Table I all the radial velocities of the stars whose spectra show the bands of carbon. Those of class N have been reduced to a velocity system which harmonizes laboratory and stellar data.

Velocities from emission lines.-Twenty stars of class N having emission lines of hydrogen give $-25.6 \mathrm{~km} / \mathrm{sec}$. for the mean difference between the radial velocities depending upon them and those from the absorption features. These stars are all variable with a mean period of 407 days and a mean range of 4 mag. Emission lines of hydrogen are usually associated with stars having a large magnitude range, and in such stars as fail to show them the explanation may be that the observations occur at the wrong phase, since the intensity of emission is known to fall to zero at certain phases. Moreover, the presence of emission in the spectrum of a star not known to vary should cause it to be suspected of variability.

Solar motion, galactic rotation, and absolute magnitude.-A least-squares solution based upon all the material for the class-N stars gives a solar motion quite similar to that for the naked-eye stars, a galactic rotation term of $13.4 \mathrm{~km} / \mathrm{sec}$., a mean distance of 0.727 kiloparsecs, a mean absolute magnitude of -1.4, and $315^{\circ}$ as the longitude of the galactic center.

The reality of the galactic rotation term is strengthened by dividing the stars into three groups, whose mean apparent magnitudes are $6.5,8.1$, and 9.3 , and solving these groups for galactic rotation alone after the elimination of the solar motion. The three results are $7.2,16.3$, and $22.4 \mathrm{~km} / \mathrm{sec}$.-a quite consistently progressive increase.

Mean absolute magnitudes for the three groups are computed on the basis of their mean apparent magnitudes and mean distances. These latter can be obtained from the constant for the increase of the galactic-rotation term per kiloparsec as obtained from the investigations of stars of class B and of Cepheid variables. Using the constant obtained by Joy for the latter stars, the values of the absolute magnitude are - I.4, - I.5, and -I.I, respectively. The constant for the $B$ stars gives absolute magnitudes 0.4 brighter.


Heretofore the radial velocities of stars of spectral classes R and N were to be found only in the following lists: 8 N stars by Hale, Ellerman, and Parkhurst, ${ }^{\text {r }}$ io R stars by W. C. Rufus, ${ }^{2} 25$ of class N by J. H. Moore, ${ }^{3}$ and 30 of class R by R. F. Sanford. ${ }^{4}$

Immediately following the completion of the last list a program for the radial velocities of stars of class N was started by the writer

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${ }^{\text {土 }}$ Pub. Yerkes Obs., 2, 341, 1903.
${ }^{2}$ Pub. Detroit Obs., 2, 135, 1916. ${ }^{3}$ Lick Obs. Bull., 10, 160-168, 1922.
${ }^{4}$ Mt. W. Contr., No. 276; Ap. J., 59, 339, 1924.
with the idea of increasing as far as possible the number obtained by Moore, an increase which would have been rather moderate if both the plates available and the spectrographic equipment had not in the meantime undergone marked improvement. With only a few exceptions, the spectrograms used in this investigation were obtained with the stellar plane-grating spectrograph designed by Merrill and described ${ }^{5}$ by him in Mount Wilson. Contribution No. 432. Suitable spectrograms of stars of spectral class N as faint as visual magnitude $8 \frac{1}{2}$ may under good conditions be obtained in the red with exposures of the order of two hours by using ammoniated Eastman 3C plates.

It thus became possible to photograph even more than had been anticipated of the stars of class N from the Henry Draper Catalogue. In addition, a considerable number of spectrograms was obtained for the purpose of checking the classification of discoveries ${ }^{6}$ of this spectral class upon objective-prism spectra photographed at Mount Wilson with the ro-inch telescope. Most of these latter stars were of the ninth visual magnitude or fainter and necessitated the use of a short-focus camera with a resultant dispersion of ino A per millimeter. Some of the other faint stars were also photographed in this manner. Otherwise, for the most part, a camera of ro-inch focus, with a dispersion of 65 A per millimeter, was employed. A dispersion of 33 A per millimeter was obtained by using an I8-inch camera for a few stars. Some exposures of exceptionally high dispersion were made with various coudé spectrographs. Such a spectrogram of Y Canum Venaticorum made with a concave-grating spectrograph has a dispersion of approximately 3.5 A per millimeter.

In the spectra of stars of this class, the identification of the complex absorption features has never been entirely satisfactory. The Swann, cyanogen, and hydrocarbon bands and certain very conspicuous lines such as those of sodium are well known. But a large percentage of the details, notably those extending into the visual region which Shane ${ }^{7}$ measured, remained unidentified.

At first, therefore, it was decided to use Moore's results as a basis for the velocities of standards for the Hartmann spectrocomparator
${ }^{5} A p . J ., 74$, 188-200, 1931.
${ }^{6}$ Pub. A.S.P., 45, 306-308, $1933 . \quad{ }^{7}$ Lick Obs. Bull., 10, 79-92, 1920.
and for the wave-lengths to be used for micrometer measurementa practice followed until a large number of spectrograms had been obtained with the grating spectrograph. During this time these wave-lengths were improved, and some features adopted at first were rejected as not being generally useful.

The region measured on the grating spectrograms includes the D lines, which, when suitably exposed, offered an opportunity of comparison with the wave-length system employed. Twenty-one spectrograms were selected, each of which furnished a good determination of the radial velocity, both from the D lines, by using solar wave-lengths, and from other tabular features. The differences were remarkably consistent and significantly large, the sodium lines giving algebraically smaller radial velocities. Further checks seemed desirable.

A good opportunity was offered when Merrill ${ }^{8}$ found that in the far red the spectra of stars of class N could be largely accounted for by the details of the cyanogen band spectrum, and when, at his suggestion, I looked for and found the same to be true in the red region.

An intercomparison of spectra of class- N stars and King's furnace spectra resulted in the identification of many features for which accurate wave-lengths could be measured on the laboratory spectrograms. A new set of wave-lengths was thus obtained which included the features already used. Radial velocities were then computed on the basis of the old tabular wave-lengths as well as on that of the new wave-lengths of these same features and also on the basis of the additional features measured. The three comparisons are given below together with their mean:

```
D lines - old tables........................... - . mkm/sec.
Revised }\lambda\lambda\mathrm{ -old }\lambda\lambda\mathrm{ (same features).............. }
New lines -old lines (old \lambda\lambda)..................... -9
    Mean....................................... - 
```

Hence velocities based upon the old tables need to be decreased by 7 km to conform to the new system.

This correction is significantly like the K term which Moore obtained from his solution for the solar motion. He was of course well

[^0]aware of the fact that this K term would have largely disappeared had he not applied a systematic correction to the velocities from low-dispersion spectrograms. He concluded to use this correction, however, since its necessity was indicated by such intercomparisons as were possible, although he was frank to point out some of their unavoidable deficiencies. His radial velocities, corrected by $-7 \mathrm{~km} / \mathrm{sec}$., may be compared with the writer's in twenty-one cases. Since three of these intercomparisons involve low weight in one case or the other, eighteen well-determined values remain common to both lists. The mean of their differences is practically zero.

It may also be remarked that the mean of the differences between the velocities of the eight class-N stars given by Hale, Ellerman, and Parkhurst and their velocities determined at Mount Wilson is $-4 \mathrm{~km} / \mathrm{sec}$.

Table I includes all the velocities of stars of class N obtained at Mount Wilson; of those few below our declination limit obtained by the D. O. Mills expedition, at Santiago, Chile, and appearing in Moore's list; and of some miscellaneous stars originally suspected of belonging to this spectral class. The velocities of stars of spectral Class R as given in Contribution No. $276^{4}$ are included, together with a few observed later. Table I should therefore contain a complete list of the known radial velocities of stars in whose spectra the bands of carbon appear.

The class-N stars from the Henry Draper Catalogue within reach of Mount Wilson and not yet observed for radial velocity are as follows: HD 44653, 46321, 47396, 48664, 52225, 57160, 57884, 58195, 58385,60952 , 172804, 190606, 191783, 195665. To these should be added three stars from the Mount Wilson list, ${ }^{6}$ Nos. 26, 27, and 32. Practically all have visual apparent magnitudes 9 or fainter.

Among the class-R stars there remain likewise the following from the Henry Draper Catalogue: HD 27108, 63130, 70138,78278 , 163838, 166097, 166129, 170282, 171399, 179355, 187216, 188934, $215673,216649,218851$. No magnitudes are given for six of these, while the mean apparent visual magnitude for the remainder is 10.4, which accounts for the lack of observations.

The Henry Draper Catalogue has, in large part, furnished its number, the BD designation, the co-ordinates for 1900 , the magnitudes, and the types for Table I. Additional information on the mag-
TABLE I＊

| $\begin{aligned} & \text { ì } \\ & \text { O } \\ & \text { M } \end{aligned}$ |  |  |
| :---: | :---: | :---: |
| $\begin{aligned} & \text { n } \\ & \text { H } \\ & \text { Z } \end{aligned}$ |  |  |
| $\begin{aligned} & \text { U } \\ & \text { U } \\ & \text { H } \\ & \text { U } \end{aligned}$ | $\cdots$ |  <br>  |
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|  | 年 |  u u u o o <br>  $1+111+111111+11++11+11$ |
| ${\underset{N}{2}}_{2}^{2}$ |  |  |
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| $\stackrel{\circ}{\circ}$ | $\infty$ |  <br>  <br>  |
|  | $\bigcirc$ |  |
|  |  |  |
| $\begin{aligned} & \dot{\circ} \\ & \text { B } \\ & \text { Q } \end{aligned}$ |  |  <br>  |
|  |  |  |

＊The small letters following the velocities represent the possible uncertainties in each from the writer＇s estimates based upon a consideration of the probable errors，
the number of spectrograms，and their quality and dispersion．They may be interpreted as follows：（a）Three or more spectrograms；uncertainty of x km／sec．possible．




TABLE I－Continued

|  |  | $\underset{H}{ \pm}$ <br> 8 <br>  |
| :---: | :---: | :---: |
| $\begin{aligned} & \text { N } \\ & \text { Hy } \\ & 0 \\ & Z \end{aligned}$ |  |  |
| $\begin{aligned} & \text { U } \\ & \text { U } \\ & \text { U } \\ & \text { U } \end{aligned}$ | $\bigcirc$ |  <br>  |
|  | $\sim$ |  <br>  |
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|  | 安 |  <br>  $1\|11++1+1\| 1 \quad\|1\| 1 \mid 1++++1+111$ |
| $\begin{aligned} & \text { M } \\ & \mu_{\mu}^{2} \end{aligned}$ |  |  |
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|  | $\begin{aligned} & \dot{x} \\ & \underset{\sim}{⿷ 匚} \end{aligned}$ |  |
| \％ | $\omega$ |  <br>  <br>  $11+111111+11++1+1111+1111+1$ |
|  | $\checkmark$ |  |
| $\begin{aligned} & z \\ & 0 \\ & 0 \\ & 4 \\ & \vdots \\ & 0 \\ & 0 \\ & \cline { 1 - 2 } \end{aligned}$ |  |  |
| $\dot{0}$80易 |  |  |
|  |  |  <br>  |


TABLE I-Continued

|  | HD No. | Designation | 1900 |  | Magnitude |  | Type | Vel.Km/Sec. |  | Galactic |  | Notes | Period |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $a$ | $\delta$ | Max. | Min. |  | Abs. | Em. | 1 | $b$ |  |  |
| I8I | 216013 | BD+ | $22^{\mathrm{h}} 5 \mathrm{I}^{\mathrm{m}} \mathrm{O}$ | $+53^{\circ} 4 \mathrm{I}^{\prime}$ | 9.4 |  | Nb |  |  | $74{ }^{\circ}$ |  |  | days |
| 182 |  | VY And | 57.3 | +4521 | 9.5 | 11.0 | Nb | - $12 e$ |  | 72 | -13 |  | 149 |
| 183 | 218851 | BD-21 ${ }^{\circ} 6376$ | $23 \quad 6.3$ | -21 32 | 9.4 | 10.8 | Ro | + 32 c |  | II | -68 | (1) | 149 |
| 184 |  | MSB 42 | 19.1 | +5526 |  |  | ( $\mathrm{N}_{3}$ ) | - 34 d |  | 79 | - 4 | (2) |  |
| 185 | 220870 | BD $+48^{\circ}{ }^{\circ} 5^{1}$ | 22.2 | +4858 | 9.7 |  | Nb | - 10 $e$ |  | 77 | - 11 |  |  |
| 186 | 222241 | ST And | 33.8 | +35 13 | 8.3 | 12.4 | Nb | + $32 c$ | + 13 | 75 | -25 -56 |  | 338 |
| 187 | 223075 | ${ }_{19} \mathrm{Psc}$ | $4 \mathrm{I} \cdot 3$ | + 256 $+\quad 550$ | $5 \cdot 3$ |  | NaNo | + $7 a$ |  | 63 | -56 |  |  |
| 188 | 223392 | $\mathrm{BD}+5^{\circ} 5^{223}$ | 44.0 | +550 +5948 | 8.8 |  | $\mathrm{R}_{3}$ | - $22 e$ |  | 66 | -53 | (1) |  |
| 189 | 224855 | WZ Cas | 56.2 | +59 48 | 7.7 |  | NaNip | - 366 |  | 85 | - 2 | (20) 280 Schj |  |
| 190 | 224959 | BD-3 ${ }^{\circ} 575$ I | 57.0 | - 323 | 9.9 |  | RoRo | -136e |  | 63 | -64 | (1) |  |
| 191 | 225217 | SU And | 59.4 | +43 | 7.9 | 8.5 | Nb | - 6 |  | 82 | $-18$ | (24) |  |

[^1]





 (34) Velocity from D lines only
(35) Composite spectrum; class Ao in the violet region. See Shane, op. cit., p. ı24.
(36) Ha appears as an emission line on a spectrogram covering the region $\lambda \lambda 6500-7600$, March 19, 1935, but with no certainty on any
nitudes and periods was obtained from Prager's catalogue ${ }^{9}$ and from the Mount Wilson discoveries previously alluded to. Galactic coordinates were taken from the Lund tables ${ }^{\mathrm{ro}}$ for the nearest $4^{\mathrm{m}}$ in $a$ and $\mathrm{I}^{\circ}$ in $\delta$. The magnitudes for some of the class -N stars in the Henry Draper Catalogue and most of those in the Mount Wilson list are not known. These latter were not in the Henry Draper Catalogue either because of extreme redness or extreme faintness or because the Harvard observations occurred at unfavorable phases in a great magnitude variation. Magnitudes in italics are photographic; the remainder are visual. Spectral classifications with numerical subscripts are from Shane's work, ${ }^{\text {II }}$ rough estimates on his system for such stars as have not been otherwise classified being placed in parentheses. Under "Abs." are given the velocities from the absorption features, while "Em." denotes velocities from the emission lines of hydrogen, generally $H a$ alone.

Velocities from the emission lines.-Two lists of stars of classes N and R with emission lines of hydrogen have been previously published, ${ }^{\mathrm{I} 2}$ and all these are again included in Table I. In these two lists the means of the difference in velocity between emission (generally $H a$ ) and absorption lines are -27 and $-25 \mathrm{~km} / \mathrm{sec}$., respectively. These, however, involve a few stars of spectral class $R$ and all the absorption-line velocities for N -type stars on the old uncorrected system. In all, twenty stars of spectral class N with emission lines of hydrogen are entered in Table I. The mean difference between their velocities from emission and absorption is $-21.6 \mathrm{~km} /$ sec ., a numerical decrease from the two previously published values, attributable mainly to the application of the systematic correction to the absorption velocities and slightly to additional observations and to the limitation to only stars of class N .

The mean period for the seventeen of these twenty stars for which data are available is 407 days. The velocity difference here found

[^2]lies between those predicted by Merrill's ${ }^{13}$ curves for stars of classes Me and Se . There is a slight correlation with period, smaller differences being associated with shorter periods, but this correlation is too poor to be stressed. With one exception these stars are variable, with a mean range of 4 mag. For some of them there are several spectrograms, representing all phases pretty well, which show that the hydrogen lines may vary from intense emission to practical extinction. Counting from maximum, the emission lines in R Leporis and U Cygni, for example, fade to extinction during the first quarter-period, remain suppressed for another quarter-period or until about light-minimum, then gradually increase, attaining maximum strength during the third quarter-period, which intensity continues until light maximum. The failure to find emission lines in the case of a star with large magnitude range might be attributed to the phase at which it was observed, the star being therefore no exception to the rule. In fact, I have found no certain evidence of bright hydrogen lines for four stars in whose spectra they were noted by Shane. ${ }^{7}$ These are RV Cygni, $7^{\mathrm{m}} \cdot \mathrm{I}-9^{m} \cdot 3$; Y Tauri, $6^{\mathrm{m}} \cdot 9^{-8 \mathrm{~m}} \cdot 9$, period 233 days; U Camelopardalis, $6^{\mathrm{m}} \cdot 9^{-9} 9^{\mathrm{m}} \cdot$, period 4 I 8 days; and V Aquilae, $6^{\mathrm{m}} 5^{-8 \mathrm{~m}}$.

It would seem, therefore, that emission lines accompany a large magnitude range, that their failure to be observed in case the range is large is not necessarily evidence that they are not present at the appropriate phases, and that their appearance in a star of class N not known to vary should arouse a suspicion of variability. MSB II $a=4^{\mathrm{h}} 46^{\mathrm{m}} .8, \delta=+49^{\circ} 46^{\prime}$ (1900), is an example of the last point.

Solar motion, galactic rotation, and absolute magnitude from the radial velocities of stars of spectral class $N$.-The recent success of Plaskett and Pearce ${ }^{\mathrm{I} 4}$ in finding evidence of galactic rotation, both from the radial velocities of the B-type stars and from their detached lines of calcium, and of A. H. Joy, ${ }^{15}$ from the Cepheid variables, demands a similar treatment of whatever other data are available. Such an investigation evidently requires objects located at relatively large distances.

[^3]Various investigators find values for the mean absolute magnitude of stars of spectral class N between the limits -I .3 and -2.5 . Since their apparent magnitudes are in only a few cases brighter than 6 and in many cases fainter than 8 , it is evident that N stars too are relatively distant objects and worthy of consideration in connection with the problem of galactic rotation. The 146 radial velocities of class-N stars in Table I are distributed among the different apparent visual magnitudes ${ }^{16}$ roughly as follows:

$$
\begin{aligned}
& \text { Brighter than 6............ . II } \\
& \text { 6.0-6.9.... . . . . . . . . . . . . . . } 27 \\
& \text { 7.0-7.9.................... . . } 32 \\
& \text { 8.0-8.9..................... . . } 28 \\
& \text { 9.0........................... } 48
\end{aligned}
$$

The velocities show a very considerable spread which has been smoothed out for the purpose of solution by forming two groups for each band of $30^{\circ}$ of galactic longitude, in one of which the galactic latitudes are pcsitive and in the other negative. Since some bands are deficient in stars with negative values of the galactic latitude, twenty groups resulted. All velocities were given equal weight in forming a normal, as it seemed more important that each group depend upon all the stars included in it than largely upon the few better observed stars. No velocity, however large, was omitted.

Except for the effect of random motion, each of these twenty mean velocities $(V)$ was assumed to be conditioned as follows:

$$
V=K+X \cos b \cos l+Y \cos b \sin l+Z \sin b+d u+e v .
$$

$l$ and $b$ are the galactic longitude and latitude. The first member on the right is the well-known $K$-term; $X, Y$, and Z are the components of the solar motion referred to galactic co-ordinates. Further,

$$
\begin{array}{ll}
u=\bar{r} A \cos 2 l_{0}, & d=\sin 2 l \cos ^{2} b, \\
v=\bar{r} A \sin 2 l_{0}, & e=-\cos 2 l \cos ^{2} b .
\end{array}
$$

$A$ is the galactic rotation effect for a distance of miloparsec and $\bar{r}$ is the mean distance in kiloparsecs; $l_{0}$ denotes the longitude of the galactic center.
${ }^{16} \mathrm{~A}$ variable star was assigned its magnitude at maximum; a photographic magnitude was reduced to a visual magnitude by the mean color index +2.6 ; and some of the Mount Wilson discoveries for which magnitudes are not available have been arbitrarily assigned to the ninth magnitude.

A least-squares solution of the twenty normal equations was then carried through, weights being assigned to each roughly proportional to the number of stars involved. The results are given in Table II.

TABLE II

$$
\begin{array}{ll}
K=-0.9 \pm \mathrm{I} .7 \mathrm{~km} / \mathrm{sec} . & Z=-\mathrm{I} 2.4 \pm 5.8 \mathrm{~km} / \mathrm{sec} \\
X=-\mathrm{I} 8.6 \pm 2.2 & u=-0 . \mathrm{I} 5 \pm 2.3 \\
Y=-6.5 \pm 2.8 & v=-\mathrm{I} 3.4 \pm 2.8
\end{array}
$$

The $K$-term is about one-half its probable error. The solar motion is $23.2 \mathrm{~km} / \mathrm{sec}$. toward the apex, whose right ascension is $\mathrm{I} 7^{\mathrm{h}} 8^{\mathrm{m}}$ and declination $+30^{\circ}$, and thus agrees much better with that obtained from the naked-eye stars ( $20 \mathrm{~km} / \mathrm{sec}$. toward the apex with $a=18^{\mathrm{h}}$ and $\delta=+30^{\circ}$ ) than it does with Moore's ${ }^{17}$ value ( $17.1 \mathrm{~km} / \mathrm{sec}$. toward the apex with $a=I 5^{\mathrm{h}}$ and $\delta=+\mp I^{\circ}$ ) obtained from the radial velocities of only twenty-five bright class-N stars.

This solution gives the galactic rotation term $(\bar{r} A) \mathrm{I} 3.4 \mathrm{~km} / \mathrm{sec}$. and the galactic center in the direction of $l_{o}=315^{\circ}$, for which Plaskett obtained $33 \mathrm{I}^{\circ}$ and Joy $324^{\circ}$. The latter's study of the Cepheid variables showed that galactic rotation increases by $18.5 \mathrm{~km} / \mathrm{sec}$. per kiloparsec from our stellar neighborhood, if absorption in space is allowed for. The mean distance in kiloparsecs may therefore be obtained, for the stars upon which it is based, by dividing the galactic rotation value ( $\bar{r} A$ ) by 18.5 . In this case the distance is 0.727 kiloparsecs, corresponding to an approximate mean parallax $\bar{\pi}=0$ ".0014. Although such a summary treatment of the data cannot give a rigorous value, it is of interest to note that the mean absolute magnitude from the foregoing value of $\bar{\pi}$ and the mean apparent magnitude, 7.9 , is - r.4. Plaskett's value of $A(=15.5)$ gives $M=-$ ı. 8 . Wilson ${ }^{18}$ obtained the approximate value - I .4 for the mean absolute magnitude, using the proper motions of ninety-two class-N stars and assuming Moore's value of the velocity of the solar motion. With the solar motion here obtained, his absolute magnitude would become -2.I. Other absolute magnitudes from proper motions are:

```
            No. of Stars
                    ?........- - I.3 Luplau-Janssen and Haarh*
                        23........ I.5 Moore }
                120........-2.6 Kapteyn }
    * A.N., 214, 388, 1921. †Lick Obs. Bull., 10, 168, 1923. \ddagger Ap. J., 32, 91, 1910.
\mp@subsup{}{}{17}\mathrm{ Op. cit., p. 168. }\mp@subsup{}{}{18}A.J., 34, 191, 1922.
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Figure I shows how well the curve from this solution fits the twenty normal places reduced to $b=0$. The ordinates are radial velocities and the abscissae, galactic longitudes. Barred circles represent the normal places from stars with negative galactic latitudes, and open circles those from stars with positive ones, accompanying numbers indicating how many stars are involved in each normal place.


Fig. i.-Solar motion and galactic rotation. Each circle represents a normal place, a bar indicating one derived from the velocities of stars in negative galactic latitudes. The number of velocities upon which a normal depends is given beside the circle. The full-line curve represents the combined solar motion and galactic rotation in the plane of the galaxy; the broken-line curve, the solar motion alone. Null, maximum, and minimum points for both galactic rotation and solar motion are given at the top of the figure.

It is frankly admitted that the scatter about the curve is considerable, which explains the large probable errors for the solution. It must be pointed out, however, that a representation of these normal places by solar motion alone would be quite unsatisfactory because the greater weight for the normals between galactic longitudes $70^{\circ}$ and $180^{\circ}$ would produce a sine-curve which would not at all represent the remaining galactic-longitude interval.

This solution is based upon class-N stars of all apparent magnitudes, but would be more convincing if the size of the galactic rotation term could be shown to depend upon mean apparent magnitude. To derive an approximate idea of this, the following procedure was adopted. It was first assumed that these stars give the ordinary solar apex with the solar motion velocity ( $23 \mathrm{~km} / \mathrm{sec}$.) here obtained,
and their individual velocities were corrected accordingly. Only stars with galactic latitudes between $+40^{\circ}$ and $-40^{\circ}$ were used, and one velocity exceeding $-100 \mathrm{~km} / \mathrm{sec}$., which may in reality belong to spectral class R, was excluded. These were next divided into three groups according to apparent magnitude: the first, the stars brighter than 7.2 ; the second, those between this limit and 8.9; and a third group, the remainder, 9.0 or fainter. Finally, a least-squares solution was carried through for the stars in each group in which the residual velocity is represented by the conditional equation

$$
\rho=\bar{r} A \sin 2\left(l-315^{\circ}\right) \cos ^{2} b .
$$

TABLE III

| No. | $\bar{r} A$ <br> Км/Sec. | $\bar{r}$ <br> Kiloparsecs |  | Mean Magnitude |  |  | $\begin{gathered} \bar{\rho} \\ \text { Km/SEC. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | App. | Abs. |  |  |
|  |  | $A=18.5$ | $A=15.5$ |  | $A=18.5$ | $A=15.5$ |  |
| 4 I | 7.2 | 0.390 | 0.465 | 6.5 | -1.4 | -I. 8 | 17.3 |
| 48. | 16.3 | 0.879 | I. 050 | 8.2 | I. 5 | 1.9 | 2I. 6 |
| 44. | 22.4 | I. 211 | I. 445 | $9 \cdot 3$ | -I.I | -I. 5 | 22.1 |

Column 2, Table III, ${ }^{19}$ gives the results of these solutions. The other columns contain, respectively: (1) the number of stars; (3) and (4) the mean distances obtained when Joy's $A$ and Plaskett's $A$ are assumed; (5) the mean apparent magnitudes; (6) and (7) the mean absolute magnitudes on the basis of the two values of $A$; and (8) the mean velocities freed from solar motion, sign being disregarded.
$\bar{r} A$ increases steadily with mean apparent magnitude; hence the reality of the rotation term from the general solution is greatly strengthened by the foregoing treatment. The spread in the derived absolute magnitudes is no more than might be expected from the probable errors, the uncertainties of the individual mean magnitudes

[^4]for the fainter stars, and the effect of space absorption. Moreover, any spread in the individual absolute magnitudes could result in a fainter mean absolute magnitude for the group of apparently faintest stars, since more of the absolutely fainter stars would conceivably enter such a group.

Although the absolute magnitudes of column 7 (using Plaskett's $A)$ agree better with Wilson's mean absolute magnitude as revised, -2.1, the absolute magnitudes of column 6 are tentatively adopted; for Joy's $A$ upon which they depend is based upon not only the radial velocities of, but also the space absorption for, the Cepheid variables, the range of whose distances considerably exceeds those for the stars of class B. The weighted mean $M$ from column 6 is -I .34 , in good agreement with the value - I. 4 given earlier from all class- N stars.

The weighted mean of the peculiar motions without regard to $\operatorname{sign}(\bar{\rho})$ is $20.4 \mathrm{~km} / \mathrm{sec}$., thus exceeding by $3.9 \mathrm{~km} / \mathrm{sec}$. the mean peculiar motion of class-M stars found by Campbell. Larger values, however, have been obtained by Merrill ${ }^{20}$ for some subdivisions of spectral classes Me and Se.

Double stars.-The following class- N stars have companions:

$$
\begin{aligned}
& a^{1900}{ }_{\delta} \\
& \text { HD } 322 \mathrm{I} 8 \mathrm{TU} \text { Tauri....... } 5^{\mathrm{h}} 39^{\mathrm{m}} \mathrm{I}+24^{\circ} 23^{\prime} 8^{\mathrm{m}^{\mathrm{m}}} 7^{-9^{\mathrm{m}}}{ }^{5} \text { Composite } \mathrm{N}_{2} \text { +Ao } \\
& \text { MSB 31........ } 745.0-\circ 38
\end{aligned}
$$

$$
\begin{aligned}
& \text { HD } 209596 \ldots .2 \text { I } 59.5+455
\end{aligned}
$$

The components of the last three stars are widely separated, with the secondaries considerably fainter than the primaries. The first and third entries furnish some data about the absolute magnitudes of the class-N primaries. In the case of TU Tauri the secondary is estimated by Shane ${ }^{2 \mathrm{I}}$ to be a class-Ao star of apparent magnitude ir. The absolute visual magnitude of TU Tauri comes out -r. 8 at maximum, if the most frequent absolute magnitude ( +0.5 ) for type Ao, as given by Strömberg, ${ }^{22}$ is assumed. A spectrogram of com-

[^5]ponent $B$ of the third entry shows a class-G6 spectrum from which the absolute magnitude was estimated to be +o.r. On the assumption of physical connection, the derived absolute magnitude of $A$ is -0.8 . Its radial velocity is $-I I \mathrm{~km} / \mathrm{sec}$. (low weight) and that of $B,+8 \mathrm{~km} / \mathrm{sec}$. (depending on a single plate). Neither the magnitudes of the components nor the spectra of the secondaries are known in the other two cases. Such evidence as the first and third pairs furnish is in as good agreement with the results for absolute magnitude from the rotation effect as could be expected.

In conclusion, it seems appropriate to admit candidly the limitations in the accuracy of the velocities in Table I, which depend in a considerable degree upon few observations and often upon spectrograms of low dispersion. The velocities from spectrograms of low dispersion when compared with velocities obtained with higher dispersion have revealed no anomalies. Sufficient stars have been repeatedly observed to establish the fact that only a very few have velocity ranges which much exceed the accidental error to be expected. Hence it seemed best to concentrate upon securing approximate velocities for the greatest possible number of stars of class N rather than struggle for greater accuracy for a few stars. This assumes that the mean of a large number of approximate velocities better typifies the mean motion of a group of stars than does the mean of a few accurate velocities, some of which might represent abnormally large peculiar motions. Indeed, the final results would have differed very little from those actually obtained if the velocities from the first spectrogram of each star had been made the basis of the solutions.

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[^0]:    ${ }^{8}$ Mt. W. Contr., No. 486; Ap. J., 79, 202, 1933.

[^1]:    NOTES TO TABLE I
    (2) See Merrill, Sanford, and Burwell, Pub. A.S.P., 45, 306, 1933. When no other designation exists for one of these stars the number is given from this publication.
    (1) Taken from Mt. W. Contr., No. 276, Table I.
    (3) Moore's velocity, in Lick Obs. Bull., 10, 160, 1922, corrected by $-7 \mathrm{~km} / \mathrm{sec}$.
    (4) Called to my attention by S. B. Nicholson, who noted its extreme redness on photographs of comet Nagata (193rb). Discovered independently by Miss Burwell and Merrill.
    (5) Welocities range from +26 to $+50 \mathrm{~km} / \mathrm{sec}$.
    (7) Velocity-range from +7.1 to $+18.4 \mathrm{~km} / \mathrm{sec}$. Coude plates range from +10.0 to $+18.4 \mathrm{~km} / \mathrm{sec}$.
    (o) Velocity range for absorption lines, +4 to $+37 \mathrm{~km} / \mathrm{sec}$. Range for emission lines, -13 to $+23 \mathrm{~km} / \mathrm{sec}$.
    (io) Velocity range for absorption lines, o to $+15 \mathrm{~km} / \mathrm{sec}$.
    (II) Class S with sometimes (?) class N added. Has $10^{\mathrm{m}}$ A-type companion. (12) One grating plate gives $+23 \mathrm{~km} / \mathrm{sec}$.

[^2]:    9"Katalog und Ephemeriden veränderlicher Sterne in 1934," Kleinere Veröff. Universitätssternwarte Berlin-Babelsberg, No. I3, 1933.
    ${ }^{10}$ John Ohlsson, Ann. Obs. Lund, No. 3, 1932.
    ${ }^{11}$ Op. cit., 13, 123, 1928.
    ${ }^{12}$ Pub. A.S.P., 42, 287, 1930; 45, 44, 1933.

[^3]:    ${ }^{13}$ Mt. W. Contr., No. 264; Ap.J., 58, 251, Fig. 2, 1923.
    ${ }_{14}$ Pub. Dom. Ap. Obs., 5, 167-237, 1933.
    ${ }^{15}$ Pub. A.S.P., 45, 202, 1933.

[^4]:    ${ }^{19}$ The data in this table are to be preferred to those already given in Pub. A.S.P., $46,228,1934$. The changes arise mainly from the use of the velocity from the solution for solar motion based on the N stars themselves; whereas the velocity derived from the naked-eye stars was used for the earlier results.

[^5]:    ${ }^{20}$ Mt. W. Contr., No. 264; Ap. J., 58, 166, 1923.
    ${ }^{21}$ Op. cit., 13, 124, 1928.
    ${ }^{22}$ Mt. W. Contr., No. 442; Ap. J., 75, 341, 193r.

